

Dynamical prediction of Arctic sea ice modes of variability

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1 ABSTRACT

2

3 This study explores the prediction skill of the northern hemisphere (NH) sea ice thickness
4 (SIT) modes of variability in a state-of-the-art coupled forecast system with respect to two
5 statistical forecast benchmarks. Application of the K-means clustering method on a
6 historical reconstruction of SIT from 1958-2013, produced by an ocean-sea-ice general
7 circulation model, identifies three Arctic SIT clusters or modes of climate variability. These
8 SIT modes have consistent patterns in different calendar months and their discrete time
9 series of occurrences show persistence on intraseasonal to interannual time scales. We use
10 the EC-Earth2.3 coupled climate model to produce 5-member 12-month-long monthly
11 forecasts of the NH SIT modes initialized on 1 May and 1 November every year from 1979
12 to 2010. We use a three-state first-order Markov chain and climatological probability
13 forecasts determined from the historical SIT mode reconstruction as two statistical
14 reference forecasts. The analysis of ranked probability skill scores (RPSSs) relating these
15 three forecast systems shows that the dynamical SIT mode forecasts typically have a higher
16 skill than the Markov chain forecasts, which are overall better than climatological forecasts.
17 The evolution of RPSS in forecast time indicates that the transition from the sea-ice melting
18 season to growing season in the EC-Earth2.3 forecasts, with respect to the Markov chain
19 model, typically leads to the improvement of prediction skill. The reliability diagrams
20 overall show better reliability of the dynamical forecasts than that of the Markov chain
21 model, especially for 1 May start dates, while dynamical forecasts with 1 November start
22 dates are overconfident. The relative operating characteristics (ROC) diagrams confirm this
23 hierarchy of forecast skill among these three forecast systems. Furthermore, ROC diagrams
24 stratified in groups of 3 sequential forecast months show that Arctic SIT mode forecasts
25 initialized on 1 November typically lose resolution with forecast time more slowly than
26 forecasts initialized on 1 May.

27

28 **Keywords:** Arctic, sea ice thickness, GCM reconstruction, K-means cluster analysis,
29 climate variability, coupled climate prediction, Markov chain model, prediction skill, RPSS,
30 reliability and ROC diagrams

31

32 **1. Introduction**

33

34 The Earth's climate system and its components, including the atmosphere, oceans and sea
35 ice, are a complex adaptive system that can exhibit multiple equilibria over a wide
36 spectrum of characteristic spatial and temporal scales (Dijkstra 2014; Serreze and Barry
37 2014). Nonlinear geophysical fluid dynamics that govern the motion of climate system
38 components can lead to the emergence of quasi-stationary flow regimes in the form of
39 persistent or recurrent large-scale modes or patterns. Weather regimes are examples of
40 such flow regimes that are manifested as particular atmospheric conditions on a regional
41 scale with time scales roughly on the range of 10-100 days (Reinhold and Pierrehumbert
42 1982; Barnston and Livezey 1987; Vautard and Legras 1988; Ghil and Robertson 2002).
43 The application of the concept of weather regimes in the analysis of mid- and high-latitude
44 synoptic systems has provided us with a deeper understanding of intrinsic climate
45 variability (Molteni et al. 1990; Michelangeli et al. 1995; Cassou et al. 2004; Guemas et al.
46 2009), with potential benefits to weather and climate prediction capability (Mo and Ghil
47 1988; Brankovic and Molteni 1997; Cassou 2008; Riddle et al. 2013) and possibly to long-
48 term climate change (Corti et al. 1999).

49

50 A set of preferred circulation patterns is also identified in other atmospheric phenomena,
51 such as the monsoon systems around the globe that can be represented through the prism
52 of active and break phases (Jones and Carvalho 2002; Goswami 2005; Taraphdar et al.
53 2010; Cook et al. 2012; Meehl et al. 2012). Also, a spectrum of tropical and mid-latitude
54 regimes of cloud variability has been determined by clustering methods (Jakob and
55 Tselioudis 2003; Gordon et al. 2005; Cheruy and Aires 2009; Gordon and Norris, 2010).
56 The ocean circulation, with dominant wind-driven elements, also exhibits coherent flow
57 regimes in dynamic regions such as the Antarctic circumpolar current and the Kuroshio
58 extension (Hughes 2005; Qiu and Chen 2005).

59

60 Sea ice circulation, which is primarily driven by surface winds and upper-ocean currents
61 (Lepparanta 2011), also has the potential to exhibit regime behavior. Sea ice thickness
62 (SIT) is an integrating medium of the surface ocean and atmosphere conditions: it has the

63 capability to contain climate information on time scales longer than seasonal (Blanchard-
64 Wrigglesworth et al. 2011; Chevallier and Salas y Méria 2012; Guemas et al. 2014b). Fučkar
65 et al. (2015) extended the conceptual framework of recurrent large-scale modes to the sea
66 ice system and identified modes of the northern hemisphere (NH) sea ice cover variability
67 that persist from intraseasonal to interannual time scales. They applied the K-means
68 clustering technique (Hastie et al. 2009; Wilks 2011) on SIT from a forced historical
69 reconstruction of global sea ice cover (based on the approach in Guemas et al. 2014a) over
70 the 1958-2013 period to determine three optimal modes or clusters of variability of the NH
71 SIT, and the associated time series of cluster occurrences. Particularly the dynamics and
72 distribution of multi-year ice strongly depend on surface wind patterns, which opens the
73 possibility of imprinting of the high- and mid-latitude winter surface conditions onto the
74 sea ice system.

75
76 In this study we examine the prediction skill of these three NH SIT modes in a state-of-the-
77 art coupled climate forecast system. We aim to determine a hierarchy in quality of
78 dynamical and statistical forecast systems for the NH SIT modes, representing predictable
79 aspects of the Arctic sea ice system on monthly and longer time scales, based on a suite of
80 prediction skill indices. The rest of the manuscript is structured in the following way.
81 Section 2 briefly describes the historical reconstruction of sea ice cover (also used in the
82 next section as one of the initialization datasets for dynamical prediction), the clustering
83 methodology used to extract Arctic sea ice modes of variability and a selection of
84 corresponding results. Section 3 describes the coupled dynamical forecast system used to
85 produce climate predictions and two statistical reference forecast systems. Section 4
86 assesses the skill of the NH SIT cluster predictions with several widely-used forecast
87 quality metrics for categorical (here cluster or mode) predictions. The final section 5
88 includes conclusions, discussions and suggestions for future research.

89
90 **2. Historical reconstruction, clustering methodology and mode decomposition**

91
92 Making in situ or remote observations of SIT is a demanding task at any scale (e.g. Haas
93 2003, Kwok 2010). Hence the most practical option for obtaining spatially and temporarily

94 complete SIT is a combination of general circulation models (GCMs) and available
95 observations (which typically contain gaps) through various data assimilation or
96 reconstruction techniques (e.g. Zhang and Rothrock 2003; Massonnet et al. 2013). We focus
97 on the NH SIT obtained from the NEMO ocean-sea-ice GCM historical multi-member
98 reconstructions of Guemas et al. (2014a). Specifically, we use 5 ensemble members that
99 reconstruct the variability and change of the global sea ice field from 1958 to 2013 with the
100 Louvain-la-Neuve sea ice model version 2 (LIM2) embedded into the version 3.2 of the
101 Nucleus for European Modelling of the Ocean (NEMO) model using the standard tripolar
102 ORCA1L42 grid (approximately 1° resolution with enhanced resolution in the tropics and
103 two poles in the NH). To account for the oceanic sources of sea ice uncertainty, the ocean
104 temperature and salinity in historical reconstructions are nudged (restored) towards their
105 monthly values in the 5-member ORAS4 ocean reanalysis (Mogensen et al. 2011;
106 Balmaseda et al. 2012). Together with introduced surface wind perturbations to account
107 for the atmospheric uncertainty, nudging each member of the sea ice reconstruction
108 towards a different ORAS4 member allows us to sample sea ice uncertainty. Guemas et al.
109 (2014a) shows that the reconstructed SIT field is in reasonable agreement with the
110 available ICESat observations (Kwok and Cunningham 2008) and a reanalysis (Massonnet
111 et al. 2013). We employ the ensemble mean of these 5 historical reconstructions as the best
112 available estimate of complete SIT field in our modeling framework.

