

1 Explainable El Niño predictability from climate mode interactions

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27 **Summary Paragraph**

28 **The El Niño-Southern Oscillation (ENSO) provides most of the global seasonal climate**
29 **forecast skill¹⁻³, yet, quantifying the sources of skilful predictions is a long-standing**
30 **challenge⁴⁻⁷. Different sources of predictability affect ENSO evolution, leading to distinct**
31 **global impacts. Artificial Intelligence (AI) forecasts offer promising advancements but**
32 **linking their skill to specific physical processes is not yet possible⁸⁻¹⁰, limiting our**
33 **understanding of the dynamics underpinning the advancements. Here we show that an**
34 **extended nonlinear recharge oscillator (XRO) model exhibits skilful ENSO forecasts at lead-**
35 **times up to 16-18 months, better than global climate models and comparable to the most**
36 **skilful AI forecasts. The XRO parsimoniously incorporates the core ENSO dynamics and**
37 **ENSO's seasonally modulated interactions with other modes of variability in the global**
38 **oceans. The intrinsic enhancement of ENSO's long-range forecast skill is traceable to the**
39 **initial conditions of other climate modes via their memory and interactions with ENSO and**
40 **is quantifiable in terms of these modes' contributions to ENSO amplitude. Reforecasts using**
41 **the XRO trained on climate model output show that reduced biases in both model ENSO**
42 **dynamics and in climate mode interactions can lead to more skilful ENSO forecasts. The**
43 **XRO framework's holistic treatment of ENSO's global multi-timescale interactions**
44 **highlights promising targets for improving ENSO simulations and forecasts.**

45 **Main**

46 The El Niño-Southern Oscillation (ENSO) exerts global environmental and socioeconomic
47 impacts via teleconnections¹⁻³. Since the first successful prediction of El Niño in 1986 (ref⁴),
48 decades of progress on the understanding and modelling of ENSO has improved prediction skill⁵⁻
49 ⁷. However, skilful prediction of ENSO at a lead-time longer than a year remains a challenge.

50 While ENSO originates from coupled ocean-atmosphere interactions in the tropical Pacific,
51 recent studies highlight that interactions with other ocean basins could potentially improve ENSO
52 prediction¹¹. For instance, many other climate modes have been shown to interact with ENSO (Fig.
53 1a), including the North and South Pacific Meridional Modes (NPMM and SPMM)^{12,13}; the Indian
54 Ocean Basin (IOB) mode¹⁴, the Indian Ocean Dipole (IOD) mode¹⁵, and the Southern Indian
55 Ocean Dipole (SIOD) mode¹⁶ in the Indian Ocean; as well as Tropical North Atlantic (TNA)
56 variability¹⁷, the Atlantic Niño (ATL3)¹⁸, and the South Atlantic Subtropical Dipole (SASD)
57 mode¹⁹ in the Atlantic Ocean. Although multiple previous studies designed forecast experiments
58 to illustrate the roles of other ocean basins in ENSO predictability, using simple coupled
59 models^{20,21,14}, atmosphere-ocean coupled general circulation models (CGCMs)^{22–26} or linear
60 inverse models^{27,28}, it remains a challenge quantifying the relative contributions of other ocean
61 basins to ENSO predictability. The employed CGCMs typically exhibit pronounced biases in
62 simulating both the climate mean state and ENSO dynamics, thus hindering skill in predicting
63 ENSO and complicating quantification of the other ocean basins impact on ENSO predictability.
64 Current linear inverse models are by construction not able to fully capture ENSO's nonlinear
65 dynamics and seasonality^{27,28}. Quantifying the sources of skilful predictions from these specific
66 physical processes has been elusive^{11,15,17,29,30}.

67 Different sources of ENSO predictability can lead to substantial event-to-event differences in
68 ENSO evolution and associated global impacts. For example, while both the 1997/98 and 2015/16
69 extreme El Niño events had similar amplitudes of Niño3.4 SST anomalies (SSTAs), they had
70 distinct precursor patterns (Fig. 1b). The 1997/98 event exhibited strong preconditioning via
71 recharged warm water volume (WWV) in the equatorial Pacific, large SST anomaly precursors in
72 the Indian Ocean (including a negative IOD during 1996 September–November (SON)), but only
73 weak SST anomalies in the extratropical Pacific. In contrast, the 2015/16 event was characterized

74 by a weaker build-up of WWV, less pronounced precursor SST anomalies in the Indian Ocean, and
75 instead large amplitude NPMW warming in 2015 March-April-May (MAM). The Atlantic Ocean
76 SST signals are largely similar for the two events, except that the MAM TNA was anomalously
77 warm in 1997 but cold in 2015. In turn, these two events evolved differently in the various basins
78 (Supplementary Fig. 1), which lead to distinct global impacts (Fig. 1c,d, Supplementary Fig. 2,
79 ref^{31,32}). These two different evolutions and impacts, affected by varied precursor patterns,
80 underscore the need to quantify the sources of prediction skill and their role in the manifestation
81 of different SST patterns more accurately.

82 Recent advances have demonstrated the value of AI in predicting ENSO with skilful forecasts
83 at long lead-time of 18-24 months⁸⁻¹⁰. Despite emerging explainable AI methodologies¹⁰, linking
84 the forecast skill of the AI model to specific physical processes is not yet possible, limiting our
85 understanding of the dynamics and physical robustness underpinning the enhanced AI skill. Here
86 we develop a low-order extended nonlinear Recharge Oscillator (XRO) model – which couples
87 the ENSO recharge oscillator with autoregressive model representations for the other modes (see
88 “*Extended Nonlinear Recharge-Oscillator Model (XRO)*” in *Methods*) – to both predict ENSO
89 events and quantify the various sources of ENSO predictability from climate mode interactions.
90 We find that our model provides skilful and, most importantly, explainable forecasts at lead-times
91 up to 16-18 months, better than global climate models and comparable to the most skilful AI ENSO
92 forecast model.

93 **Efficacy boosted by climate interactions**

94 We evaluate the XRO in simulating ENSO through a 43,000 yearlong stochastically forced
95 simulation (See “*Stochastically forced XRO simulations*” in *Methods*) with parameter estimates
96 derived from 1979-2022 observations (black curves in Extended Data Fig. 1). The XRO accurately
97 simulates the fundamental observed characteristics of ENSO including its seasonal

98 synchronization, Niño3.4 positive skewness, its interannual spectral peak, the 6-9 months lead of
99 WWV over ENSO SST, its irregular interannual oscillations, and the spring persistence barrier
100 (Fig. 2a-d, Supplementary Text 1 and Figs. 3-4). The XRO also accurately reproduces the observed
101 seasonal characteristics of the other climate modes including their seasonal synchronizations and
102 autocorrelations (Supplementary Figs. 5-6). In addition, the XRO realistically simulates the
103 observed lead-lag relationships between ENSO and all the other climate modes with the range of
104 XRO realization cross-correlations encompassing the observations (Fig. 2e-l). Simulating these
105 observed relationships is a major challenge for climate models (Supplementary Fig. 7).

106 Next, we perform out-of-sample XRO reforecasts by fitting the model for 1950-1999 (50
107 years) and verifying it independently for the 2002-2022 period (See *“Out-of-sample reforecasts”*
108 *in Methods*). The correlation skills of the Niño3.4 reforecasts are compared with a nonlinear RO
109 model (nRO), the real-time International Research Institute for Climate and Society (IRI)
110 operational models, and the most skilful AI ENSO forecast model^{8,9} (Fig. 2m). Interestingly, the
111 skill of the simple nRO is comparable with the ensemble mean of the IRI statistical models. With
112 mode interactions considered, the XRO outperforms the ensemble mean of the IRI dynamical
113 models at long lead-time (>9 months) with skill scores comparable to the AI model. We also test
114 the model by verifying the early period (1950-1970) and the middle period (1972-1992)
115 independently. The XRO outperforms the nRO regardless which of the verification periods is used
116 to assess the skill (Extended Data Fig. 2), suggesting the importance of mode interactions for
117 ENSO forecast skill regardless of the intrinsic decadal changes in ENSO predictability^{33,34}.

118 To get sufficient sample sizes of ENSO events, we next focus on the satellite era (1979-2022)
119 and perform in-sample control reforecasts using the XRO and nRO (denoted as XRO and nRO in
120 the figures, respectively, see *“Control XRO and nRO reforecasts” in Methods*). The nRO ranks in
121 the middle of the skill range for the existing state-of-the-art dynamical prediction systems (Fig.

122 2n). The XRO systematically outperforms the individual dynamical models and multi-model
123 ensemble mean. The correlation skill of XRO is still above 0.5 at a lead-time of 18 months, which
124 is again comparable to the most skilful AI model (Fig. 2n). We also employ two additional
125 approaches to confirm the robustness of the XRO parameter fitting and reforecasting performance
126 during 1979-2022 (See “*Cross-validated reforecasts*” and “*Large ensemble simulations and*
127 *perfect model reforecasting experiments*” in *Methods*, Supplementary Fig. 8). First, the XRO
128 cross-validated by sequentially leaving n -year data out still provides skilful prediction of Niño3.4
129 SSTA up to 17 months in advance and is insensitive to the exclusion of a range between 2 to 7
130 years of data (Supplementary Fig. 8a). Second, the XRO was repeatedly trained using each
131 member of large ensemble CGCM simulations (LENS) and forecasted on the same member
132 (“Same-Member” experiment) and an independent realization (“Cross-Member” experiment),
133 respectively. All four LENS models’ perfect experiments using the same observational record
134 length (43-year) demonstrate the uncertainty in parameter estimation leads to XRO reforecasting
135 correlation skill error of less than 0.1 within 21 lead months (Supplementary Fig. 8b-d).

136 We further assess the seasonality of the Niño3.4 forecast correlation skill during 1979-2022
137 in Fig. 2o-p and Supplementary Fig. 9. Like most of the dynamical models, the nRO exhibits a
138 pronounced spring predictability barrier (SPB) in May-June-July, when the forecast skill decreases
139 rapidly (vertical blue lines in Fig. 2o). The SPB is much less pronounced in the XRO model, which
140 maintains a 0.5 correlation skill up to 16 months for all different initial times (Fig. 2p). The superior
141 efficacy of XRO in ENSO forecasting is further illustrated by the root mean square error metric
142 (Supplementary Fig. 10).

143 Sources outside the tropical Pacific

144 The XRO formulation allows us to explicitly isolate and quantify the roles of different mode
145 interactions in ENSO’s dynamical behaviour and predictability. Three previous approaches have

146 been employed to assess the impact of climate variability in various ocean basins on ENSO
147 predictability, using CGCMs, intermediate complexity models, and/or conceptual models. They
148 include: (i) *partial initialization* experiments, which set the ocean initial conditions for a specific
149 basin to the model climatology, while using the observed initial conditions everywhere else^{21,28};
150 (ii) *partially coupled* experiments, which apply strong SST restoring toward the model climatology
151 in a specific region during the model integration, while keeping the atmosphere and ocean fully
152 coupled elsewhere^{22,24,28}; (iii) *relaxing towards observations* experiments, in which model SSTAs
153 are strongly nudged towards observations in a specific region, while elsewhere the model is fully
154 coupled^{23,26}. We apply these strategies to our XRO model in corresponding sets of ENSO
155 reforecasting sensitivity experiments: (i) uninitialized experiments (referred to as U_j), (ii)
156 decoupled experiments (D_j), and (iii) relaxation towards observations experiments (R_j), (see
157 [“Quantitative reforecasting experiments” in Methods](#) and [Extended Data Table 1](#)). We further
158 investigate the total contribution of *all* the modes in each ocean basin to ENSO’s predictability by
159 grouping modes together: the extratropical Pacific Ocean (ExPO) includes NPMM and SPMM;
160 the Indian Ocean (IO) IOB, IOD, and SIOD; and the Atlantic Ocean (AO) TNA, ATL3, and SASD.
161 The ExPO+IO+AO experiments demonstrate the combined effects of all the non-ENSO modes.

162 All the sensitivity experiments qualitatively indicate that coupling information from the ExPO,
163 IO, and AO basins enhances ENSO forecast skill ([Fig. 3a](#)), consistent with previous
164 findings^{23,24,26,28,35}. However, only the uninitialized experiment framework is a suitable approach
165 to quantify the nearly additive relative contributions of each basin to ENSO forecast skill
166 ([Extended Data Fig. 3a,d,e](#)) without artificially overestimating the contribution of climate
167 variability in other basins to ENSO predictability ([Extended Data Fig. 3b,c,d,e](#)). Therefore,
168 hereafter we use the uninitialized experiment framework to quantify the impact of each individual
169 basin’s or mode’s initial condition on subsequent ENSO forecast skill.

170 Allowing for climate mode interactions enhances ENSO forecast skill, and significantly
171 weakens the SPB with an improvement of correlation skill up to 0.2 ($P < 0.08$, Fig. 3b). The
172 enhancement of ENSO forecast skill from climate mode interactions is primarily through the initial
173 condition memory of the different climate modes, demonstrated by the large difference between
174 control and the uninitialized ExPO+IO+AO experiment (Fig. 3c, Supplementary Fig. 11a). The
175 initial states of the other modes can persist for a few months and effectively impact ENSO in
176 specific seasons. In contrast, as evidenced by the minor differences between uninitialized
177 ExPO+IO+AO experiment and decoupled ExPO+IO+AO experiment, the coupled feedbacks with
178 these modes induced by ENSO's initial state only slightly reinforce and accelerate phase-transition
179 of ENSO events (Supplementary Fig. 11b). This results in an increase in forecast skill during the
180 ENSO transition phase (Jun⁺¹-Sep⁺¹ targets, Fig. 3d) but a decrease in forecast skill during the
181 ENSO peak phases (Nov⁺¹-Mar⁺¹ targets, Fig. 3d). Additional reforecasting experiments (See
182 *"Losing memory experiments" in Methods, Extended Data Fig. 4*) confirm that gradually
183 preserving the initial condition memory of climate modes outside the equatorial Pacific
184 incrementally improves ENSO forecast skill from that of the nRO to that of the XRO.

185 We further illuminate the roles of individual basins in ENSO predictability by comparing the
186 difference between the control and uninitialized experiments for the ExPO, IO, and AO basin
187 experiments (Figs. 3e-g). The contributions of each basin have strong seasonality. For instance,
188 the effect of ExPO initialization is most pronounced when forecasts start from November-June,
189 and target December-March when the ENSO signal is large (Fig. 3e). This effect is dominated by
190 the NPMM initialization, whereas the SPM initialization is less impactful (Extended Data Fig.
191 5a-b). In contrast, the effect of IO initialization is most pronounced when forecasts start from July-
192 November, the time of the year when the IOD develops and peaks (Fig. 3f). The IO effect is
193 dominated by the IOD, with a secondary contribution from the IOB, and the SIOD playing only a

194 minor role (Extended Data Fig. 5c-e). This result is in contrast with the previous finding based on
195 the decoupled linear inverse model experiments¹⁴ which suggested that the IOB plays a more
196 significant role than the IOD in weakening the ENSO SPB. The discrepancy may stem from the
197 lack of seasonality and nonlinearity in their model, along with potential overestimations arising
198 from their decoupled model experiment strategy. The AO also results in a weakening of the ENSO
199 SPB when forecasts are initialized from December-April (Fig. 3g), with major contributions from
200 the TNA and SASD, while Atlantic Niño initialization has a negligible effect (Extended Data Fig.
201 5f-h). These contributions of mode interactions to ENSO forecast skill are further supported by the
202 root mean square error metric (Supplementary Fig. 12).

203 **ENSO intensification from remote sources**

204 Next, we quantify the roles of mode interactions on the individual ENSO event reforecasts,
205 illustrated by the time series of predicted Niño3.4 SSTAs for the XRO, decoupled ExPO+IO+AO
206 ($D_{\text{ExPO+IO+AO}}$), and uninitialized ExPO+IO+AO ($U_{\text{ExPO+IO+AO}}$) experiments at lead-time of 0-21
207 months (Fig. 4a-c). The zero lead-time refers to the observed values. The Niño3.4 forecasts in the
208 $U_{\text{ExPO+IO+AO}}$ experiment closely resemble those of the $D_{\text{ExPO+IO+AO}}$ experiment, again indicating
209 that the skill improvement in the control XRO arises from the memory of the other climate mode
210 initializations. These two sensitivity reforecasts can predict the El Niño and La Niña event
211 occurrences at lead-time of 3-9 months and usually underestimate the amplitude of Niño3.4 SSTAs.
212 The XRO systematically outperforms the uninitialized/decoupled ExPO+IO+AO experiments
213 with more accurate amplitude prediction of Niño3.4 SSTAs and extended skilful prediction of El
214 Niño and La Niña event occurrences at longer lead-time of 6-18 months (Fig. 4a). For instance,
215 the 1986/1987 El Niño event could be predicted 18 months in advance with XRO in our hindcast,
216 as opposed to only 6 months in advance with uninitialized/decoupled ExPO+IO+AO experiments.

217 To better understand the influence of a specific climate mode on individual ENSO events, we
218 examined the differences in ENSO SSTAs and WWV anomalies between control and uninitialized
219 experiments for the 1997/98 El Niño and 1998/99/00 triple La Niña episodes (Fig. 4d-k) as well
220 as for the full period (Extended Data Fig. 6). The ENSO forecast differences due to the
221 initialization of other modes are pronounced when those SSTAs have sufficiently large amplitudes
222 and during the season in which their interaction with ENSO is relatively strong. These effects of
223 the non-ENSO modes usually last longer than their own SSTA persistence, indicating the activation
224 of ENSO coupled recharge-discharge feedbacks as shown by the ENSO SSTA and WWV
225 anomalies alternating with a few months lag.

226 In the extratropical Pacific, positive SSTAs for both the NPMM and SPMM in boreal spring
227 can enhance ENSO SST warming 6-9 months later (Fig. 4d,h). However, the underlying
228 mechanisms differ for the two different hemispheres. The NPMM warming leads to recharged
229 WWV anomalies and subsequent ENSO SST warming, highlighting the important role of the trade
230 wind charging mechanism³⁶. In contrast, the SPMM warming directly generates SST warming on
231 the equator, followed by sequential WWV discharge, which aligns with the finding that ENSO is
232 thermally driven by the SPMM³⁷(Extended Data Fig. 6a-b).

233 We also find that coupling with the NPMM tends to favour multi-year ENSO events, such as
234 the 1998/99/00 La Niña. The first year La Niña in 1998/99 set the stage for a strong spring NPMM
235 cooling in 1999 (consistent with the strong nearly-instantaneous feedback mechanism³⁸), which in
236 turn reinforced WWV discharge and colder SSTAs (by ~ 0.3 °C) in the second year. This strong
237 WWV discharged state persisted and re-intensified into the third year, causing SSTA to decrease
238 (~ 0.4 °C) in the winter of the third year (Fig. 4d). Similar patterns are evident in multi-year La
239 Niña events in 2007/08, 2010/11, and 2020/21/22 (blue shadings in Extended Data Fig. 6a). We
240 emphasize that this contribution is also evident for the opposite ENSO phase, as seen in multi-year

241 El Niño events in 1986/87, 2014/15, and 2018/19 ([Extended Data Fig. 6a](#)). These results support
242 the hypothesis that the coupling between NPMM and ENSO favours the existence of multi-year
243 ENSO events^{39–41}.

244 In the Indian Ocean, the 1996 boreal autumn negative IOD event was found to induce a
245 ~ 0.4 °C Niño3.4 SSTA increase ~ 15 months later, thus contributing to the 1997/98 super El Niño
246 ([Fig. 4f](#)). Conversely, the 1997 boreal autumn positive IOD event led to a ~ 0.5 °C Niño3.4 SSTA
247 decrease ~ 15 months later, thus playing a role in the 1998/99 La Niña ([Fig. 4f](#)). This aligns with
248 previous finding¹⁵ that negative IOD event favours the build-up of WWV (i.e., recharge) and
249 contributes to the development of El Niño in the following year via the Bjerknes feedback. The
250 SIOD mode, characterized by an SST east-west dipole over the southern IO, tends to induce
251 ~ 0.2 °C Niño3.4 SSTA increase/decrease ~ 12 -16 months later, often offsetting the IOD's effect
252 ([Fig. 4g](#)). The IOB, although largely forced by ENSO, helps to accelerate the phase-transition of
253 ENSO events⁴². For example, the IOB warming in 1998 contributed to a ~ 0.2 °C Niño3.4 SSTA
254 decrease during the 1998/99 La Niña, about half the magnitude of the IOD-induced change ([Fig.](#)
255 [4e](#)). These results corroborate the findings in [Fig. 3e](#) that the Indian Ocean's influence on ENSO
256 predictability is predominantly governed by the IOD.

257 In the Atlantic Ocean, the TNA warming favours Niño3.4 SSTA decrease 6-12 months later
258 by about ~ 0.3 °C ([Fig. 4i](#)), consistent with a previous finding¹⁷. The 1997 boreal summer Atlantic
259 Niña (ATL3 cold anomalies) was found to weakly favour Niño3.4 SSTA increase 6-12 months
260 later by about ~ 0.15 °C ([Fig. 4j](#)). The positive phase of the SASD in 1997 contributed to a ~ 0.3 °C
261 Niño3.4 SSTA increase 9-12 months later ([Fig. 4k](#)), in line with previous findings¹⁹. The Atlantic
262 Ocean's influence is predominantly governed by the TNA and secondly by the SASD and ATL3.

263 For the 20/21/22 triple La Niña events, the strong positive IOD in 2019 autumn is among the
264 most important contributors to the first year SSTA cooling ([Extended Data Fig. 6d](#)), and the

265 NPMM cooling is among the most important sources in amplifying the second year SSTA decrease
266 (Extended Data Fig. 6a), consistent with previous findings^{43,44}. The ongoing 2023/2024 El Niño
267 occurrence can be predicted up to 18 months in advance in the decoupled ExPO+IO+AO
268 experiment (Fig. 4b), largely due to the highly recharged WWV state caused by the preceding
269 “triple-dip” La Niña events. The XRO refines the amplitude prediction for the 2023/2024 El Niño
270 at longer lead-time of 9-18 months (Fig. 4a), with positive contributions from the preceding IOD
271 and IOB conditions (Extended Data Fig. 6c,d).

272 Composites of the uninitialized experiments for the peak phase of El Niño/La Niña years (Fig.
273 4l) support that climate mode interactions contribute to the observed Niño3.4 SSTA anomalies, in
274 addition to the generally stronger contribution from the equatorial Pacific recharge/discharge
275 dynamics intrinsic to ENSO. The additional contributions are mainly from the NPMM, IOD, and
276 TNA with large inter-event spread, with other modes playing secondary roles. The impacts are
277 asymmetric (i.e., different impacts for El Niño and La Niña events) from some modes such as the
278 IOB, SPM, and SASD. The impact from the IOB on La Niña SSTA is much more pronounced
279 than on El Niño SSTA, consistent with previous findings¹⁴.

280 **Predictability reduced by model biases**

281 Next, we turn to the impacts of biases in comprehensive climate models on ENSO forecast
282 skill. We conducted additional XRO model forecast experiments by using the operator parameters
283 trained using the 91 historical simulation outputs from the Coupled Model Intercomparison Project
284 (CMIP) phase 5 and 6 (see “*The XRO reforecasting experiments based on CMIP model outputs*”
285 *in Methods*, Extended Data Table 2, red curves in Extended Data Fig. 1). Figure 5a reveals that the
286 forecast skill of XRO^m, when trained solely on each CMIP CGCM, shows a wide inter-CGCM
287 spread at lead-time from 7 to 17 months. Importantly, the forecast skill when the model is trained
288 on CMIP output is consistently lower than for the model trained on observational data (Extended

289 [Data Fig. 7a](#)). This suggests that biases in all climate models reduce the ability of these CGCMs
290 to forecast ENSO correctly.

291 We modified each XRO^m to remove these dynamical biases, by individually substituting the
292 parameters obtained from the observations into three key components of the model: ENSO's
293 internal dynamics (L_{ENSO}), the remote climate mode feedbacks onto ENSO (C_1), and the ENSO
294 teleconnections to the remote modes (C_2). Correcting the ENSO dynamics (L_{ENSO}) generally
295 enhances forecast skill at all lead-times (red curve in [Fig. 5b](#), [Extended Data Fig. 7b](#)). This
296 indicates that the way ENSO's core dynamics are biased in climate models is a major factor in
297 lower ENSO forecast skill. Correcting the remote climate mode feedbacks onto ENSO (C_1) also
298 improves the ENSO forecasts for lead-time up to 16 months (magenta curve in [Fig. 5b](#), [Extended](#)
299 [Data Fig. 7c](#)). Thus, mode coupling is critical for ENSO development, as another source of bias.
300 Correcting the ENSO teleconnections (C_2) yields reduced ENSO skill (blue curve in [Fig. 5b](#),
301 [Extended Data Fig. 7d](#)), but greatly improves the forecast skill for other modes, such as the IOD
302 ([Extended Data Fig. 8](#)). These results suggest that reduced biases in model ENSO dynamics and
303 in climate mode interactions lead to more skilful ENSO forecasts.

304 **Pantropical SST predictability**

305 Lastly, we demonstrate that ENSO-climate mode interactions also enhance the SST
306 predictability of other climate modes. For instance, the lead-time of skilful IOB forecast extends
307 from 5 months in the uninitialized ENSO experiment to 19 months in the XRO control experiment
308 ([Supplementary Fig. 13c,j](#)). The all-month IOD forecast skill extends to 5 months (the SON
309 forecast to 8 months), supporting earlier findings that long lead IOD predictability arises from
310 ENSO and is impacted by the signal-to-noise ratio⁴⁵. The improvement is also evident for SSTA
311 modes in the Atlantic Ocean (about 1 month, [Supplementary Fig. 13f,g,h](#)). Interestingly, there is

312 no skill improvement to NPMM and SPMM, possibly because their initial state already includes
313 ENSO information given the strong nearly-instantaneous feedback with ENSO (Fig. 2e,f, ref³⁸).

314 In addition to ENSO amplitude, our XRO model can be expanded to also consider ENSO
315 spatiotemporal diversity by using two ENSO SST indices (e.g. the Niño3 and Niño4 indices, as in
316 the model XRO2, *see “The XRO2 ENSO types and pantropical SSTA forecasts” in Methods*). The
317 XRO2 is able successfully predict the EP-type characteristic of the 1997/98 El Niño, and the
318 mixed-type characteristic of the 2015/16 El Niño, up to 9 months in advance (Supplementary Table
319 3). In contrast, the NMME dynamical models fail to predict the correct type for the 1997/98 event,
320 possibly due to long-standing model biases of westward-displaced ENSO SST anomalies⁴⁶. The
321 successful prediction of ENSO spatial diversity in the XRO has important implications for
322 predicting global climate impacts that differ strongly for contrasting ENSO SSTA patterns.
323 Furthermore, the skill of forecasted pantropical SSTA at 9-month lead using the regression model
324 of ten forecasted SST indices outperforms the operational dynamical models in most regions
325 except the Caribbean Sea (Supplementary Fig. 14). The successful forecasts of ENSO types and
326 pantropical SSTA within the XRO framework highlight the essential importance of accurately
327 representing ENSO-climate mode interactions in climate models for effective seasonal forecasting.

