



# A Subjective Bayesian Framework for Synthesizing Deep Uncertainties in Climate Risk Management

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### Key Points:

- We introduce a Bayesian framework to transparently synthesize and characterize deep uncertainties with the goal to support decision-making
- We demonstrate the framework using a simple case study of house elevation for coastal flood risk management
- Estimates of performance or robustness under deep uncertainty necessarily involve subjective judgments

### Supporting Information:

Supporting Information may be found in the online version of this article.

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**Abstract** Projections of nonstationary climate risks can vary considerably from one source to another, posing considerable communication and decision-analytical challenges. One such challenge is how to present trade-offs under deep uncertainty in a salient and interpretable manner. Some common approaches include analyzing a small subset of projections or treating all considered projections as equally likely. These approaches can underestimate risks, hide deep uncertainties, and are mostly silent on which assumptions drive decision-relevant outcomes. Here we introduce and demonstrate a transparent Bayesian framework for synthesizing deep uncertainties to inform climate risk management. The first step of this workflow is to generate an ensemble of simulations representing possible futures and analyze them through standard exploratory modeling techniques. Next, a small set of probability distributions representing subjective beliefs about the likelihood of possible futures is used to weight the scenarios. Finally, these weights are used to compute and characterize trade-offs, conduct robustness checks, and reveal implicit assumptions. We demonstrate the framework through a didactic case study analyzing how high to elevate a house to manage coastal flood risks.

**Plain Language Summary** Identifying sound strategies to manage risks driven by climatic changes is a complex task given the large uncertainties surrounding projections of coupled natural-human systems. These uncertainties often arise from choices experts have to make, for example, about how to formulate scientific models of future water levels. Different experts can disagree about these choices, leading to different projections. Analyzing decisions in such a situation of deep uncertainty poses nontrivial challenges. For example, picking a single representative projection can under-estimate risk and result in poor decisions. Similarly, communicating results separately for each projection can overwhelm decision-makers. To make matters worse, typical approaches to this problem are mostly silent on what assumptions make a difference for the decisions at hand. We develop and demonstrate a framework to address these challenges. The framework provides a transparent approach to (a) combine a large number of deeply uncertain projections to a more interpretable sample set and (b) provide insights about which assumptions and modeling choices influence decisions. We demonstrate the approach with a relatively simple example question of how high to elevate a house in the face of deeply uncertain projections of future water levels.

## 1. Introduction

Aging infrastructure and changes in regulations, finance, patterns of population and infrastructure use, and climate challenge the ability of critical infrastructures to meet design objectives (Doss-Gollin et al., 2020, 2021; Chester et al., 2020; M. Ho et al., 2017; Tye & Giovannetone, 2021). To achieve acceptable performance with reasonable planning efforts, current practice in engineering, infrastructure design, and regulation relies heavily on standards that specify design events or conditions that buildings and infrastructure should safely withstand (Bruneau et al., 2017). For example, the Federal Emergency Management Agency (FEMA), local governments, and engineering consultants produce local floodplain maps in many communities. Buildings in the designated floodplain are subject to specific regulations, such as flood insurance requirements as an eligibility requirement for federally backed mortgages (Kousky & Kunreuther, 2014) or minimum elevations for new construction (ASCE, 2006; FEMA, 2011). Although this paper focuses on flooding, similar approaches inform mitigation strategies for a wide range of other hazards (American Society of Civil Engineers, 2013).

Standards-based risk management frameworks have many advantages, including scalability, explainability, and simplicity. However, the choice of standard is a complex design and policy choice. Risk-based design and cost

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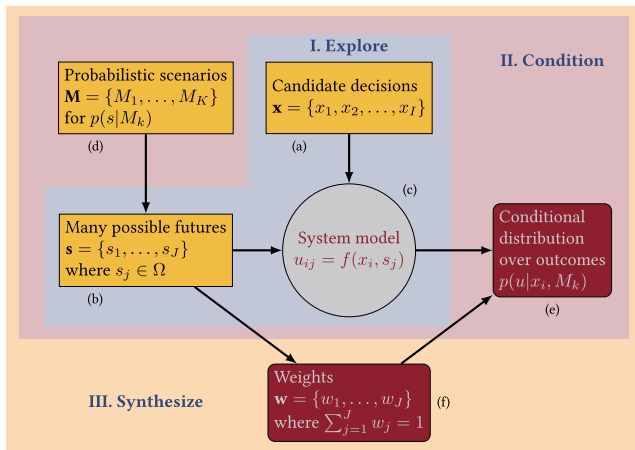
benefit analysis (Eijgenraam et al., 2014; van Dantzig, 1956; Xian et al., 2017) offer a quantitative framework for comparing possible standards by emphasizing “a proportionate response to risk, so that the amount invested in risk reduction is in proportion to the magnitude of the risk and the cost-effectiveness with which that risk may be reduced” (Merz et al., 2010). This provides a formal basis for choices such as protecting hospitals and critical infrastructure to a higher degree than ordinary buildings (ASCE, 2013). However, these methods are silent on how standards should balance trade-offs, not only between cost and performance but also between other stakeholder values such as sense of place, distributive justice, and safety (Besette et al., 2017; Helgeson et al., 2022; Keller et al., 2021; Quinn et al., 2017; Vezér et al., 2018).

Moreover, because estimates of performance trade-offs require implicit or explicit assumptions about the likelihood of different possible futures. Current practice emphasizes nominally objective methods that can be applied consistently across locations. For example, the United States Geological Survey Bulletin 17C specifies procedures for estimating flood frequency (England et al., 2019). Similarly, the National Oceanic and Atmospheric Administration (NOAA) Atlas 14 provides estimates of the intensity, duration, and frequency of extreme rainfall (National Weather Service & Office of Water Prediction, 2022; Perica et al., 2018). One statistical assumption these analyses make is stationarity (the assumption that past and future hazard come from the same probability density function [PDF]), but global climate change and local environmental changes have cast scrutiny on this assumption (Doss-Gollin et al., 2019; Merz et al., 2014; Milly et al., 2008). While some methods have been proposed for incorporating nonstationarity into risk analyses (see Salas et al., 2018, for a review), these assume specific forms of a trend which may not adequately represent physical processes or sample only a subset of uncertainties (Doss-Gollin et al., 2019; Montanari & Koutsoyiannis, 2014; Serinaldi & Kilsby, 2015). At least in part because of the challenges associated with developing objective methods to select from diverging projections of future hazard, official guidance continues to rely on the stationarity assumption (England et al., 2019; Perica et al., 2018).

The limitations of objectivist approaches to projecting risk extend beyond estimating nonstationary climate hazards. Human-natural systems are never closed and model results are never unique, and thus validation and verification of models representing these systems is necessarily qualitative and subjective (Oreskes et al., 1994). In other words, no model exists that could represent the full truth, and the future is therefore deeply uncertain (Haasnoot et al., 2021; Keller et al., 2021; Lempert, 2002; Walker et al., 2013). To address these challenges, a growing literature on decision making under deep uncertainty (DMDU) emphasizes the value of identifying decisions that are robust, in some sense, to deep uncertainties (Borgomeo et al., 2018; Herman et al., 2015; McPhail et al., 2019; Moody & Brown, 2013). Within this literature has emerged a debate regarding the value and use of probabilistic information (see Taner et al., 2019, and references therein). On the one hand, scholars have pointed out that predictions are inherently unreliable, and representing deep uncertainties through probability distributions frequently over-estimates predictive skill (Groves & Lempert, 2007; Lempert & Schlesinger, 2000). On the other, assessments of which decisions are robust depend on subjective choices about how to define robustness and how to sample uncertainties (McPhail et al., 2019; Quinn et al., 2020; Reis & Shortridge, 2020) and thus nominally nonprobabilistic methods can obscure rather than solve the problems of probabilistic approaches (Schneider, 2001, 2002).

In this paper we offer a conceptual step toward bridging this divide by presenting a framework that is designed to combine the strengths of both approaches. In the first step, exploratory or bottom-up modeling is used to build insight and identify potential system vulnerabilities (Banks, 1993; Brown et al., 2012; Moallemi, Kwakkel, et al., 2020). In the second step, we integrate exploratory ensembles of deep uncertainties into a single probabilistic representation (we refer to this as “synthesizing” deep uncertainties) to formally estimate performance metrics and trade-offs using subjective probability distributions. Drawing from the literature on building predictive models when all models are wrong (Box, 1976; Gelman & Shalizi, 2013; Piironen & Vehtari, 2017), we interpret these probability distributions not as statements of fact, but rather as a self-consistent framework for reasoning about how different assumptions lead to different inferences. An advantage of our approach is that it facilitates computationally efficient analysis of how alternative probabilistic models would affect estimated performance metrics and trade-offs.