113
114 We build on the results of Fučkar et al. (2016) where the K-means clustering was used on
115 the ensemble monthly mean SIT from the 1958-2013 reconstruction discussed above to
116 determine K cluster centroids or modes (where the optimal number of cluster for the NH
117 SIT is $K=3$) and their time series of occurrences. The applied clustering methodology aims
118 to minimize the Euclidean distance between the members of a given cluster and
119 maximizing the distance between the centroids of the different clusters, so the time series
120 of cluster occurrences reveals the unique centroid (mode) to which the system is the
121 closest in a particular month (Wilks 2011). K-means clustering was chosen to reduce the
122 data dimensionality in a simple manner (using Euclidian distance) that avoids the
123 statistical constraints inherent in other unsupervised learning methods like principal

124 component analysis (PCA), such as orthogonality and linearity. Prior to cluster analysis, the
125 Arctic SIT was first coarse grained into 32 regions to make the method computationally
126 efficient and because there are typically less than 15 effective degrees of freedom of the
127 Arctic SIT fields in a GCM (Blanchard-Wrigglesworth and Bitz, 2014). Also, to determine
128 robust Arctic SIT variability clusters, a 2nd order polynomial approximation of the long-
129 term change was removed prior to applying the K-means clustering. This step is necessary
130 because, otherwise, the time series of NH SIT cluster occurrences in each month or season
131 is overwhelmed by the strong long-term decline in the NH SIT field (Kwok and Rothrock
132 2009). The monthly SIT centroid or mode patterns are determined as the average of the
133 anomalous NH SIT in each month belonging to each cluster or mode over the period of
134 interest.

135

136 The three NH SIT modes that were identified over the 1958-2013 period are: the Central
137 Arctic Thinning (CAT) mode (cluster 1), the Atlantic Pacific Dipole (APD) mode (cluster 2)
138 and the Canadian Siberian Dipole (CSD) mode (cluster 3). Furthermore, Fučkar et al., 2016
139 shows that their anomalous patterns range from predominately negative (thinning) CAT
140 mode to predominately positive (thickening) CSD mode. These three modes are consistent
141 throughout the calendar year but with small seasonal cycle variations in their centroid
142 patterns. For example, Fig. 1 shows the anomalous pattern of the CSD mode for different
143 calendar months. The monthly time series of the NH SIT mode occurrences are combined
144 into an occurrence matrix in Fig. 2 that markedly exhibits persistence on intraseasonal to
145 interannual time scales of the CAT, APD and CSD modes in the historical reconstruction.

146

147 **3. Dynamical prediction system and two statistical reference methods**

148

149 In this study we analyze five-member EC-Earth2.3 climate predictions in the standard
150 configuration. EC-Earth2.3 is a state-of-the-art coupled Earth system model
151 (<http://www.ec-earth.org/>) based on the operational seasonal forecast system of the
152 European Centre for Medium-Range Weather Forecasts (ECMWF) (Hazeleger et al. 2010;
153 2012). The atmospheric component is the ECMWF's Integrated Forecasting System (IFS)
154 with the standard horizontal resolution T159 and 62 vertical layers up to 5 hPa. IFS also

155 contains the land-surface H-TESSSEL model (Balsamo et al. 2009). This EC-Earth version
156 includes the NEMO2 ocean model (Madec, 2008), embedding the LIM2 sea ice model
157 (Fichefet and Morales Maqueda 1997; Bouillon et al. 2009), in the standard ORCA1L42
158 tripolar grid and 42 vertical layers. NEMO-LIM2 is coupled with IFS/H-TESSSEL through
159 OASIS3 every 3 hours (Valcke, 2013).

160
161 We performed 12-month ensemble climate predictions using a full-field initialization from
162 the selected atmospheric and oceanic reanalyses and sea ice reconstruction on every 1 May
163 and 1 November from 1979 to 2010. The atmospheric component is initialized from the
164 ERA-interim reanalysis (Dee et al., 2011) with initial perturbations between the members
165 computed using singular vectors (Du et al, 2012). The oceanic component of each climate
166 prediction member is initialized from one of the 5 members of the ORAS4 ocean reanalysis
167 (Balmaseda et al. 2012). The associated sea ice component of each climate prediction
168 member is initialized using one of the 5 members from the global sea ice reconstruction of
169 Guemas et al. (2014a).

170
171 This study addresses the question of how skillful the EC-Earth2.3 monthly predictions of
172 Arctic SIT modes are out to a 12-month forecast horizon. However, in the rest of this
173 section we first focus on two benchmark statistical forecasts: climatological probability
174 forecast and a first-order Markov chain (Wilks 2011). A simple climatological forecast is
175 based on recorded frequency of the three Arctic SIT modes, separately for each
176 climatological month, in the historical reconstruction. We cross-validate all statistical
177 forecasts by excluding the forecast year from the training data. For example, based on Fig.
178 2, the climatological probability forecast for May 1979 is 22/55, 15/55 and 18/55 for CAT,
179 APD and CSD modes, respectively.

180
181 A more elaborate statistical method that can potentially account for the historical
182 persistence of Arctic SIT modes is a three-state first-order Markov Chain (Wilks 2011). It
183 has the Markovian property, i.e. the future state of the system depends only on the current
184 state of the system and not on any previous state: $\Pr\{X_{t+1} | X_t, X_{t-1}, \dots, X_1\} = \Pr\{X_{t+1} | X_t\}$.
185 Markov chain models of discrete states have been applied to determine the evolution of a

186 number of weather and climate phenomena (e.g. Fraedrich and Klauss 1983; Ghil and
 187 Robertson 2002; Jones 2009). For continuous variables this process is referred to as a first-
 188 order autoregressive (AR1) model or red noise process. For the three Arctic SIT modes and
 189 their discrete occurrences, the Markovian property means that the probability of
 190 occurrence of a particular mode in month $f+1$ depends only on which of three modes
 191 occurred in month f based on the matrix of transition probabilities. We estimate
 192 conditional transition probabilities p_{ji} (which indicate the probability of mode i in the
 193 current month transitioning to mode j in the next month) combined for all months from the
 194 reconstructed historical record of Arctic SIT mode occurrences shown in Fig. 2.

195
 196 A K -state first-order Markov chain transition probabilities constitute a $K \times K$ transition
 197 matrix \mathbf{T} , where $K=3$ is for the Arctic SIT modes. The diagonal elements of \mathbf{T} (the probability
 198 of the Arctic SIT mode remaining in its current state) represent the persistence of the
 199 Arctic SIT mode, whereas the off-diagonal elements represent the transition to other
 200 modes. The initial state vector for this problem consists of a value of 1 for the initial
 201 monthly state of Arctic SIT mode and 0 for the two other modes. For example, if we are
 202 making a forecast for May through the following April, and if the Arctic mode in the
 203 preceding April is in CAT mode (or cluster 1), then the initial state vector is:

$$\mathbf{x}^{(0)} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}. \quad (1)$$

206
 207 For a first-order Markov chain forecast, the state vector indicating the probability of Arctic
 208 SIT mode occurrences at forecast month f months is given by

$$\mathbf{x}^{(f)} = \mathbf{T}^f \mathbf{x}^{(0)}. \quad (2)$$

211
 212 For the present application, $\mathbf{x}^{(f)}$ represents a probabilistic SIT mode forecast, where f varies
 213 from 1 to 12 months. For a very large forecast horizon f the first-order Markov chain
 214 forecast converges to the climatological forecast.