328 Discussion

329 The XRO model constitutes a parsimonious representation of the climate system in a reduced
330 variable and parameter space that still captures the essential dynamics of interconnected global
331 climate variability. We emphasize that the improvement of ENSO predictability in the XRO
332 relative to that in the nRO ultimately all resides in the initial condition memory of the other climate
333 modes, which is propagated forward by the unbiased operator. Thus, to improve ENSO predictions,
334 climate models must correctly capture the recharge oscillator dynamics of ENSO and additionally,
335 three compounding aspects of other climate modes: (i) the initial conditions of each mode, (ii) the

336 seasonally modulated damping rate (i.e., the memory) of each mode, and (iii) the seasonally
337 modulated teleconnection to ENSO from each mode. Tracing biases from the SSTA budget at the
338 process level with the XRO framework can be used to inform climate model development.
339 Moreover, the explainable predictability of pantropical climate variability as encapsulated by the
340 XRO may be further enhanced by including multi-timescale interactions associated with the
341 Madden-Julian Oscillation and westerly wind bursts at higher frequencies. The XRO framework
342 can also provide a pathway for better understanding observed decadal and long-term changes in
343 ENSO variability^{33,34} and ENSO predictability^{47–50}.

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451

452 **Figure Legends**

453 **Figure 1. Different sources of ENSO predictability and associated different global impacts.**

454 **a**, Observed SSTA standard deviation pattern calculated from the detrended ORAS5 reanalysis
455 during 1979-2022. The different coloured boxes represent area-averaged SSTA index regions for
456 ENSO and other selected climate modes ([Supplementary Table 1](#)). **b**, Observed standardized
457 Niño3.4 index and various potential precursor indices for the 1997/98 and 2015/16 El Niño events,
458 with the numbers in the parentheses indicating the preceding (-1), current (0), and subsequent (1)
459 years. The error bars show the spread (one standard deviation) among different observational
460 products ([Supplementary Table 2](#)). The lead correlation of various indices with regard to the NDJ
461 Niño3.4 index is indicated near the bottom of the plot. **c-d**, Observed precipitation anomalies
462 (percentage) relative to climatology (shading) during (c) 1997/98 December-March (DJFM) and
463 (d) 2015/16 DJFM. Contours denote the significant positive (green) and negative (brown)
464 correlations between DJFM precipitation anomalies and the DJFM Niño3.4 SSTA index that
465 exceed the 95% confidence level, based on Student's *t*-test. [The observed 1997/98 and 2015/16 El](#)
466 [Niño events were associated with different precursor patterns and global climate impacts, despite](#)
467 [similar Niño3.4 index amplitude.](#)

468 **Figure 2. Superior Efficacy of the XRO in simulating and reforecasting ENSO. a-c,**

469 Seasonally varying standard deviation (a), skewness (b), and power spectrum (c), respectively, of
470 Niño3.4 using ORAS5 (*black*) and the XRO stochastic simulation (*red*). **d-l**, monthly cross-
471 correlations between Niño3.4 and different indices indicated in the titles; Dashed grey curves show
472 the auto-correlation of Niño3.4 and vertical blue dashed lines denote a lead-time of 6(WWV),
473 6(NPMM), 4(SPMM), 12(IOB), 14(IOD), 10(SIOD), 9(TNA), 6(ATL3), and 9(SASD) months
474 respectively; Abscissas indicate lead-time in months (negative values representing Niño3.4 lag).
475 Red shading indicates the 10%-90% ensemble spread of simulated 43-year segments, obtained
476 from splitting a 43,000-year XRO simulation into 1000 non-overlapping parts. **m**, All-months

477 correlation skill of 3-month running-mean Niño3.4 as a function of forecast lead for forecasts
 478 verified on 2002-2022 for the out-of-sample nRO (*magenta*) and XRO (*red*) fitted on 1950-1999,
 479 the AI model (*blue*), the XRO control fitted on 1979-2022 (*black*) and IRI operational models, the
 480 ensemble mean of dynamical models (*dark purple curve*), and ensemble-mean of statistical models
 481 (*dark cyan curve*). **n**, Same as **m**, but for Niño3.4 forecast skills for nRO (*magenta*) and XRO (*red*)
 482 control forecasts, AI model forecasts (*blue*), and NMME dynamical model forecasts (multi-model
 483 ensemble mean in *black*, ensemble-means from individual models in *other colours*). Validation
 484 period is 1979-2022 except for the AI and NMME models (period indicated in the legend). **o-p**,
 485 Correlation skill of nRO and XRO Niño3.4 forecasts as a function of initialization month (ordinate)
 486 and target month (abscissa; superscripts 0, 1, and 2 denote the current and subsequent years,
 487 respectively). Hatching highlights forecasts with a correlation <0.5 . Dashed vertical blue lines
 488 denote the spring predictability barrier. **The XRO accurately simulates the fundamental observed**
 489 **ENSO characteristics, its lead-lag relationships with other climate modes, and provides skilful**
 490 **forecasts at lead-times up to 16-18 months.**

491 **Figure 3. Quantifying the increased ENSO forecast skills from the coupled influences outside**
 492 **equatorial Pacific during 1979-2022. a**, the all-months correlation skill of the 3-month running
 493 mean Niño3.4 index as a function of the forecast lead month in the control experiment (XRO,
 494 *black line*), the uninitialized ExPO+IO+AO experiment ($U_{\text{ExPO+IO+AO}}$, removing initial conditions
 495 of other basins; *red line*), the decoupling ExPO+IO+AO experiment ($D_{\text{ExPO+IO+AO}}$, removing the
 496 coupling of ENSO with other basins; *blue line*), and the relaxing ExPO+IO+AO to observations
 497 experiment ($R_{\text{ExPO+IO+AO}}$, adding perfect “future” information of other basins in a hindcast case;
 498 *magenta line*). **b-d**, the skill difference of the Niño3.4 index as a function of initial time and target
 499 month between XRO and $D_{\text{ExPO+IO+AO}}$ (b), between XRO and $U_{\text{ExPO+IO+AO}}$ (c), and between
 500 $U_{\text{ExPO+IO+AO}}$ and $D_{\text{ExPO+IO+AO}}$ (d). **e-g**, Same as d, but for difference between control and the
 501 uninitialized ExPO, IO, and AO experiments, respectively. Hatching indicates that the correlation
 502 difference is significant at 90% confidence level using the two-tailed Fisher z-transformation test.
 503 **The sensitivity experiments demonstrate the importance of the extratropical Pacific, Indian Ocean,**
 504 **and Atlantic Ocean in enhancing ENSO forecast skill, with distinct seasonal dependence. The**
 505 **interbasin memory sustains ENSO forecast skill beyond the spring predictability barrier with the**
 506 **IO and AO contributing skill in boreal summer and the ExPO in boreal winter.**

507 **Figure 4. Delineating contributions to ENSO amplitudes from other climate modes. a, b, c,**
 508 Time series of Niño3.4 forecasts for the (a) XRO model, (b) decoupled ExPO+IO+AO experiment,

509 and (c) uninitialized ExPO+IO+AO experiment, as function of target time and forecast lead. **d-k**,
510 the difference of Niño3.4 SSTAs (shading) and WWV anomalies (contours with interval of 0.6 m,
511 positive in red and negative in black dashed, zero omitted), as a function of forecast start month
512 and target month, between the control and uninitialized climate mode experiments for NPMM,
513 IOB, IOD, SIOD, SPMM, TNA, ATL3, and SASD, respectively. Vertical reference dashed lines
514 denote December of El Niño (red) and La Niña (blue) years, respectively. In **d-k**, the normalized
515 observed time series of each climate-mode SSTA index is indicated on the bottom axis; the black
516 arrows indicate the flow of forecast integration started from the selected time in the bottom. **l**,
517 Composite difference of Nov-Dec-Jan Niño3.4 SSTA forecasts during El Niño events (red) and
518 La Niña events (blue) between control and uninitialized U_m experiments started from months in a
519 specific preceding season (-1 and 0 in parentheses denote preceding and current year, x axis from
520 left to right is $U_{Niño3.4}$, U_{WWV} , U_{NPMM} , U_{SPMM} , U_{IOB} , U_{IOD} , U_{SIOD} , U_{TNA} , U_{ATL3} , and U_{SASD} ,
521 respectively); the events are selected when Nov-Dec-Jan Niño3.4 indices are greater than their
522 standard deviation, which includes 7 El Niño events (1982, 1986, 1991, 1997, 2002, 2009, 2015)
523 and 5 La Niña events (1988, 1998, 1999, 2007, 2010). The error bars show one standard deviation
524 spread among the 7 El Niño/5 La Niña events. [The XRO sensitivity experiments quantify the
525 pathways via which the other climate modes influence El Niño and La Niña events.](#)

526 **Figure 5. Linking biases in the dynamics captured by the XRO to climate model deficiencies**
527 **in forecasting ENSO during 1979-2022.** (a) The all-months correlation skill of the 3-month
528 running mean Niño3.4 index in XRO^m trained solely on 91 individual CMIP model outputs (*grey*
529 *curves*), and in XRO trained on observations (*red*) and multi-model ensemble mean NMME
530 models (*black*). (b) The ensemble mean and 10%-90% spread band of the changes in correlation
531 skill of the Niño3.4 index, obtained by either correcting ENSO's internal linear dynamics
532 ($XRO_{L_{ENSO}}^m - XRO^m$, *red*), or correcting the remote climate mode feedbacks onto ENSO ($XRO_{C_1}^m -$
533 XRO^m , *magenta*), or correcting ENSO's teleconnections to the remote climate modes ($XRO_{C_2}^m -$
534 XRO^m , *blue*). [Reforecasts using the XRO trained on climate model output, show that reduced
535 biases in model ENSO dynamics and in climate mode interactions lead to more skilful ENSO
536 forecasts.](#)

537

538 **Methods**

539 ***Extended Nonlinear Recharge-Oscillator model (XRO)***

540 The XRO model consists of a nonlinear recharge oscillator model for ENSO^{51,52} coupled to
541 stochastic-deterministic models (i.e., seasonally modulated first order autoregressive models) for
542 the other climate modes^{53–55}:

$$543 \quad \frac{d}{dt} \begin{pmatrix} \mathbf{X}_{\text{ENSO}} \\ \mathbf{X}_M \end{pmatrix} = \mathbf{L} \begin{pmatrix} \mathbf{X}_{\text{ENSO}} \\ \mathbf{X}_M \end{pmatrix} + \begin{pmatrix} \mathbf{N}_{\text{ENSO}} \\ \mathbf{N}_M \end{pmatrix} + \sigma_{\xi} \xi, \quad (1)$$

$$544 \quad \frac{d\xi}{dt} = -r_{\xi} \xi + \mathbf{w}(t), \quad (2)$$

545 where $\mathbf{X}_{\text{ENSO}} = [T_{\text{ENSO}}, h]$ and $\mathbf{X}_M = [T_{\text{NPMM}}, T_{\text{SPMM}}, T_{\text{IOB}}, T_{\text{IOD}}, T_{\text{SIOD}}, T_{\text{TNA}}, T_{\text{ATL3}}, T_{\text{SASD}}]$ are
546 state vectors of ENSO and other climate modes, respectively. This model allows for two-way
547 interactions between ENSO and the other modes. Two indices are used to describe the oscillatory
548 behaviour of ENSO^{52,56}. They consist of SSTAs averaged over the Niño3.4 region 170°–120°W,
549 5°S–5°N (T_{ENSO}) and thermocline depth anomalies averaged over the equatorial Pacific 120°E–
550 80°W, 5°S–5°N (h), i.e., the WWV index (with a constant factor of the area it covers). For other
551 climate modes, we consider the SST indices of multiple climate modes ([Supplementary Table 1](#))
552 that have been shown to interact with ENSO, including the NPMM^{12,38,57} and SPMM¹³ in the
553 extratropical Pacific, the IOB^{14,58,59}, IOD^{60,61,15,43}, and SIOD¹⁶ in the Indian Ocean, and TNA^{17,62},
554 ATL3^{63,18,43,64} and SASD^{65,19} in the Atlantic Ocean. We recognise the possibility of enhancing
555 ENSO forecast skill by incorporating additional modes of variability, provided they directly
556 interact with ENSO, exhibit substantial memory extending beyond months, and offer additional
557 sources of variability beyond the chosen eight.

558 The dynamics governing the state matrix \mathbf{X} (consisting of 10 variables) contains linear (\mathbf{L}),
 559 nonlinear (\mathbf{N}), and stochastic ($\boldsymbol{\xi}$) terms. The linear dynamics contains four key submatrices,
 560 organized as follows:

$$561 \quad \mathbf{L} = \begin{pmatrix} \mathbf{L}_{\text{ENSO}} & \mathbf{C}_1 \\ \mathbf{C}_2 & \mathbf{L}_M \end{pmatrix}, \quad (3)$$

562 where the linear operator submatrix \mathbf{L}_{ENSO} describes the ENSO internal recharge-discharge
 563 dynamics^{52,66}, \mathbf{L}_M represent the internal processes and interactions among the other climate modes;
 564 \mathbf{C} are coupling submatrices, with \mathbf{C}_2 describing the impact of ENSO on other climate modes²⁹ and
 565 \mathbf{C}_1 describing the feedback of other modes on ENSO. To implement nonlinear dynamics
 566 associated with ENSO asymmetry, quadratic nonlinearities $b_1 T_{\text{ENSO}}^2 + b_2 T_{\text{ENSO}} h$ are incorporated
 567 into the SSTA equation of ENSO following Jin et al.⁵¹ and An et al.⁶⁷, specifically, $\mathbf{N}_{\text{ENSO}} =$
 568 $[b_1 T_{\text{ENSO}}^2 + b_2 T_{\text{ENSO}} h, 0]$. These nonlinearities can be related to deterministic nonlinear ocean
 569 advection^{68,67}, as well as to atmospheric nonlinearity implicitly through the nonlinear SST-wind
 570 stress feedback⁶⁹⁻⁷¹. A local quadratic nonlinearity $b_3 T_{\text{IOD}}^2$ is also incorporated in the SSTA
 571 equation for the IOD following the recent insights from An et al.⁷² that IOD asymmetry is
 572 dominated by local nonlinear processes. The nonlinear terms for modes other than the IOD are set
 573 to zero given their observed smaller asymmetry and skewness ([Supplementary Fig. 5i-j,m-p](#), ref⁷³),
 574 specifically, $\mathbf{N}_M = [0,0,0, b_3 T_{\text{IOD}}^2, 0,0,0,0]$. Lastly, $\boldsymbol{\xi}$ is stochastic forcing due to weather and other
 575 high-frequency noise such as the Madden-Julian Oscillation and westerly wind bursts, which is
 576 approximated as red noise with decorrelation time scales of r_ξ and amplitudes of σ_ξ , respectively.
 577 Specifically, $\mathbf{w}(t)$ in Eq. (2) denotes white noise with a Gaussian distribution $N(0, 2r_\xi)$ ensuring
 578 that the variance of $\boldsymbol{\xi}$ is maintained at the unit level. We acknowledge the importance of the
 579 multiplicative (state-dependent) noise forcing on ENSO^{74,75}, however, accurately estimating the
 580 magnitude of the state-dependence remains a challenge with the observational data length.

581 Due to the strong seasonal dependence of ENSO and other climate modes, we incorporate
 582 seasonality by estimating the operator matrix and nonlinear parameters as

$$583 \quad \mathbf{L} = \mathbf{L}_0 + \sum_{j=1}^2 (\mathbf{L}_j^c \cos j\omega t + \mathbf{L}_j^s \sin j\omega t), \quad (4)$$

$$584 \quad \mathbf{N} = \mathbf{N}_0 + \sum_{j=1}^2 (\mathbf{N}_j^c \cos j\omega t + \mathbf{N}_j^s \sin j\omega t), \quad (5)$$

585 where $\omega = 2\pi/(12 \text{ months})$, and the subscripts 0, 1 and 2 indicate the mean, annual cycle, and
 586 the semi-annual components, respectively. The linear operator and nonlinear coefficients for the
 587 observations and CMIP simulations are estimated simultaneously by using multivariate linear
 588 regression and expressing the state vector tendency in Eq. (1) through a forward-differencing
 589 scheme following ref^{76,77}. Compared to the conventional method, which estimates the annual cycle
 590 of operators by splitting the monthly data on each calendar month, our approach enables us to
 591 obtain the seasonal modulated operators without reducing sample size by a factor of 12. We
 592 emphasize that our approach constitutes the minimum number of degrees of freedom necessary to
 593 represent the seasonality. There are 50 parameters for each tendency equation of the 10 variables
 594 in the system (except 60 for T_{ENSO} and 55 for T_{IOD}). To meet the rule of thumb for regression
 595 sample size (at least 10 subjects per predictor)⁷⁸, 40–50 years of data is required to achieve a robust
 596 fit. The total number of parameters is 515, which are orders of magnitude fewer degrees of freedom
 597 than the AI models in comparison have, the latter which have substantially more than 100,000 free
 598 parameters⁸.

599 The noise parameters are determined from the residuals of the XRO fit. There are 20 total
 600 noise parameters, i.e., a noise amplitude and decorrelation time scale for each of the 10 variables
 601 in the system. The noise amplitude \square_{\square} is estimated from the standard deviations of the residuals

602 of the XRO fit. The decorrelation time scales are estimated as $r_{\xi} = -\ln(\mathbf{a}_1)/\delta t$, where \mathbf{a}_1 is the
 603 lag-1 autocorrelation of the residual of the XRO fit. The order of observed noise time scale r_{ξ}^{-1} is
 604 about 0.25 ~ 0.70 months.

605 The XRO builds on the legacies of the Hasselmann stochastic climate model capturing upper
 606 ocean memory in SST variability, and the recharge oscillator model for the oscillatory core
 607 dynamics of ENSO. As a multivariate dynamical system, comparing with previous linear inverse
 608 models^{79,28,27,80,35}, the XRO offers an enhanced capability in representing the dynamics of ENSO
 609 (including recharge/discharge dynamics) and climate mode interactions, encompassing their
 610 seasonality and nonlinearity, which are of crucial importance in improving ENSO forecast skill.
 611 Moreover, the state vectors for linear inverse models are typically derived from the leading
 612 principal components truncated within the Empirical Orthogonal Function space, which, however,
 613 may not always represent physical processes.

614 *Nonlinear RO model (nRO)*

615 To highlight the climate mode interactions, we compared the XRO model with a nRO, which
 616 is described as:

$$617 \quad \frac{d}{dt} \mathbf{X}_{\text{ENSO}} = \mathbf{L}_{\text{ENSO}} \mathbf{X}_{\text{ENSO}} + \mathbf{N}_{\text{ENSO}} + \sigma_{\xi_{\text{ENSO}}} \boldsymbol{\xi}_{\text{ENSO}}. \quad (5)$$

618 This model includes only processes internal to the tropical Pacific. The parameters for the nRO
 619 model are fitted separately.

620 *Observational data*

621 We use eight observational SST and 3-dimensional ocean temperature datasets to account the
622 uncertainties in estimating the SST in global oceans and subsurface state in the equatorial Pacific
623 ([Supplementary Table 2](#)). They include three observational SST reconstructions: HadISST (Hadley
624 Centre Sea Ice and Sea Surface Temperature dataset version 1.1)⁸¹, ERSST v5 (Extended
625 Reconstructed Sea Surface Temperature version 5)⁸² and COBE-SST 2 (Centennial in situ
626 Observation-Based Estimates of Sea Surface Temperature version 2)⁸³ for 1871-2023; and five
627 reanalysed SST and ocean temperature datasets: GECCO3 for 1950-2018 (the German
628 contribution to Estimating the Circulation and Climate of the Ocean version 3)⁸⁴, GODAS for
629 1980-2023 (Global Ocean Data Assimilation System)⁸⁵, ORAS5 for 1958-2023 (the ECMWF
630 Ocean Reanalysis System 5)⁸⁶, ORA20C for 1900-2009 (ensemble of 10-member ECMWF Ocean
631 Reanalysis of the 20th Century)⁸⁷, PEODAS for 1960-2014 (the Predictive Ocean Atmosphere
632 Model for Australia Ensemble Ocean Data Assimilation System)⁸⁸, and SODA224 for 1871-2010
633 (Simple Ocean Data Assimilation Phase 2.2.4)⁸⁹. The thermocline depth is defined as the depth of
634 the 20°C isotherm. We also use surface air temperature from the ERA5 reanalysis⁹⁰, and gridded
635 precipitation from the Climate Prediction Center Merged Analysis of Precipitation (CMAP)⁹¹ for
636 1979-2022. The monthly anomaly fields were calculated by removing the monthly climatology for
637 the period of 1979-2022 and the quadratic trend over the whole period. We have focused on the
638 satellite era from 1979 onwards because SST observations are sparse in the pre-satellite period.

639 *Climate forecast and hindcast data*

640 We use the 3-month averaged Niño3.4 index forecasts from the operational International
641 Research Institute for Climate and Society (IRI) ENSO Forecast product⁵. We also use SST
642 hindcasts and real-time forecasts from ten models participating in the North American Multi-

643 Model Ensemble (NMME) project⁹². The ensemble sizes range from 10 to 24 for each model
644 ([Supplementary Table 4](#)). The monthly forecast anomalies were calculated with respect to the
645 monthly climatology from January 1982 to December 2010 for each member and forecast lead.
646 For CCSM4 and CFSv2, we eliminate the discontinuous forecast biases by calculating the forecast
647 anomalies using two different climatological periods of 1982–98 and 1999–2010, respectively,
648 following ref⁴⁵.

649 In addition, we use the Niño3.4, Niño3, and Niño4 indices forecasts from an AI model (the
650 3D-Geoformer ENSO neural network model⁹) covering the period of 1983-2021. This model
651 demonstrated ENSO forecast skills comparable with the convolutional neural networks (CNN)
652 model developed by Ham et al.⁸, which is among the most skilful AI ENSO forecasts^{93,94}.

653 *Stochastically forced XRO simulations*

654 To assess the XRO’s performance in simulating ENSO and mode interactions, we conducted
655 stochastically forced simulations using the operators and stochastic forcing matrices estimated
656 from the ORAS5 reanalysis for 1979-2022 (*black curves* in [Extended Data Fig. 1](#)). We numerically
657 integrate Eqs. 1-2 with a time step of 0.01 month for 45,000 years and archive monthly-averaged
658 states for the analysis. The last 43,000 years were analysed and split into 1000 non-overlapping
659 epochs of 43-year each, aligning with the observational record length. An example of simulated
660 Niño3.4 SSTA index for the 10 consecutive centuries is shown in [Supplementary Fig. 3](#).

661 *Out-of-sample reforecasts*

662 To perform robust out-of-sample testing of the XRO performance, we next use observational
663 data including the pre-satellite period since at least 40-50 years of data are required to get a robust

664 XRO fit. We choose to discard data before 1950 since there are large uncertainties in the SSTA and
665 equatorial thermocline depth indices (Supplementary Fig. 15). Therefore, we fitted the XRO and
666 nRO models on 1950-1999 (50 years) data, conducted deterministic retrospective 21-month
667 forecasts by integrating the XRO (Eq. 1) and nRO (Eq. 5) initialized from observed state values
668 for the period of 2002-2022, and verified the model against observations in the 2002-2022 period,
669 To access the impact of the decadal change in the performance of the XRO in forecasting ENSO,
670 we also verified the model on two other 21-year no-overlapping periods: the previous period 1950-
671 1970 (in which period of 1973-2022 data was used for training) and the middle period 1972-1992
672 (in which the periods of 1950-1970 and 1994-2022 data was used for training). The multi-data-
673 products ensemble mean SSTA and WWV anomaly indices were used for fitting and verification.

674 *Control XRO and nRO reforecasts*

675 Using the operator and stochastic forcing parameters estimated from the ORAS5 reanalysis
676 for 1979-2022, we conducted a control experiment by integrating the XRO (Eq. 1) initialized from
677 observed state values of $[T_{\text{ENSO}}, h, T_{\text{NPMM}}, T_{\text{SPMM}}, T_{\text{IOB}}, T_{\text{IOD}}, T_{\text{SIOD}}, T_{\text{TNA}}, T_{\text{ATL3}}, T_{\text{SASD}}]$ with
678 retrospective 21-month forecasts for the period of January 1979–October 2023 (referred to XRO).
679 The ensemble mean forecast of 100-members is almost identical to the deterministic forecast in
680 which the stochastic forcing terms are neglected during the integration (Supplementary Fig. 16a,b).
681 Although the 100-member stochastic XRO forecasts provide an opportunity for probabilistic
682 ENSO forecasts (Supplementary Fig. 16c-f), here we focus on the deterministic skill and neglect
683 the stochastic forcing terms in all the remaining forecast experiments. Similarly, we conducted a
684 nRO deterministic experiment by integrating Eq. (5) initialized from observed state values of
685 $[T_{\text{ENSO}}, h]$.

686 ***Cross-validated reforecasts.***

687 We carried out cross-validated forecasts using both the XRO and nRO models from the
688 ORAS5 reanalysis for 1979-2022, employing a jackknife subsampling approach. We sequentially
689 excluded 3-year segments of data (1979-81, 1982-85, 1986-89, 1990-93, 1994-97, 1998-2001,
690 2002-05, 2006-09, 2010-13, 2014-17, 2018-21, and 2022), then trained the model operator
691 parameters based on the remaining data. Subsequently, we generated forecasts for each month
692 during the years not included in the model fitting. The uncertainty in the fitted parameters is
693 illustrated as *black shading* in [Extended Data Fig. 1](#). The skill of cross-validated forecast is not
694 sensitive to the choice of excluding from 2 to 7 years ([Supplementary Fig. 8a](#)).

695 ***Large ensemble simulations and perfect model reforecasting experiments***

696 To assess of the robustness of the XRO fitting and forecasting performance, we use large
697 ensemble (LENS) historical simulations for four climate models: Community Earth System Model
698 version 1 (CESM1)⁹⁵, version 2 (CESM2)⁹⁶, Model for Interdisciplinary Research on Climate
699 version 6 (MIROC6)⁹⁷, and Max Planck Institute for Meteorology Earth System Model version
700 1.1 (MPI-ESM)⁹⁸. Each LENS was generated by repeatedly running the same model simulation
701 with identical external forcing but with small initial condition differences. The number of members
702 for each LENS used in this study are as follows: 39 for CESM1, 100 for CESM2, 50 for MIROC6,
703 and 99 for MPI-ESM. We use the historical period of 1959-2002, aligning it with the observational
704 record length (43 years).