We illustrate our approach through a didactic case study of whether to elevate a hypothetical house, and if so how high. Prior studies have found that floodproofing and building-scale vulnerability reduction measures, including house elevation, can effectively reduce local flood damages in many contexts (Aerts, 2018; de Moel



**Figure 1.** Outline of the proposed decision-analytic framework. In Section 2.1 we use an exploratory framework to quantify the performance of candidate decisions under a large ensemble of possible futures. In Section 2.2 we illustrate the “multiple probability density function problem” by creating probability distributions over outcomes that are conditional upon specific probabilistic scenarios. In our case study, these scenarios correspond to combinations of emissions pathways with physical models for sea level rise. Then in Section 2.3 we describe the need for synthesizing insight across scenarios. Finally in Section 3 we provide a formal framework for doing so.

et al., 2014; de Ruig et al., 2020; Kreibich et al., 2005; Mobley et al., 2020; Rözer et al., 2016; Slotter et al., 2020), and both local building codes (American Society of Civil Engineers, 2006, 2013; Bruneau et al., 2017) and federal policy (The Federal Emergency Management Agency, 2011) require elevation in some cases. Guidance for homeowners, notably from FEMA, recommends elevating to the base flood elevation (BFE; typically the 100 year flood) plus a freeboard (ASCE, 2015; FEMA, 2014) but recent research has demonstrated that neglecting uncertainty in the cost-benefit analysis can lead to poor decisions (Zarekarizi et al., 2020). Focusing on deep uncertainty in sea level rise (SLR) over the 70 years design life of a hypothetical house, we seek to answer the research question “how can decision analysis transparently synthesize deep uncertainties?” To shed light on this question in a single paper, we necessarily are silent on key issues that would be relevant to real-world decision-makers including alternative decision levers, the potential for adaptive decision rules, and rival problem framings.

We proceed as follows. In Section 2 we present three formal decision analytic frameworks for analyzing an ensemble of SLR simulations, building through existing approaches for exploratory modeling scenario analysis to identify a need for synthesizing across scenarios. We present a formal framework for transparently synthesizing deep uncertainties in Section 3. In Section 4 we describe the didactic case study. Next, in Section 5, we present results for each of the three decision lenses and discuss the advantages and limitations of each theoretical approach. In Section 6 we discuss limitations of the study and future research needs. Finally in Section 7 we discuss key findings and implications for policy and practice.

## 2. Conceptual Framework

In this section we introduce a conceptual framework and notation for decision analysis under deep uncertainty. Many bottom-up exploratory modeling frameworks used in climate risk management and related fields use a system model ( $f$  in Figure 1) to characterize the system's response to a wide range of plausible futures, often called states of the world (SOWs) ( $s$  in Figure 1). This analysis is often used to explore vulnerabilities and build knowledge about the system (Banks, 1993), and in general exploratory modeling frameworks aim to avoid making explicit judgments about the relative likelihood of different futures.

However, as discussed in Section 1, estimates of trade-offs between desired performance metrics (e.g., cost and reliability) depend on probabilistic models of uncertainty. In this paper we present a method for integrating the SOWs used in exploratory modeling into a formal decision analytic framework using a subjective probability distribution over the space of possible futures, which is used to infer implicit weights over the SOWs. This approach is particularly suited for problems where the SOWs are generated from or conditioned on specific scenarios (e.g., representative concentration pathway [RCP] scenarios) or where there are multiple models of the underlying processes (e.g., multiple parameterizations of the response of local sea levels to global temperature), which can lead to the “multiple PDF problem” (discussed in Section 2.2). A motivating advantage is that it makes assumptions about the likelihoods of different SOWs transparent to decision-makers.

### 2.1. Exploratory Modeling

A first analytical step is to use the model in an “exploratory” mode. Exploratory modeling strives to avoid making explicit assumptions about the likelihood of different SOWs and instead seeks to generate new knowledge (Banks, 1993) by systematically exploring a large number of possible futures, emphasizing interactions between different uncertainties (Reed et al., 2022). Exploratory modeling is often paired with analyses that identify relevant scenarios (Groves & Lempert, 2007; Lamontagne et al., 2018) or summarize a system's response to forcing (Poff et al., 2015; Srivier et al., 2018; Steinschneider et al., 2015). Despite the aversion to strong assumptions about the likelihood of different futures, subjective modeling decisions such as the choice of system model,

the set of candidate decisions, the criteria used to assess outcomes, and the choice of how to sample SOWs can strongly influence results (Moallemi, Zare, et al., 2020; Quinn et al., 2017, 2020).

## 2.2. Scenario-Conditional Probabilistic Analysis

Although exploratory modeling is a useful framework for understanding systems, there are many questions that it cannot answer. For example, answering questions like “what is the 95th percentile of metric  $u$  under decision  $x$ ” or “what is the probability of exceeding a critical threshold” requires an implicit or explicit probability distribution over outcomes (see Schneider, 2002, for a general discussion).

One way to interpret an ensemble of SOWs is as iid draws from some probabilistic data generating process. This commonly arises when a single deep uncertainty (e.g., an emissions pathway) is used as an input for a stochastic model. To clarify language, we draw a distinction between a SOW, which is a single realization of a possible future, and a *probabilistic scenario*, which we define loosely as a set of assumptions for which probabilistic projections (i.e., SOWs) are available or can be simulated. For example, in the case study described in Section 4.1 we use four physical models of the processes relevant to SLR and four RCP scenarios to generate a total of 16 probabilistic scenarios.

We illustrate this distinction in boxes (d and e) of Figure 1, denoting the particular scenario  $M_k$ . We assume that each scenario is probabilistic, that is that SOWs are drawn independent and identically distributed (IID) from  $M_k$ , the set of outcomes  $u_{i,j}$  can be interpreted as IID draws from the conditional distribution over outcomes,  $p(u|x, M_k)$ . This “scenario-conditional” probabilistic interpretation of SOWs allows for fully probabilistic quantification of uncertainty and optimization, conditional on a particular scenario. For example, Fletcher, Lickley, and Strzepek (2019) use stochastic dynamic programming to quantify the value of flexibility in water resources planning. However, only a single RCP scenario (RCP 8.5) is used. While the analysis could be repeated for other RCP scenarios, the scenario-conditional analysis framework can only qualitatively characterize uncertainty *between* scenarios (Ruckert et al., 2019; Sharma et al., 2021; Wong & Keller, 2017).

We can also apply this theoretical lens to examine the approach, common in DMDU applications, of sampling parameters from a set of fixed ranges. The *scenario* in this case is thus the choice of bounds on the parameters; it is consistent with our above definition of a probabilistic scenario because SOWs can be sampled using probabilistic methods. For example, Sriver et al. (2018) sample parameters describing the rate of SLR across a range of values to inform coastal adaptation. Similarly, Trindade et al. (2020) checks the performance of candidate decisions against an ensemble of synthetic time series of streamflow, water demand, and other parameters by sampling parameters that transform the available data over a plausible range. Analyses that use this methodology are implicitly assuming a single probabilistic model in which different variables are drawn from independent Uniform distributions. Many limitations of Uniform and other noninformative priors have been documented in the literature, including (a) that they can induce unrealistic implicit priors over functions of parameters and (b) results are sensitive to the parameterization of a given process (Seaman et al., 2012). Yet while replacing Uniform distributions with alternatives such as maximum-entropy distributions can address some of these challenges (e.g., Gupta et al., 2022), subjective modeling choices remain necessary. Our primary concern here is not that these subjective modeling assumptions are wrong—this is, almost surely, inevitable—but that when these assumptions are opaque and presented without critique or validation (see Gelman et al., 2020, regarding the importance of iterative critique) they may lead to inscrutable decision processes and poor decisions.

## 2.3. Synthesizing Deep Uncertainties for Decision Analysis

Scenario-conditional probabilistic analysis allows for uncertainty quantification and optimization, and is valuable in many contexts. However, scenarios are often explicitly provided without probabilities or likelihoods (e.g., the shared socio-economic pathways; van Vuuren et al., 2008). Thus, any such analysis is silent on the question of how to combine information across different scenarios. We term this the “multiple PDF problem.” Decision making around the multiple PDF problem is susceptible to the cognitive biases that interfere with decision-making under uncertainty more generally (Morgan, 1990; Srikrishnan et al., 2022; Tversky & Kahneman, 1974). For example, while many analyses treat all scenarios as equally likely, this is often inconsistent with available information and can lead to poor decisions and outcomes (Wigley & Raper, 2001; E. Ho et al., 2019; Hausfather & Peters, 2020). Other analyses suggest using the worst-case scenario as a conservative measure. However, this approach is also

problematic, since (a) there are no fundamental limits on what constitutes a worst-case scenario and (b) improving performance under unlikely worst-case scenarios may lead to substantially impaired performance under more likely scenarios, which may or may not be acceptable to relevant stakeholders. There is thus a critical need for synthesizing insights across multiple probabilistic scenarios.

### 3. Re-Weighting SOWs to Synthesize Across Scenarios

In this section we provide a formal method for integrating exploratory ensembles of deep uncertainties into a single probabilistic representation. Our objective is to develop a framework that (a) is conceptually and practically amenable to exploratory modeling; (b) makes subjective modeling choices explicit and transparent; and (c) allows decision analysts to estimate a probability distribution over outcomes.