215
 216 We now assess the quality of probabilistic forecasts of Arctic SIT modes generated by the
 217 three-state first-order Markov chain (2) with respect to a climatological frequency forecast.
 218 We generate 12-month forecasts for 1 May and 1 November start dates over the 1979-2010
 219 period matching the period of available EC-Earth2.3 predictions. For each forecast, in our
 220 cross-validation approach, we estimate a new transition matrix \mathbf{T} based on the transition
 221 frequencies for the whole historical reconstruction excluding the 12 target forecast
 222 months, as explained above. Hence, our estimate of the transition matrix \mathbf{T} varies slightly
 223 for each of the 32 forecast years and both start dates in order to ensure that the training
 224 and forecast data remain independent, but \mathbf{T} has no other dependence. The Arctic SIT
 225 modes tend to persist for multiple seasons, including through the changes between sea-ice
 226 growing and melting seasons (Fig. 2), hence we constructed \mathbf{T} without seasonal
 227 dependence. Table 1 shows the mean \mathbf{T} of CAT, APD and CSD modes for the 1958-2013
 228 period constituted as the average of cross-validated transition matrices for forecast years
 229 from 1979 to 2010 (using both start dates).

230
 231 We evaluate the skill of the first-order Markov chain forecasts with the ranked probability
 232 skill score (RPSS) based on the ranked probability score (RPS). RPS is the sum of squared
 233 differences between the cumulative forecast and reconstruction vectors that is defined for
 234 a single month as

$$235 \quad \text{RPS} = \sum_{i=1}^K (\sum_{j=1}^i F_j - \sum_{j=1}^i O_j)^2, \quad (3)$$

236
 237 where F_j is forecast probability of occurrence of SIT cluster j and O_j is the reconstructed
 238 historical occurrence of Arctic SIT mode j (either 0 for non-occurrence or 1 for occurrence).
 239 RPS is an extension of the Brier Score for the assessment of probabilistic categorical
 240 forecast having more than two categories that also ranges from 0 for perfect skill to 1 for
 241 no skill (Wilks 2011). Through the incorporation of cumulative probabilities, this measure
 242 takes into account that the clusters are generally ordered from lowest to highest SIT
 243 anomalies. The RPSS for a single monthly forecast is computed as

244

245
$$\text{RPSS} = 1 - \frac{\text{RPS}}{\text{RPS}_{ref}}, \quad (4)$$

246 where RPS_{ref} in this case stands for the RPS of climatological probability forecast RPS_{clim} .
 248 RPSS values greater than zero indicate greater skill of the first-order Markov chain than a
 249 climatological forecast, while 1 indicates perfect skill, and values below 0 indicate lower
 250 skill than a climatological forecast.

251 Fig. 3 shows the RPSS median, $\langle \text{RPSS} \rangle = 1 - \langle \text{RPS} \rangle / \langle \text{RPS}_{ref} \rangle$, from start year 1979 to 2010
 253 of the first-order Markov chain forecasts, with respect to the climatological forecast, as a
 254 function of forecast month for both start dates of EC-Earth2.3 seasonal predictions. For the
 255 first 5 forecast months the median RPSS of both 1 May and 1 November start dates indicate
 256 significantly positive skill. Afterwards the median RPSS of forecast initialized in autumn
 257 drops rapidly to the vicinity of zero. This rapid skill drop in Fig. 3 coincides with a switch
 258 from the boreal sea-ice growing season to melting season in April. This is compatible with
 259 findings of Holland et al. (2011) with the NCAR Community Climate System Model, version
 260 3, where summer thermodynamic forcing reduces inherent predictability. Similarly, Day et
 261 al. (2014) shows that a melt season “predictability barrier” is a robust feature of five global
 262 climate models.

263 A skill index or single-number summary of forecast quality such as the RPSS provides
 264 valuable insight, but more comprehensive understanding of forecast performance requires
 265 analysis of the joint distribution of the forecasts and the historical reconstruction used for
 266 verification. The reliability diagram shows the historical event frequency versus the
 267 forecast probability divided into a number of bins (Wilks 2011; Jolliffe and Stephenson
 268 2012). It examines how well forecast probabilities correspond to the actual event
 269 frequencies, or how well “calibrated” the forecast probabilities are. Fig. 4 shows that first-
 270 order Markov chain forecasts of the CSD mode (bottom panels) are on average less reliable,
 271 i.e. the calibration function lies farther away from the perfect reliability diagonal, than the
 272 forecasts of the CAT and APD modes (top and middle panels). The observed relative
 273 frequency of the CSD mode tends to be higher than the forecast probability, which indicates
 274 a negative forecast bias in the Markov chain forecasts. Other than this bias, the Markov
 275

276 chain forecasts are relatively reliable for the other modes, with no clear tendency for
277 overconfidence or underconfidence. The histograms of the forecast probabilities in the
278 lower right corner of each plot are peaked near the climatological frequency of occurrence
279 of each mode, which reflects the loss of sharpness (i.e., the range of probabilities) in the
280 forecasts as the forecast horizons advance.

281
282 In summary, the three-state first-order Markov chain model provides better skill and more
283 insight into the predictability of the Arctic SIT modes than a simple climatology.
284 Persistence could account for useful skill for about 5 months, and longer in the case of
285 spring initialization. The skill of the Markov chain and climatological forecast will be used
286 in the following section as benchmarks for the Arctic mode predictions with EC-Earth2.3

287

288 **4. Skill assessment of dynamical predictions of Arctic SIT modes**

289
290 After introduction of two statistical models for reference forecasts we assess the
291 performance of 5-member 12-month-long EC-Earth2.3 coupled climate predictions of the
292 Arctic SIT modes in capturing the reconstructed historical SIT mode variability over the
293 1979-2010 period. EC-Earth2.3 monthly predictions of mean SIT in the 32 selected regions
294 in the NH defined in Fučkar et al. (2015) are trend bias corrected (Kharin et al. 2012;
295 Fučkar et al. 2014) to minimize their root mean square error. We use various prediction
296 skill measures, such as accuracy, RPSS, reliability diagram and relative operating
297 characteristic (ROC: hit rate versus false alarm rate) diagram to examine dynamical
298 forecast quality.

299
300 Accuracy simply tells us what fraction of the ensemble forecasts in a specific month
301 predicts the correct Arctic SIT mode. Fig. 5 shows matrices of accuracy of ensemble EC-
302 Earth2.3 SIT mode forecasts as a function of the forecast month on the abscissa and the
303 start year on the ordinate (along with the historical SIT mode in a month just before the
304 start date). Specifically, if the majority of ensemble members make a wrong prediction
305 (accuracy less than 0.6) in a forecast month, this month is shaded with grey color in Fig. 5,
306 otherwise it is shaded with the designated primary color of the recorded historical SIT

307 mode (from Fig. 2). For the first 6 forecast months, on average the accuracy of EC-Earth2.3
308 predictions is larger when initialized in fall than in spring. For the longer forecast horizons
309 in Fig. 5, the opposite is indicated. This indicates that the switch from sea-ice melting
310 season to growing season in the dynamical system typically leads to improvement of
311 prediction skill, while often the opposite is the case for the switch from growing season to
312 melting season. Also, every forecast month shaded with one of the primary colors in Fig. 5
313 has RPS values smaller than 0.2 (not shown).