705 We performed the “perfect model” reforecast, where the XRO model was trained by the
706 LENS output and tasked to reforecast itself instead of the observations. We carried out twin
707 experiments for each LENS ([Supplementary Fig. 8b-e](#)). The “Same-Member” reforecast

708 experiment, in which the XRO model is repeatedly fitted for a member, forecasted, and verified
709 against the same member. This aligns with the XRO control experiment for the observations. In
710 the “Cross-Member” reforecast experiment, the XRO model is fitted for a specific member but
711 forecasted and verified against a different member (an independent realization in the LENS).
712 Specifically, we forecast ensemble member j using the two versions of XRO models, which were
713 fitted on member $j-1$ and $j-2$ data, respectively, and repeat the process for all members within the
714 LENS. The skill difference between the Cross-Member experiment and the Same-Member
715 experiment isolates the uncertainty of XRO parameter fitting and its impact on reforecasting skill.
716 All four LENS results using the same observational record length (43-year) confirm that the
717 uncertainty in parameter estimation leads to XRO reforecasting correlation skill error of less than
718 0.1 within 21 lead months (Supplementary Fig. 8b-e).

719 *Quantitative reforecasting experiments*

720 To rigorously dissect the interplay between ENSO and the different climate modes in the
721 different ocean basins, we designed three sets of sensitivity experiments to mimic the experiment
722 protocol of previous CGCM studies:

723 **a) Uninitialized experiments:** We performed uninitialized mode- \square experiments (U_j) by setting
724 the initial condition of \square_{\square} to zero, while keeping everything else the same as in the control
725 experiment. The effect of the mode- \square initial condition can be assessed as the difference between
726 the control and U_j (XRO- U_j). To disentangle the role of a specific ocean basin’s initial conditions,
727 we also conducted uninitialized experiments by setting the initial conditions of all modes to zero
728 in the corresponding ocean basins. For example, the uninitialized extratropical Pacific Ocean
729 experiment (referred to as U_{ExPO}) is the same as the control experiment but with the initial
730 conditions of the NPM and SPM set to zero. Similarly, U_{IO} , U_{AO} and $U_{\text{ExPO+IO+AO}}$ denote the

731 uninitialized Indian Ocean, uninitialized Atlantic Ocean, and uninitialized “all other basins”
732 experiments, respectively. In addition, the uninitialized ENSO SSTA (U_{Nino34}) and WWV
733 anomaly (U_{WWV}) experiments are same as XRO, except that the initial conditions of T_{ENSO} and h
734 are set to zero, respectively. The uninitialized ENSO (U_{ENSO}) experiment is same as XRO, but the
735 initial conditions of both T_{ENSO} and h are set to zero. The difference in the climate system response
736 between the control experiment and U_j isolates the effect of mode- j /basin- j 's initialization.

737 ***b) Decoupled experiments:*** We performed decoupled mode- j experiments (referred to D_j) – in
738 which specific mode(s) are suppressed – by strongly increasing the diagonal damping rate of
739 mode- j in the L operator to an e -folding time scale of 5 days. This mimics the partially coupled
740 experiments in fully coupled climate models that restore the ocean surface temperature toward
741 prescribed conditions. The differences between the control experiment and D_j isolate the role of
742 mode- j in the system. To disentangle the role of the different ocean basins, we conducted
743 decoupled ocean basin experiments. For example, the decoupled extratropical Pacific Ocean
744 experiment (referred to D_{EXPO}) removes both the NPMM and SPMM from the system. Similarly,
745 the decoupled Indian Ocean experiment (D_{IO}) removes the IOB, IOD and SIOD together from the
746 system; the decoupled Atlantic Ocean experiment (D_{AO}) removes the TNA, ALT3, and SASD
747 together from the system; and the decoupled all other modes experiment ($D_{\text{EXPO+IO+AO}}$) removes
748 all other modes except ENSO. We note that the $D_{\text{EXPO+IO+AO}}$ experiment is very close to the nRO
749 in which the parameters were fitted separately. The difference between the control experiment and
750 D_j isolates the effect of mode- j /basin- j 's coupling. The sum of individual basin decoupled
751 experiments exceeds the effect of decoupling all at once ([Extended Data Fig. 3b,d,e](#)), suggesting
752 the presence of indirect pathways due to interactions among basins.

753 **c) Relaxation towards observations experiments:** We performed relaxation ocean basin- j
754 experiments (referred to R_j) by relaxing the SSTA indices towards the observations in the
755 corresponding ocean basins with a time scale of 5 days. For example, the relaxation extratropical
756 Pacific Ocean experiment (referred to as R_{ExPO}) is the same as the control but with the NPMM
757 and SPMM being relaxed to the observations. Similarly, R_{IO} , R_{AO} , and $R_{\text{ExPO+IO+AO}}$ denote the
758 relaxation Indian Ocean, relaxation Atlantic Ocean, and relaxation all other basins except the
759 equatorial Pacific experiments. The difference between the control experiment and R_j highlights
760 the effect from perfect “future” knowledge of basin- j . The relaxation towards observations
761 experiments greatly overestimate ENSO forecast skill because of built in presumed perfect
762 predictions for the stochastic excitations and ENSO’s impacts on the modes in these basins
763 (*magenta curves* in [Extended Data Fig. 3d,e](#)).

764 ***Losing memory experiments***

765 We carried out “losing memory” experiments by artificially adding additional damping to the
766 original diagonal damping rates of all other non-ENSO modes in the \square_{\square} operator ([Extended Data](#)
767 [Fig. 4](#)). The prescribed damping rates are $(5 \text{ day})^{-1}$, $(30 \text{ day})^{-1}$, $(90 \text{ day})^{-1}$, $(180 \text{ day})^{-1}$, and $(360$
768 $\text{day})^{-1}$, in the different experiments, ranging from strong damping (no memory) to less damping
769 (long memory).

770 ***Deseasonalizing experiments.***

771 We carried out deseasonalizing experiments to illustrate the role of the operator parameters’
772 annual and semi-annual cycles in ENSO forecast skill ([Supplementary Fig. 17](#)). In the $\text{XRO}_{\text{ac}=0}$
773 model, we considered only the annual mean component (\mathbf{L}_0 and \mathbf{N}_0 in Eqs. 3-4, each tendency

774 equation has ~ 10 parameters, a total number of parameters of $103 = 10 \times 10 + 3$. 10–15 years
775 of data is required to meet the rule of thumb for regression sample size (at least 10 subjects per
776 predictor) ⁷⁸. In the $XRO_{ac=1}$ model, we considered both the annual mean and annual cycle
777 components in the operator ($L_0, L_1^c, L_1^s, N_0, N_1^c$ and N_1^s in Eqs. 3-4, each tendency equation has
778 ~ 30 parameters, the total number of parameters is $309 = 3 \times 100 + 3 \times 3$). At least 25 years of
779 data is required ⁷⁸. The difference between XRO and $XRO_{ac=0}$ isolates the combined impacts of
780 the annual and semi-annual cycles in the operator parameters, whereas the difference between
781 XRO and $XRO_{ac=1}$ isolates the impact of just the semi-annual cycle in the operator parameters. The
782 parameters for the $XRO_{ac=0}$, and $XRO_{ac=1}$ experiments can be either refitted separately
783 (Supplementary Fig. 17a-d) or taken from the XRO control experiment (Supplementary Fig. 17e-
784 h). Regardless which parameter estimation method is used, we find that the seasonal cycle is
785 critically important in suppressing SPB for ENSO, while the semi-annual cycle is less important.

786 *Removing nonlinearity experiments*

787 We carried out “removing nonlinearity” experiments to illustrate the role of the XRO
788 nonlinear operators in ENSO forecast skill (Supplementary Fig. 18). In the XRO_{linear} experiment,
789 we consider only linear operators and set N_{ENSO} and N_M to zero. In the $XRO_{linearENSO}$ experiment,
790 we only consider linear operators and N_M , but set N_{ENSO} to zero. In the $XRO_{linearIOD}$ experiment,
791 we only consider linear operators and N_{ENSO} , but set N_M to zero. The difference between XRO
792 and XRO_{linear} isolates the impact of the nonlinear operator parameters, whereas the difference
793 between XRO and $XRO_{linearENSO}$ isolates the impact of the ENSO nonlinear operator parameters.
794 The parameters for the XRO_{linear} , the $XRO_{linearENSO}$, and $XRO_{linearIOD}$ experiments can be either
795 refitted separately (Supplementary Fig. 18a-d) or taken from the XRO control experiment
796 (Supplementary Fig. 18e-h). Regardless which of method we use to obtain the parameters, we find

797 that the ENSO nonlinear dynamics are critically important for ENSO forecast skill, especially for
 798 forecasting the amplitude of the peak phase and the fast transition from El Niño to La Niña. Further,
 799 we find that the impact of IOD's nonlinearity on ENSO forecast skill is neglectable.

800 ***Prediction skill metrics and significance tests***

801 The forecast skill is quantified using the anomaly correlation coefficient (ACC) and root mean
 802 square error (RMSE) metrics⁹⁹. The ACC is computed as the Pearson correlation coefficient
 803 between the deterministic forecast (f) and the observations (o):

$$804 \quad ACC = \frac{cov(f, o)}{\sigma_f \cdot \sigma_o}, \quad (6)$$

805 and the RMSE is defined as

$$806 \quad RMSE = \sqrt{(f - o)^2}, \quad (7)$$

807 where σ_f and σ_o are the standard deviations of the observations and forecast, respectively.

808 The Fisher z-transformation was used to test statistical significance of the ACC differences
 809 as follows:

$$810 \quad Z = 0.5 \frac{\ln\left(\frac{1+r_1}{1-r_1}\right) - \ln\left(\frac{1+r_2}{1-r_2}\right)}{\sqrt{\frac{1}{n_1-3} + \frac{1}{n_2-3}}}, \quad (8)$$

811 where r_1 and r_2 are the correlation coefficients, n_1 and n_2 are the sample sizes of the first and
 812 second group samples. The absolute value $|Z|$ is then compared against a critical value from the t -
 813 distribution for a two-tailed test. We rejected the null hypothesis that the two correlations are not
 814 significantly different at 90% confidence level if $|Z|$ exceeds the critical value.

815 ***The XRO reforecasting experiments based on CMIP model output***

816 We analyse monthly mean SST and 3-dimensional ocean temperature fields from 91 CMIP5
817 and CMIP6 historical simulations (Supplementary Table 5). All model outputs were re-gridded to
818 a common $1^\circ \times 1^\circ$ horizontal resolution using bilinear interpolation. The monthly anomaly fields
819 were calculated by removing the monthly climatology for the period of 1900-1999 and the
820 quadratically detrended over the full 100-year period.

821 Using the linear and nonlinear operators trained solely on CMIP model m output for 1900-
822 1999, we conducted retrospective 21 months forecasts with initial conditions from the observations
823 for the period of January 1982– October 2023 (referred to XRO^m). To understand the impacts of
824 model biases on ENSO dynamics and its coupling with other modes, we also conducted sensitivity
825 experiments by correcting the different components of the linear and nonlinear operators with the
826 observed parameters (See Extended Data Table 2). For example, the experiment XRO_L^m is the same
827 as XRO^m , but with the linear operator L being replaced by the observed L operator. The difference
828 $XRO_L^m - XRO^m$ is used to isolate the effect of correcting model m 's linear dynamics biases.
829 Similarly, the experiments $XRO_{L_{\text{ENSO}}}^m$, $XRO_{C_1}^m$, and $XRO_{C_2}^m$ were conducted to isolate the impacts
830 of model m 's biases on the internal linear ENSO dynamics, the coupling feedback to ENSO
831 parameters, and ENSO teleconnection dynamics, respectively.

832 ***The XRO2 ENSO types and pantropical SSTA forecasts***

833 The additional XRO model (referred to XRO2) was set up to predict different types of El
834 Niño (i.e., ENSO diversity). We introduced two SSTA indices in the state vectors of ENSO, i.e.,
835 Niño3 index (SSTAs averaged over $150^\circ\text{--}90^\circ\text{W}$, $5^\circ\text{S--}5^\circ\text{N}$) and Niño4 index (SSTAs averaged over
836 $160^\circ\text{E--}150^\circ\text{W}$, $5^\circ\text{S--}5^\circ\text{N}$): $\mathbf{X}_{\text{ENSO}} = [T_{\text{Niño3}}, T_{\text{Niño4}}, h]$ instead of using Niño3.4. The quadratic

837 nonlinearities $b_1 T_{\text{Niño3}}^2 + b_2 T_{\text{Niño3}} h$ are only incorporated into the SSTA equation of $T_{\text{Niño3}}$, in
838 presence of the strong asymmetry of Niño3 index whereas the less pronounced asymmetry of
839 Niño4 index: $N_{\text{ENSO}} = [b_1 T_{\text{Niño3}}^2 + b_2 T_{\text{Niño3}} h, 0, 0]$. All other terms are the same as the standard
840 XRO model. Using the operator parameters estimated from the ORAS5 reanalysis for 1979-2022,
841 we conducted similar retrospective 21-month forecasts for the period of January 1979–October
842 2023. The hindcast skills of Niño3 and Niño4 indices are better than those from the NMME
843 dynamical models and comparable to the AI model. The forecasts of Niño3 and Niño4 indices
844 were used to define the El Niño types in terms of the EP-type, CP-type, and mixed-type, following
845 ^{100,8}. The unified complex ENSO index (UCEI) is defined as

$$846 \quad UCEI = (N_3 + N_4) + (N_3 - N_4)i = r e^{\theta i}, \quad (9)$$

847 where

$$848 \quad r = \sqrt{(N_3 + N_4)^2 + (N_3 - N_4)^2}, \quad (10)$$

849 and

$$850 \quad \theta = \begin{cases} \arctan \frac{N_3 - N_4}{N_3 + N_4} & \text{when } N_3 + N_4 > 0 \\ \arctan \frac{N_3 - N_4}{N_3 + N_4} - \pi & \text{when } N_3 + N_4 < 0 \end{cases} \quad (11)$$

851 where N_3 and N_4 denote the Niño3 and Niño4 indices, respectively; The El Niño type is
852 determined from θ as follows:

$$853 \quad \left\{ \begin{array}{ll} 15^\circ \leq \theta < 90^\circ & EP \text{ El Nino} \\ -15^\circ \leq \theta < 15^\circ & Mixed \text{ El Nino} \\ -90^\circ \leq \theta < -15^\circ & CP \text{ El Nino} \end{array} \right\}. \quad (12)$$

854 We also conducted out-of-sample XRO2 ENSO type reforecasts by fitting on 1950-1990 with the
855 multi-products ensemble mean indices and verifying on 1991-2022 ([Supplementary Table 3](#)).

856 With the forecasted ten SSTA indices, the pantropical SSTA (30°S-30°N) at each grid point
857 (SSTA_j) can be predicted using the seasonal regression model:

$$858 \quad \text{SSTA}_j = c_0 \mathbf{X} + A_c \mathbf{X} \cos \omega t + A_s \mathbf{X} \sin \omega t + B_c \mathbf{X} \cos 2\omega t + B_s \mathbf{X} \sin 2\omega t, \quad (13)$$

859 where c_0 , A_c , A_s , B_c , and B_s have ten coefficients associated with each SSTA index, respectively.
860 We also conducted the cross-validated XRO2 forecasts and pantropical SSTA forecast by
861 excluding 3-year data out and trained XRO2 operators and SSTA regression coefficients, then
862 forecasts for each month during the years not included in the model fitting.

863 Further details are provided in the Supplementary Information, relying on references¹⁰¹⁻¹¹³.

864 **Data availability**

865 Datasets used in this paper are freely available. Observational data: links in Supplementary Table
866 2. NMME: <https://iridl.ldeo.columbia.edu/SOURCES/.Models/.NMME/>; 3D-Geoformer ENSO
867 AI model forecast: [http://msdc.qdio.ac.cn/data/metadata-special-](http://msdc.qdio.ac.cn/data/metadata-special-detail?id=1602252663859298305)
868 [detail?id=1602252663859298305](http://msdc.qdio.ac.cn/data/metadata-special-detail?id=1602252663859298305); CESM1 LENS: [https://www.cesm.ucar.edu/community-](https://www.cesm.ucar.edu/community-projects/lens/data-sets)
869 [projects/lens/data-sets](https://www.cesm.ucar.edu/community-projects/lens/data-sets); CESM2 LENS: [https://www.cesm.ucar.edu/community-](https://www.cesm.ucar.edu/community-projects/lens2/data-sets)
870 [projects/lens2/data-sets](https://www.cesm.ucar.edu/community-projects/lens2/data-sets); MPI-ESM LENS: <https://esgf-data.dkrz.de/projects/mpi-ge/>; CMIP5
871 outputs: <https://esgf-node.llnl.gov/projects/cmip5/>; and MIROC6 LENS and CMIP6 outputs:
872 <https://esgf-node.llnl.gov/projects/cmip6/>. All the map figures (Fig. 1a,c,d, and Supplementary
873 Figs. 1, 2, 14) were generated using python Cartopy version 0.22.0
874 (<https://zenodo.org/records/8216315>). The source data for figures in the main text is available at
875 <https://doi.org/10.5281/zenodo.10951443>.

876 **Code availability**

877 The XRO model code is deposited at <https://doi.org/10.5281/zenodo.10681114>. The code to
878 calculate the predictive skill is available at <https://github.com/pangeo-data/climpred>.

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1033 contribution 5579.

1034 **Author contributions**

1035 FFJ, SZ, and MFS conceptualized the research. SZ designed the model and experiments, conducted
1036 the analysis, produced the figures, and wrote the initial manuscript, in discussion with FFJ. FFJ,
1037 WC, MFS, and SZ structured the paper. ATW, MFS, and SZ designed the LENS perfect model
1038 experiments. MAC coined the acronym “XRO”. All authors contributed to interpreting the results
1039 and improving the paper.

1040 **Competing interests**

1041 The authors declare no competing interests.

1042 **Additional information**

1043 Supplementary information: The online version contains supplementary material available at X

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1045

1046 **Extended Data Legends**

1047 **Extended Data Fig. 1| Seasonally-modulated strength of mode interactions in observations**
1048 **and CMIP5/6 models, as diagnosed from the linear part of the XRO model.** (a) ENSO
1049 recharge-oscillator coefficients, (b) Coupling processes denoted by the contribution of other modes
1050 to the tendencies of ENSO SSTA and WWV anomalies, (c) ENSO-forced processes denoted by
1051 the contribution of ENSO SSTA and WWV anomalies to the SSTA tendency of other modes, (d)
1052 Interactions among NPMM, SPMM, IOB, IOD, SIOD, TNA, ATL3, and SASD. The coefficient
1053 L_{ij} has been normalized by a factor of σ_j/σ_i , where σ_i and σ_j are the monthly standard deviations
1054 of the indices in row i and column j , respectively, so that all coefficients are comparable, and the

1055 units are year⁻¹. The diagonal panels (*blue frames*) show the damping rate for each index. The
 1056 black curves with shading show the XRO fit to the ORAS5 reanalysis (with 10%-90% spread band
 1057 from the cross-validated fitting excluding 3-year data, see “*Cross-validated reforecasts*” in
 1058 *Methods*), and the red curves with shading show the ensemble mean with 10%-90% spread band
 1059 of the 91 CMIP5/6 historical simulations. ENSO can be strongly driven by climate modes in
 1060 extratropical Pacific, Indian Ocean, and Atlantic Ocean, which in some seasons are as important
 1061 as the dynamics internal to the equatorial Pacific. Most of the non-ENSO modes are more strongly
 1062 driven by ENSO (and their own damping) than by any of the other non-ENSO modes in other
 1063 basins. The climate models underestimate the strength of most of the mode interactions and miss
 1064 the seasonality.

1065 **Extended Data Fig. 2| Decadal change in the ENSO forecast correlation skill. a**, The all-
 1066 months correlation skill of the 3-month running mean Niño3.4 index verified on 1950-1970 for
 1067 the out-of-sample XRO fitted on 1973-2022 (*red curve*), out-of-sample nRO fitted on 1973-2022
 1068 (*magenta curve*), in-sample XRO fitted on 1950-1970 (*black dashed curve*) and in-sample XRO
 1069 fitted on the full-period 1950-2022 (*blue dashed curve*). The bottom inset shows the time series of
 1070 Niño3.4 index for out-of-sample training (*blue*) and verifying (*orange*) periods, respectively. **b-c**,
 1071 same as **a**, but verifying on 1972-1992 and 2002-2022, respectively. *The XRO is superior to the*
 1072 *nRO regardless the verifying periods and decadal changes of ENSO forecast skill.*

1073 **Extended Data Fig. 3| Test of additivity (i.e., linearity) of the sensitivity experiments. a**,
 1074 Regression slope and linear correlation coefficients for the Niño3.4 SSTA forecasts between the
 1075 effects of the uninitialized ExPO+IO+AO experiment ($XRO - U_{ExPO+IO+AO}$) and the sum of the
 1076 effects of the individual uninitialized ExPO, IO, and AO experiments ($3 * XRO - U_{ExPO} - U_{IO} -$
 1077 U_{AO}). **b** and **c**, same as **a**, but for decoupling experiments ($XRO - D_{ExPO+IO+AO}$ vs. $3 * XRO -$
 1078 $D_{ExPO} - D_{IO} - D_{AO}$) and relaxing towards observation experiments ($XRO - R_{ExPO+IO+AO}$ vs. $3 *$
 1079 $XRO - R_{ExPO} - R_{IO} - R_{AO}$), respectively. **d, e** the all-months correlation skill (**d**) and RMSE (**e**)
 1080 of the 3-month running mean Niño3.4 index, as a function of the forecast lead month in the control
 1081 experiment (*black line*) and sensitivity experiments: the uninitialized ExPO+IO+AO experiment
 1082 (*solid red line*) and sum of uninitialized ExPO, IO, and AO individually (*dashed red line*), the
 1083 decoupling ExPO+IO+AO experiment (*solid blue line*) and sum of decoupling ExPO, IO, and AO
 1084 individually (*dashed blue line*), and the relaxing ExPO+IO+AO to observation experiment (*solid*
 1085 *magenta line*) and sum of relaxing ExPO, IO, and AO to observation individually (*dashed magenta*
 1086 *line*). *The individual basin uninitialized experiments are additive with the slopes and correlations*

1087 at all lead months being very close to 1. But the individual basin decoupling experiments and the
1088 individual relaxation towards observations experiments are not additive, owing to a nonlinear
1089 dependence on the operator parameters. The sum of the effects of decoupling ExPO, IO, and AO
1090 individually is much larger than the effect of decoupling ExPO+IO+AO, suggesting that the
1091 decoupling experiment framework overestimates the contribution of each basin, given the presence
1092 of indirect pathways due to interactions among basins.

1093 **Extended Data Fig. 4| Influence of the memory effect outside the equatorial Pacific on ENSO**
1094 **forecast skill.** Shown are the all-months correlation skill (a) and RMSE (b) of the 3-month running
1095 mean Niño3.4 index, as a function of the forecast lead month in the XRO forecast (*black*), the nRO
1096 forecast (*grey triangle*), and the “Losing memory” sensitivity experiments (*colour curves*) by
1097 adding different damping rates (ranging from a strong damping rate of $-(5 \text{ day})^{-1}$ implying no
1098 memory to a weak damping rate of $-(360 \text{ day})^{-1}$ implying longer memory) to the non-ENSO modes
1099 (See “*Losing memory experiments*” in *Methods*). The initial condition memory effect of the
1100 climate modes outside equatorial Pacific extends the skill of ENSO forecasts.

1101 **Extended Data Fig. 5| Contribution of each climate mode’s initialization to ENSO correlation**
1102 **skill.** Shown is the forecast skill difference of the Niño3.4 SSTA index, as a function of initial time
1103 and target month, between the control and uninitialized climate mode sensitivity experiments for
1104 the NPMM, SPMM, IOB, IOD, SIOD, TNA, ATL3, and SASD, respectively. The contributions
1105 of the IOD, NPMM, and TNA dominate the ENSO forecast skill improvement.

1106 **Extended Data Fig. 6| Impacts of climate-mode initialization to ENSO forecasts.** Shown is the
1107 difference of Niño3.4 SSTA (shading) and WWV anomalies (contours with interval of 0.6 m,
1108 positive in red and negative in black dashed, zero omitted), as a function of forecast lead and target
1109 time, between control and uninitialized climate mode experiments for NPMM, SPMM, IOB, IOD,
1110 SIOD, TNA, ATL3, and SASD, respectively. Vertical reference dashed lines denote December of
1111 El Niño (red) and La Niña (blue) years, respectively. The normalized time series of each climate
1112 mode SSTA index is indicated in the bottom axis; the black arrows indicate the flow of forecast
1113 integration started from the selected time in the bottom. The XRO sensitivity experiments quantify
1114 how the initial states of key climate modes affect subsequent ENSO events.