A particular need is to estimate the expectation of functions over SOWs (i.e., box e in Figure 1). If the  $J$  SOWs are drawn IID from some distribution that credibly represents the true likelihood of different futures then the expected value of such a function,  $f(\mathbf{s})$ , can be readily approximated using the Monte Carlo estimate  $\mathbb{E}[f(\mathbf{s})] \approx \frac{1}{N} \sum_{j=1}^N f(\mathbf{s}_j)$ . However, this is often not the case. For example, in Section 4 we will consider decision analysis where the SOWs are sampled from multiple physical models and RCP scenarios, considering that not all RCP scenarios are equally likely and that not all physical models are equally skillful. In this case, the formula may be adjusted to a weighted Monte Carlo estimate:

$$\mathbb{E}[f(\mathbf{s})] \approx \sum_{i=1}^N w_i f(\mathbf{s}_i), \quad (1)$$

where  $\sum_{j=1}^J w_j = 1$ .

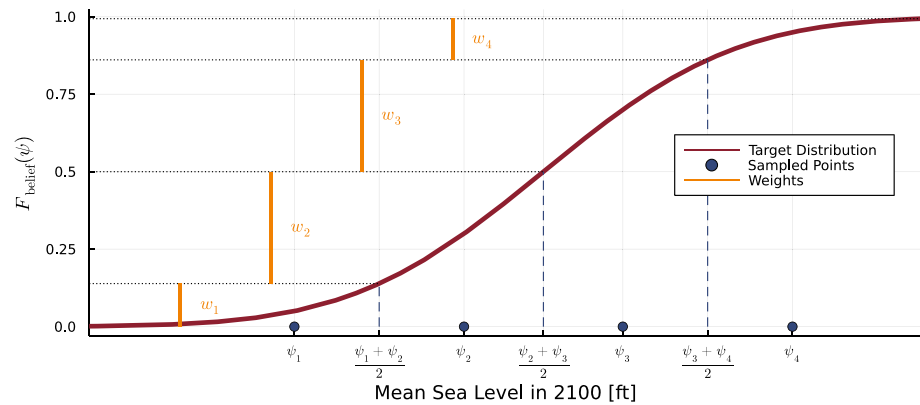
The challenge then becomes to suitably estimate the  $w_j$ . Many such methods exist; drawing from joint probability methods for statistical analysis of tropical cyclones, we employ a grid-based approach (Johnson et al., 2013; Resio, 2007; Toro et al., 2010). First, we project the SOWs  $\mathbf{s} \in \Omega$  onto a low-dimensional representation, which we denote  $\psi_1, \psi_2, \dots, \psi_J \in \Psi$ . Then, we partition the parameter space into a region corresponding to each SOW and integrating the probability  $p(\psi)$  over each region.

Implementing this approach requires choosing a probability distribution for this low-dimensional representation of the SOWs,  $p(\psi)$ , reflecting subjective belief about the SOWs. We denote this  $p_{\text{belief}}(\psi)$  to emphasize that it represents a subjective belief about the SOWs, rather than an objectively verifiable choice. In general we do not expect that stakeholders and experts will agree on  $p_{\text{belief}}$  because there is not, even conceptually, an objectively correct choice (Oreskes et al., 1994; Walker et al., 2013). However, we posit that since we cannot be “right,” it is valuable to maximize the transparency of our implicit probabilistic assumptions, and suggest that writing down an explicit model for  $p_{\text{belief}}$  supports this aim. Choices for  $p_{\text{belief}}$  can be drawn from many sources, including expert elicitation or results of previous analyses. These models can be interpreted as prior beliefs about SLR that could be incorporated into a Bayesian analysis as additional data is collected in the future, and thus can draw from literature on Bayesian prior selection and prior predictive checks (Gelman et al., 2020).

We present here the case where the  $\psi_j$  are one-dimensional; extensions to higher dimensions are possible. We first sort the  $\psi_j$  from least to greatest so that  $\psi_{j-1} \leq \psi_j$ , ( $j \neq 1$ ). Defining a cumulative distribution function  $F_{\text{belief}}(\psi) = \int_{-\infty}^{\psi} p_{\text{belief}}(\psi') d\psi'$ , we calculate weights as

$$w_j = \begin{cases} F_{\text{belief}}\left(\frac{\psi_1 + \psi_2}{2}\right) & j = 1 \\ F_{\text{belief}}\left(\frac{\psi_j + \psi_{j+1}}{2}\right) - F_{\text{belief}}\left(\frac{\psi_{j-1} + \psi_j}{2}\right) & 1 < j < J \\ 1 - F_{\text{belief}}\left(\frac{\psi_{J-1} + \psi_J}{2}\right) & j = J. \end{cases} \quad (2)$$

This step is illustrated in Figure 2. By the definition of cumulative distribution functions,  $F_{\text{belief}}(b) - F_{\text{belief}}(a) = \int_a^b p_{\text{belief}}(\psi') d\psi'$ . Diagnostic checks, such as examining the histogram of weights (not shown), may be useful protections against degeneracy.



**Figure 2.** Schematic of method to re-weight states of the world as defined in Equation 2. This method is illustrated for a hypothetical target distribution (dark red line) and  $J = 4$  samples  $\psi_1, \psi_2, \psi_3, \psi_4$  (blue dots). As shown in Equation 2, the weights  $w_j$  (orange vertical lines) are calculated based on the cumulative distribution function of the target distribution at the halfway points  $\frac{1}{2}[\psi_j + \psi_{j+1}]$  (vertical dashed lines).

The aim of this re-weighting framework is to integrate an ensemble of SOWs used for exploratory modeling into formal decision analysis, even when the SOWs deliberately over- or under-sample some regions of the parameter space. As in Section 2.2, we must condition on a model: where the analysis of Section 2.2 conditions upon deep uncertainties, the approach outlined in this section synthesizes across them. Considering multiple probabilistic models for  $p_{\text{belief}}$  can also be useful for understanding the sensitivity of the decision to the choice of  $p_{\text{belief}}$ . Further, the sensitivity, or lack thereof, of different objectives to the choice of  $p_{\text{belief}}$  may be useful for identifying future research needs.

#### 4. Demonstrating the Concept With a Case Study

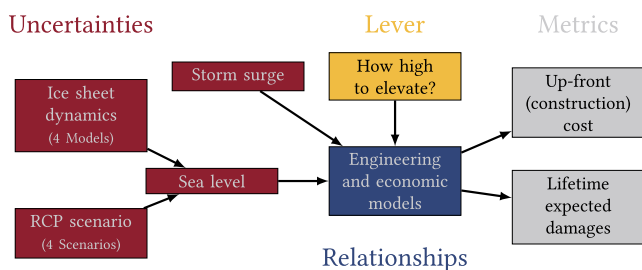
To illustrate the proposed decision analytic framework, we model a one-time decision of whether to elevate a house, and if so by how much (Figure 3). Following the approach outlined in Zarekarizi et al. (2020), we focus on a case study of a *hypothetical* house in Norfolk, VA. For interpretability, we focus on deep uncertainty in mean relative sea level (MSL) and treat storm surge and other model parameters as shallow uncertainties as shown in Table 1. We use the notation developed in the previous section to describe the case study. Specifically,

1. The decision vector  $\mathbf{x}$  is comprised of discrete possible house heightenings ( $\Delta h$ ); we consider  $\Delta h = 0 \text{ ft}, 0.25 \text{ ft}, \dots, 12 \text{ ft}$ .
2. The SOWs describe annual time series of MSL over the  $T = 70$  years house lifetime so  $\mathbf{s} \in \mathbb{R}^T$
3. The system model  $f$  quantifies up-front costs (the cost of elevating) and lifetime expected damages (the structural cost of experiencing floods), given a decision  $x_i$  and SOW  $s_j$ , by integrating economic and engineering damage models over a probability distribution for storm surge. We elaborate upon these metrics in Section 4.3.

In the remainder of this section we describe data sources and treatment of SLR (Section 4.1), storm surge (Section 4.2), damages and metrics (Section 4.3), and finally the subjective probabilistic models  $p_{\text{belief}}$  used to apply the re-weighting method described in Section 2.3 to this case study (Section 4.4).

##### 4.1. Sea Level Rise

We analyze simulations of MSL at Sewells Point, VA from four probabilistic physical models using data published in Ruckert et al. (2019). The four



**Figure 3.** Conceptual diagram of the considered example. A state of the world (SOW) consists of a description of the uncertain factors (red). We model a problem with a single lever (yellow), which is how high to elevate a house ( $\Delta h$ ). For each SOW (red) and each value of  $\Delta h$ , the system model (blue) is used to calculate performance metrics (gray). We also compute a third metric, expected lifetime costs, which is the sum of up-front costs and lifetime expected damages.