314
315 RPSS matrices of EC-Earth2.3 SIT mode forecasts as a function of the forecast month on the
316 abscissa and the start year on the ordinate in Fig. 6 (using a three-state first-order Markov
317 chain as the statistical reference forecast) roughly resemble the accuracy matrices shown
318 in Fig. 5. Particularly after spring initialization for the forecast horizons longer than 5
319 months, when a majority of ensemble members correctly predict the historical mode, RPSS
320 exhibits high skill (marked by darker shades of purple color), which demonstrates a
321 significant added value of the dynamical forecast over the first-order Markov chain in
322 growing season. Fig. 7 compresses RPSS matrices by presenting the RPSS median in Fig. 6
323 along the start years 1979 to 2010 (i.e. along the ordinate) to show that the first-order
324 Markov chain initialized on 1 May outperforms EC-Earth2.3 forecasts in the first month.
325 This could be potentially attributed to initialization shock and missing or crudely
326 represented physical processes in the sea ice model LIM2 such as melt ponds, wind
327 redistribution of snow and simple solar penetration scheme. These processes are very
328 important during the melting season, but much less so during the growing season (Notz
329 2012). The RPSS median of the dynamical forecasts initialized in spring (red curve in Fig. 7)
330 show the emergence of positive skill with respect to the first-order Markov chain model
331 after the first forecast month. Fig. 7 shows a higher skill of the dynamical forecast
332 initialized in autumn than in spring over the first 5 months, but on the longer forecast
333 horizons this relationship reverses with the switch between melting and growing seasons.
334 Such behavior is in accord with findings that SIT and sea ice volume have typically greater
335 skill in winter than in any other season (Day et al. 2014; Guemas et al. 2014b). Overall, the
336 RPSS medians in Fig. 7 corroborate the information in Fig. 5 and Fig. 6. Furthermore, the

337 prevailing dominance of dynamical system over the Markov chain model emphasizes the
338 importance of well-resolved physical processes for the skill of the forecast system.

339
340 The RPSS matrices of EC-Earth2.3 mode forecasts with respect to climatological probability
341 forecasts as the reference (Fig. S1) show a better match with the accuracy matrices in Fig. 5
342 than with the RPSS matrices in Fig. 6. This again indicates that the first-order Markov chain
343 forecast is a more challenging statistical benchmark for the dynamical forecast system than
344 the climatological forecast. Furthermore, the RPSS median (over the start years 1979 to
345 2010) of the dynamical forecasts with respect to the climatological reference in Fig. 8
346 confirms that the Markov chain model is better than climatological probabilities in
347 capturing the persistence of Arctic SIT modes in the historical reconstruction. The RPSS
348 medians in Fig. 8 show a monotonic decline of positive skill with forecast time in contrast
349 to emergent RPSS median behavior with forecast time in Fig. 7 for 1 May initialization.

350
351 How reliable are dynamical forecasts of the three Arctic SIT modes in comparison with the
352 three-state first-order Markov chain model? The left panels in Fig. 9 indicates that the EC-
353 Earth2.3 probabilistic mode forecasts initialized on 1 May are more reliable than the
354 corresponding Markov chain forecasts (the left panels in Fig. 6), i.e. they are on average
355 closer to the diagonal of perfect reliability. There is only a slight tendency for
356 overconfidence in the CAT mode forecasts (Fig. 9a), but overall the dynamical forecasts are
357 well calibrated. The forecast probability histograms have greater spread than those of the
358 Markov chain model, indicating the dynamical forecasts have greater sharpness,
359 particularly at the longer forecast horizons. Overall, the left panels in Fig. 9 indicate that
360 the 5-member ensemble is sufficient for producing reliable probabilistic forecasts of SIT
361 mode occurrences when the forecasts are initialized in spring.

362
363 The EC-Earth2.3 probabilistic SIT mode forecasts initialized on 1 November, however, are
364 not nearly as well calibrated (the right panels in Fig. 9). All of Arctic SIT mode forecasts are
365 overconfident, especially those of the APD mode (Fig. 9e). These results suggest that the
366 ensemble size of 5 members is insufficient for reliable probabilistic mode forecasts when
367 EC-Earth2.3 is initialized in autumn: the model is underdispersive (i.e. ensemble spread is

368 too small). A possible explanation is that the dynamic SIT modes are more sensitive to the
369 large internal atmospheric variability in the winter months, hence more ensemble
370 members of EC_Earth2.3 would probably better capture the wide range of possible
371 realizations of internal variability of the Arctic sea ice system.

372
373 How good is the ability of the EC-Earth2.3 multi-member forecast system to discriminate
374 between the correct and incorrect Arctic SIT mode predictions? Resolution is an attribute
375 of forecast quality (Murphy 1993) that measures the success of a forecast system in
376 distinguishing one type of event, i.e. one SIT mode from another. To gain insight into the
377 resolution of probabilistic prediction skill, we combine hit rates and false alarm rates of the
378 three Arctic SIT modes. The hit rate of a mode k tells us what fraction of mode k is correctly
379 forecasted: it is equal to the number of correct mode k forecasts (hits) divided by the total
380 number of mode k events (hits plus misses). The false alarm rate of a mode k tells us what
381 fraction of forecasts produced mode k when mode k did not occur: it is equal to the number
382 of false alarms of mode k divided by the total number of not- k mode events. The hit rate
383 ignores false alarms, while false alarm rate ignores misses so they are commonly combined
384 in a ROC diagram that shows hit rate against false alarm rate as the decision threshold
385 varies (Wilks 2011; Jolliffe and Stephenson 2012).

386
387 Fig. 10 shows ROC diagrams for each Arctic SIT mode separately (in different rows of
388 panels) and compares their potential skill in EC-Earth2.3 forecasts and two statistical
389 forecasts for two selected start dates (in different columns of panels) combined over all 12
390 forecast months. The aim of a forecast system is to attain the perfect resolution that would
391 correspond to a hit rate of 1 and false alarm rate of 0, i.e. the point in the upper left corner
392 of a ROC diagram. The diagonal in the ROC diagram represents zero skill level (random
393 forecast with equal probability of hit rate and false alarm rate). Fig. 10 overall confirms a
394 hierarchy in prediction skill of our three forecast systems: EC-Earth2.3 mode forecasts
395 have better resolution than the first-order Markov chain forecasts (except for the CSD
396 mode forecasts initialized on 1 November in Fig. 10f), while the Markov chain forecasts
397 never have less resolution than the climatological probability forecasts. The area under the
398 ROC curve (AROC) is a practical scalar measure of skill on the range from 0.5 for no skill

Commented [NJ1]: What is the decision threshold in this case? I assume it's the probability threshold that discriminates between one action (forecasting the occurrence of mode k) versus an alternate action (not forecasting mode k). In any case, I think this decision threshold should be clarified in the text.

399 (diagonal) to 1 for perfect forecast (ROC curve passing through the upper-left corner).
400 AROC values in the lower right corner in panels of Fig. 10 show that for each Arctic SIT
401 mode EC_Earth2.3 and Markov chain forecasts have slightly higher skill when initialized on
402 1 May than on 1 November over the 1979-2010 period. AROC values also indicate that the
403 difference of resolution between EC-Earth2.3 and Markov chain forecasts, on average, is
404 bigger after initialization on 1 November than on 1 May possibly to due better resolved key
405 processes and higher predictability in winter than in summer.

406
407 How does the resolution of the EC-Earth2.3 and Markov chain forecast systems evolve with
408 forecast time? Fig. 11 and the associated Table 2 compare their ROC curves and the areas
409 under the ROC curves, respectively, in sequential steps of 3 forecast months. We see that
410 the dynamical forecasts of each Arctic SIT mode typically have better resolution than the
411 Markov chain forecasts, for both start dates, during each 3-month forecast range. This is
412 furthermore evident when one compares the AROC values in (x.1) and (x.2) columns in the
413 same row in Table 2. We can attest that dynamical forecasts have better resolution than the
414 Marko Chain forecasts in all instances except one (4-6 forecasts months of CSD mode
415 initialized in fall). Furthermore, it appears that the dynamical forecast resolution degrades
416 with advancing forecast horizon at a faster rate after spring initialization than after fall
417 initialization for CAT and APD modes while the opposite is the case for CSD mode. This
418 indicates that on average the sea-ice growing season has potentially a higher predictability
419 than melting season. The first-order Markov chain Arctic SIT mode forecasts initialized in
420 autumn can reach skill even below the diagonal (i.e., the area under the ROC curve of less
421 than 0.5) at longer forecast horizons, meaning that they cannot offer any useful skill and
422 should be excluded from possible practical applications.