1115 **Extended Data Fig. 7| Impacts on ENSO forecast skill of correcting biases in the XRO**
1116 **parameters fitted to individual CMIP simulations.** Shown is the difference of the all-months
1117 correlation skill for the Niño3.4 SSTA index, between the corrected-parameter forecast experiment

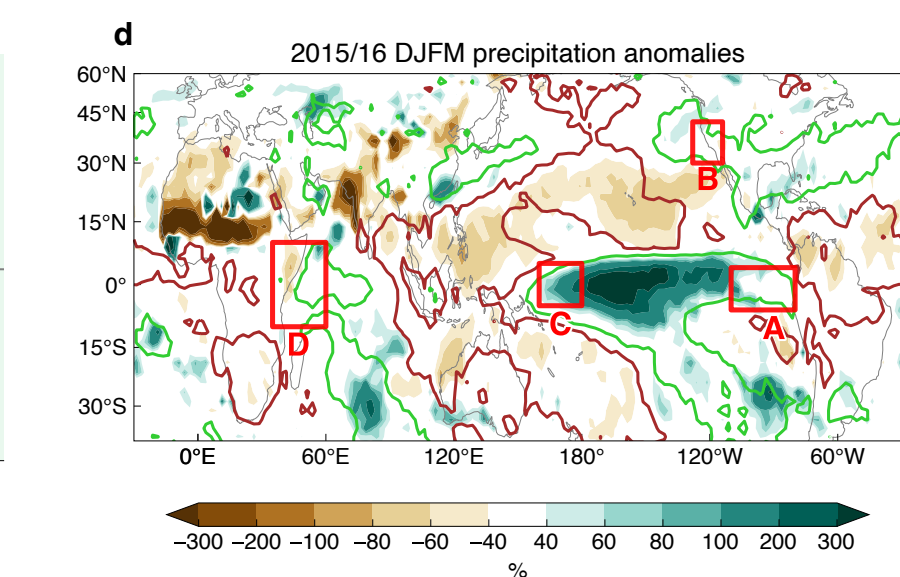
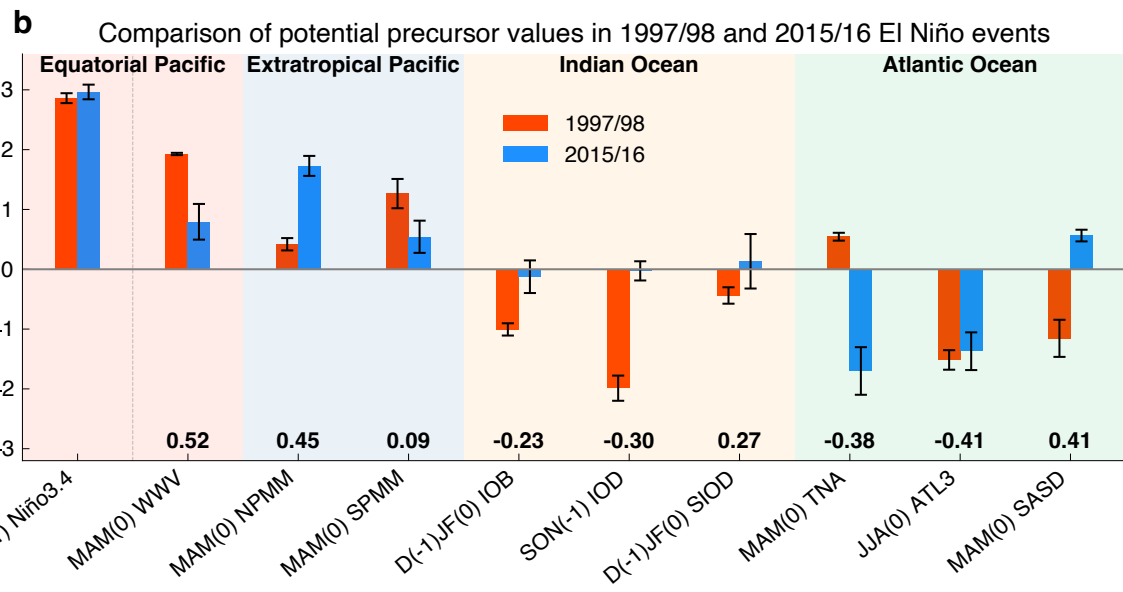
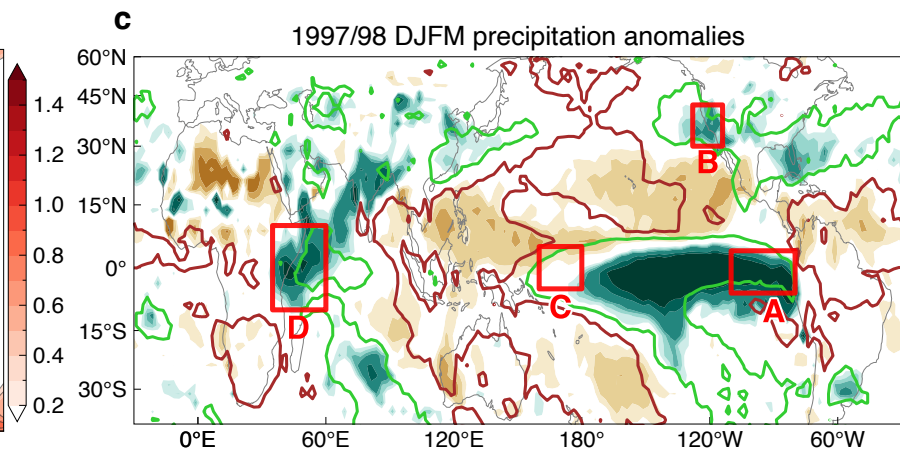
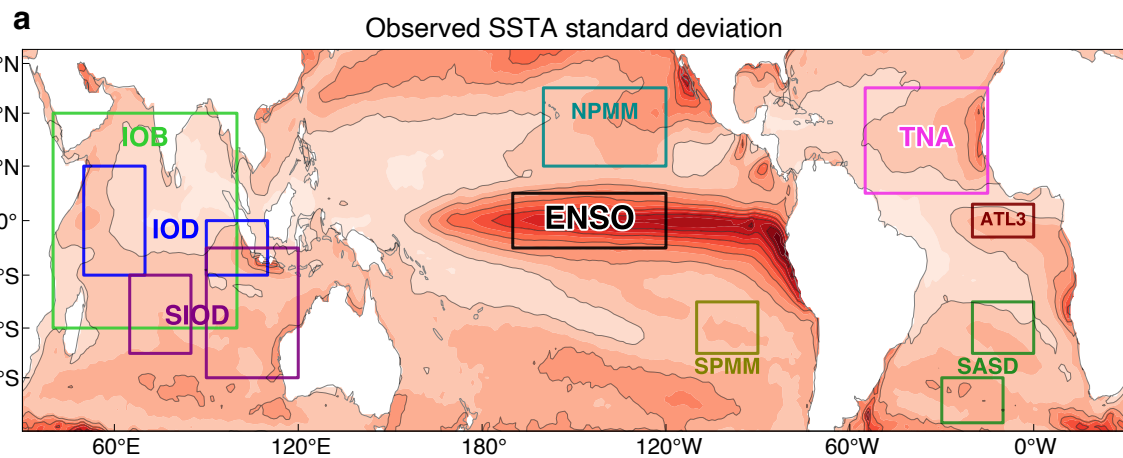
1118 and the XRO^m experiment trained solely on CMIP model outputs. (a) Effect of correcting linear
1119 operators (XRO_L^m- XRO^m), (b) effect of correcting ENSO internal linear dynamics (XRO_{L_{ENSO}}^m -
1120 XRO^m), (c) effect of correcting remote climate mode feedbacks onto ENSO (XRO_{C₁}^m - XRO^m), and
1121 (d) effect of correcting ENSO teleconnections to remote climate modes (XRO_{C₂}^m - XRO^m). The
1122 model is sorted by the averaged correlation skill of the XRO^m forecast at 6-15 lead months.
1123 Reforecasts using the XRO trained on global climate model output show that correcting CGCMs'
1124 dynamical biases in ENSO and climate mode interactions lead to more skilful ENSO forecasts.
1125 Most important is correcting ENSO biases (which improves skill at longest lead-times), followed
1126 by correcting the remote climate mode impact on ENSO (which improves skill at intermediate
1127 leads). Less skill is gained by improving ENSO's teleconnection to the remote modes.

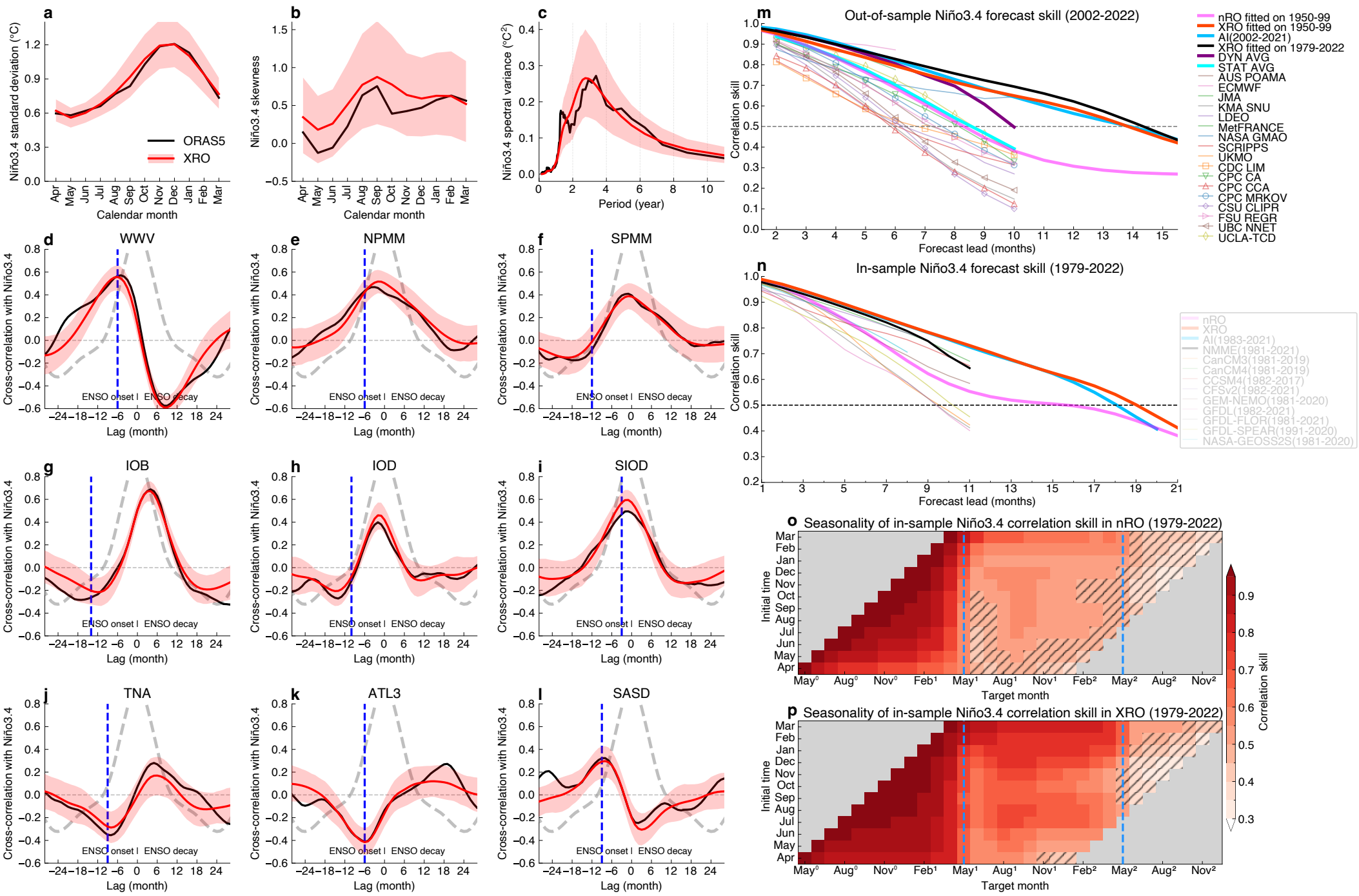
1128 **Extended Data Fig. 8| Correlation forecast skill for the Indian Ocean Dipole, using the XRO**
1129 **trained with climate model outputs.** (a) The correlation skill of the IOD index in Sep-Oct-Nov
1130 (SON) as a function of forecast lead, in the XRO^m trained solely on 91 individual CMIP model
1131 outputs (grey curves), the XRO trained on observations (red curve), and the original (not XRO)
1132 multi-model mean of the ensemble means of the forecasts from the NMME models (black). (b) the
1133 ensemble mean and 10%-90% spread band of the changes in correlation skill for the IOD index,
1134 obtained by correcting the ENSO internal linear dynamics (XRO_{L_{ENSO}}^m - XRO^m, *red*), or the remote-
1135 mode feedbacks onto ENSO (XRO_{C₁}^m - XRO^m, *magenta*), or the ENSO teleconnections to remote
1136 modes (XRO_{C₂}^m - XRO^m, *blue*). Reforecasts using the XRO trained on climate model output show
1137 that reducing CGCM biases in the dynamics of ENSO's climate mode interactions improves IOD
1138 forecasts.

1139 **Extended Data Table 1|** Details of the XRO forecasting experiments based on observations
1140 (1979-2022).

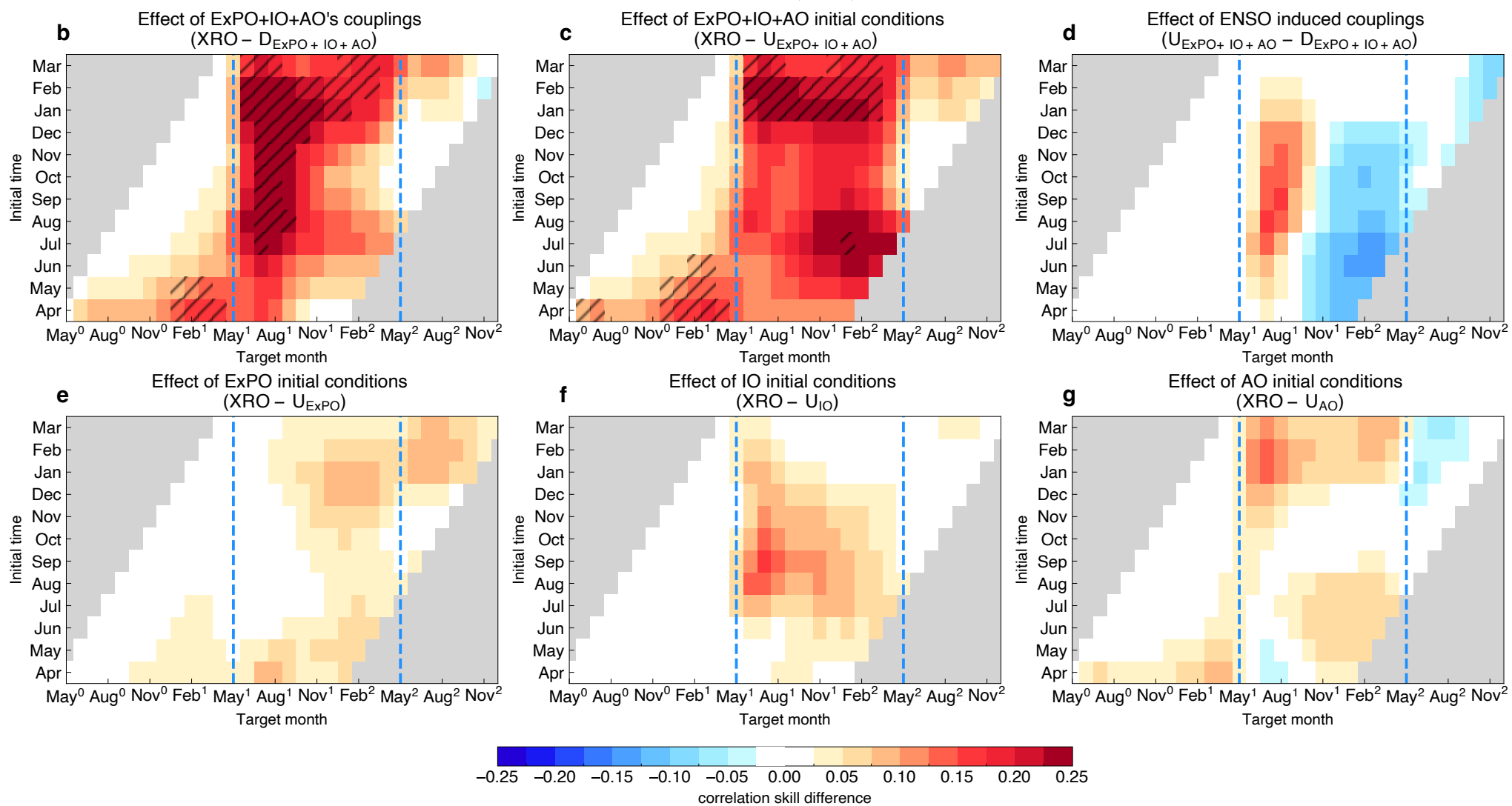
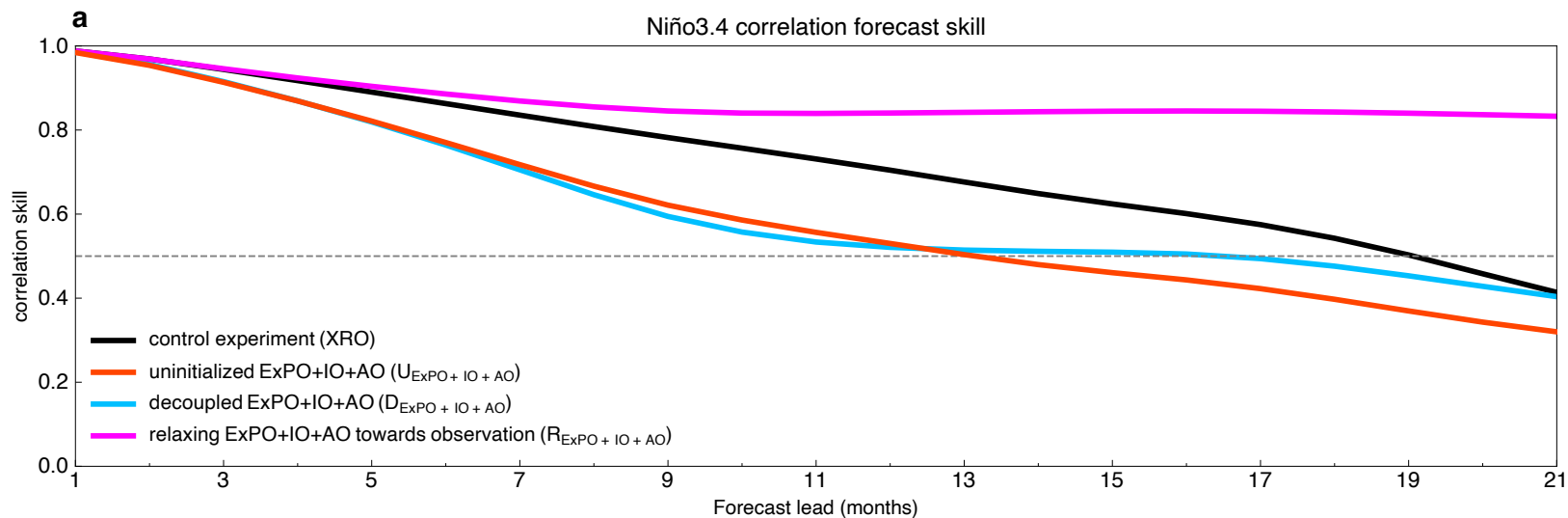
1141 **Extended Data Table 2|** Details of the XRO forecasting experiments using global climate model
1142 output as training data.

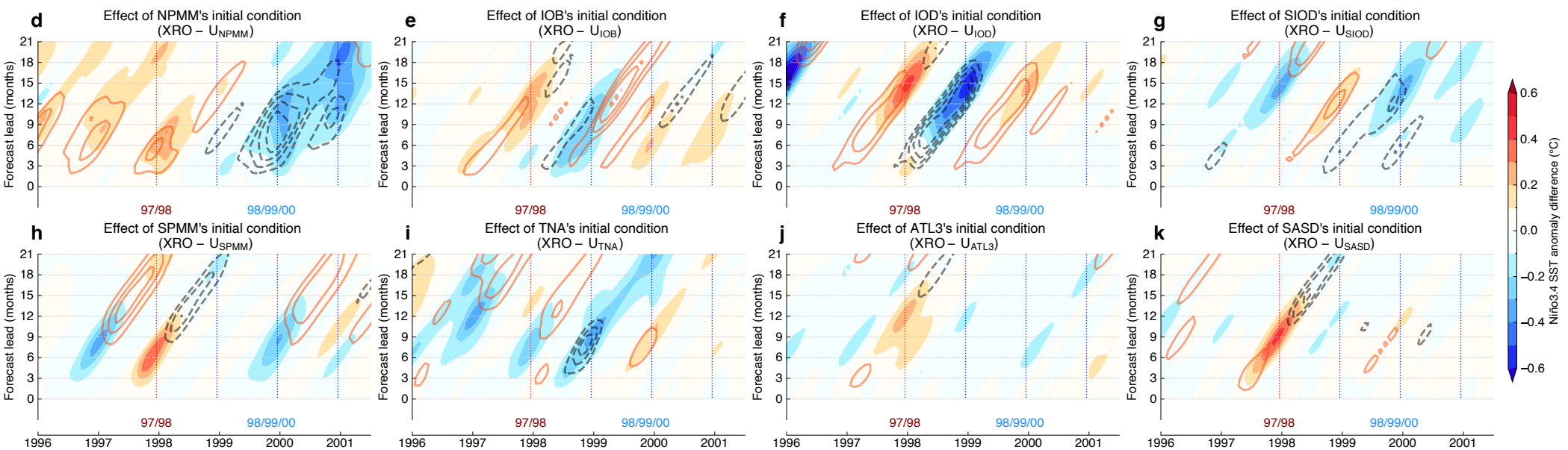
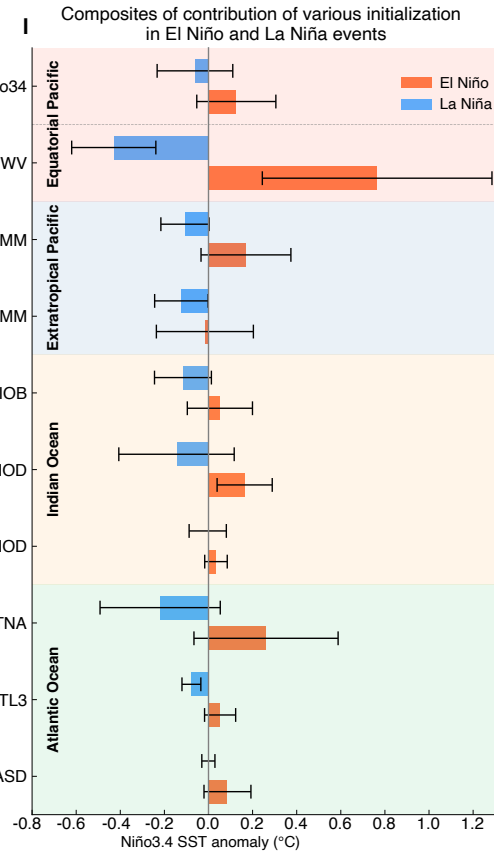
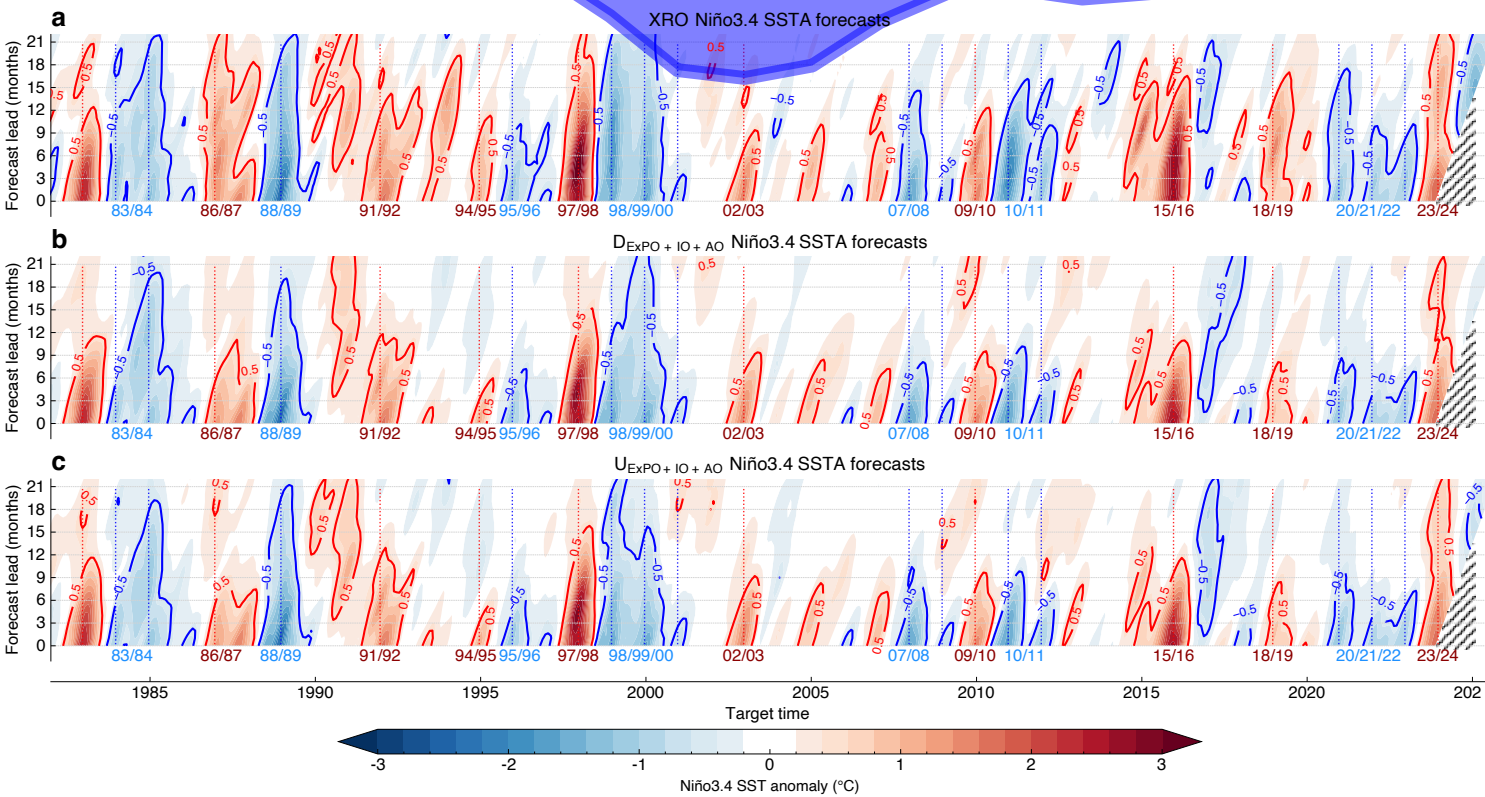
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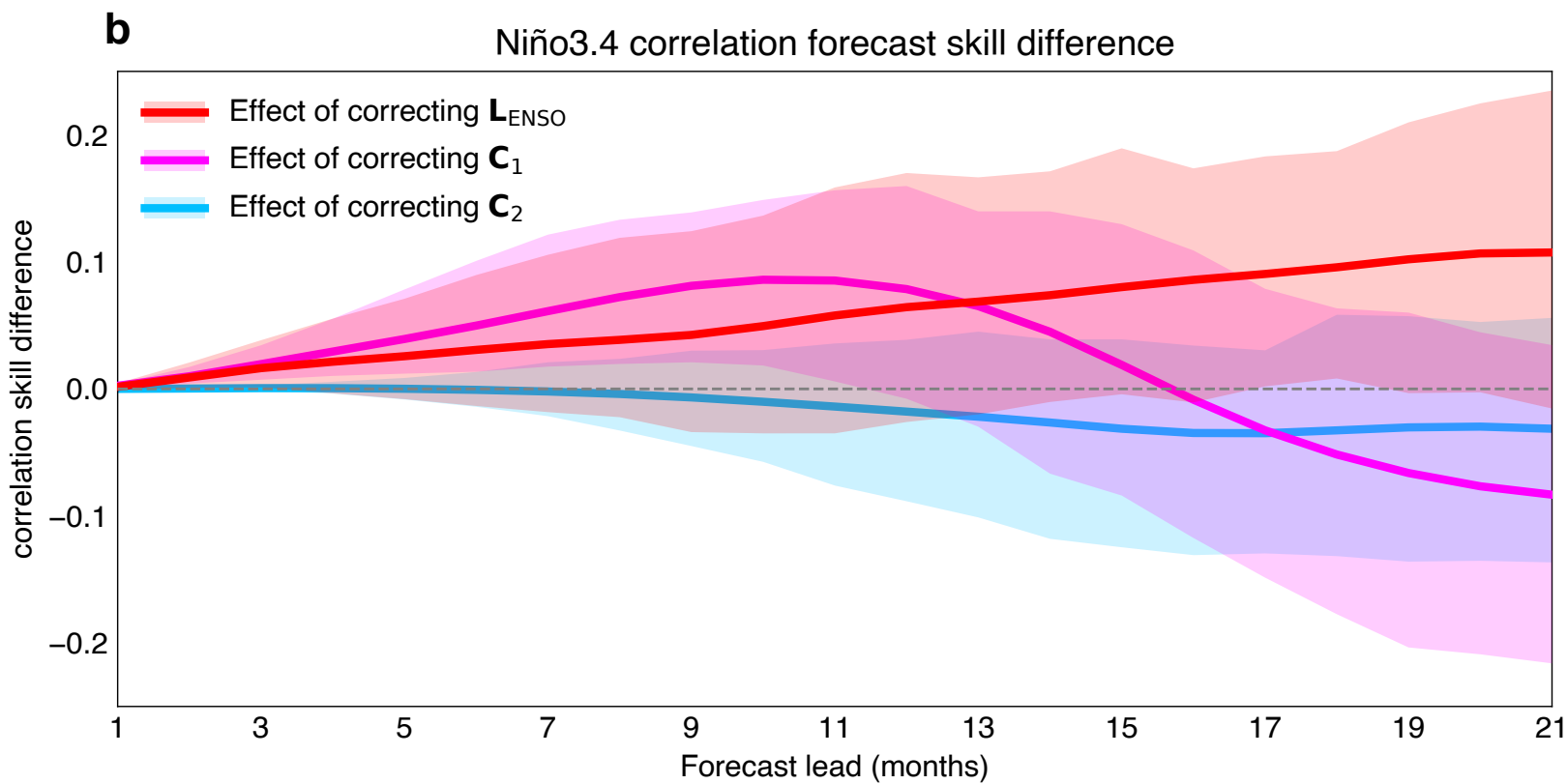
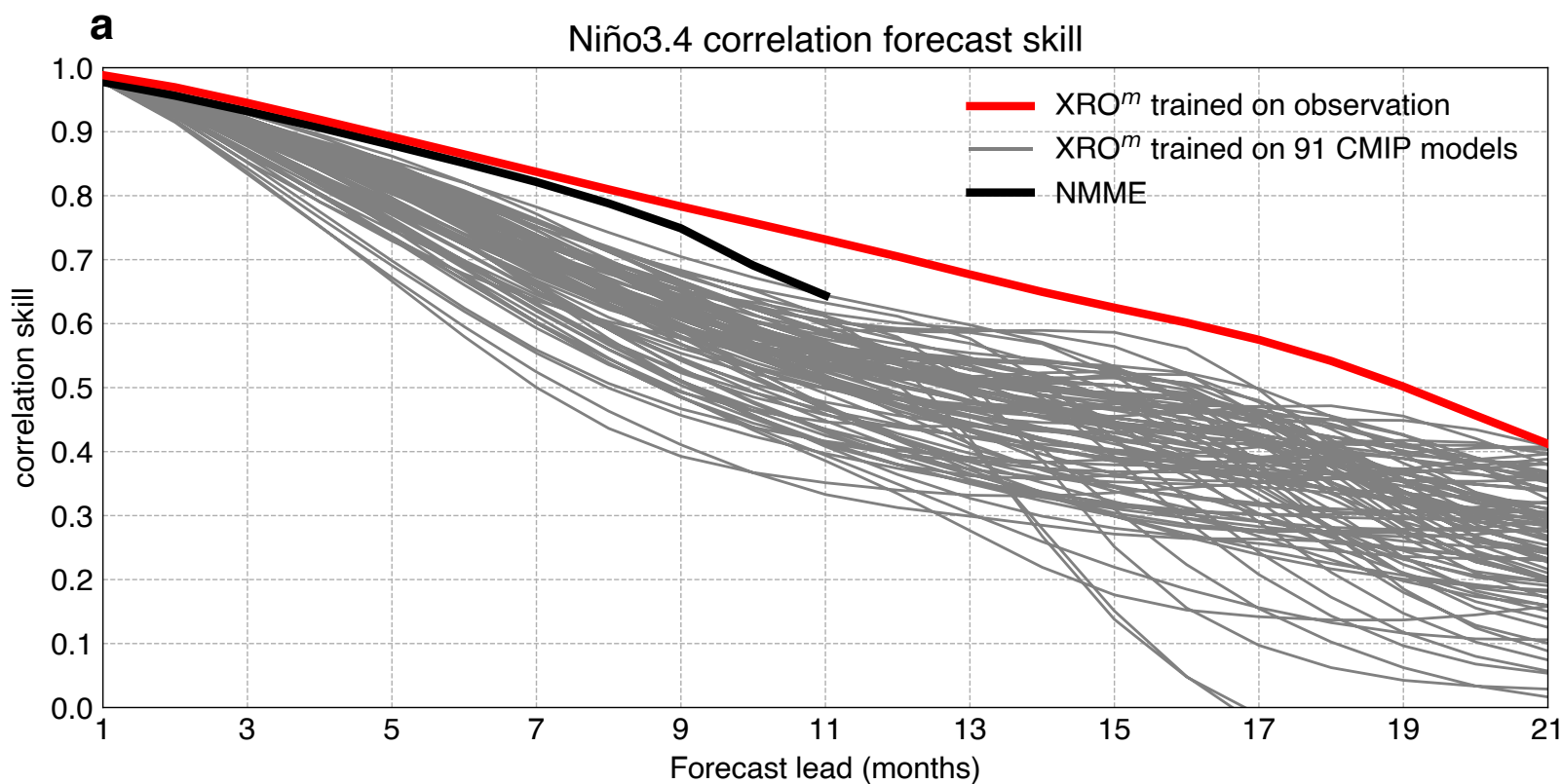