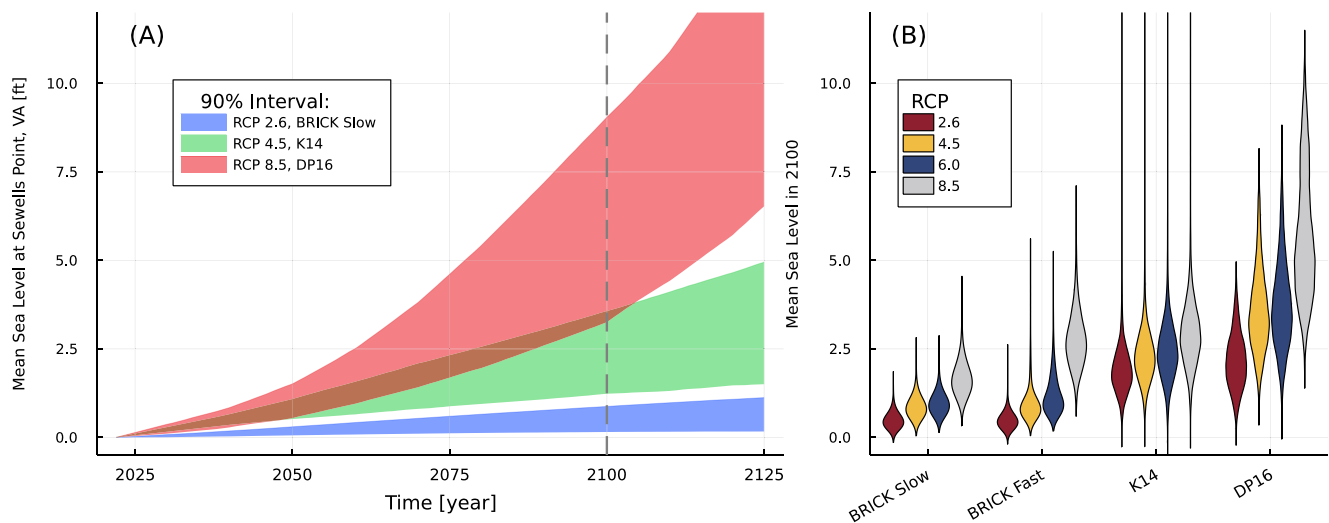
**Table 1**  
Summary of Parameters, Their Notation, And How Their Uncertainty Is Represented

Name	Symbol	Uncertainty
MSL	$\bar{y}(t)$	Deeply uncertain: four physical models $\times$ four RCP scenarios
Storm surge	$y'(t)$	Probabilistic: Bayesian inference on a stationary GEV model
Annual maximum flood	$y(t)$	Deterministic: $y(t) = \bar{y}(t) + y'(t)$
Discount rate	$\rho$	Deterministic: 2.5% per year
Depth-damage	$D(h-y)$	Deterministic: based on HAZUS model (see Zarekarizi et al., 2020)
Elevation cost	$C(\Delta h)$	Deterministic: a piecewise linear model following Zarekarizi et al. (2020)
Initial height	$h_0$	Deterministic: 1 ft below the BFE, unless otherwise noted
House floor area	–	Deterministic: 1,500 ft <sup>2</sup>
Structural value	–	Deterministic: \$200,000
House lifespan	$T$	Deterministic: 70 years

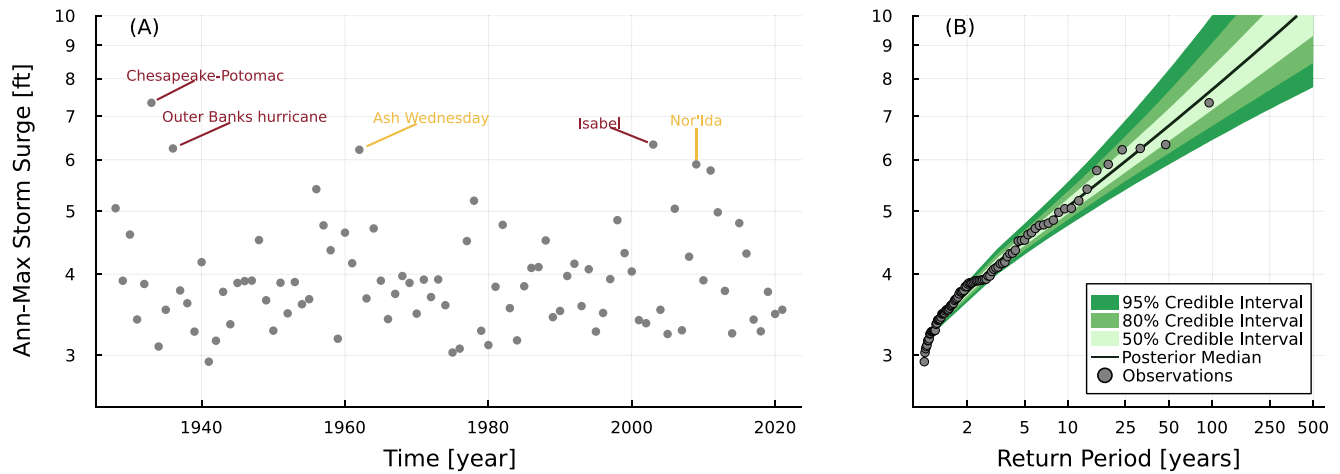
Note. Symbols describing the decision-analytic framework are described in Figure 1.

physical process models considered are (a) the BRICK model (version 0.2) with slow (“BRICK Slow”) and (b) fast (“BRICK Fast”) ice sheet dynamics (Wong et al., 2017), (c) the Kopp et al. (2014) model (“K14”), and (d) the DeConto and Pollard (2016) model (“DP16”). The Kopp et al. (2014) and DeConto and Pollard (2016) models have a 10 year time step, which we linearly interpolate onto a 1 year time step for consistency. Estimates of nonstationary MSL also depend on anthropogenic forcing, which is itself deeply uncertain (E. Ho et al., 2019; Srikrishnan et al., 2022). To sample this uncertainty, we use simulations from each physical model under four RCP scenarios, yielding sixteen time-varying probabilistic scenarios of MSL.

The choices of physical model and RCP scenario jointly determine future MSL  $p(\bar{y}|t)$ . Figure 4a shows the time-varying 90% credible intervals of MSL for three representative models. The divergence between the best-case (blue) and worst-case (red) models is small in the early 21st century and increases rapidly thereafter. Figure 4b shows the PDFs of mean sea level in 2100 (dashed vertical line in panel (a)) under each of the 16 probabilistic scenarios considered. The stark differences between different scenarios of SLR arise primarily from different representations of Antarctic Ice Sheet contributions to global SLR and statistical calibration methodologies. For a more detailed discussion we refer the reader to Ruckert et al. (2019). We return in Section 5.2 to the challenge of decision making given multiple scenarios.



**Figure 4.** Projections of future mean sea level depend strongly on the choices of physical model and forcing (a): 90% confidence intervals for mean sea level at Sewells Point, VA as a function of time for a representative subset of three probabilistic models (out of sixteen) (b): probability distribution of mean relative sea level at Sewells Point, VA in the year 2100 for each probabilistic model considered.



**Figure 5.** Annual maximum storm surges (after subtracting mean relative sea level) at Sewells Point, VA from the freely available National Oceanic Atmospheric Administration tides and currents data archive (National Oceanographic and Atmospheric Administration, 2022) (a): time series of historic storms. Red (yellow) arrows denote notable tropical cyclones (Nor'easters) (b): return periods. Dots indicate observed values; their  $x$ -value is their plotting position using the Weibull formula (Equation S5 in Supporting Information S1). Gray lines show the 50%, 80%, and 95% posterior confidence intervals from the Bayesian GEV fit (Section 4.2).

#### 4.2. Storm Surges

Following prior work (e.g., Garner & Keller, 2018; Sriver et al., 2018), we model annual maximum floods  $y(t)$  as the sum of sea level  $\bar{y}(t)$ , described in the previous subsection, and annual maximum storm surges  $y'(t)$ , neglecting any potential hydrodynamic interactions.

We use data on storm surge at Sewells Point, VA (gauge 8638610) from the NOAA tides and currents data archive (National Oceanographic and Atmospheric Administration, 2022). Hourly recordings of water level are available from 1928 to the present; we use data from the period 1 January 1928 to 31 December 2021. For each calendar year we first remove the annual mean, then calculate the maximum water level. We refer this time series of annual maximum storm surges as  $y'(t)$ . We display this time series of annual maxima storm surges in Figure 5a. The largest recorded surge was the Chesapeake-Potomac hurricane of 1933, which caused a surge of over 7 ft at this gauge, but other hurricanes and Nor'easters have caused surges above 6 ft.

We model future storm surge using a stationary GEV model:

$$y'(t) \sim \text{GEV}(\mu, \sigma, \xi), \quad (3)$$

where  $y'(t)$  is the storm surge (above MSL) in year  $t$  and a GEV distribution with location, shape, and scale parameters  $\mu$ ,  $\sigma$ , and  $\xi$ , respectively, has the PDF given in Equation S1 in Supporting Information S1. This model assumes stationarity, neglecting any potential time dependence.