423

424 **5. Summary, conclusions and future directions**

425

426 The concept of weather regimes offers a framework for the analysis of weather and climate
427 variability through decomposition into dominant modes and their associated time series.
428 Fučkar et al (2015) has extended this concept of regime behavior to the NH SIT variability
429 and determined three Arctic clusters or modes (CAT, APD and CSD) by applying the K-

430 means cluster analysis on a historical reconstruction of SIT from 1958 to 2013 (Guemas et
431 al. 2014a). The focus is on SIT because it has a capability to act as a buffer of climate signals
432 on intraseasonal and longer time scales (e.g. Blanchard-Wrigglesworth et al. 2011, Guemas
433 et al. 2014b). The K-means nonhierarchical clustering is a type of unsupervised statistical
434 learning method complementary to the PCA, but not constrained by the orthogonality and
435 linearity assumption inherent to the PCA (Hastie et al. 2009; Wilks 2011).

436

437 A state-of-the-art EC-Earth2.3 coupled forecast system (Hazeleger et al. 2010; 2012) is
438 used to produce 5-member 12-month climate predictions using full-field initialization on 1
439 May and 1 November every year from 1979 to 2010. Dynamically forecasted monthly SIT
440 in the Arctic, after trend bias correction (e.g. Fučkar et al. 2014) is classified into three
441 Arctic SIT modes from the historical reconstruction discussed above. We apply a three-
442 state first-order Markov chain model and climatological probability forecasts of the Arctic
443 SIT modes as statistical benchmarks for our EC-Earth2.3 mode predictions. The median
444 RPSS of the Markov chain forecasts with respect to climatology forecasts shows prevailing
445 positive skill over the first 5 forecast months after both fall and spring initialization.

446

447 The RPSS of the dynamical SIT mode forecasts with respect to the Markov chain forecasts
448 shows negative skill for the first forecast month after initialization on 1 May, likely due to
449 initialization shock and missing physical processes, but afterwards the RPSS is positive for
450 both start dates. An interesting feature of RPSS is that the dynamical forecasts initialized in
451 spring perform better than the dynamical forecasts initialized in fall from forecast month 6
452 onward. Such behavior indicates that the transition from the sea-ice melting season to
453 growing season in EC-Earth2.3 typically leads to improvement of skill. This is also likely
454 related to a higher inherent predictability of SIT in winter than in other seasons (Day et al.,
455 2014; Guemas et al., 2014b). The reliability diagrams of EC-Earth2.3 forecasts show high
456 reliability of all modes after initialization on 1 May, while after initialization on 1 November
457 the dynamical system appears to be overconfident (possibly due to a small ensemble size).
458 The ROC diagrams confirm the existence of this hierarchy in forecast quality of the forecast
459 systems: EC-Earth2.3 Arctic SIT mode predictions have on average a higher skill than the
460 first-order Markov chain predictions which are a notable improvement from the

461 climatological probability forecasts. Further analysis of the ROC curves across different
462 forecast horizons reveals that the dynamical CAT and APD mode forecasts initialized in fall
463 lose resolution at a lower rate in forecast time than forecasts initialized in spring. In other
464 words, the inferior performance of dynamical model during melting season may lead to
465 higher SIT forecast errors, which would hint at the existence of “a summer predictability
466 barrier”.

467
468 Possible future lines of investigation could include the application of the multivariate K-
469 means clustering encompassing a set of polar climate variables using different types of
470 observations, reanalyses and reconstructions. Also, such promising climate prediction skill
471 of “coarse-grained” aspects of the Arctic system such as CAT, APD and CSD modes of SIT
472 field will hopefully encourage exploration of their skill in other state-of-the-art coupled
473 climate models. Our and many other coupled climate models still miss some of the critical
474 physical processes with high impacts on sea ice cover in summer such as melt ponds, wind-
475 driven snow dynamics, etc. Hence, a possibility of improved skill and utility of dynamical
476 climate predictions during the boreal sea-ice melting season should also guide efforts to
477 improve the physics of sea ice models and initialization methods of coupled forecast
478 systems.

479
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481
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495 historical reconstruction with ORCA1 NEMO-LIM2 is available upon request.

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Transition matrix	$X_i = \text{CAT}$	$X_i = \text{APD}$	$X_i = \text{CSD}$
$P\{x_{i+1} = \text{CAT} \mid X_i\}$	0.814	0.105	0.071
$P\{x_{i+1} = \text{APD} \mid X_i\}$	0.132	0.852	0.055
$P\{x_{i+1} = \text{CSD} \mid X_i\}$	0.054	0.043	0.874

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Table 1. The first-order Markov chain transition matrix of conditional probabilities for the three NH SIT modes of clusters reconstructed over the 1958-2013 period. This mean transition matrix (averaged over both 1 May and 1 November start dates and forecast years from 1979 to 2010) shows the probability of the cluster pattern listed in a column transitioning to the cluster pattern listed in a row.

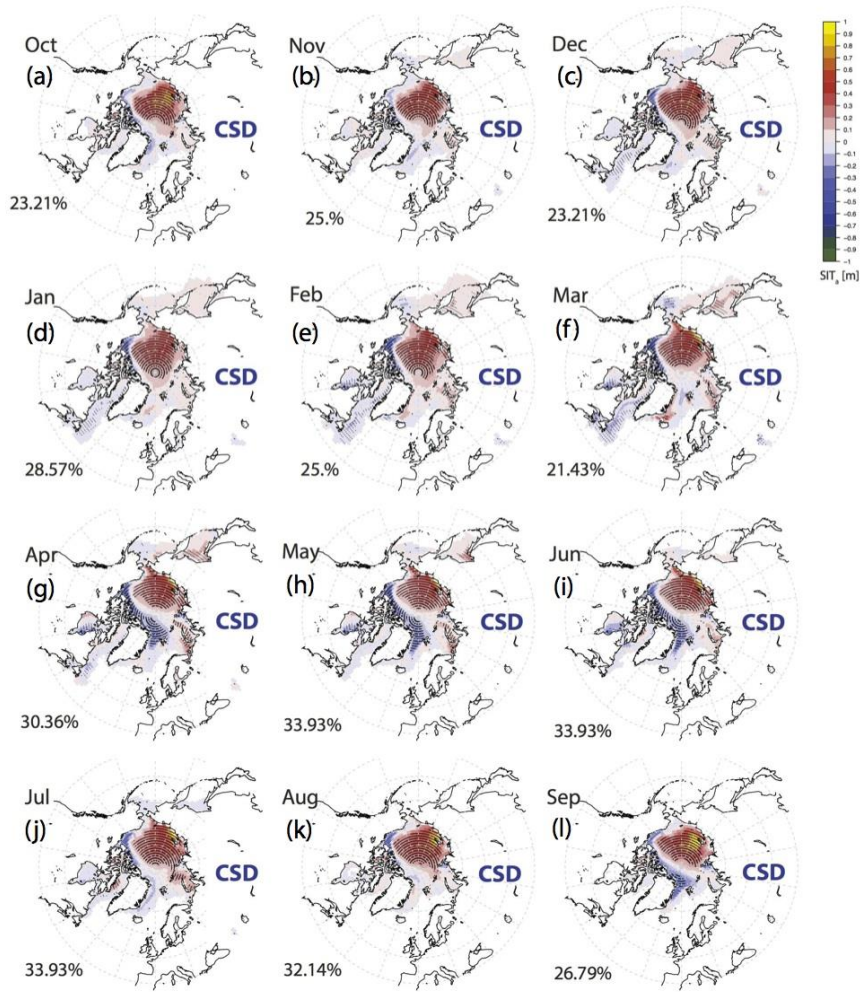
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AROC		1 May IC		1 November IC	
NH SIT mode	Forecast months	EC-Earth v2.3	MC1	EC-Earth v2.3	MC1
		(a.1)	(a.2)	(d.1)	(d.2)
CAT	1-3	0.943	0.913	0.993	0.821
	4-6	0.793	0.654	0.791	0.666
	7-9	0.769	0.576	0.693	0.573
	10-12	0.589	0.479	0.704	0.448
		(b.1)	(b.2)	(e.1)	(e.2)
APD	1-3	0.934	0.824	0.936	0.859
	4-6	0.892	0.762	0.712	0.696
	7-9	0.755	0.656	0.589	0.406
	10-12	0.616	0.600	0.647	0.420
		(c.1)	(c.2)	(f.1)	(f.2)
CSD	1-3	0.954	0.851	0.939	0.944
	4-6	0.886	0.724	0.754	0.802
	7-9	0.884	0.678	0.623	0.531
	10-12	0.763	0.648	0.688	0.528