Niño3.4 correlation forecast skill







Supplementary Information for “Explainable El Niño predictability from climate mode interactions”

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Supplementary Text

Supplementary Text 1. Efficacy of the XRO in simulating ENSO and other climate modes

First, the XRO captures the observed seasonal synchronization of ENSO, with the Niño3.4 SSTA standard deviation peaking in November-December-January (Fig. 2a). This seasonal synchronization is primarily governed by the seasonal modulation of the SSTA growth rate due to the tropical Pacific background seasonal cycle (*Stein et al. 2014; Chen and Jin 2021; Levine and McPhaden 2015*). Second, the XRO successfully replicates El Niño-La Niña asymmetry, manifesting as positively skewed Niño3.4 SSTAs (Fig. 2b). This asymmetry arises from multiple nonlinear physical processes, such as oceanic nonlinear dynamical heating (*An and Jin 2004; An et al. 2020*) and nonlinear SST-wind stress coupling due to the nonlinear dependence of deep convection on SST (*Kang and Kug 2002; Choi et al. 2013; Geng et al. 2020*). Third, the observed ENSO periodicity is reasonably captured, with a Niño3.4 spectral peak at periods of 2-6 years (Fig. 2c). The XRO also captures the lead-time of warm water volume (WWV) anomaly ahead of ENSO SSTA by approximately 6-9 months (Fig. 2d), which is largely controlled by ENSO periodicity (*Zhao et al. 2021*). Fourth, the XRO generates the observed irregular interannual oscillations between El Niño and La Niña, including occurrences of single- and multi-year ENSO events (Supplementary Fig. 3). Various mechanisms governing multi-year ENSO occurrences have been well-documented, including nonlinearity (*Okumura et al. 2011; DiNezio and Deser 2014*), ENSO-combination mode and anomalous Ekman transport (*Iwakiri and Watanabe 2021, 2022*), the NPM and North Pacific Oscillation (*Ding et al. 2022; Geng et al. 2023; Park et al. 2021; Kim et al. 2023*), as well as inter-basin interactions with tropical Indian and/or Atlantic Oceans (*Kim and Yu 2022*). Notably, the XRO model incorporates all these elements either explicitly or implicitly (See “*Extended Nonlinear Recharge-Oscillator model (XRO)*” in *Methods*). Fifth, the XRO accurately reproduces the rapid decline in ENSO SSTA autocorrelation across boreal spring, commonly referred to as the spring persistence barrier (Supplementary Fig. 4).

The XRO reproduces the seasonal synchronization of the other climate modes that is seen in observations (Supplementary Fig. 5a-h), which in this model is largely caused by the seasonally varying damping rates of the individual modes, together with their coupled interactions (see diagonal axis in Extended Data Fig. 1). Notably, ENSO-driven processes play a pronounced role in the seasonal synchronization of some of the modes. For instance, the IOB warming, forced by El Niño, reaches its mature phase during boreal spring and summer, following the mature phase of El Niño (Supplementary Fig. 5c). The variance of the TNA peaks in boreal spring, due to both the seasonal modulation of its damping rate and the remote forcing from ENSO (*Chen et al. 2021; Jiang et al. 2023*). Moreover, the XRO reasonably reproduces the observed asymmetries of both the IOB and IOD, manifesting as positively skewed SSTAs in the central and western tropical Indian Ocean, and negatively skewed SSTAs in the eastern Indian Ocean near Java and Sumatra (Supplementary Fig. 5k-l). The positive skewness of the IOB primarily arises as a response to the skewed remote forcing from ENSO, while the IOD asymmetry is dominated by local nonlinear processes (*An et al. 2023*). Furthermore, the XRO accurately reproduces the observed seasonal autocorrelation of the other modes (Supplementary Fig. 6).

Supplementary Tables

Supplementary Table 1. Definition of SST indices for climate modes used in the study.

Climate Mode	Acronym	Description	References
El Niño-Southern Oscillation	ENSO	SSTAs averaged over Niño3.4 region 170°–120°W, 5°S–5°N	<i>(Trenberth 1997)</i>
North Pacific Meridional Mode	NPMM	SSTAs averaged over 160°–120°W, 10°–25°N	<i>(Richter et al. 2022)</i>
South Pacific Meridional Mode	SPMM	SSTAs averaged over 110°–90°W, 25°–15°S	<i>(Zhang et al. 2014)</i>
Indian Ocean Basin mode	IOB	SSTAs averaged over 40°–100°E, 20°S–20°N	<i>(Xie et al. 2009)</i>
Indian Ocean Dipole mode	IOD	SSTAs averaged over 50°–70°E, 10°S–10°N minus those averaged over 90°–110°E, 10°S–0°N	<i>(Saji et al. 1999)</i>
Southern Indian Ocean Dipole mode	SIOD	SSTAs averaged over 65°–85°E, 25°–10°S minus those averaged over 90°–120°E, 30°–10°S	<i>(Jo et al. 2022)</i>
Tropical North Atlantic variability	TNA	SSTAs averaged over 55°–15°W, 5°–25°N	<i>(Enfield et al. 1999)</i>
Atlantic Niño	ALT3	SSTAs averaged over 20°W–0°E, 3°S–3°N	<i>(Nnamchi et al. 2015)</i>
South Atlantic Subtropical Dipole	SASD	SSTAs averaged over 60°–0°W, 45°–35°S minus those averaged over 40°W–20°E, 30°–20°S	<i>(Rodrigues et al. 2015)</i>

Supplementary Table 2. Observational data used in the study.

Dataset (Period)	Variables	Description and Reference	Source
HadISST (1871-2023)	SST	Hadley Centre Sea Ice and Sea Surface Temperature dataset version 1.1 (<i>Rayner et al. 2003</i>)	https://www.metoffice.gov.uk/hadobs/hadisst/
ERSSTv5 (1871-2023)	SST	Extended Reconstructed Sea Surface Temperature version 5 (<i>Huang et al. 2017</i>)	https://psl.noaa.gov/data/gridded/data.noaa.ersst.v5.html
COBE-SST2 (1871-2023)	SST	Centennial in situ Observation-Based Estimates of Sea Surface Temperature version 2 (<i>Hirahara et al. 2014</i>)	https://ds.data.jma.go.jp/tcc/tcc/products/elnino/cobesst_doc.html
GECCO3 (1950-2018)	SST, Temp*	German contribution to Estimating the Circulation and Climate of the Ocean version 3 (<i>Köhl 2020</i>)	https://icdc.cen.uni-hamburg.de/thredds/catalog/ftp/thredds/EASYInit/GECCO3/regular_1x1_grid/catalog.html
GODAS (1950-2023)	SST, Temp	Global Ocean Data Assimilation System (<i>Behringer and Xue 2004</i>)	https://psl.noaa.gov/data/gridded/data.godas.html
ORAS5 (1958-2023)	SST, Temp	ECMWF Ocean Reanalysis System 5 (<i>Zuo et al. 2019</i>)	https://doi.org/10.24381/cds.67e8eeb7
ORA20C (1900-2009)	SST, Temp	ECMWF Ocean Reanalysis of the 20th Century (<i>de Boisséson et al. 2018</i>)	https://www.cen.uni-hamburg.de/en/icdc/data/ocean/easy-init-ocean/ecmwf-ensemble-of-ocean-reanalyses-of-the-20th-century-ora-20c.html
PEODAS (1960-2014)	SST, Temp	Predictive Ocean Atmosphere Model for Australia Ensemble Ocean Data Assimilation System (<i>Yin et al. 2011</i>)	http://opendap.bom.gov.au:8080/thredds/catalogs/bmrc-poama-catalog.html
SODA224 (1871-2010)	SST, Temp	Simple Ocean Data Assimilation Phase 2.2.4 (<i>Carton and Giese 2008</i>)	https://apdrc.soest.hawaii.edu/dods/public_data/SODA
ERA5 (1979-2022)	Surface air temperature	ECMWF Atmospheric Reanalysis v5 (<i>Hersbach et al. 2020</i>)	https://doi.org/10.24381/cds.f17050d7
CMAP (1979-2022)	Precipitation	Gridded precipitation from the Climate Prediction Center Merged Analysis of Precipitation (<i>Xie and Arkin 1997</i>)	https://psl.noaa.gov/data/gridded/data.cmap.html

*Temp is 3-dimensional ocean temperature

Supplementary Table 3. El Niño type forecasts for the Nov-Dec-Jan target season, based on Niño3 and Niño4 indices at a 9-month lead-time.

Year	ORAS5	XRO2 fitted on 1979-2022 (lead=9)	XRO2 fitted on 1950-1990 (lead=9)	AI (lead=9)	NMME (lead=9)
1982	EP	EP	-	-	MIX
1986	MIX	MIX	-	MIX	MIX
1991	MIX	MIX	MIX	MIX	MIX
1997	EP	EP	EP	MIX	MIX
2002	MIX	MIX	MIX	Neutral state	MIX
2009	MIX	EP	Neutral state	MIX	MIX
2015	MIX	MIX	MIX	MIX	MIX

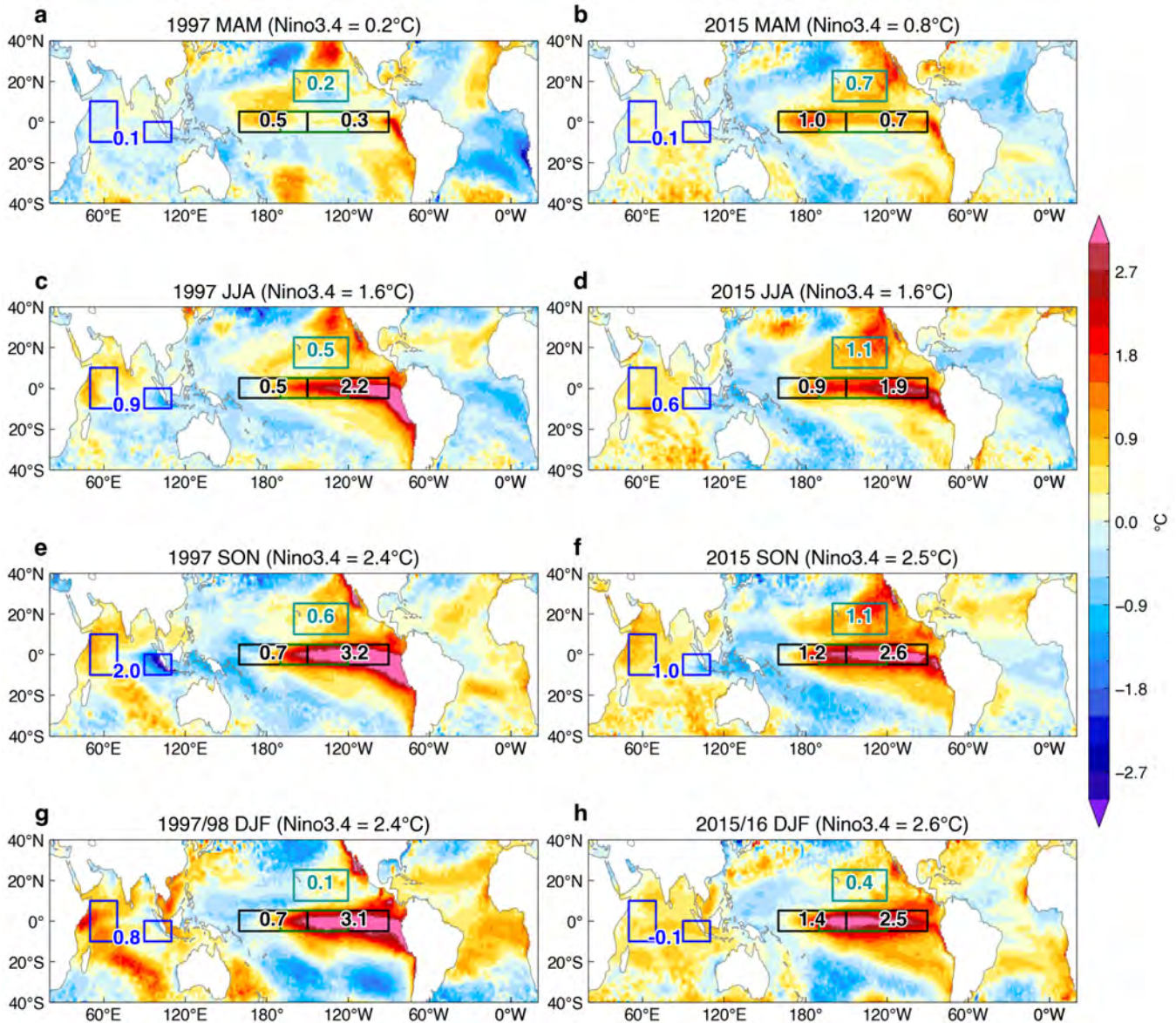
Supplementary Table 4. Details of the NMME models used in this study.

Model	Name used here	Period	Ensemble size	Maximum lead time (months)
CMC1-CanCM3	CanCM3	January 1981–December 2019	10	11
CMC2-CanCM4	CanCM4	January 1981–December 2019	10	11
COLA-RSMAS-CCSM4	CCSM4	January 1982–December 2017	10	11
NCEP-CFSv2	CFSv2	January 1982–July 2022	24	9
GEM-NEMO	GEM-NEMO	January 1981–December 2020	10	11
GFDL-CM2p1-aer04	GFDL	January 1982–December 2021	10	11
GFDL-CM2p5-FLOR-A06	GFDL-FLOR	March 1980–December 2021	12	11
GFDL-CM2p5-FLOR-B01	GFDL-FLOR	March 1980–December 2021	12	11
GFDL-SPEAR	GFDL-SPEAR	January 1991–December 2020	15	11
NASA-GEOSS2S	NASA-GEOSS2S	January 1981–December 2020	10	8

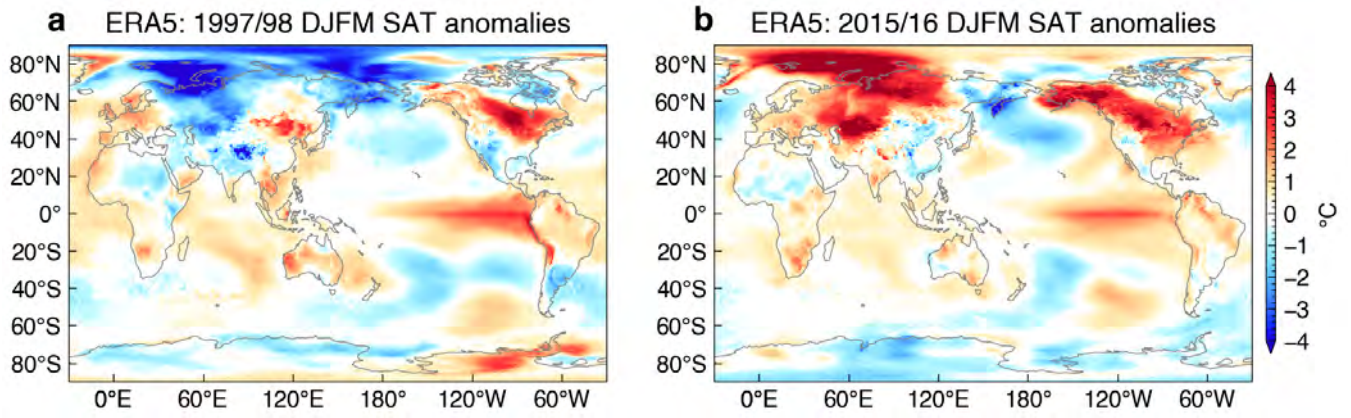
Supplementary Table 5. Lists of the 91 CMIP5/6 climate models used in this study.

CMIP5 No.	CMIP5 Models	Member	CMIP6 No.	CMIP6 Models	Member
1	ACCESS1-0	rlilpl	1	ACCESS-CM2	rlilplf1
2	ACCESS1-3	rlilpl	2	ACCESS-ESM1-5	rlilplf1
3	bcc-csm1-1	rlilpl	3	AWI-CM-1-1-MR	rlilplf1
4	bcc-csm1-1-m	rlilpl	4	BCC-CSM2-MR	rlilplf1
5	BNU-ESM	rlilpl	5	BCC-ESM1	rlilplf1
6	CanESM2	rlilpl	6	CAMS-CSM1-0	rlilplf1
7	CCSM4	rlilpl	7	CAS-ESM2-0	rlilplf1
8	CESM1-BGC	rlilpl	8	CESM2	r4ilplf1
9	CESM1-CAM5	rlilpl	9	CESM2-FV2	rlilplf1
10	CESM1-FASTCHEM	rlilpl	10	CESM2-WACCM	rlilplf1
11	CESM1-WACCM	rlilpl	11	CESM2-WACCM-FV2	rlilplf1
12	CMCC-CESM	rlilpl	12	CIESM	rlilplf1
13	CMCC-CM	rlilpl	13	CMCC-CM2-HR4	rlilplf1
14	CMCC-CMS	rlilpl	14	CMCC-CM2-SR5	rlilplf1
15	CNRM-CM5	rlilpl	15	CMCC-ESM2	rlilplf1
16	CSIRO-Mk3-6-0	rlilpl	16	CNRM-CM6-1	rlilplf2
17	FGOALS-g2	rlilpl	17	CNRM-ESM2-1	rlilplf2
18	FGOALS-s2	rlilpl	18	CanESM5	rlilplf1
19	FIO-ESM	rlilpl	19	E3SM-1-0	rlilplf1
20	GFDL-CM3	rlilpl	20	E3SM-1-1	rlilplf1
21	GFDL-ESM2G	rlilpl	21	E3SM-1-1-ECA	rlilplf1
22	GFDL-ESM2M	rlilpl	22	EC-Earth3	rlilplf1
23	GISS-E2-H-CC	rlilpl	23	EC-Earth3-Veg	rlilplf1
24	GISS-E2-H	rlilpl	24	FGOALS-f3-L	rlilplf1
25	GISS-E2-R-CC	rlilpl	25	FGOALS-g3	rlilplf1
26	GISS-E2-R	rlilpl	26	FIO-ESM-2-0	rlilplf1
27	HadCM3	rlilpl	27	GFDL-CM4	rlilplf1
28	HadGEM2-AO	rlilpl	28	GFDL-ESM4	rlilplf1
29	HadGEM2-CC	rlilpl	29	GISS-E2-1-G	rlilplf1
30	HadGEM2-ES	rlilpl	30	GISS-E2-1-G-CC	rlilplf1
31	IPSL-CM5A-LR	rlilpl	31	GISS-E2-1-H	rlilplf1
32	IPSL-CM5A-MR	rlilpl	32	HadGEM3-GC31-LL	rlilplf3
33	IPSL-CM5B-LR	rlilpl	33	INM-CM4-8	rlilplf1
34	MIROC5	rlilpl	34	INM-CM5-0	r10ilplf1
35	MIROC-ESM-CHEM	rlilpl	35	IPSL-CM6A-LR	rlilplf1
36	MIROC-ESM	rlilpl	36	MIROC6	rlilplf1
37	MPI-ESM-LR	rlilpl	37	MIROC-ES2L	rlilplf2
38	MPI-ESM-MR	rlilpl	38	MPI-ESM-1-2-HAM	rlilplf1
39	MPI-ESM-P	rlilpl	39	MPI-ESM1-2-HR	rlilplf1
40	MRI-CGCM3	rlilpl	40	MPI-ESM1-2-LR	r10ilplf1
41	MRI-ESM1	rlilpl	41	MRI-ESM2-0	rlilplf1
42	NorESM1-ME	rlilpl	42	NESM3	rlilplf1
43	NorESM1-M	rlilpl	43	NorESM2-LM	rlilplf1
			44	NorESM2-MM	rlilplf1
			45	SAM0-UNICON	rlilplf1
			46	TaiESM1	rlilplf1
			47	UKESM1-0-LL	rlilplf2
			48	NorCPM1	rlilplf1

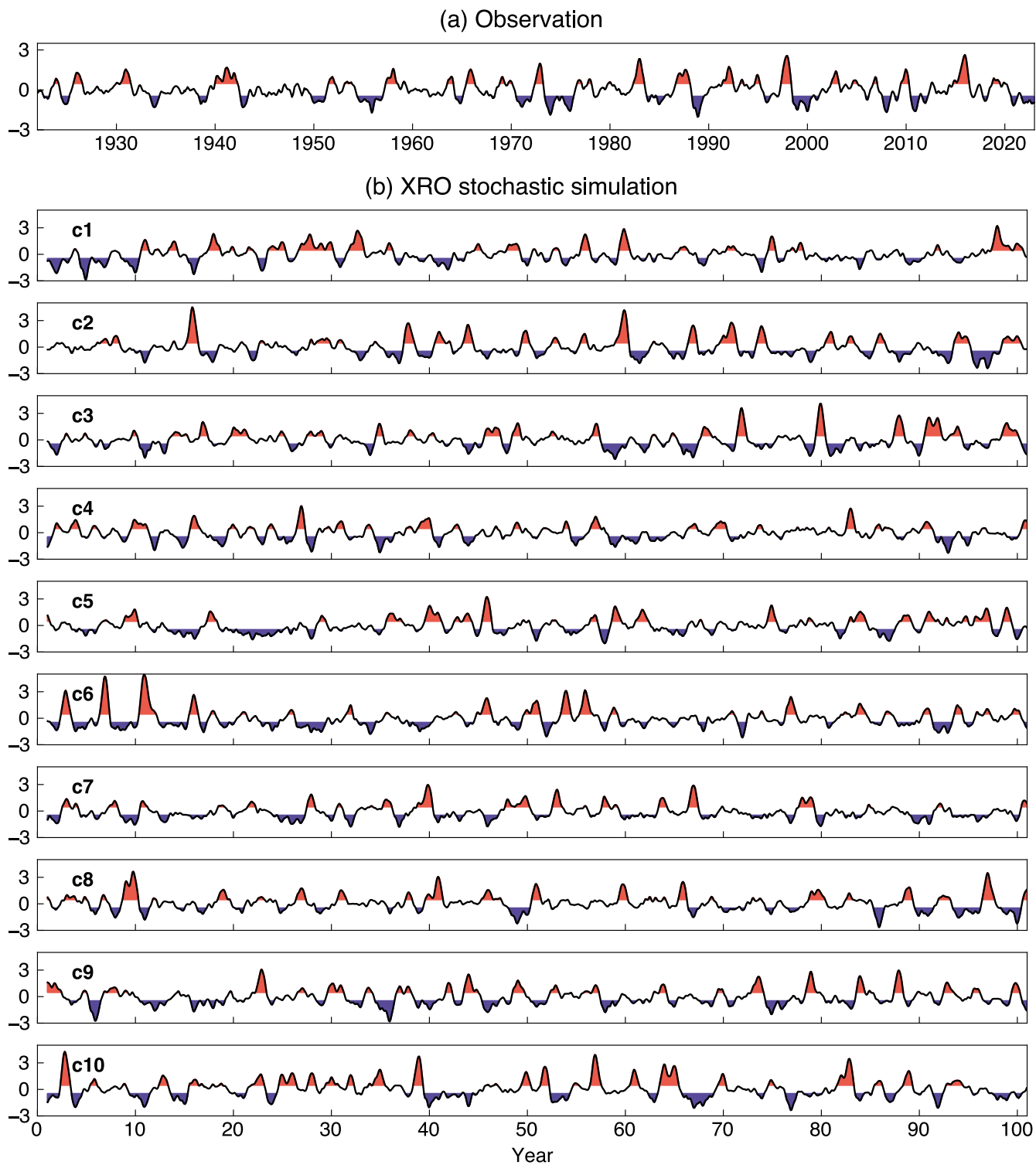
Supplementary Figures



Supplementary Fig. 1 | Observed differences in tropical SSTA pattern and evolution between the 1997/98 and 2015/16 El Niño events derived from ORAS5 reanalysis. The SSTAs during (a) 1997 MAM, (b) 2015 MAM, (c) 1997 JJA, (d) 2015 JJA, (e) 1997 SON, (f) 2015 SON, (g) 1997/98 DJF and (h) 2015/16 DJF. In each panel, the values of Niño3, Niño4, IOD, and NPMM SSTAs are indicated in the corresponding boxes, and the value of Niño3.4 is indicated in the title. The 1997/98 and 2015/16 El Niño events have different SSTA patterns in the central and far eastern equatorial Pacific, as well as different associated IOD and NPMM intensities. The 1997 event exhibits eastern Pacific El Niño characteristics with the warmest SSTAs in the far eastern equatorial Pacific and a strong concurrent IOD, partly due to stronger WWV preconditioning. In 2015, the SSTA peak is located closer to the central Pacific, possibly due to the strong coupling of the NPMM and central equatorial Pacific SST.