Our approach to model assessment is based on the concept of principled workflow design for model building and checking (see Gelman et al., 2020, for details). One model choice, analogous to the choice of statistical distribution or the assumption of stationarity, is the choice of how to represent prior information. We include two forms of prior information. First, we constrain the shape parameter to be positive,  $\xi > 0$ , to reflect knowledge about the support of  $y'$ , which for a variable distributed according to Equation S1 in Supporting Information S1 is:

$$\text{supp } y' = \begin{cases} \xi < 0 : & y' \in (-\infty, \mu - \sigma/\xi) \\ \xi > 0 : & y' \in (\mu - \sigma/\xi, \infty). \end{cases}$$

Since storm surges cannot be negative, only the latter is physically defensible, justifying our choice to constrain the shape parameter to be positive. Second, we add weakly informative priors. Rather than applying prior information directly over the joint distribution of the parameters  $\mu$ ,  $\sigma$ ,  $\xi$ , we instead apply a prior over extreme quantiles of the distribution, as in Coles and Tawn (1996). Specifically, we apply Inverse Gamma priors over the 2, 10, 100, and 500 years return levels, with means of 4, 6, 10, and 15 ft and standard deviations of 1.5, 1.75, 2.25, and



2.75 ft, respectively. The parameters of the Inverse Gamma distribution can be calculated from these moments (see Equation S3 in Supporting Information S1). These means and standard deviations were chosen to represent plausible physical ranges (Figure S4 in Supporting Information S1).

For inference, we draw 10,000 samples from the posterior distribution  $p(\mu, \sigma, \xi|y')$  using Hamiltonian Markov Chain Monte Carlo (Betancourt, 2018; Hoffman & Gelman, 2011) implemented in the Turing package of the Julia programming language (Besançon et al., 2021; Bezanson et al., 2012; Ge et al., 2018; Perkel, 2019; Tarek et al., 2020). Diagnostics suggest (though cannot guarantee) convergence (see Table S1 in Supporting Information S1). We evaluate the model's fit using posterior predictive checks (see Gelman et al., 2020, Section 2.4 and references therein). Using the lag 1 and 2 partial autocorrelations, sample maximum, sample minimum, sample median, and Mann-Kendall test value as Bayesian test statistics, we find that draws from the posterior predictive distribution match the observed test statistics credibly (Figure S9 in Supporting Information S1) although panels (a and b) suggest the possibility of temporal structure not captured by our stationary IID model. Future efforts could represent this structure by conditioning the parameters of the distribution on relevant climate indices (as in Farnham et al., 2018, 2017; Ossandón et al., 2021; Wong, 2018).

Other model validations lend confidence to the stationary GEV model selected. For example, Figure 5b shows the estimated return periods for these storm surges; the estimated return period (shading) matches the empirical plotting position (dots) and a positive control test (Figure S6 in Supporting Information S1) validates the model's ability to recover known parameter values.

### 4.3. Damages and Metrics

The system model ("relationships" in Figure 3) is comprised of two key pieces. The first is a fragility model that estimates the expected flood damages for a particular year ("expected annual damages"), given the elevation of the house and the mean sea level for that year. The second model converts a time series of annual expected damages into lifetime expected damages.

We define expected annual damages in year  $t$  as the expectation of the damage function with respect to storm surge. This expectation depends on the house's height ( $h = h_0 + \Delta h$ ) where  $h_0$  is the initial height relative to the gauge and  $\Delta h$  is the amount by which the house is elevated. The expected annual damage is thus

$$\text{EAD}(t) = \mathbb{E}[D(h - \bar{y}(t))] = \int_{y'} p(y') D(h - (\bar{y}(t) + y')) dy', \quad (4)$$

where  $D(h-y)$  is a deterministic function specifying damage as a function of flood depth (relative to the house) and  $p(y')$  is the probability density of storm surge. Following Zarekarizi et al. (2020), we use the Hazard U.S. (HAZUS) depth-damage curves provided by FEMA; this depth-damage relationship is shown in Figure S1 in Supporting Information S1. For comparison, Figure S1 in Supporting Information S1 also shows the "Europa" depth-damage relationship developed by the Joint Research Center of the European Commission's science and knowledge service (Huizinga & Szewczyk, 2016). Both models show damage increasing with flood depth before reaching an upper limit but differ in the value of the upper limit and the rate at which damages approach it. Although Zarekarizi et al. (2020) demonstrate that the choice of fragility function is important for informing house elevation, we use only the HAZUS model for simplicity.

The expected annual damage is sometimes calculated by assuming analytically tractable functional forms for the depth-damage relationship and for the distribution of hazard (e.g., van Dantzig, 1956). However, the convolution of the HAZUS depth-damage equation with the GEV posterior does not have a tractable analytic solution. Instead, we estimate this convolution through a Monte Carlo method (see Section S1.2 in Supporting Information S1 for details). Then, because the expectation in Equation 4 depends only on  $h - \bar{y}(t)$ , we calculate expected annual damages for a wide range of possible heights, then use this to train a computationally efficient surrogate model (using linear interpolation; see Section S1.3 in Supporting Information S1).

The second component of the system model converts a time series of EAD into lifetime expected damages, which we define as the up-front discounted sum of expected annual damages:

$$\text{LED} = \sum_{t=t_i}^{t_f} \gamma^{(t-t_i)} \text{EAD}(t), \quad (5)$$

**Table 2**  
Subjective Probability Distributions Over Sea Level Rise From 2022 to 2100, That is.,  $p_{\text{belief}}(\psi)$

Name	Parameters		Percentiles (in ft)				
	$\alpha$	$\theta$	2.5	25.0	50.0	75.0	97.5
Slow SLR	1.75	0.50	0.08	0.39	0.72	1.19	2.57
Uncertain SLR	1.75	1.25	0.21	0.98	1.79	2.97	6.41
Rapid SLR	3.50	1.25	1.06	2.66	3.97	5.65	10.01

*Note.* The name of the distribution, the parameters of the Gamma distribution with shape  $\alpha$  and scale  $\theta$ , and the 2.5, 25, 50, 75, and 97.5th percentiles (values in ft).

where  $\gamma = 1 - \rho$  ( $\rho$  being the discount rate), the initial time  $t_i = 2022$ , and the end time  $t_f = t_i + T - 1$ . Although Zarekarizi et al. (2020) show that uncertainty in the discount rate is important for decision support, we use a fixed discount rate (see Table 1) for the purposes of this didactic study. For a more theoretical discussion see Arrow et al. (2013).

To assess the performance of a given decision for a specific SOW (“Metrics” in Figure 3), we calculate the following metrics for each decision-SOW combination.

1. “Up-front cost” is the cost of elevating a house. Following Zarekarizi et al. (2020), we use estimates of construction cost from the Coastal Louisiana Risk Assessment (Fischbach et al., 2012). We normalize this cost by house value; this cost curve is shown in Figure S3 in Supporting Information S1 and shows a large up-front cost plus a piecewise linear marginal cost.
2. “Lifetime expected damages” is calculated following Equation 5.
3. “Expected lifetime costs” is the sum of lifetime expected damages and up-front costs.

#### 4.4. Subjective Probability Distributions for Sea Level Rise

We construct three probabilistic models for  $p_{\text{belief}}(\psi)$ , which represents the amount of SLR from 2022 to 2100.

We use a Gamma distribution for all three probability distributions, parameterized following Equation S4 in Supporting Information S1. The distributions were chosen to be illustrative, rather than to reflect any particular scientific consensus. The Gamma distribution is a flexible distribution that can be used to model skewed, lower-bounded distributions, making it an appropriate choice for modeling subjective uncertainty about SLR. Table 2 specifies the parameters of these distributions, as well as some quantiles of the distributions. Their PDFs are also plotted in Figure 8a.

We developed these subjective distributions for didactic purposes, to illustrate a range of possible beliefs. We can compare them, for example, with analysis published by NOAA, which project 1.94, 2.62, 4.2, 5.25, and 6.89 ft for the low, intermediate, low intermediate, intermediate high, and high scenarios, respectively (Sweet et al., 2022, Table 2.4). We can also compare to the analyses of Srivier et al. (2018) which uses a rescaled Beta distribution with bounds of 0.83–8.2 ft and a most plausible estimate of 3.1 ft. Our samples bound all of these estimates.