783
784 Table 2. The areas under ROC curves (AROC) in Fig. 11 for a sequence of forecasts
785 advancing in time, combining three forecast months at the time (1-3, 4-6, 7-9 and 10-12),
786 with 1 May and 1 November start dates over the 1979-2010 period. The columns are
787 sorted by the forecast system: EC-Earth2.3 dynamical forecast and MC1 for three-state
788 first-order Markov chain forecast, while rows are sorted by the NH SIT modes (CAT, APD
789 and CSD).

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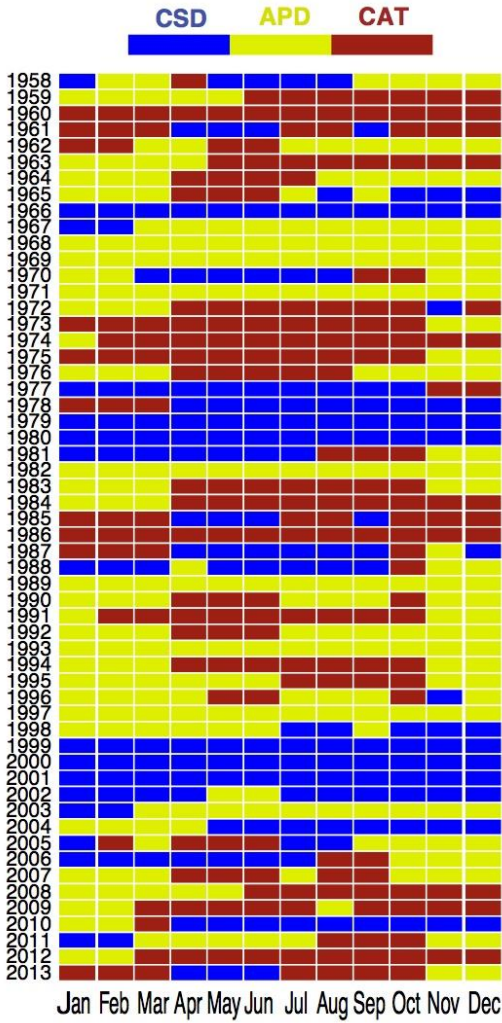
793
794 Fig. 1 Monthly centroid patterns of the NH sea ice thickness (SIT) for the Canadian-Siberian
795 dipole (CSD) mode or cluster 3 - on average the thickest of three NH SIT modes - in a
796 historical reconstruction of sea ice cover from 1958 to 2013. The occurrence rate of the
797 CSD mode in the specific month, over the period of interest, is shown in the lower left
798 corner of each panel.

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804 Fig. 2 Time-series map of occurrences of the ensemble-mean monthly NH SIT modes or
805 clusters in a historical reconstruction of sea ice cover from 1958 to 2013.

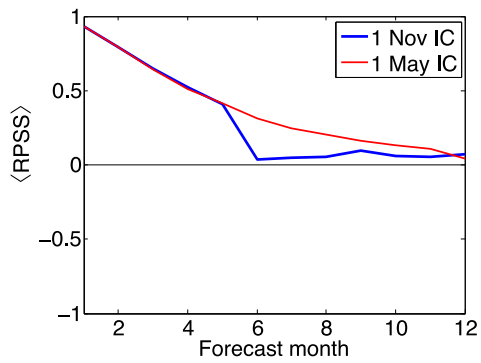
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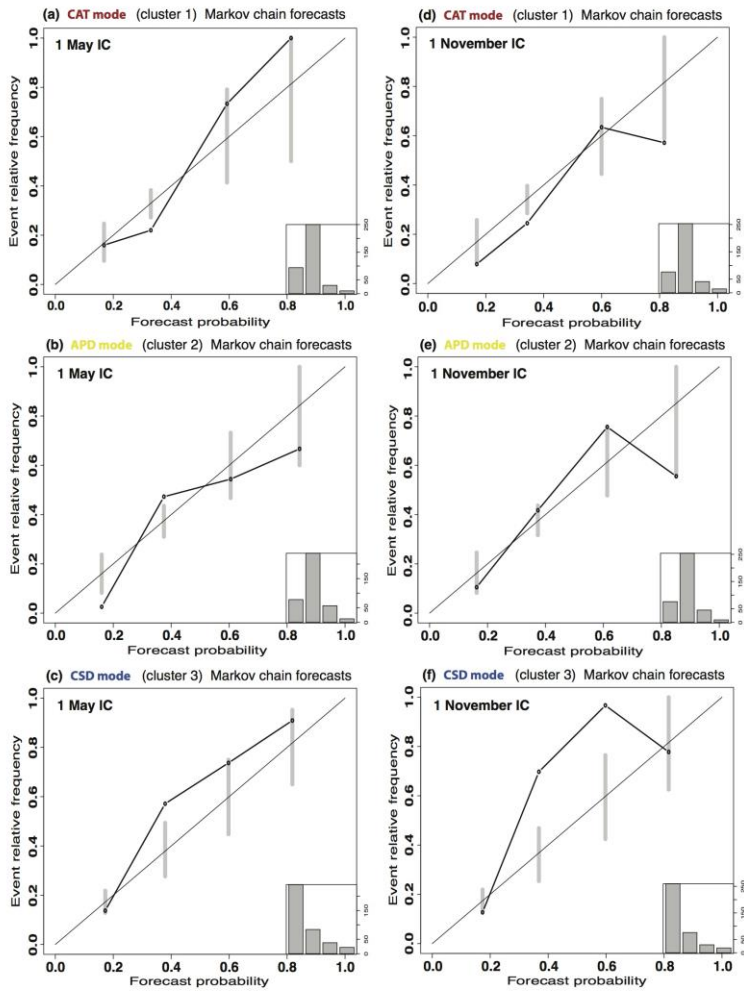
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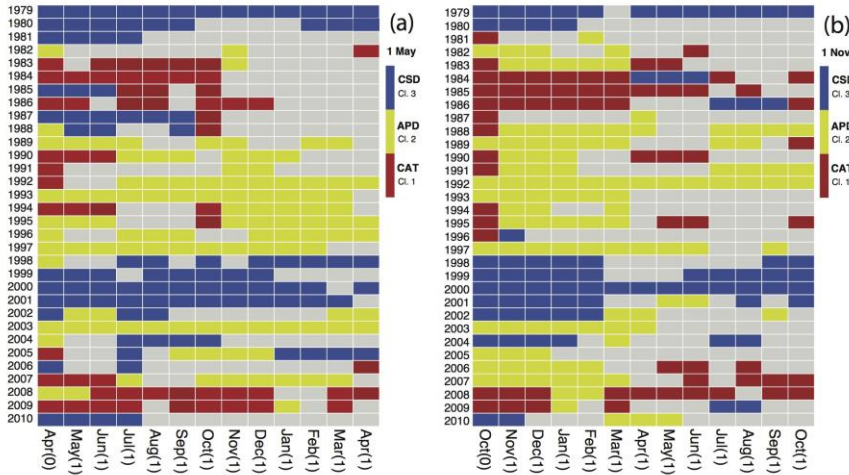


812
813 Fig. 3 Ranked probability skill scores (RPSS) as a function of forecast month for three-state
814 first-order Markov chain forecast of the NH SIT modes with respect to climatological
815 forecast as the reference. Red and blue curves show the median of RPSS for 1 May and 1
816 November start dates, respectively, over the 1979-2010 period.