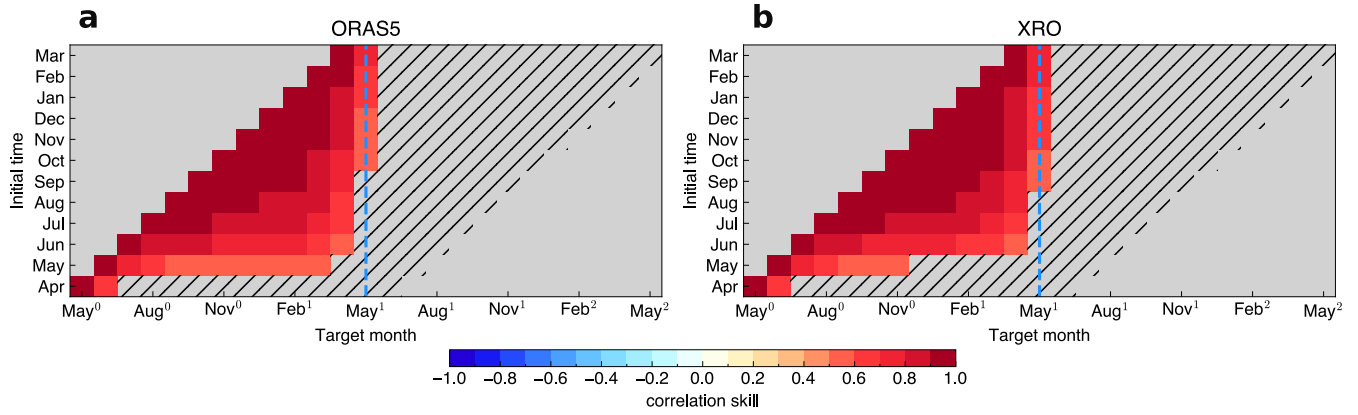


Supplementary Fig. 2 | Observed surface air temperature (SAT) anomalies for the 1997/98 and 2015/16 El Niño events during December-March (DJFM). The (a) 1997/98 and (b) 2015/16 El Niño events were associated with different pan-Arctic SAT, consistent with Jeong et al. (2022).

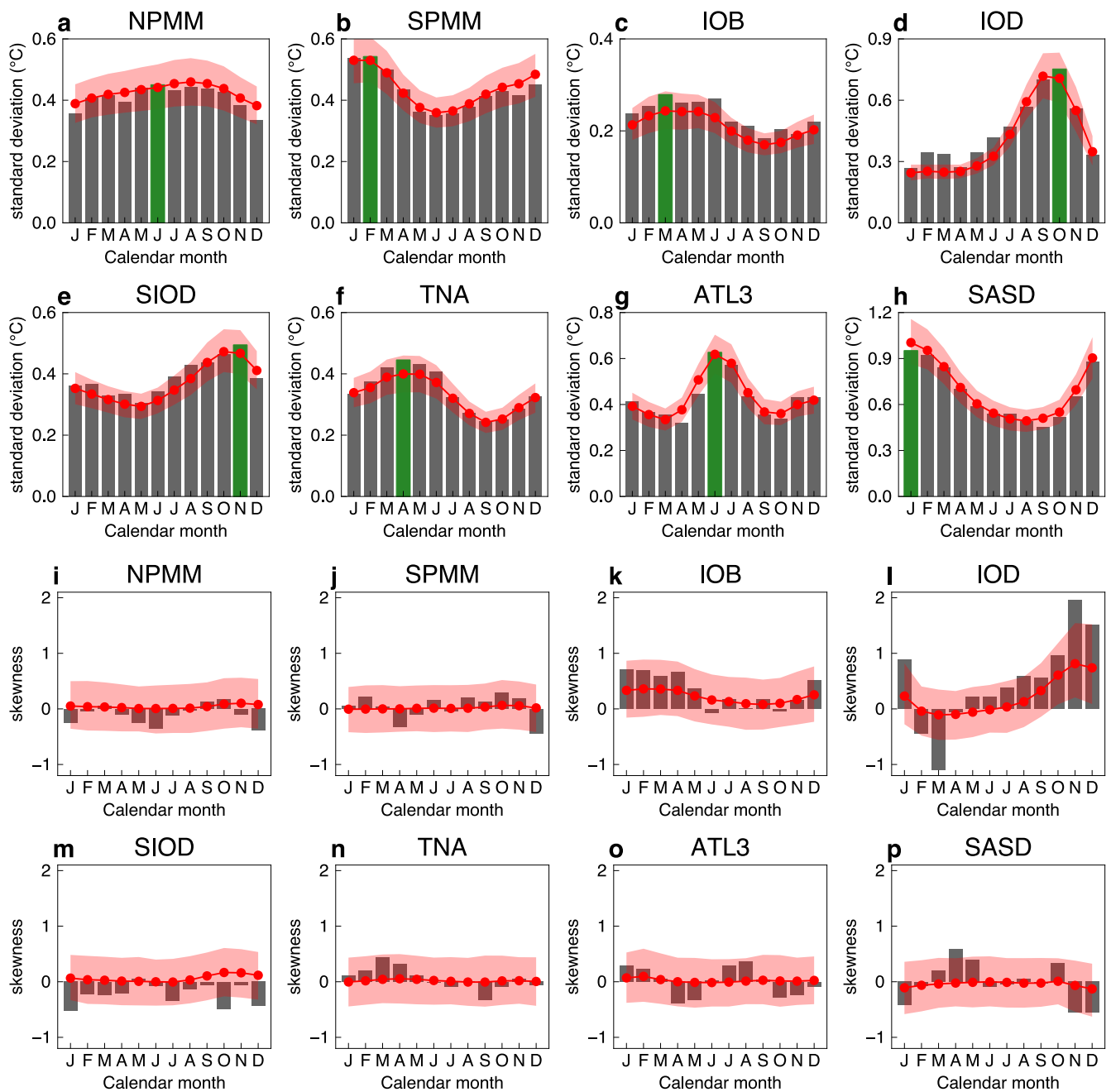


Supplementary Fig. 3| ENSO time series in the observation and XRO stochastic simulation. The 3-month running mean of Niño3.4 SSTA for (a) the ensemble mean of multiple observational SST datasets for 1923-2022 (Supplementary Table 2), and (b) the 10 consecutive centuries (numbered) from the XRO stochastic simulation. The red/blue shading denote the SSTA above 0.5 / below -0.5°C, respectively. The XRO stochastic simulation reproduces the irregular interannual oscillations between El Niño and La Niña.

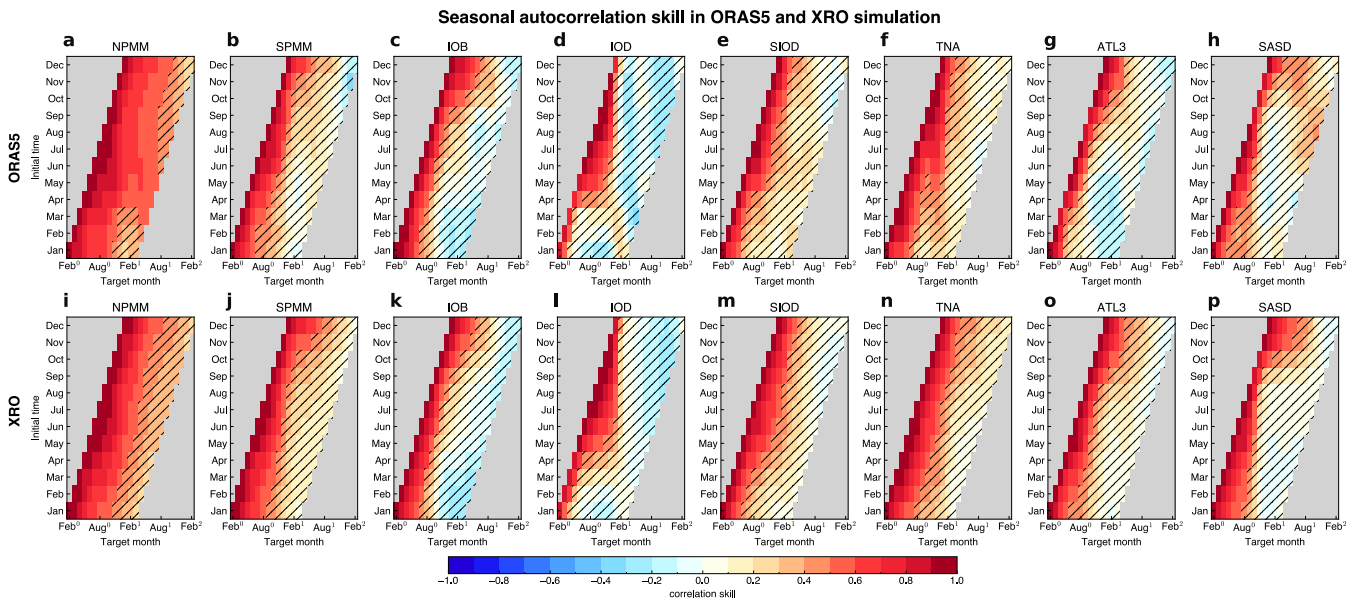
Seasonal Niño3.4 autocorrelation skill in ORAS5 and XRO simulation



Supplementary Fig. 4| Seasonal autocorrelation of Niño3.4 SST index. Correlations of Niño3.4 index with itself, as a function of initialization month (ordinate) and target month (abscissa) for the ORAS5 reanalysis (1979-2022) (a) and for the XRO stochastic simulations (b, ensemble mean). Hatching highlights correlation skills less than 0.5. The dashed vertical blue lines denote the spring predictability barrier season. The XRO accurately reproduces the rapid decline in ENSO SSTA autocorrelation across boreal spring.

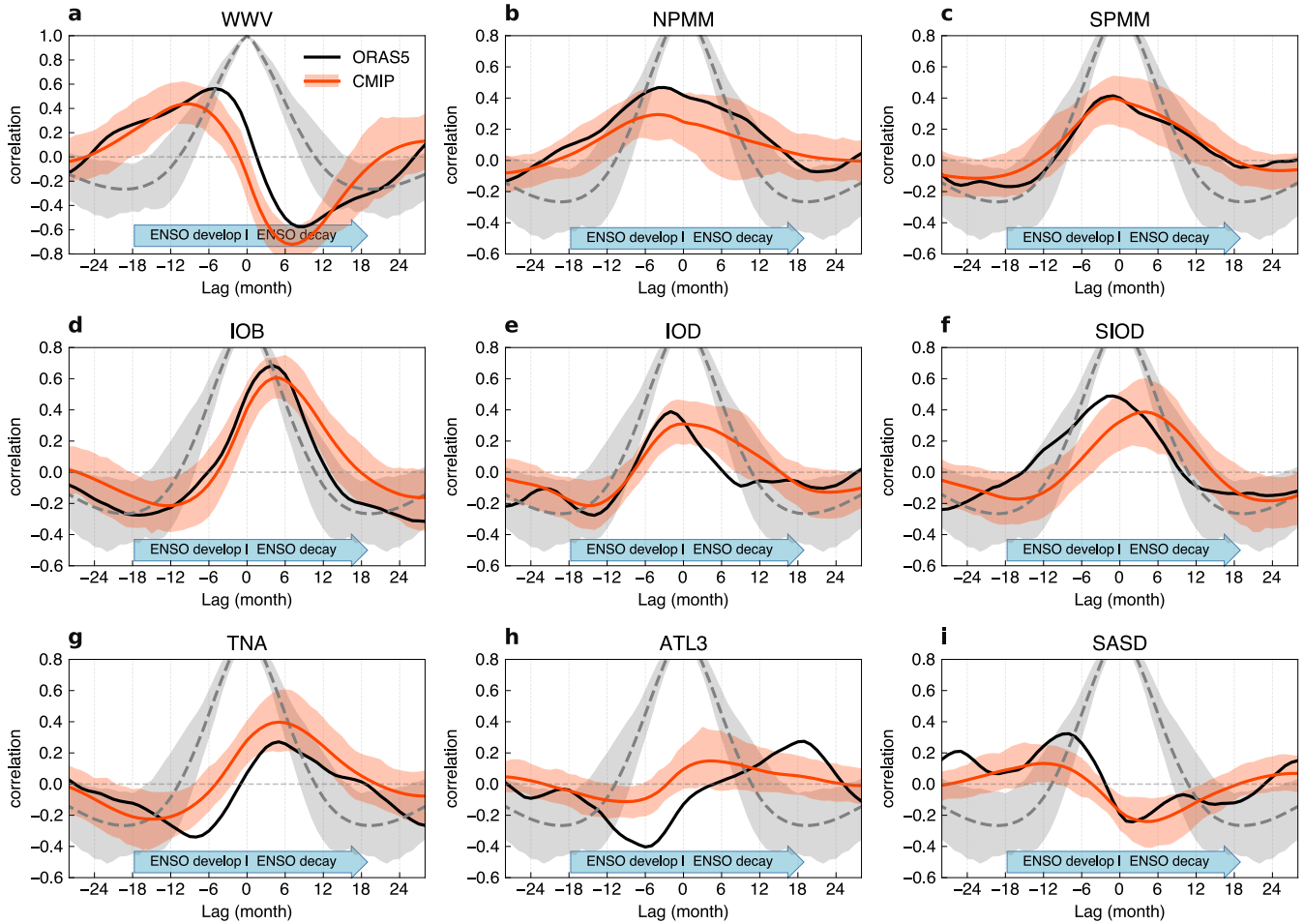


Supplementary Fig. 5 | Seasonal statistics of SSTA indices for the other climate modes. a-h, Seasonally varying standard deviation of the SSTA indices for the NPMM, SPMM, IOB, IOD, SIOD, TNA, ATL3, and SASD, respectively, in the ORAS5 observations (1979-2022) (*bars*) and the XRO stochastic simulations (*red curves*). Red shading indicates the 10%-90% spread bands of simulated 43-year epochs, obtained from splitting a 43,000-year XRO simulation into 1000 non-overlapping blocks. The month of peak standard deviation for each observed mode is indicated in green. **i-p,** Same as a-h, but for seasonally varying skewness. The XRO accurately simulates the observed seasonal synchronization of specific climate modes, and reasonably reproduces the observed warm/cold asymmetries of both the IOB and IOD.



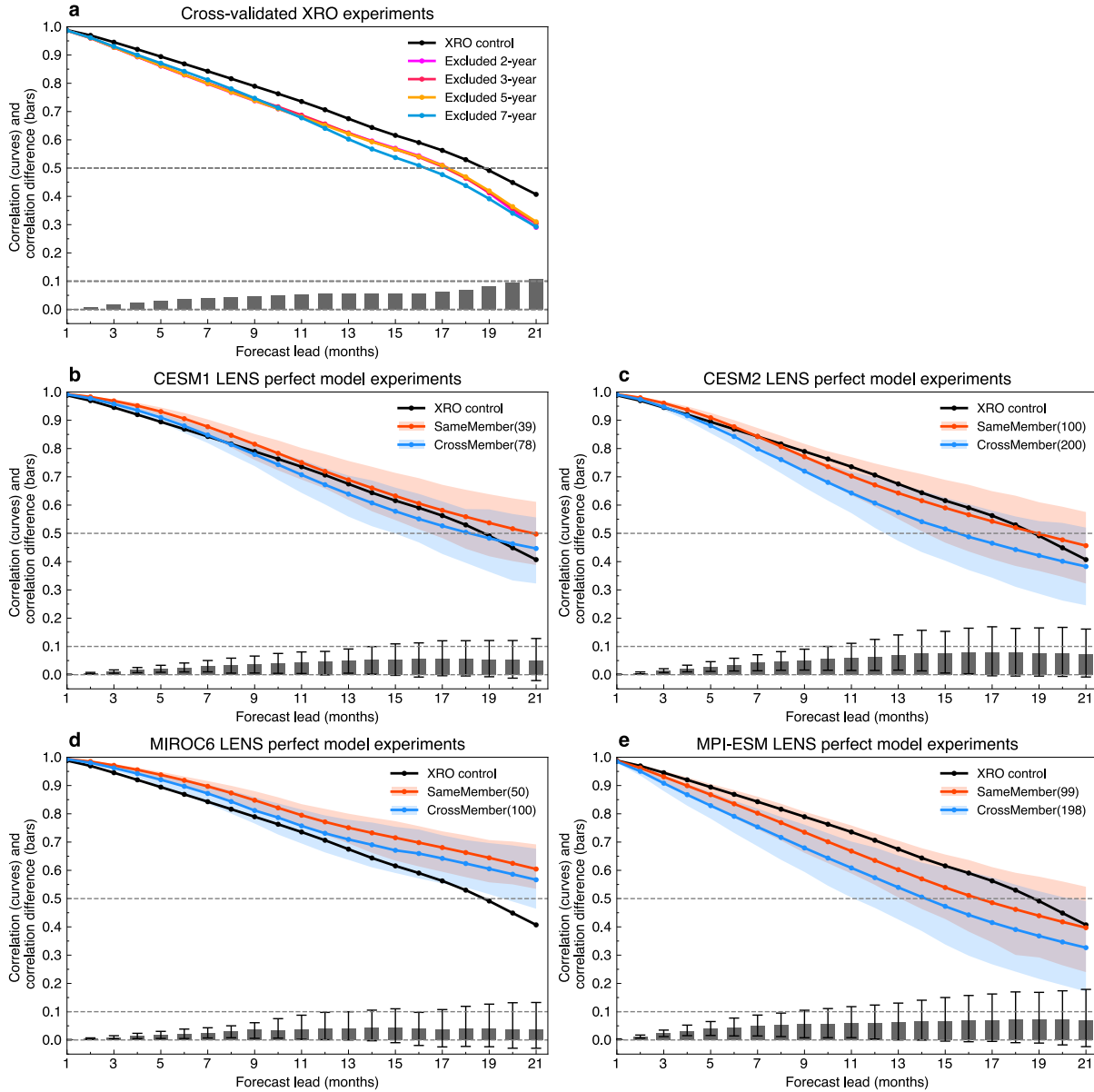
Supplementary Fig. 6 | Seasonal autocorrelation of SSTA indices for other climate modes. Correlations of each index with itself, as a function of initialization month (ordinate) and target month (abscissa) for the ORAS5 reanalysis (1979-2022) (upper row) and for the XRO stochastic simulations (bottom row, ensemble mean). Hatching highlights correlation skills less than 0.5. The XRO accurately reproduces the seasonal autocorrelation structures of the other climate modes.

Cross-correlation of Niño3.4 SSTA with various indices in ORAS5 and CMIP5/6 simulations

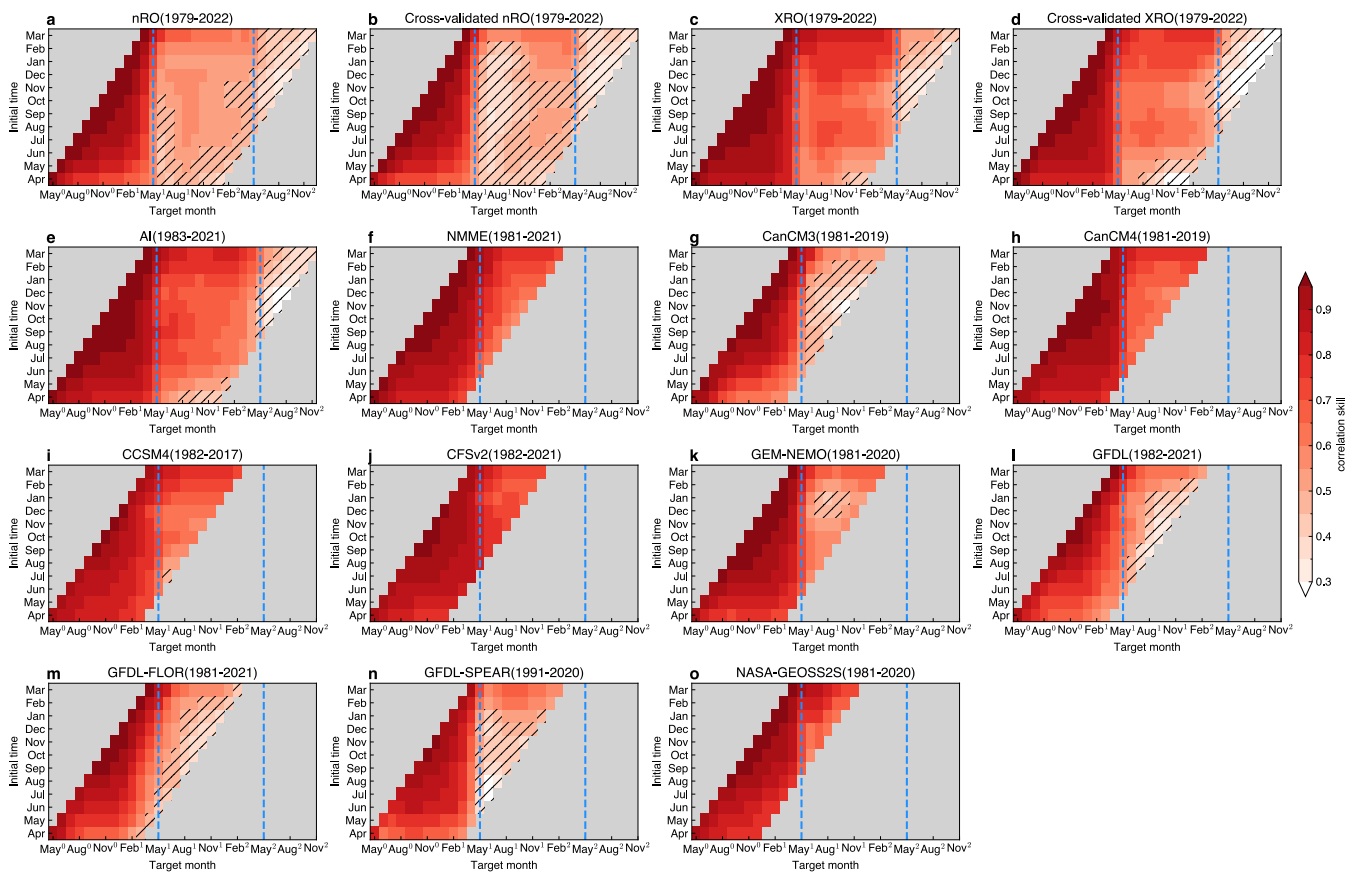


Supplementary Fig. 7 | ENSO’s lead-lag relationship with equatorial Pacific warm water volume (WWV) index and SSTA indices of other climate modes in CMIP historical simulations. Shown as monthly cross-correlations of each index with the lagged Niño3.4 index in ORAS5 reanalysis (1979-2022) (*black*) and CMIP5/6 historical simulations (1900-1999) (ensemble mean in red curves; red shading indicates the 10%-90% spread bands of 91 individual models). The dashed curves show the ensemble mean autocorrelation of Niño3.4 index in CMIP5/6 historical simulations (shading indicates the 10%-90% spread bands of 91 individual models). Abscissas are the lead-time, with negative values representing months for which the Niño3.4 index lags, and positive values representing months for which the Niño3.4 index leads. It is challenging for climate models to realistically simulate the observed ENSO SSTA lead-lag relationship with WWV anomalies and the SSTA indices for the other climate modes, especially for WWV index and Atlantic Ocean SST indices.