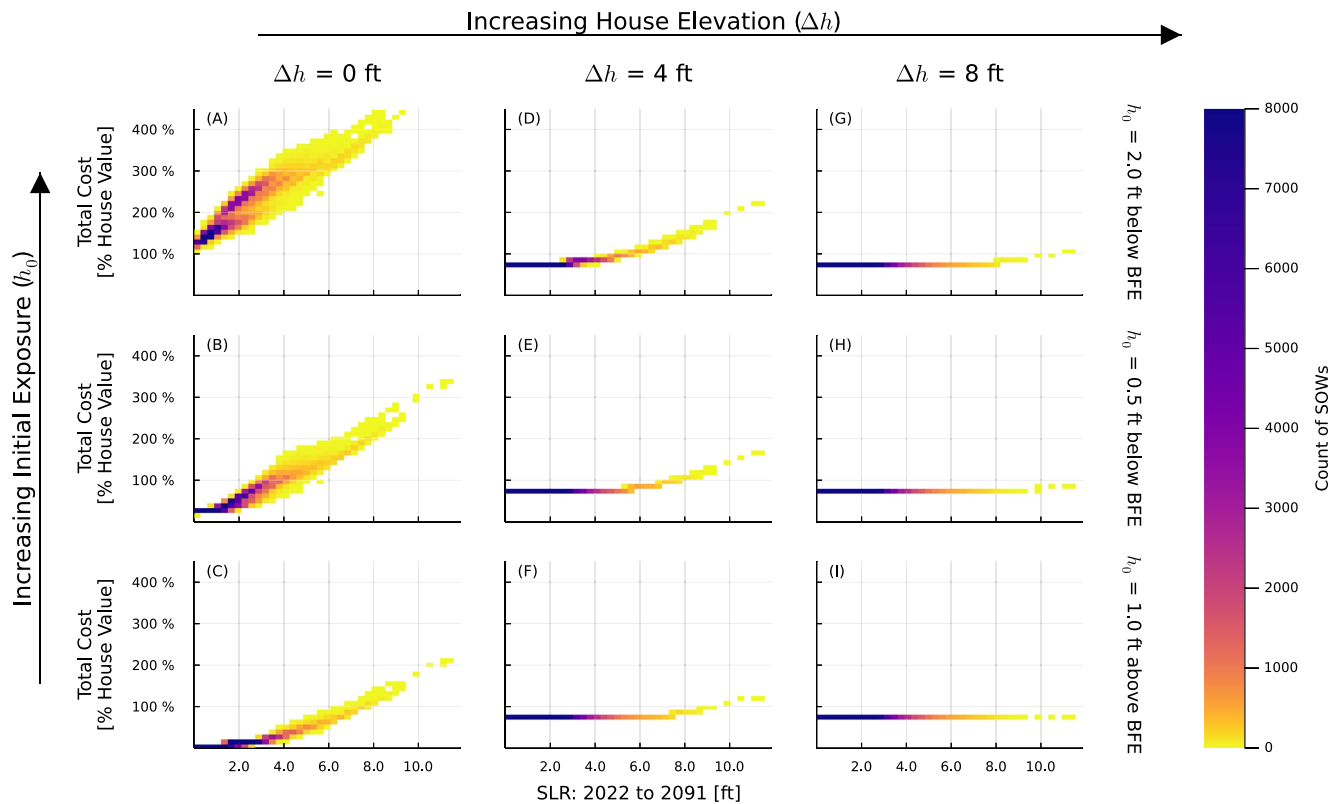
## 5. Results and Discussion

We illustrate our approach to synthesizing uncertainties by sequentially analyzing the house elevation problem through multiple lenses for DMDU. This allows us to demonstrate the advantages and limitations of each approach, and to highlight the value of synthesizing across multiple scenarios.

### 5.1. Exploratory Modeling

We begin by using our model in an “exploratory” mode with an aim of learning about interactions between system dynamics and decisions.

One application of exploratory analysis is to reveal the range and variation in outcomes, conditional on taking a particular decision. Figure 6 shows the dependence of expected lifetime costs (damages plus up-front costs; y-axis) as a function of SLR over the house lifetime (x-axis), height increase ( $\Delta h$ ; columns), and initial elevation ( $h_0$ ; rows). The outcomes with lowest total lifetime costs arise when the house is not elevated ( $\Delta h = 0$ ) and SLR is minimal (bottom left corners). The outcomes with highest total lifetime costs arise when the house is elevated only slightly and SLR is rapid. As  $\Delta h$  increases, the best-case scenario becomes more expensive because up-front costs increase, but worst-case scenarios become less expensive because even if SLR is substantial, damages will be negligible.



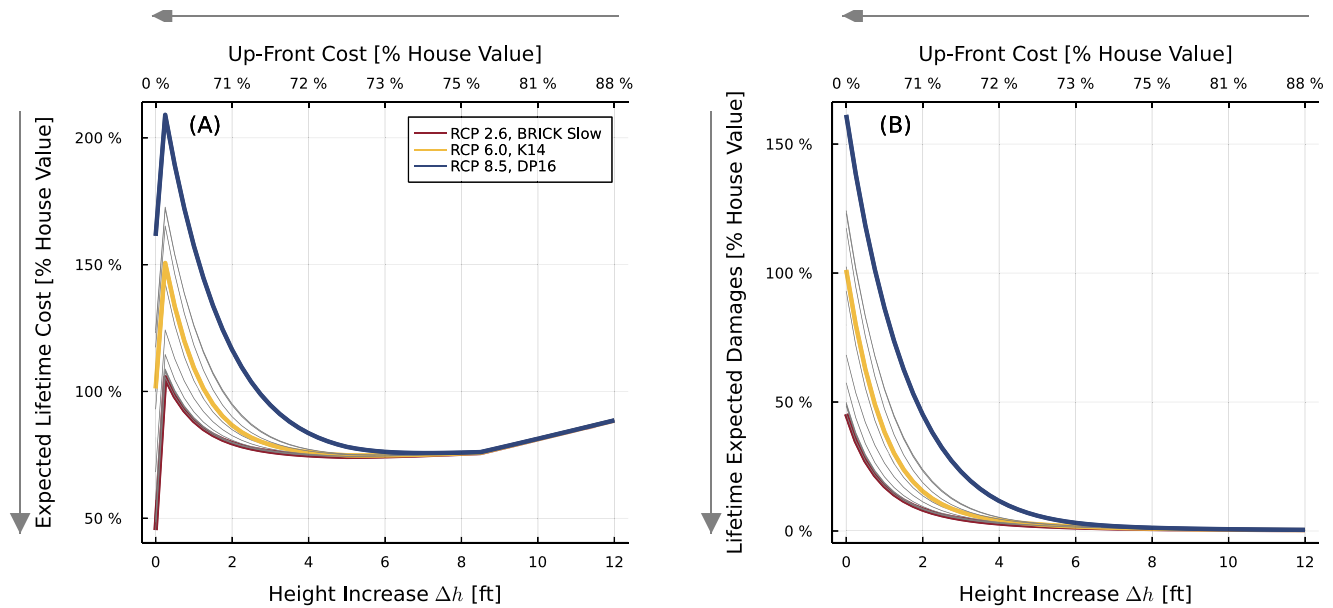
**Figure 6.** Scenario maps show the dependence of expected lifetime cost (damages plus up-front cost) as a function of mean relative sea level (MSL) in 2100 for several values of initial height ( $h_0$ ) and house elevation ( $\Delta h$ ). Colors indicate the number of states of the worlds of falling within each box. The lowest-cost outcomes occur when exposure is low ( $h_0$  is large and sea level rise [SLR] is minimal) and the house is not elevated (no up-front cost). The highest-cost outcomes arise when exposure is high ( $h_0$  is small and SLR is rapid) and investment is inadequate. In all cases, elevating the house reduces the variance in total lifetime cost. Values are sensitive to model constants; see Table 1.

This analysis answers “what-if” questions like “given  $h_0$  and  $\Delta h$ , what is the range of total costs a homeowner could face if SLR over the house lifetime is 1 ft or 10 ft.” For some decision-makers, contextualizing this information against a few scenarios of SLR (e.g., those of Sweet et al., 2022) may prove sufficient for decision making. However, this analysis is silent on how to estimate cost-benefit comparisons, return periods, and other trade-offs.

## 5.2. Scenario-Conditional Probabilistic Analysis

We now turn to the scenario-conditional analysis described in Section 2.2. Whereas the exploratory analysis of the previous subsection interpreted each time series of future sea level as a sample from the space of possible futures, we can also interpret each SOW as a draw from one of the 16 probabilistic scenarios of SLR shown in Figure 4. As discussed in Section 2.2, this allows a formal estimation of decision metrics, conditional on the chosen scenario.

As discussed in Section 2.2, this probabilistic interpretation allows us to compute expected values of functions. For example, Figure 7a plots the expected total lifetime cost as a function of  $\Delta h$  for the 16 probabilistic scenarios considered (we highlight three representative models). This panel shows lifetime expected damages as a function of  $\Delta h$ , shown in Figure 7b, plus the up-front cost of construction. Because there are high fixed costs associated with building (see cost curve in Figure S3 in Supporting Information S1), it generally does not make sense to raise the house by only a small amount, since this incurs these fixed costs without providing substantial damage reduction. Figure 7 shows that estimates of trade-offs between up-front cost and expected lifetime costs are highly sensitive to the chosen scenario. For small  $\Delta h$ , expected costs are low under optimistic scenarios (e.g., RCP 2.6 with slow ice sheet dynamics; red lines) and high under pessimistic scenarios (e.g., RCP 8.5 with the DP16 model; blue lines). Estimates of the optimal decision are highly sensitive to the choice of scenario. For example, under the most pessimistic scenario (blue line), the cost-minimizing height increase is 6 ft, which incurs



**Figure 7.** Each probabilistic model or scenario leads to a different estimate of the Pareto frontier. For emphasis, we highlight three representative models: the Brick Slow model (Wong et al., 2017) under RCP 2.6, the K14 (Kopp et al., 2014) model under RCP 6.0 and the DP16 model (DeConto & Pollard, 2016; Kopp et al., 2017) under RCP 8.5 (a): trade-off between up-front cost (which is a monotonic function of height increase) and expected lifetime costs (b): trade-off between up-front cost and lifetime expected damages (Equation 5). Light gray lines show estimates for all 16 models (four representative concentration pathway [RCP] scenarios  $\times$  four physical process models) considered. Colored lines highlight three representative models for emphasis. The gray arrows indicate the direction of preference.