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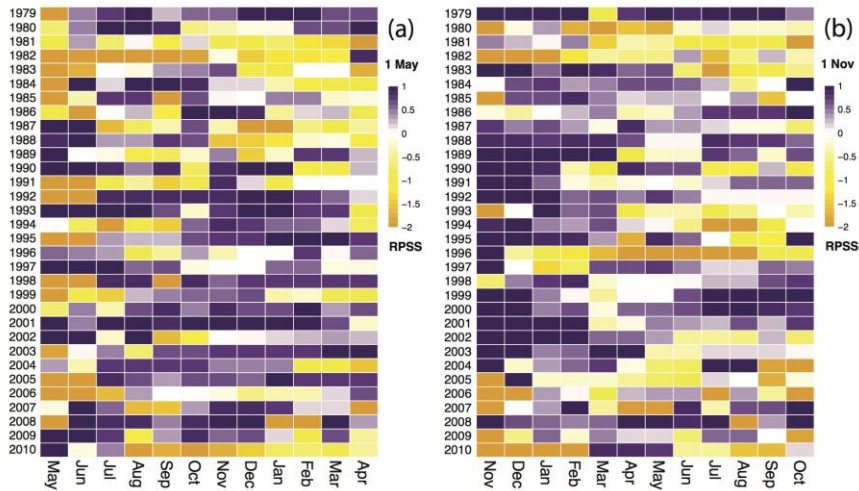


819
 820 Fig. 4 Reliability diagrams of the three-state first-order Markov chain forecasts of the NH
 821 sea ice thickness CAT, APD and CSD modes in the top, middle and bottom panels,
 822 respectively, encompassing all forecast months. The left (right) panels show forecasts with
 823 1 May (1 November) start dates from 1979 to 2010. The grey consistency bars indicate
 824 95% confidence intervals (after 1000 bootstrap resamples). Each panel contains
 825 refinement histogram (number of events per bin) in the lower right corner.
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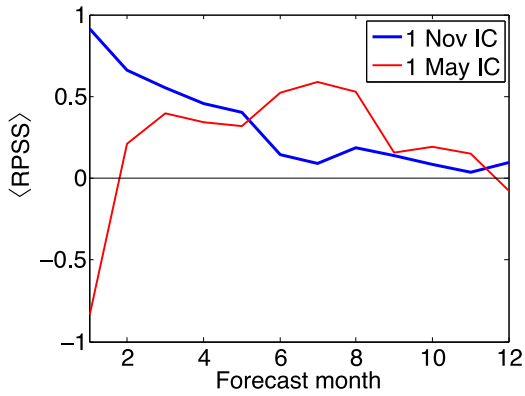
827
 828 Fig. 5 Accuracy of EC-Earth2.3 12-month 5-member ensemble predictions of the NH SIT
 829 modes for 1 May and 1 November start dates in the left and right panels, respectively, from
 830 1979 to 2010. The color of a forecast month is saturated to the designated primary color of
 831 a historical reconstructed NH SIT mode if the majority of 5 EC-Earth2.3 ensemble members
 832 correctly predict this mode (accuracy of 0.6, 0.8 and 1.0), otherwise the forecast month is
 833 marked grey (accuracy of 0, 0.2 and 0.4). The additional first column in both panels –
 834 April(0) and October(0) - shows the historical NH SIT mode in the month just before the
 835 start date.

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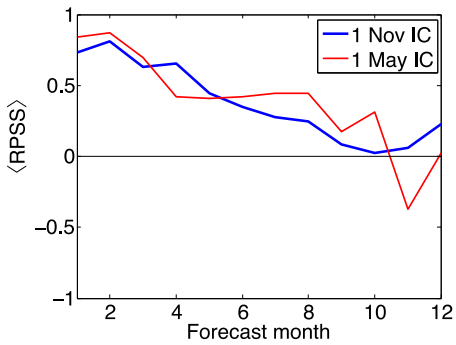
852 Fig. 6 RPSS of EC-Earth2.3 12-month 5-member ensemble predictions of the NH SIT modes
 853 - with respect to three-state first-order Markov chain forecast as the reference - for 1 May
 854 and 1 November start dates in the left and right panels, respectively, from 1979 to 2010.
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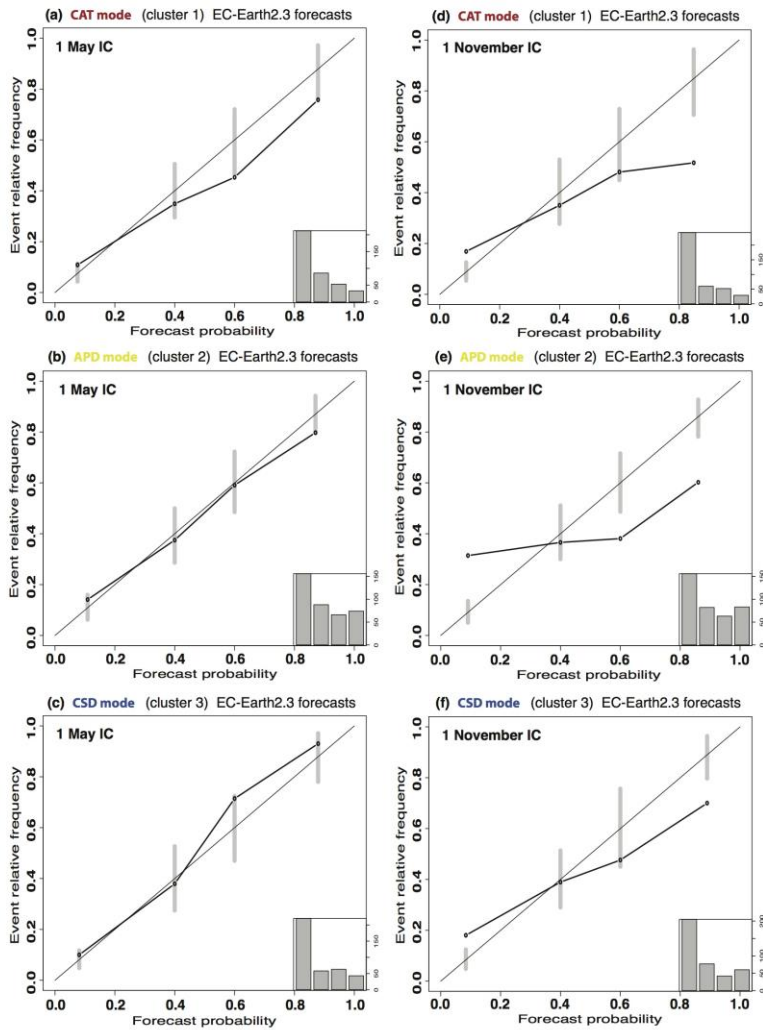
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 881 Fig. 7 RPSS as a function of forecast month for EC-Earth 5-member ensemble prediction of
 882 the NH SIT modes with respect to three-state first-order Markov chain forecast as the
 883 reference. Red and blue curves show the median of RPSS for 1 May and 1 November start
 884 dates, respectively, over the 1979-2010 period.