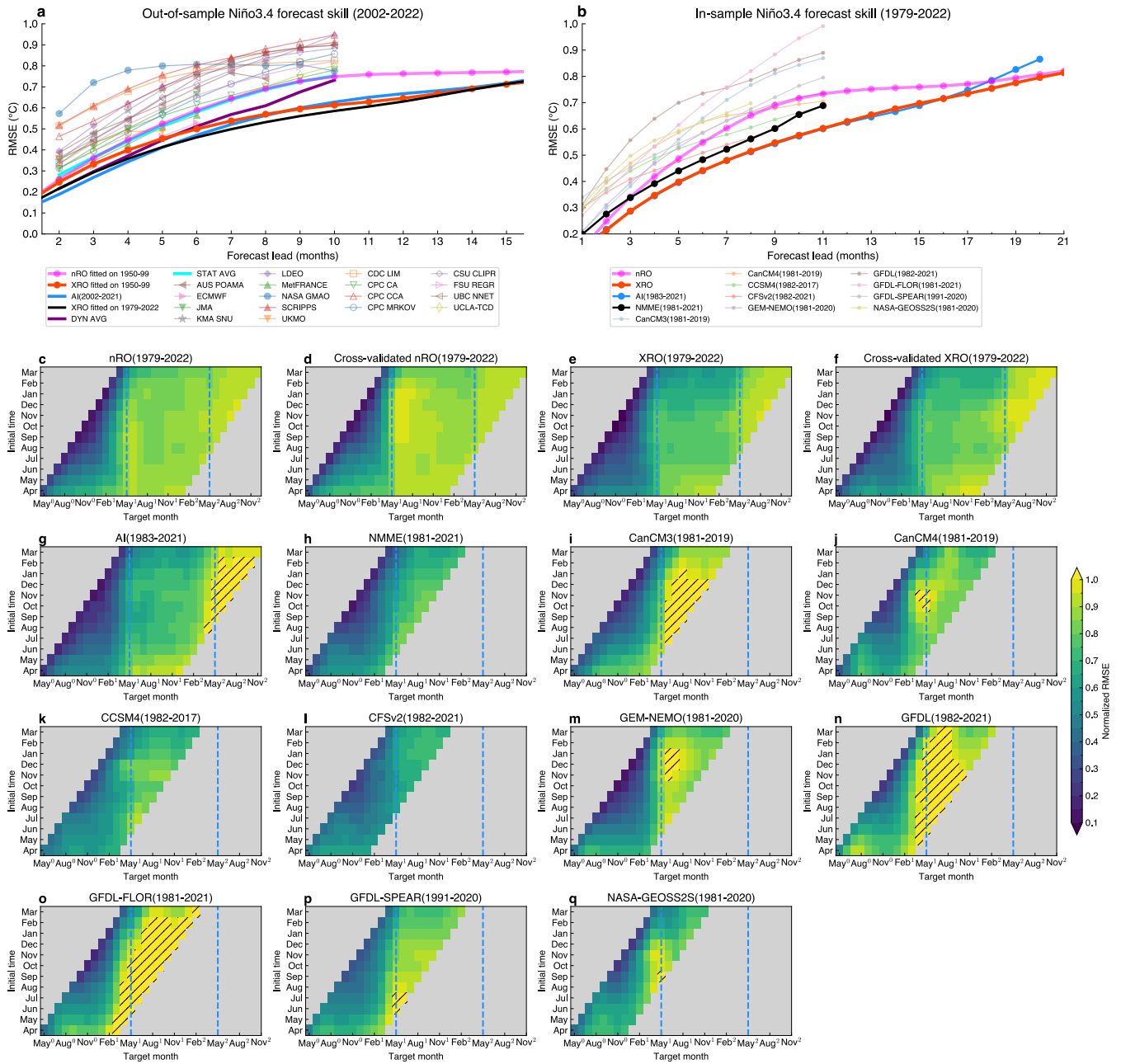
Niño3.4 correlation skill using the XRO based on ORAS5 (1979-2022) and LENS (1959-2002)



Supplementary Fig. 8| Robustness of the XRO parameter fitting and reforecasting ENSO. **a**, the all-months correlation skill of the 3-month running mean Niño3.4 index during 1979-2022 as a function of forecast lead for the XRO control forecast (*black curve*) and cross-validated XRO forecast that excluded from 2 to 7 years data (*coloured curves*), the mean skill difference between cross-validated XRO forecast and control forecast (*bars*). The dashed lines indicate 0.5, 0.1, and zero correlation skills. **b-d**, Same as **a**, but for skill for LENS perfect model “Same-Member” and “Cross-Member” experiments for CESM1, CESM2, MIROC6, and MPI-ESM during 1959-2002, respectively (See “*Large ensemble simulations and perfect model reforecasting experiments*” in *Methods*). The shadings denote the 10%-90% spread among the ensemble members within each LENS. The bottom bars denote the mean difference between “Same-Member” and “Cross-Member” experiments with error bars denote the 10%-90% spread among the ensemble members within each LENS. The XRO fitting and reforecasted ENSO is robust with uncertainty in Niño3.4 correlation skill less than 0.1 within 21 lead months.

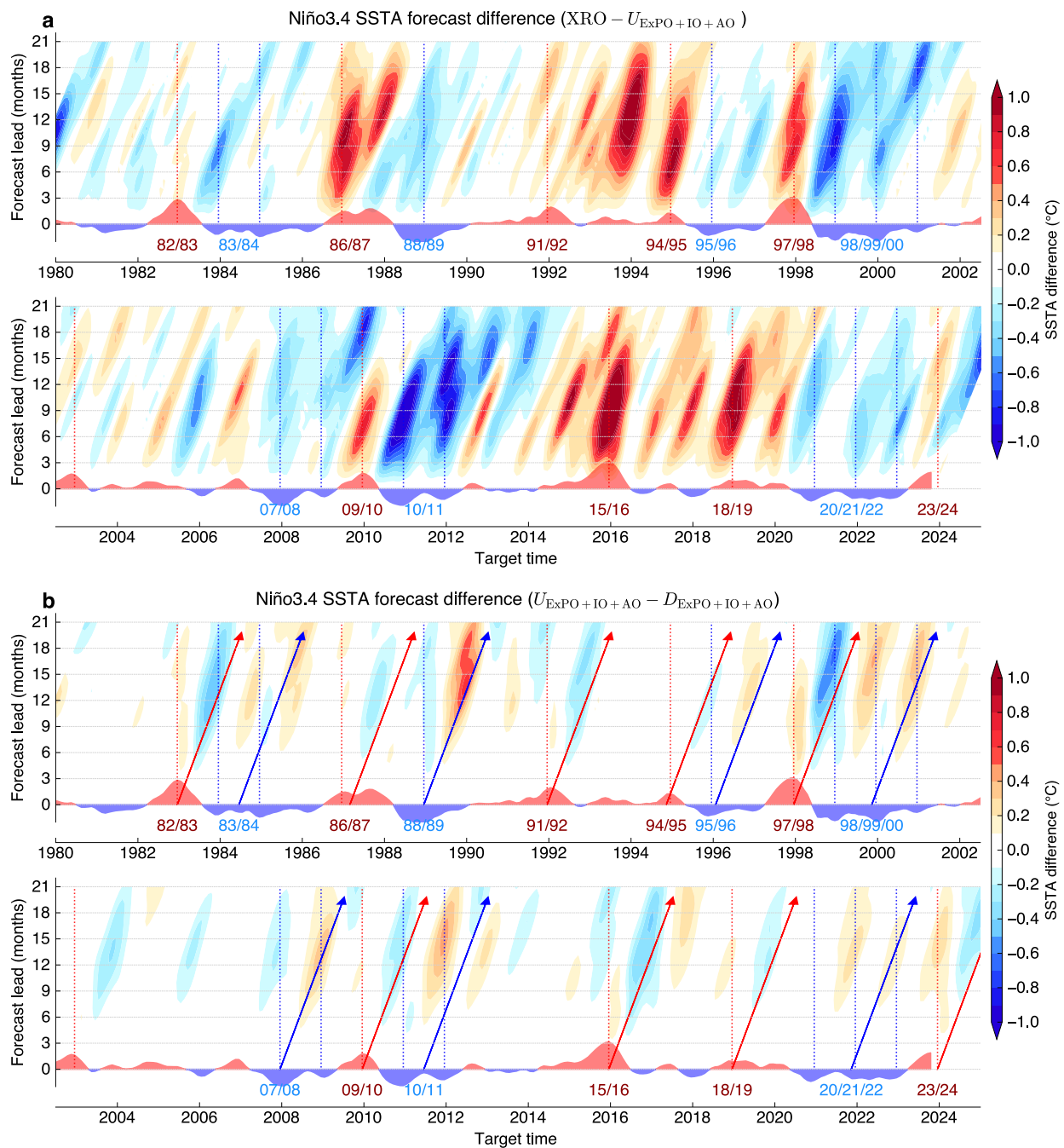


Supplementary Fig. 9 | Seasonality of correlation forecast skill for ENSO. The correlation skills verified during 1979–2022 of various model forecasts of the Niño3.4 SSTA index, as a function of the start month (ordinate) and target month (abscissa; superscripts 0, 1, 2 denote the current and subsequent years, respectively), for the nRO (a), Cross-validated nRO (b), XRO (c), Cross-validated XRO (d), AI model (e), multi-model mean of NMME ensemble means (f), and ensemble means from individual dynamical models in the North American Multi-Model Ensemble (NMME)(g-o). Hatching highlights the forecasts with correlation skill less than 0.5. The dashed vertical blue lines denote the spring predictability barrier season. The nRO and most of the dynamical models exhibit a pronounced spring predictability barrier in May–June–July. The SPB is much less pronounced in the XRO, which is comparable in skill with the AI model in all seasons.

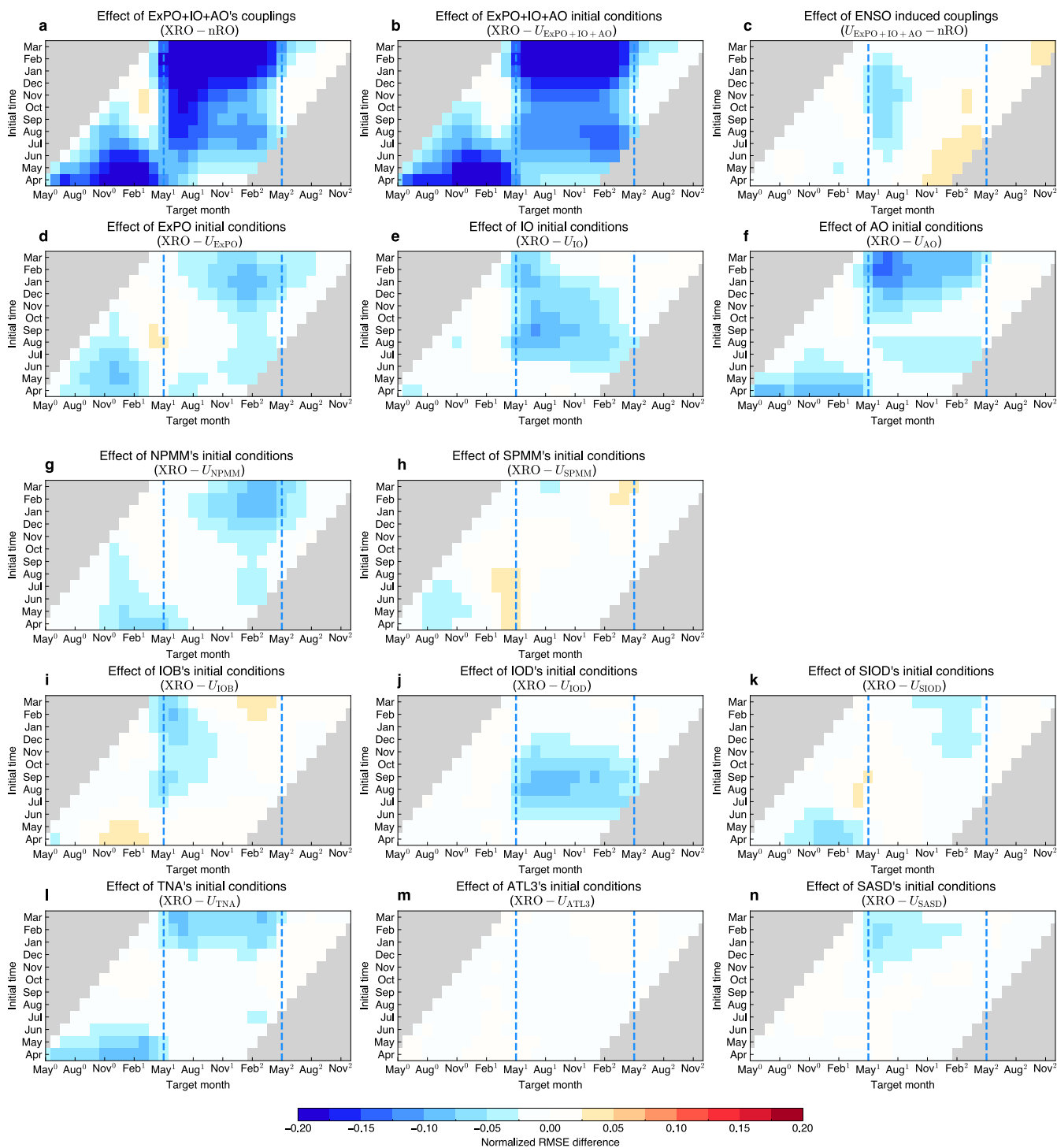


Supplementary Fig. 10 | Root Mean Square Error (RMSE) forecast metric for ENSO. a, The all-months RMSE forecasts verified on 2002-2022 of the 3-month running mean Niño3.4 SSTA index, as a function of the forecast lead month in the out-of-sample nRO fitted on 1950-1999 (*magenta*), out-of-sample XRO fitted on 1950-1999 (*red*), the AI model, the XRO control fitted on 1979-2022 (*black curve*) and operational models aggregated by the International Research Institute for Climate and Society (IRI), ensemble mean of dynamical models (DYN AVG, *dark purple curve*), ensemble mean of statistical models (STAT AVG, *dark cyan curve*). **b,** same as **a**, but for RMSE skill of Niño3.4 forecasts verified 1979-2022 in the in-sample nRO (*magenta*), in-sample XRO model (*red*), AI model (*blue*), dynamical models from the North American Multi-Model Ensemble (NMME) project (multi-model ensemble of NMME in *black*, ensemble mean from individual models in *other colours*); **c-q,** The relative RMSE of

Niño3.4 SSTA forecasts, normalized by the seasonally-varying standard deviation of the observations, as a function of the forecast start month (ordinate) and target month (abscissa; superscripts 0, 1, 2 denote the current and subsequent years, respectively), for the nRO, cross-validated nRO, XRO, cross-validated XRO, AI model, dynamical models from the North American Multi-Model Ensemble (NMME) project (multi-model ensemble of NMME, ensemble mean from individual models). The dashed vertical blue lines denote the spring predictability barrier season. The superior efficacy of the XRO in ENSO forecasting is supported by the RMSE metric.

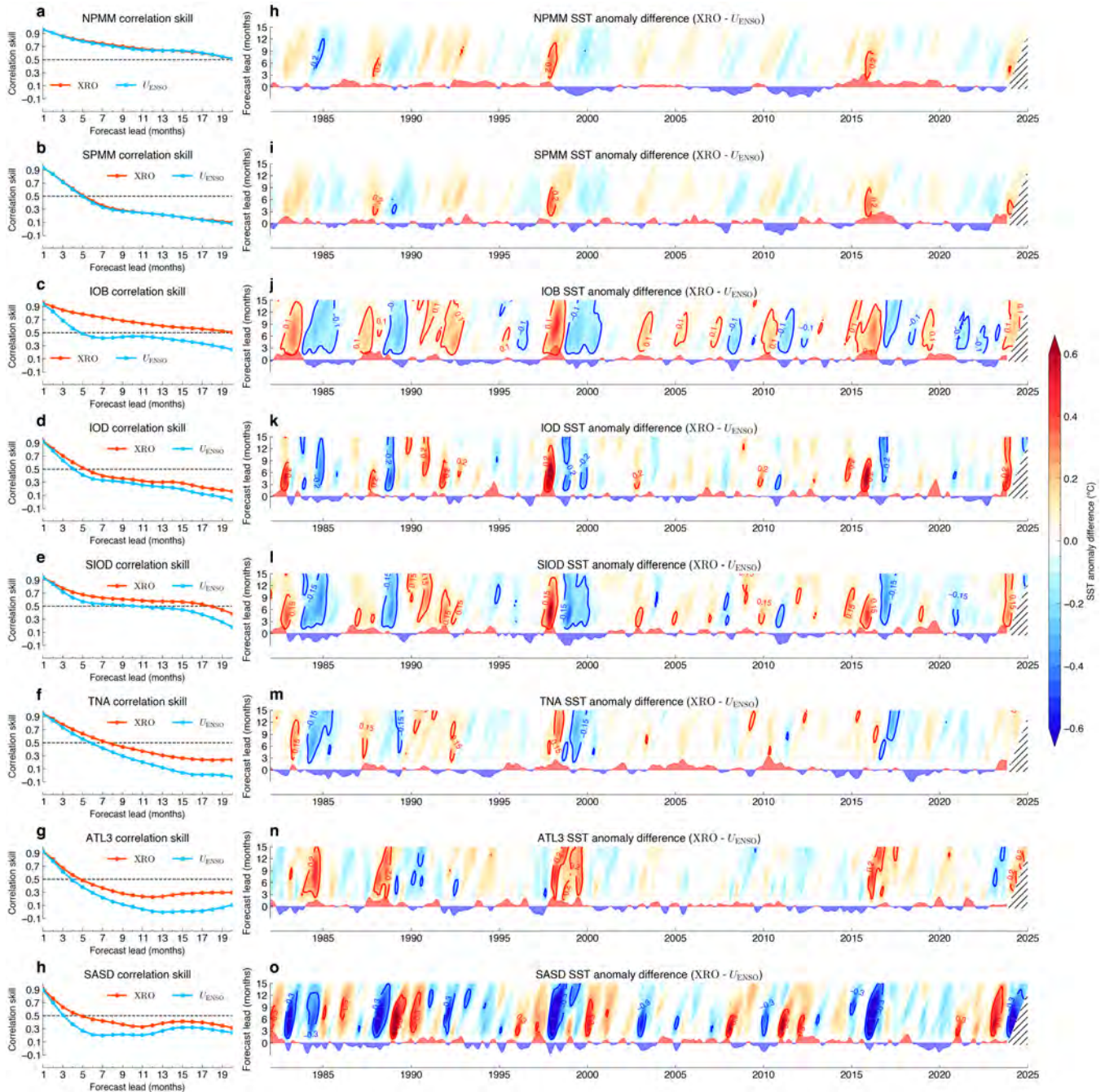


Supplementary Fig. 11 | Comparison role of climate-mode interactions on Niño3.4 forecast between the component due to other climate modes' initial state and the component due to the ENSO initial state. Shown are the differences of Niño3.4 SSTA (*shading*) as a function of forecast lead and target time between the control and uninitialized ExPO+IO+AO experiment (a), and between the uninitialized ExPO+IO+AO and decoupled ExPO+IO+AO experiment forecasts (b). Vertical reference dashed lines denote December of El Niño (red) and La Niña (blue) years, respectively. The observed normalized time series of Niño3.4 SSTA index is indicated in the bottom axis. In b, the arrows indicate the flow of forecast integration started from the selected time. The other climate modes mainly affect ENSO via their initial condition memory.



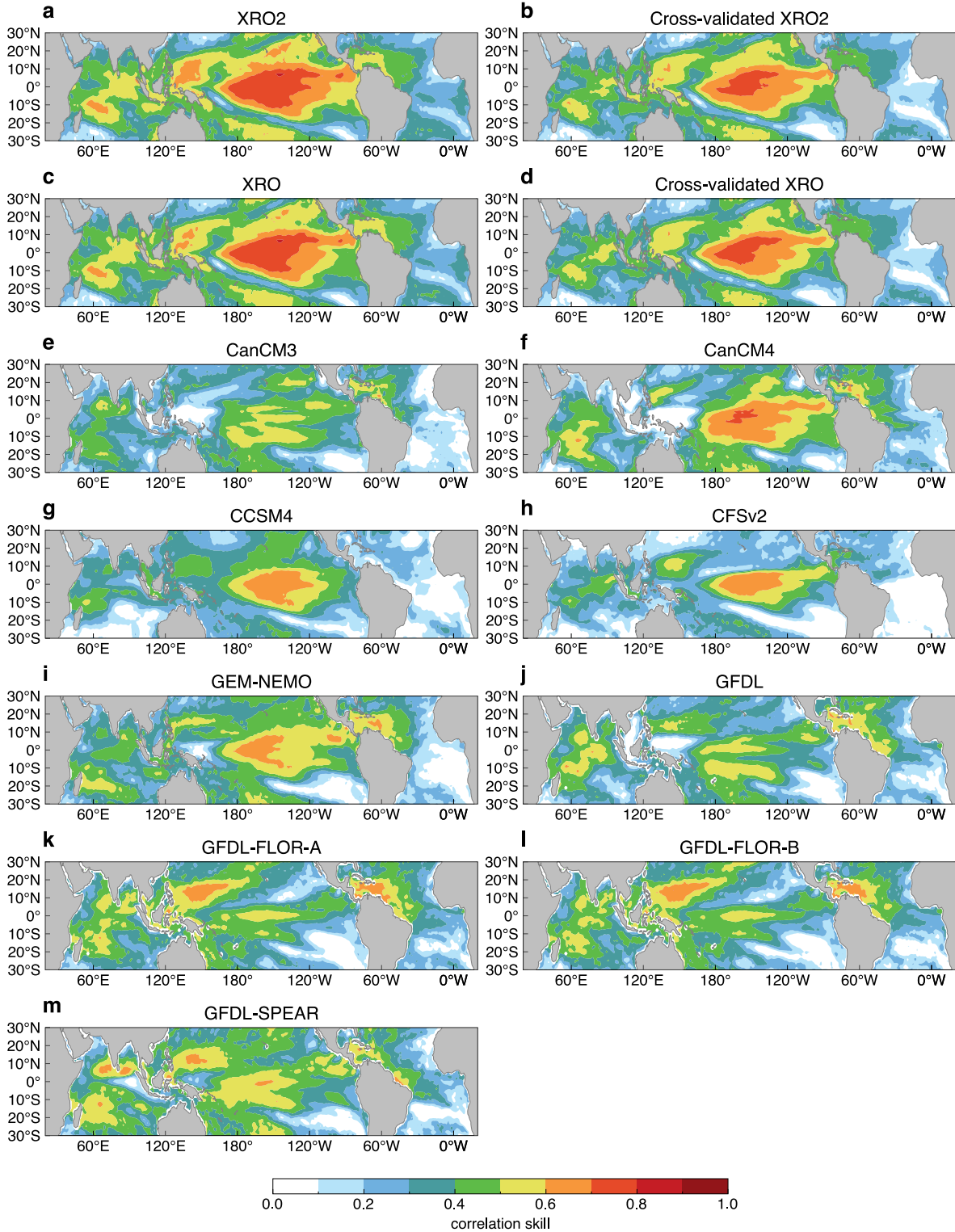
Supplementary Fig. 12| Quantifying the reduced ENSO forecast Root Mean Square Error (RMSE) from the coupled influences outside equatorial Pacific during 1979-2022. Shown is the relative RMSE difference of the Niño3.4 SSTA forecasts, normalized by the seasonally-varying standard deviation of the observations, as a function of the forecast start month (ordinate) and target month (abscissa; superscripts 0, 1, 2 denote the current and subsequent years, respectively). **a-d**, the skill difference between XRO and $D_{\text{ExPO+IO+AO}}$ (a), between XRO and $U_{\text{ExPO+IO+AO}}$ (b), and between $U_{\text{ExPO+IO+AO}}$ and $D_{\text{ExPO+IO+AO}}$ (c); **e-n**, the skill difference between control and the uninitialized ExPO, IO, AO, NPMM, SPMM, IOB, IOD, TNA, and SASD (n),

SIOD, TNA, ATL3, and SASD experiments, respectively. The importance of climate mode interactions in ENSO forecasting is supported by the RMSE metric.



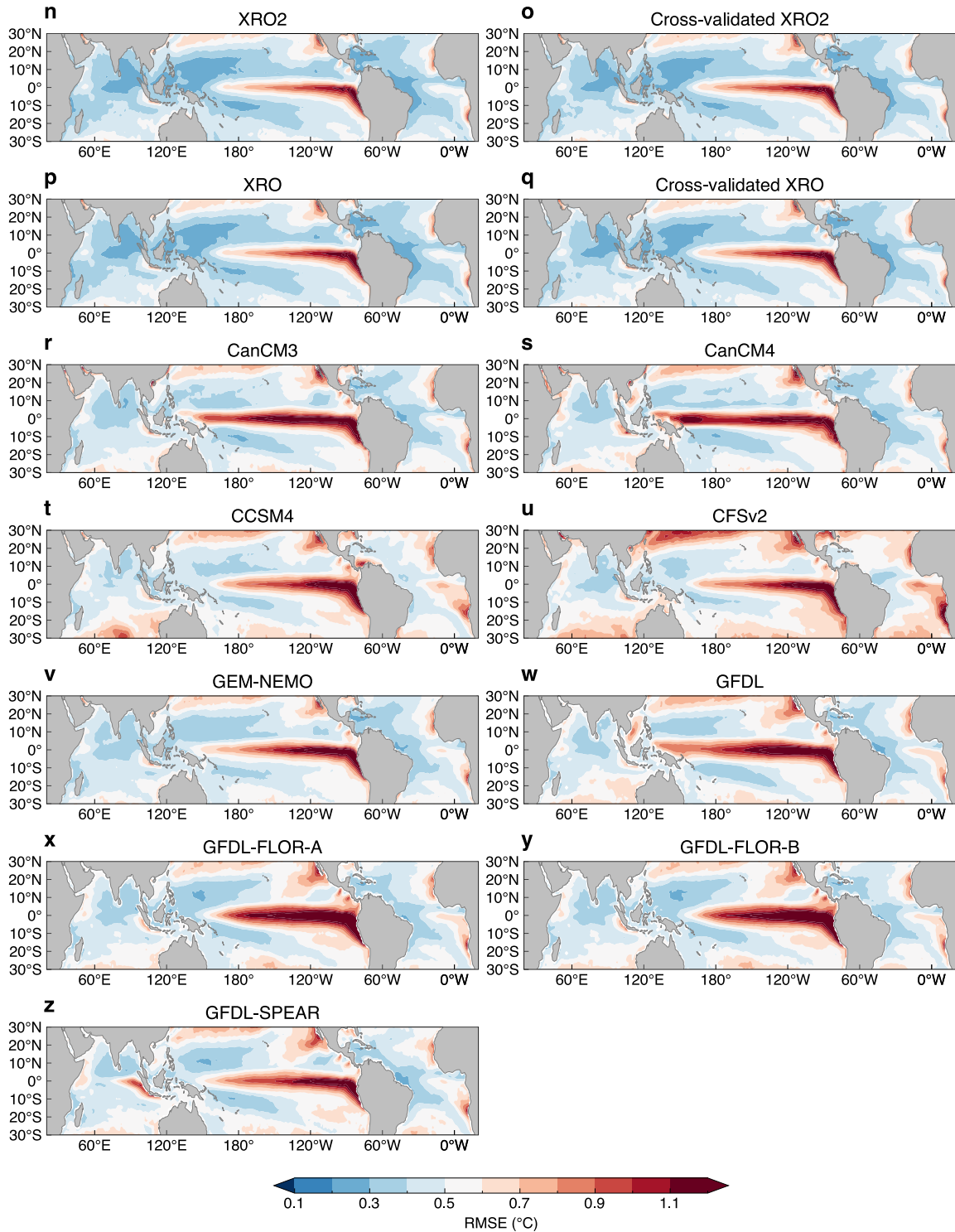
Supplementary Fig. 13 | Impact of ENSO's initialization to other climate mode forecasts. Left panels (a-h) show the all-months correlation skill of the 3-month running mean each climate mode index during 1979-2022 as a function of forecast lead for the XRO control forecast (*red curve*) and uninitialized ENSO experiment (U_{ENSO}) forecast (*blue curve*). Right panels (h-o) show the difference of other climate mode SSTA (shading) as a function of forecast lead and target time, between control and uninitialized ENSO experiment (U_{ENSO}). The normalized time series of each climate mode SSTA index is indicated in the bottom axis. The XRO sensitivity experiments quantify how the initial states of ENSO affect the predictability of the other climate modes.