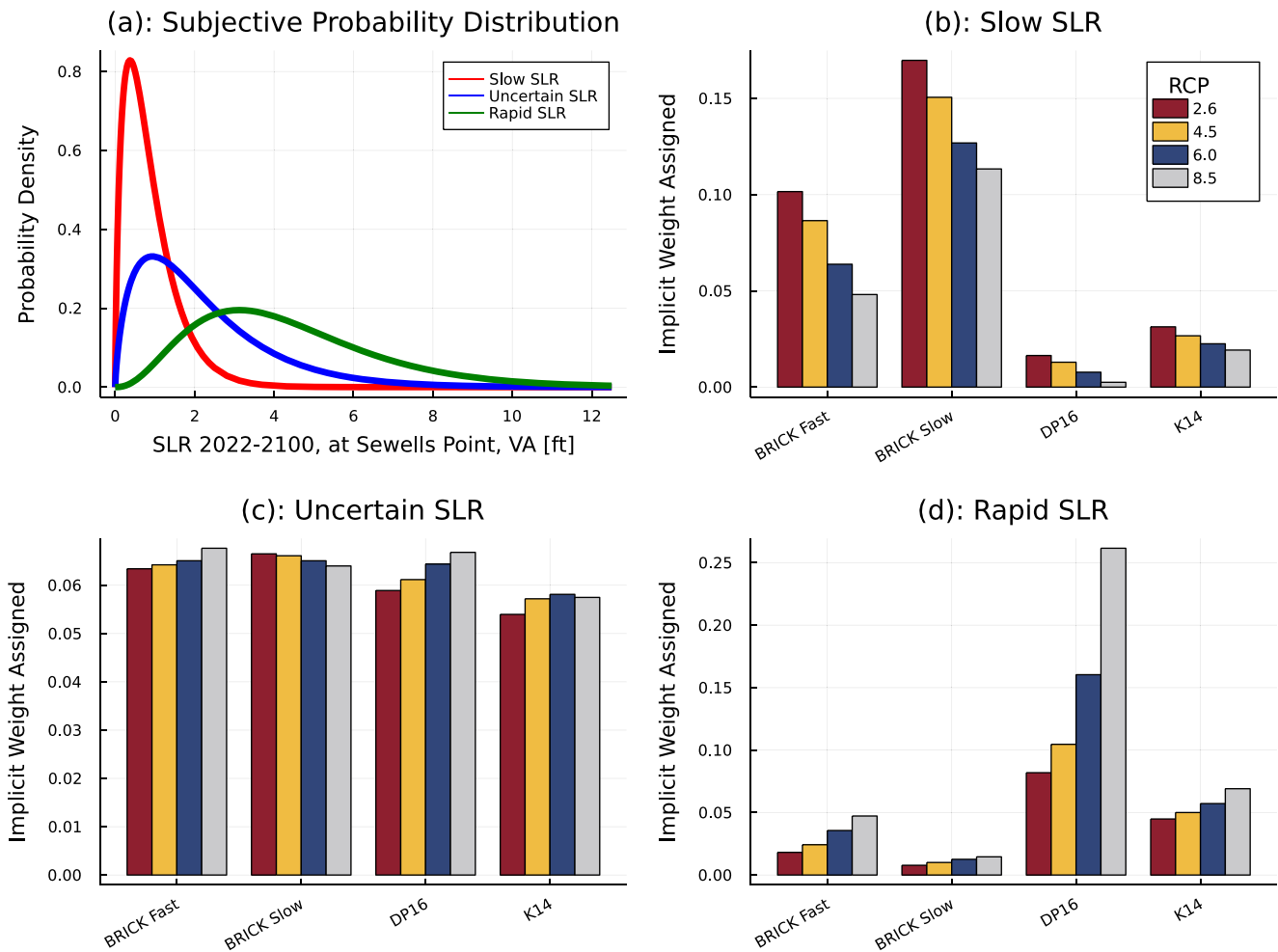
an up-front cost of 73% of the house value but reduces lifetime expected damages by over 150% of house value. Under the most optimistic scenario (gray line), the cost-minimizing decision is to not elevate, as elevating 6 ft incurs the same up-front cost yet reduces lifetime expected damages by less than 50% of house value.

This approach is, in a sense, another form of exploratory modeling: instead of considering a very large ensemble of SOWs, we consider a much smaller set of probabilistic scenarios. Scenario-conditional analysis can be attractive because it allows modelers to focus on their domain expertise (e.g., the response of ice sheets and global sea levels to a particular climate future). However, conditioning simulations on a set of climate futures and physical models presents what we term “the multiple PDF problem” because it leaves decision makers with many PDFs to choose from and hence many trade-off curves to navigate. The multiple PDF problem has also been discussed in other contexts. For example, Sharma et al. (2021) model the reliability of stormwater infrastructure under different climate models and downscaling methods, finding diverging estimates of future rainfall hazard, even under a single RCP scenario. Similarly, Wong and Keller (2017) construct 18 probability distribution functions for future flood risk in New Orleans, considering multiple models for ice sheet dynamics and storm surge and multiple RCP scenarios. As a last example, Haasnoot et al. (2021) identify global adaptation needs for different SLR scenarios. Although this scenario-conditional analysis is appropriate for understanding differences between models, its key limitation is that it *places the burden for deciding which probabilistic scenario to design for onto the end user*. Since not all house owners or contractors have expertise in assessing the relative likelihood of different climate futures, they may not be well positioned to make this decision.

### 5.3. Synthesizing Deep Uncertainties for Decision Analysis

The SOW re-weighting framework described in Section 3 can help overcome the limitations of scenario-conditional analysis. In this section we illustrate how this approach can help to shed light on climate risk management under deep uncertainty. We present results using each of the models for  $p_{\text{belief}}$  outlined in Section 4.4; these three distributions are shown in Figure 8a.

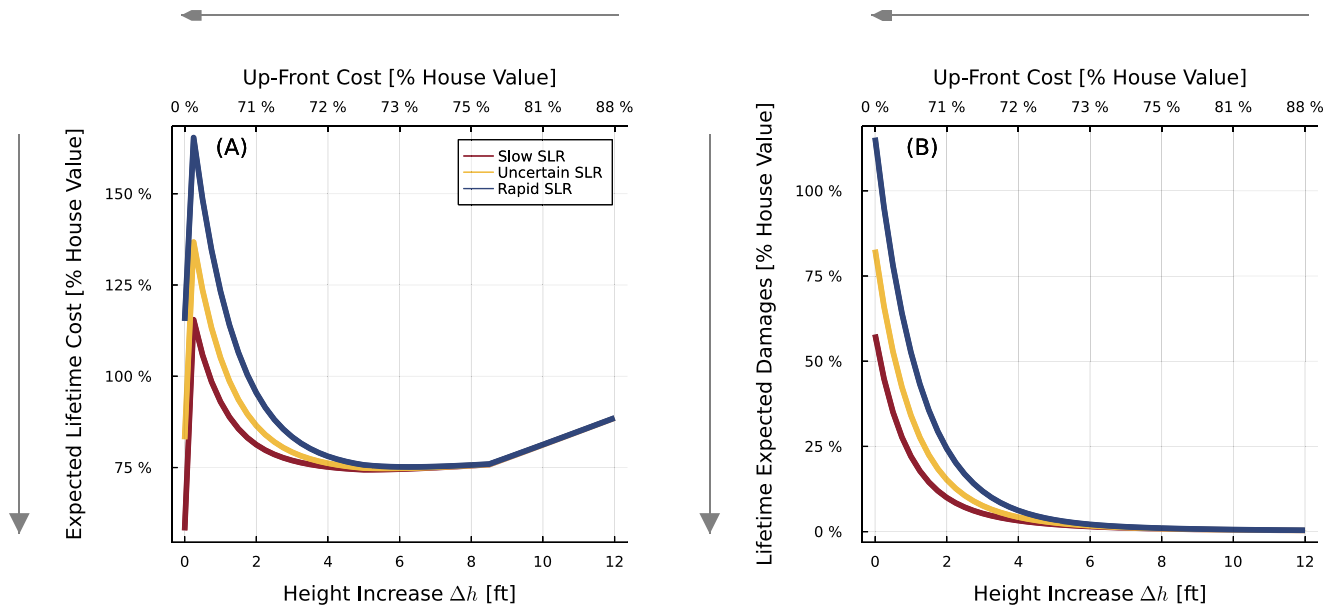
One application of this method is to diagnose the assumptions which which different  $p_{\text{belief}}$  are consistent. Figure 8b–d) shows the total weight that each choice of  $p_{\text{belief}}$  assigns to SOWs generated by each RCP scenario and physical model. Specifically, weights are computed as the sum of weights assigned to each SOW sampled