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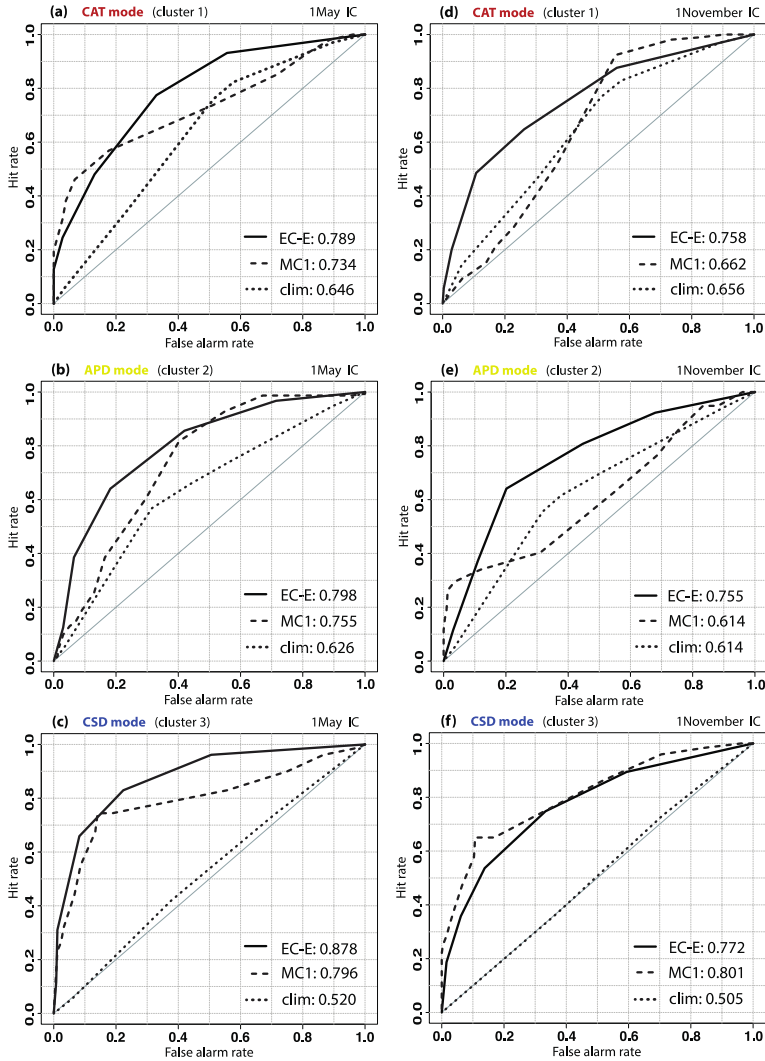


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 889 Fig. 8 RPSS as a function of forecast month for EC-Earth 5-member ensemble prediction of
 890 the NH SIT modes with respect to climatological forecast as the reference. Red and blue
 891 curves show the median of RPSS for 1 May and 1 November start dates, respectively, over
 892 the 1979-2010 period.

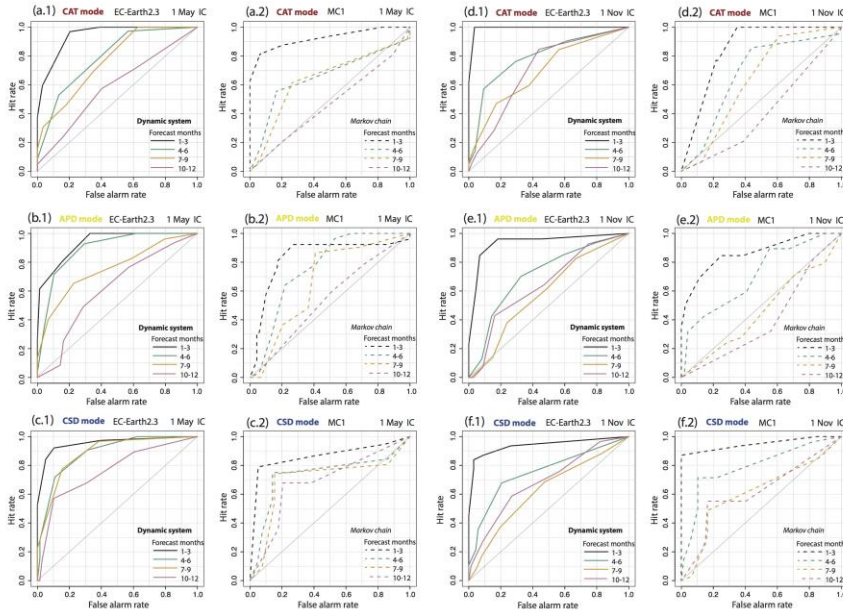
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 896 Fig. 9 Reliability diagrams of EC-Earth2.3 5-member ensemble predictions of the NH sea ice
 897 thickness CAT, APD and CSD modes in the top, middle and bottom panels, respectively,
 898 encompassing all forecast months. The left (right) panels show forecasts with 1 May (1
 899 November) start dates from 1979 to 2010. The grey consistency bars indicate 95%
 900 confidence intervals (after 1000 bootstrap resamples). Each panel contains refinement
 901 histogram (number of events per bin) in the lower left corner.
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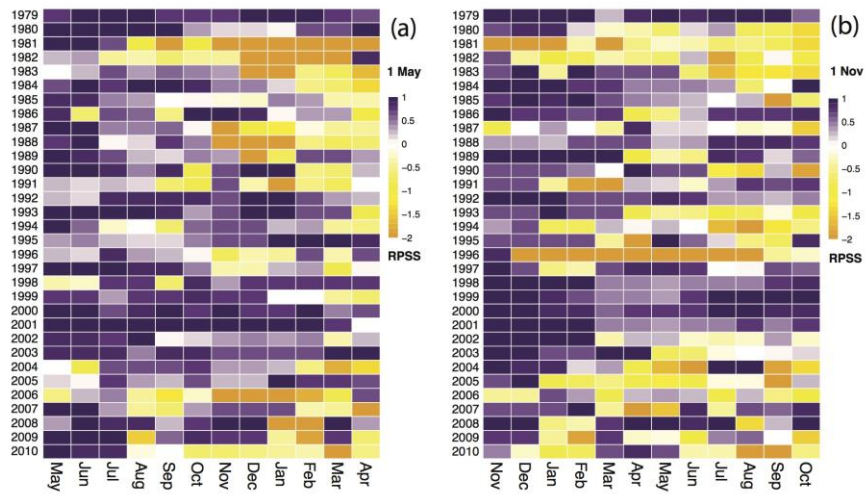
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 904 Fig. 10 Relative operating characteristic (ROC) diagrams of the various forecasts of the NH
 905 sea ice thickness CAT, APD and CSD modes in the top, middle and bottom panels,
 906 respectively, encompassing all forecast months. The solid, dashed and dotted curves show
 907 EC-Earth2.3, three-state first-order Markov chain and climatological forecast, respectively.
 908 The values in the right bottom corner of each panel show areas under ROC curves. The left
 909 (right) panels show forecasts with 1 May (1 November) start dates from 1979 to 2010.
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 912 Fig. 11 Relative operating characteristic (ROC) diagrams of the various forecasts of the NH
 913 sea ice thickness CAT, APD and CSD modes in the top, middle and bottom panels,
 914 respectively. The set of solid and dashed curves show EC-Earth2.3 forecasts in (x.1)
 915 columns and three-state first-order Markov chain (MC1) forecast in (x.2) columns,
 916 respectively, sequentially encompassing 3 forecast months at the time. The two left (right)
 917 panels show forecasts with 1 May (1 November) start dates from 1979 to 2010.

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934 Supplementary information:
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937
938 Fig. S1. RPSS of EC-Earth2.3 12-month 5-member ensemble predictions of the NH SIT
939 modes - with respect to climatological forecast as the reference - for 1 May and 1 November
940 start dates in the left and right panels, respectively, from 1979 to 2010.
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