SSTA forecast correlation skill at 9-month lead

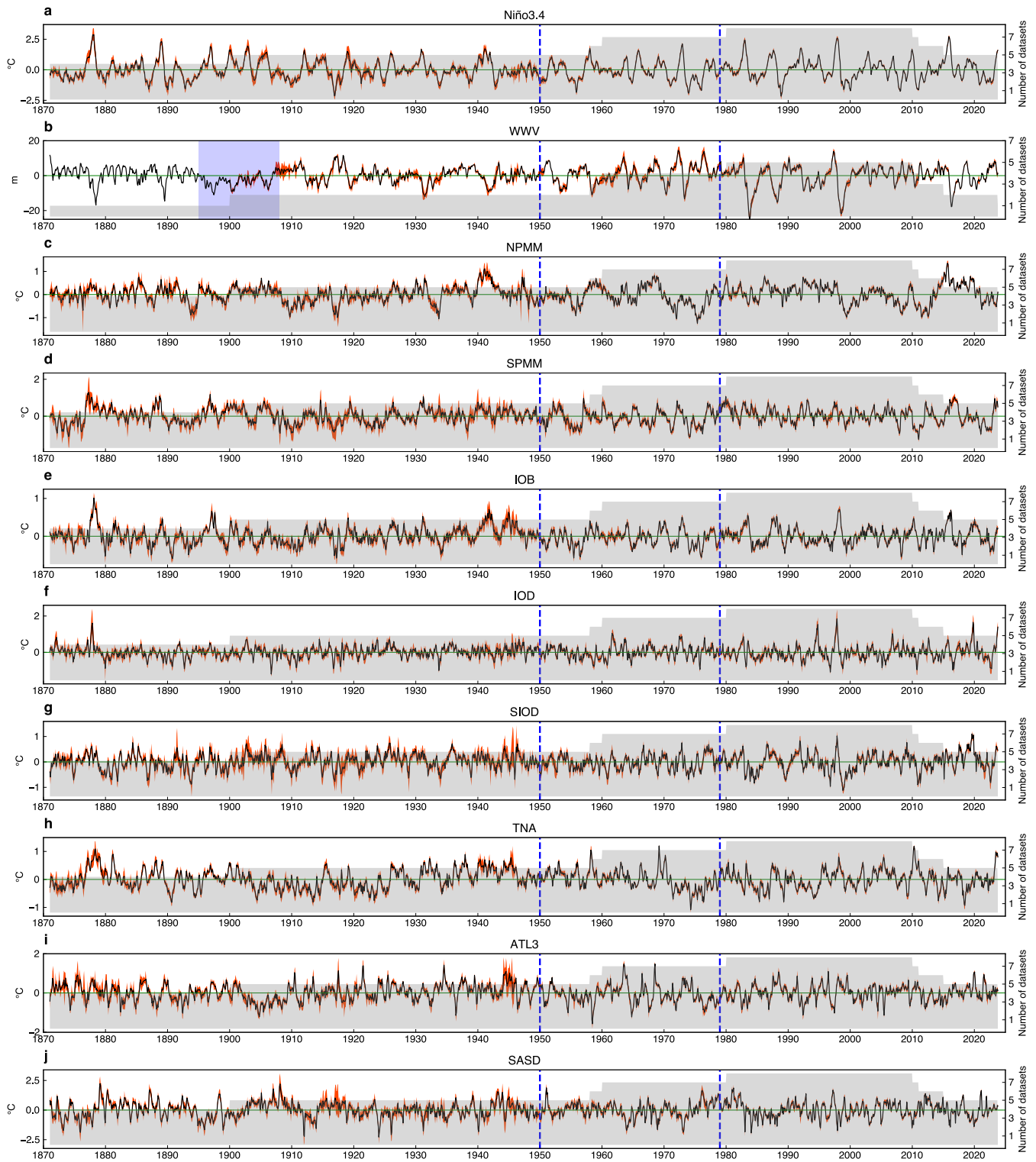


(continued)

SSTA forecast RMSE skill at 9-month lead

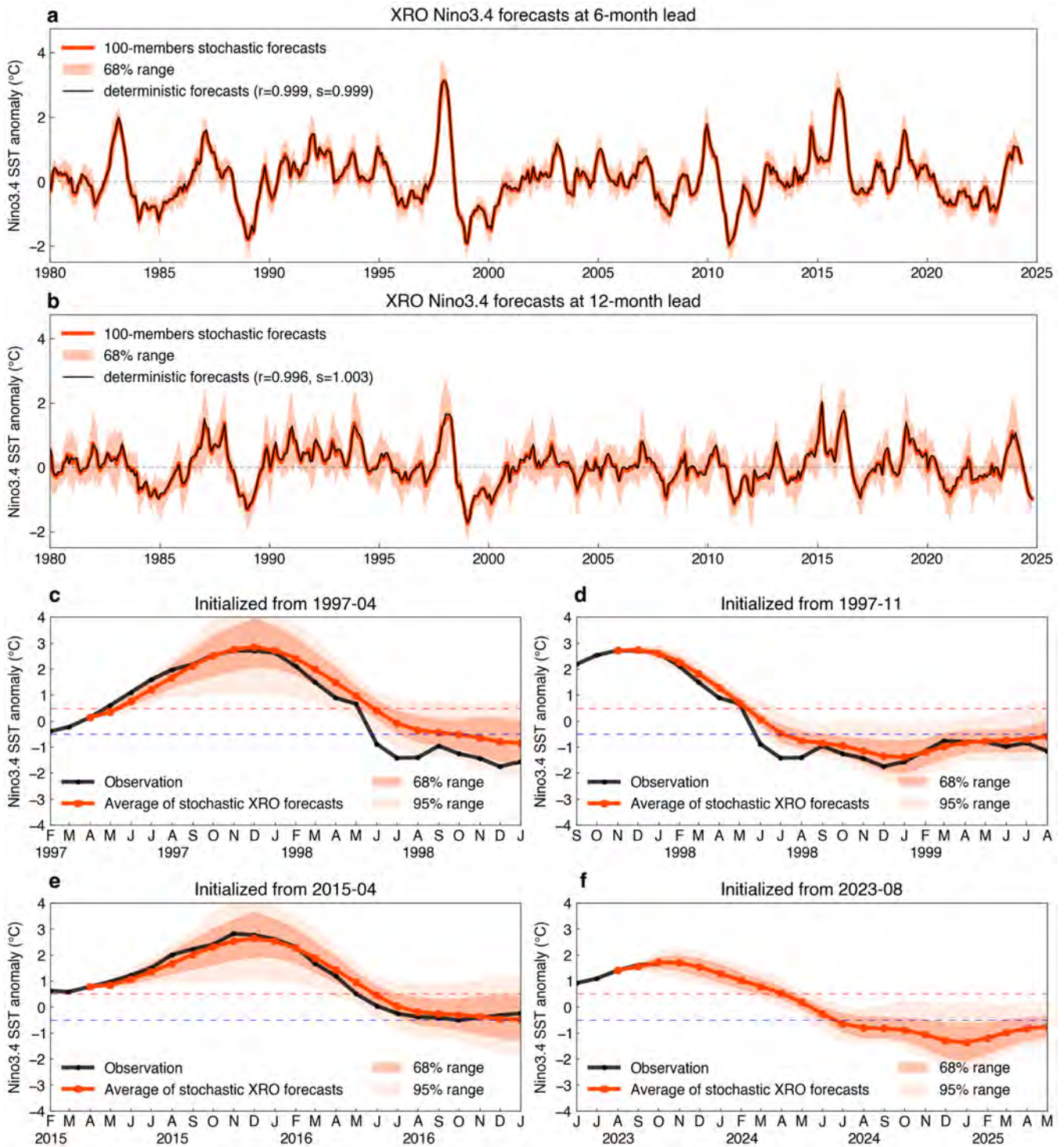


Supplementary Fig. 14| Pantropical SSTA forecast skill at 9-month lead time verified on 1982-2022. Correlation skill (a-m) and RMSE (n-z) for the SST forecasts include XRO2, cross-validated XRO2, XRO, cross-validated XRO, and the available nine NMME models. The XRO2 provide more skilful SSTA forecast than the operatorial climate models in most of the pantropical regions.



Supplementary Fig. 15| Time series of various SSTA indices and WWV anomaly index in multiple observation/reanalysis datasets. SST datasets include (HadISST: 1871-2023, ERSSTv5: 1871-2023, COBE-SST2: 1871-2023, ORAS5: 1958-2023, SODA224: 1871-2010, ORA20C: 1900-2009, PEODAS: 1960-2014, GECCO3: 1948-2018, GODAS: 1980-2023), WWV datasets include (ORAS5: 1958-2023, SODA224: 1871-2010, ORA20C: 1900-2009, PEODAS: 1960-2014, GECCO3: 1948-2018, GODAS:

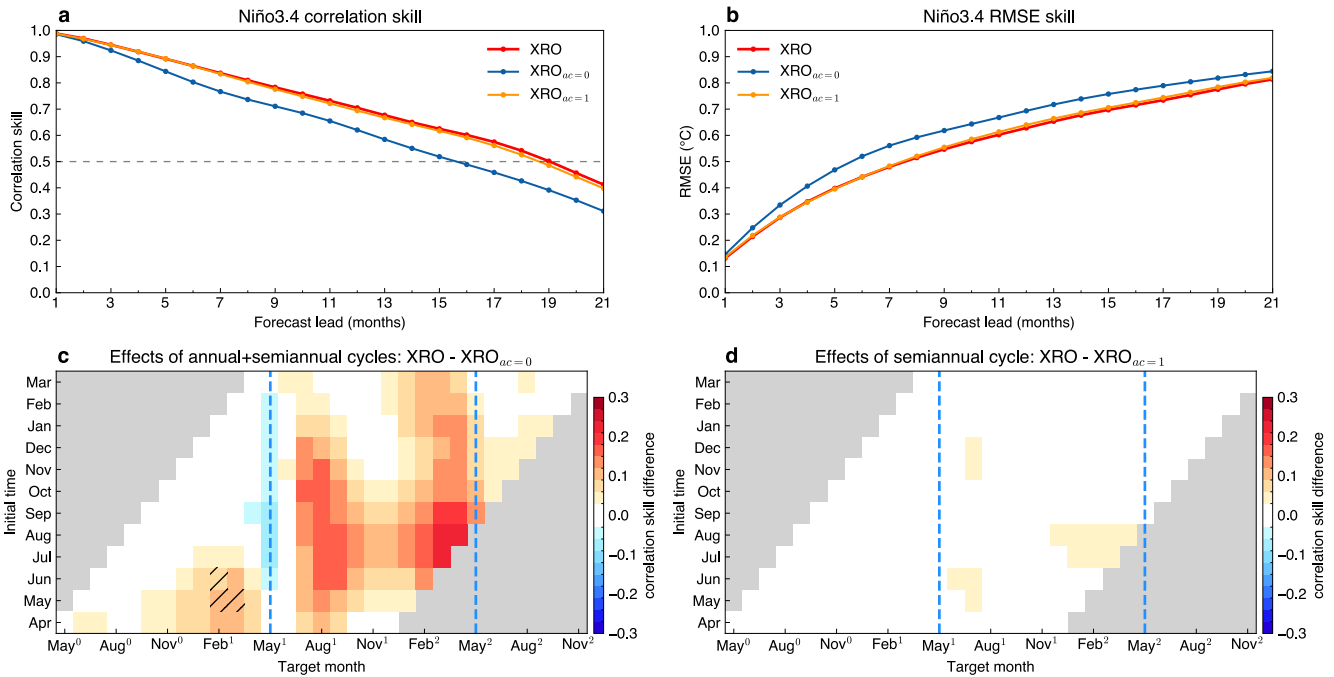
1980-2023). The monthly anomalies were calculated by removing the monthly climatology for 1980-2010 and the quadratic trend over the whole period. The black curve is mean of all datasets, the red shading denotes the 10%-90% inter-dataset spread, the grey shading indicates the number of datasets calculated for each month, the blue vertical reference lines denote January of 1950 and 1979. There are large uncertainties in the data before 1950, especially for equatorial Pacific WWV and SSTA in other basins (large inter-dataset spread shown by red shadings), and during time of World War II (1936-1949). There are also periods that are not physically consistent with current theory or understanding of ENSO, for instance, the multiple El Niño events occurred when a long period of discharged WWV state during 1895-1908 (blue shading period, compare with the Nino34 SSTA and WWV anomaly).



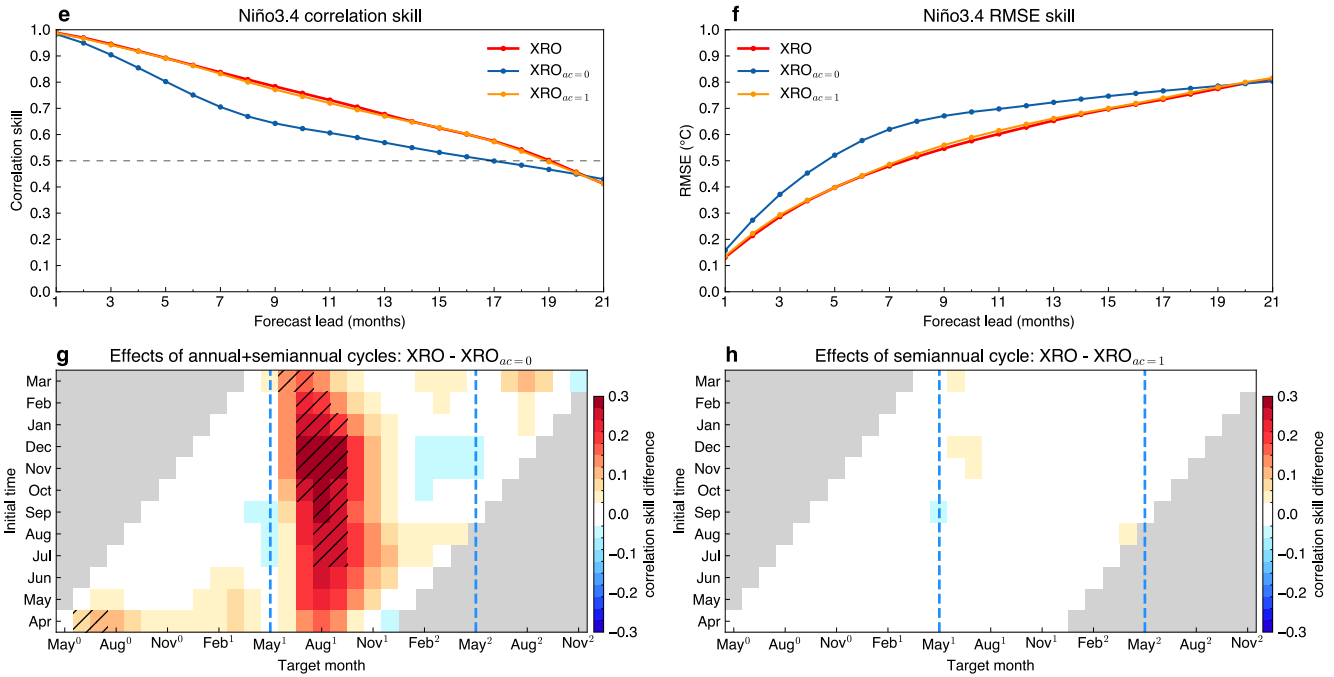
Supplementary Fig. 16 100-member stochastic forecasts of ENSO by the XRO. **a-b**, Time series of XRO-forecasted Niño3.4 SSTA, at lead-times of (a) 6 months and (b) 12 months. Black curves correspond to a deterministic forecast, in which the stochastic forcing term is neglected during the integration. Forecasts from a 100-member stochastic XRO ensemble are shown in red (dark red for the ensemble mean, red shadings indicate the central 68% range of the ensemble members). The correlation and regression slope between the deterministic forecast and the stochastic ensemble mean are indicated in the

corresponding legends. **c-f**, Niño3.4 SSTA forecasts initialized in (a) 1997 April, (b) 1997 November, (c) 2015 April, and (d) 2023 August. Red curves show the ensemble-mean XRO forecast; dark red envelope is the central 68% range of the ensemble members; lighter red is the central 95% range; black curves show the observations. The ensemble mean of the XRO stochastic forecasts is almost identical to the deterministic XRO forecast. The XRO stochastic forecasts provide an opportunity for probabilistic ENSO forecasts. The seasonality of the ENSO growth rate leads to a substantial spread in forecast outcomes from November to February. This inherent spread reflects a higher degree of uncertainty in predicting the peak amplitude of ENSO during this period. Conversely, from April to June, the forecast spread is narrower. However, this does not necessarily imply a better forecast skill, as the actual signal during this period is quite weak, resulting in a low signal-to-noise ratio.

**Effects of operator annual and semiannual cycles on ENSO's forecast skills
(Parameters refitted separately)**



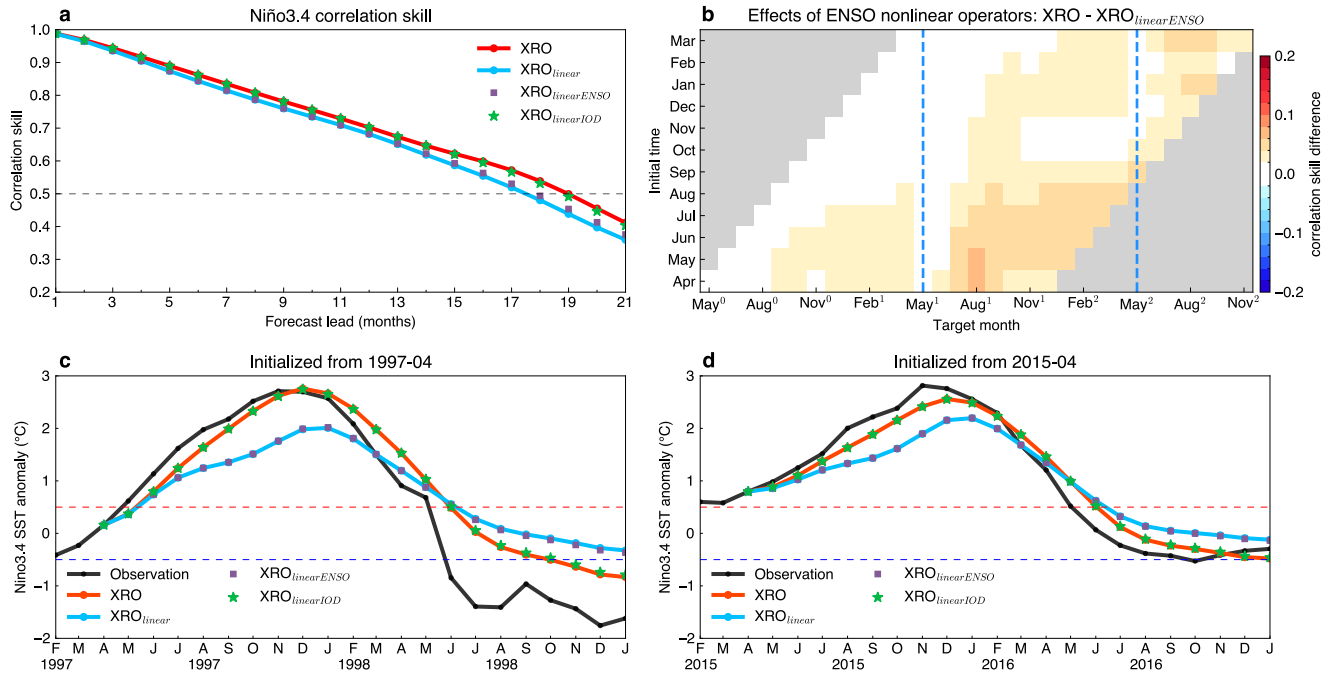
**Effects of operator annual and semiannual cycles on ENSO's forecast skills
(Parameters taken from XRO control)**



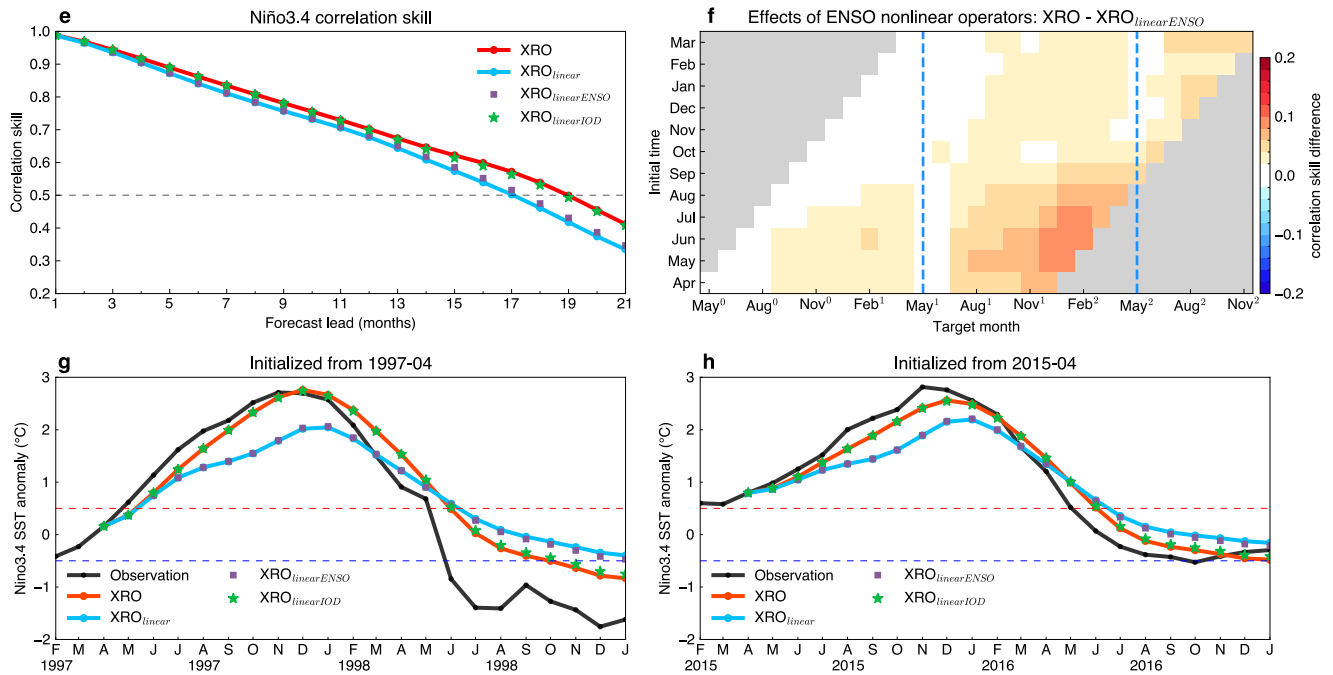
Supplementary Fig. 17| Effects of the XRO operator's annual and semiannual cycles on its ENSO forecast skill during 1979-2022. a-b, The all-months (a) correlation skill and (b) RMSE of the forecasted 3-month running mean Niño3.4 SSTA index, as a function of forecast lead, for the XRO in which the annual mean, annual cycle, and semiannual components are all considered in the linear and nonlinear parameters (*red*), XRO_{ac=0} in which only the annual mean component is considered (*blue*), and XRO_{ac=1}

in which both the annual mean and annual cycle components are considered (*orange*). **c-d**, the skill difference of the Niño3.4 index, as a function of start month (ordinate) and target month (abscissa), between XRO and the deseasonalized experiments: (c) $XRO_{ac=0}$ and (d) $XRO_{ac=1}$. Hatching indicates that the correlation difference is significant at 90% confidence level using the two-tailed Fisher z-transformation test. The dashed vertical blue lines denote the spring predictability barrier (SPB) season. **a-d**, the parameters for $XRO_{ac=0}$ and $XRO_{ac=1}$ are refitted separately; **e-h**, same as **a-d**, but for $XRO_{ac=0}$ and $XRO_{ac=1}$ in which the parameters are taken from the XRO control experiment. The seasonal cycle is critically important for suppressing the SPB for ENSO, while the semi-annual cycle is less important.

**Effects of nonlinear operators on ENSO's forecast skills
(Parameters refitted separately)**



**Effects of nonlinear operators on ENSO's forecast skills
(Parameters taken from XRO control)**



Supplementary Fig. 18| Effects of the XRO nonlinear operators on its ENSO forecast skill during 1979–2022. **a**, The all-months (a) correlation skill of the forecasted 3-month running mean Niño3.4 SSTA index, as a function of forecast lead for the XRO control (*red*), XRO_{linear} (*blue*), XRO_{linear}ENSO (*purple square*), and XRO_{linear}IOD (*green stars*). **b**, the skill difference of the Niño3.4 index, as a function of start month (ordinate) and target month (abscissa), between XRO and XRO_{linear}ENSO. The dashed vertical blue lines denote the spring predictability barrier season. **c-d**, monthly Niño3.4 SSTA forecasts initialized in

(a) 1997 April and (b) 2015 April for the XRO control (*red*), XRO_{linear} (*blue*), $XRO_{\text{linearENS0}}$ (*purple square*), and $XRO_{\text{linearIOD}}$ (*green stars*); black curves show the observations. **a-d**, the parameters for XRO_{linear} , $XRO_{\text{linearENS0}}$, and $XRO_{\text{linearIOD}}$ are refitted separately; **e-h**, same as **a-d**, but for XRO_{linear} , $XRO_{\text{linearENS0}}$, and $XRO_{\text{linearIOD}}$ in which the parameters are taken from the XRO control experiment. The ENSO nonlinear dynamics are critically important for ENSO forecast skill, especially for forecasting the amplitude of the peak phase and fast transition from El Niño to La Niña. The impact of the IOD's nonlinearity on ENSO forecast skill is neglectable.

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