**Figure 8.** Impact of different subjective probability distributions for local sea level on implicit weight given to each representative concentration pathway (RCP) scenario and physical model. We develop three distributions representing plausible probabilistic beliefs ( $p_{\text{belief}}$ ) over mean relative sea level at Sewells Point, VA in 2100, relative to the present. The probability density functions of these distributions are shown in panel (a). In panels (b–c) we show the relationship between these distributions and the 16 probabilistic models (four representative concentration pathway scenarios and four physical representations) available. Specifically, (b–c) show the average weight given to each model by each choice for  $p_{\text{belief}}$ .

from that model. For example, the rapid SLR scenario (green line in Figure 8) places most weight on SOWs produced by the DP16 model, and particularly on RCP 8.5 which by some accounts is unlikely given current policy (Hausfather & Peters, 2020; Srikrishnan et al., 2022). Conversely, the slow SLR scenario (red line) places most weight on the BRICK models, particularly RCP 2.6 (also unlikely given current policy; Hausfather & Peters, 2020; Srikrishnan et al., 2022) and RCP 4.5. The uncertain SLR scenario (blue line) allocates approximately equal weight across models. Decision analysts can use this approach as a diagnostic to understand the assumptions implicit to their choice of  $p_{\text{belief}}$ .

This method can also be used to calculate expectations, allowing us to revisit the trade-off diagrams of Figure 7. Figure 9 shows the total lifetime cost (panel A) and lifetime expected damages (panel B) under each choice of  $p_{\text{belief}}$ . Notably, they give different guidance. Under an assumption of rapid SLR, elevating the house by approximately 6 ft costs 73% of house value and reduces damages by over 100% of house value, yielding a benefit to cost ratio of approximately 1.25. Under an assumption of slow SLR, the same decision reduces damages only by 50% of house value, yielding a benefit to cost ratio of approximately 0.7. Under the intermediate/uncertain SLR assumption, the expected lifetime costs are similar for elevating or not elevating the house, and thus the benefit to cost ratio is nearly 1. Under all assumptions, elevating by only a few feet is impractical because it involves paying the large fixed costs of elevation (Figure S3 in Supporting Information S1) but offers relatively little flood reduction. Based on this analysis, we would recommend that the owner if this hypothetical home elevate by



**Figure 9.** As Figure 7, but with Pareto frontiers for the full distribution of outcomes using the three models of  $p_{\text{belief}}$  (colors).

approximately 4–6 ft or not at all. Alternatively, the homeowner could choose to defer the decision of whether, and how high, to elevate; our analysis did not consider this possibility but there is a rich literature on flexible design and engineering options analysis in climate risk analysis (e.g., Fletcher, Lickley, & Strzepek, 2019; Fletcher, Strzepek, et al., 2019; Hui et al., 2018; Garner & Keller, 2018; Herman et al., 2020; de Neufville & Smet, 2019).

## 6. Limitations and Research Needs

Several limitations to our study merit further discussion. The first category has to do with limitations of the underlying method proposed for re-weighting SOWs. For example, we develop a subjective probabilistic model  $p_{\text{belief}}(\Psi)$  over MSL in the year 2100. Although this is a low-dimensional representation of the full time series, it is not a sufficient statistic. In other words, many possible low-dimensional representations are possible and time series with the same MSL in 2100 May differ in other ways. For problems with more sources of uncertainty, such as multisector problems, choosing an appropriate low-dimensional representation may prove challenging. In such settings, diagnostics and sensitivity analyses may shed light on the appropriateness of different modeling choices. A related concern is that we developed our three distributions for  $p_{\text{belief}}(\Psi)$  in an ad hoc fashion that may not represent well-calibrated beliefs. Although this is appropriate for our didactic illustration, recent advances in Bayesian elicitation of expert opinion (see Mikkola et al., 2021, and references therein) can be applied to improve decision making in real world case studies. More fundamentally, our method assumes that there exists an expert capable of integrating over the many processes that drive SLR, from global greenhouse gas emissions to the global carbon cycle to climate sensitivity and ice sheet response (Morgan, 2014). An alternative approach would be to build a probabilistic model for each of these steps, and to use each as an input to the next to develop a fully probabilistic model for SLR. Yet while some progress has been made developing probabilistic models for specific elements of this model chain (e.g., Srikrishnan et al., 2022; Wong et al., 2017), this remains a computational and conceptual challenge.

The second category of limitations has to do with the case study and our interpretation of the house elevation decision problem. This problem intersects with decisions about where to live and how to manage household finances, both of which are highly complex. One extension of our analysis would be to consider additional decision objectives. In particular, we hypothesize that incorporating improved representations of risk aversion into decision support may substantially improve their usability. One could also extend the analysis to consider additional sources of uncertainty such as depth-damage relationships (Nofal et al., 2020; Rözer et al., 2019), the cost of elevating a house, the house lifespan, the effective discount rate, and value of the land on which the house is built (Zarekarizi et al., 2020). Finally, while here we consider the decision to be a one-time decision, one could

also frame this as a sequential decision problem. The analysis of sequential decision problems applies tools from control theory and reinforcement learning to identify policies that map “triggers” (i.e., state variables) to decisions (Herman et al., 2020). Yet although framing the decision through a sequential lens can increase adaptability and improve outcomes (Fletcher, Miotti, et al., 2017; Garner & Keller, 2018), decisions and outcomes remain highly sensitive to the characterization of uncertainty (Herman et al., 2020), and thus the problem of synthesizing across deep uncertainties remains relevant.

These limitations motivate several directions for future research. From a methodological perspective, developing model chains that capture uncertainties in global energy and economic pathways, global climate sensitivity, and local hazard response (see Figure 1 of Moss & Schneider, 2000) offers a principled framework for fully probabilistic estimation of local hazard, subject to (still necessarily subjective) probabilistic models for key parameters. From a decision support perspective, improved understanding of the conditions under which household-scale strategies for flood risk management, like elevation, achieve relevant objectives could support improved resilience and adaptation. Additionally, since developing bespoke analyses for each house may be impractical, identifying decision rules that are applicable across different house characteristics may improve usability and guidance. Finally, there are many parallels between DMDU and subjective Bayesian literature on building predictive models in the “ $\mathcal{M}$ -closed” case when “all models are wrong” (Box, 1976; Gelman & Shalizi, 2013), and thus future work can demonstrate how to incorporate techniques from Bayesian workflow (see Gelman et al., 2020) into DMDU methodologies.

## 7. Conclusions

This study develops a framework designed to increase the transparency of quantitative decision analysis under deep uncertainty. We develop a framework capable of blending iterative, stakeholder-driven exploratory modeling (see, e.g., Helgeson et al., 2022) with subjective probabilistic expert assessment. Such an approach is urgently needed given that deeply uncertain nonstationarity hazards pose a fundamental challenge to classical methods of hazard estimation. We use a didactic case study of house elevation in the coastal zone to illustrate a method for transparently synthesizing across deep uncertainties.

The proposed SOW re-weighting framework can be applied to inform critical challenges in climate risk management. An obvious area of application is to the design of infrastructure. For example, much of the stormwater infrastructure in the United States is inadequate for current and anticipated future climates (Lopez-Cantu & Samaras, 2018). Yet upgrading this infrastructure is costly and subject to large uncertainties between rainfall models (Sharma et al., 2021) and RCP scenarios. Similarly, decisions like levee heightening (Garner & Keller, 2018; Odde et al., 2017; van Dantzig, 1956) and sea wall design (United States Army Corps of Engineers, Galveston District & Texas General Land Office, 2021; Appendix D., pp. 2–59) are subject to deep uncertainties including SLR. Investments in water resources planning and management also depend on assumptions of future water demand, availability, and technologies (Trindade et al., 2019). And analyses of climate change mitigation options, such as estimates of the social cost of pollutants (Errickson et al., 2021) or cost-minimizing energy transition pathways, are conditional on probabilistic models for inputs like technology prices and population.

Of course, all models are ultimately wrong (Box, 1976). Thus seeking decisions that perform well across a range of assumptions, and improving the decision space through robust design and flexibility, can improve outcomes. Yet whenever decisions are compared quantitatively, assumptions about the probability of different possible futures are necessarily made. We call for researchers studying climate risk management to make these implicit assumptions explicit, and we suggest that coordinated guidance can help practitioners determine better design criteria.

## Data Availability Statement

All code, including source code, is available under the GNU Public License (version 3) at <https://github.com/jdossgollin/2022-elevation-robustness>. This code is written in the open source Julia programming language and detailed instructions for reproducing our results are provided. A permanent, citeable archive of the precise version of the codes used in this study is also available on Zenodo at <https://doi.org/10.5281/zenodo.6814588>.

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