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3 **Hybrid Machine Learning Framework for Hydrological Assessment**  
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## Abstract

This study introduces a novel hydrological assessment tool (HAT) based on hybrid machine learning (HML) framework. The HML framework combines an unsupervised clustering technique and a supervised classification technique, to determine reasonable performance ratings (unsatisfactory, satisfactory, good, and very good) and build a practical assessment tool. Hydrologically significant error indices are used to cluster the performance rating groups and train the HAT. The HAT was applied to the National Water Model (NWM), which is operated in real time for the continental United States (CONUS). For establishing, training, and validating the HAT, data from October 2013 to February 2017 were used, and a performance assessment was conducted on the NWM in the San Francisco Bay Area. As a result, the HAT determined the performance ratings that were reliable in terms of the statistics and hydrograph. It was confirmed that the HAT could perform an accurate hydrograph assessment as the concordance rate of the performance ratings was 98%. The NWM was evaluated against 57 USGS streamflow gauges using the HAT and was found to perform with 46% on average, good and very good ratings. The HML framework, an integral part of the HAT, is expected to be useful not only in hydrological analysis but also across all geophysical fields that deal with physical processes.

**Keywords:** Hydrological assessment, Hybrid machine learning, National water model, Streamflow evaluation, Performance ratings

## 60 **1. Introduction**

61

62 Identifying and predicting the response of hydrologic systems by using a simulation  
63 model are very important for reducing damages from natural disasters (Abbott et al., 1986;  
64 Dutta et al., 2003; Rozalis et al., 2010; Yoo et al., 2012; Kim et al., 2018a; 2018b). This is  
65 because a hydrologic model can identify in advance the potential occurrence of various  
66 water-related natural disasters as it estimates and predicts the flow and volume from surface  
67 to groundwater runoff in time and space (Henderson and Wooding, 1964). Moreover, by  
68 virtue of advanced remote sensing techniques, quantitative precipitation estimation schemes  
69 (Kim et al., 2015), and correction methods (Yoo et al., 2014; Kim and Yoo, 2014) to improve  
70 accuracy of meteorological inputs (e.g. precipitation), hydrological products from models  
71 will play a role in a wide range of disciplines. Many types of hydrologic models have  
72 advanced from the basic lumped approach that combines characteristics across an entire  
73 watershed to provide forecast information at an outlet point to distributed hydrologic models  
74 that account for spatially varying characteristics across the watershed and can be used to  
75 simulate a local-scale flood (Liang et al., 1994; Arnold et al., 1998; Singh et al., 2002). In  
76 contrast to the evolution and improvement of hydrologic modeling, general hydrological  
77 evaluation methods have remained simple, most relying on a few error indices. A  
78 hydrological evaluation method is not simply to determine whether there are many or few  
79 errors; it should reasonably determine the reliability of outputs and present objective indices  
80 understandable to users. The limitations of current hydrological evaluation methods must be  
81 overcome, and a new assessment tool is required that can objectively evaluate any hydrologic  
82 model performance.

83 There are many potential and important uses for the hydrological evaluation method  
84 in hydrology. Its main purposes include calibrating the model, evaluating its performance,

85 and communicating with stakeholders. The hydrologic model, which has a complex structure  
86 and various parameters, requires a calibration process depending on the status of outputs, and  
87 the evaluation of its results determines the necessity, strategy, and extent of calibration  
88 (Moriasi et al., 2007). As the model's performance differs depending on the status of inputs  
89 arising from various meteorological forcings and geographical characteristics and the status  
90 of calibration, the hydrological evaluation method is useful for evaluation of its performance  
91 (Beven, 1993; Freer et al., 1996). Furthermore, the hydrological evaluation method serves as  
92 to provide guidance on the model's reliability to forecasters and operators who use the  
93 hydrologic model outputs for decision-making flood warnings and mitigation (Al-Sabhan et  
94 al., 2003).

95 For current hydrological evaluation, the graphical and statistical methods are  
96 commonly used (Green and Stephenson, 1986; Legates and McCabe, 1999; Coffey et al.,  
97 2004). The graphical method is used for a qualitative evaluation by comparing observations  
98 and simulated hydrographs, and the statistical method is used for a quantitative evaluation  
99 based on statistics for various error indices (ASCE, 1993). In general, the statistical method is  
100 based on an evaluation method that statistically divides the error index range and determines  
101 outputs in terms of various ratings (Santhi et al., 2001; Moriasi et al., 2007). Such an  
102 evaluation framework relatively straightforward process, and hence, its advantage is that it is  
103 readily applied. Nevertheless, its limitation is that it cannot present standardized ratings for  
104 various error indices. More importantly, the evaluation framework based on a single error  
105 index cannot reflect the complementary interaction between different error indices. It is also  
106 questionable how reasonably the error index range defined statistically represents the  
107 performance of a hydrologic model (Donigian et al., 1983; Ramanarayanan et al., 1997;  
108 Gupta et al., 1999; Singh et al., 2004).

109           Several requirements must be satisfied in developing a robust hydrological assessment  
110 tool. First, a statistical meaningful index, including error indices should be sought to ensure  
111 the objectivity of an evaluation framework. Second, a combination of complementary error  
112 indices, not a single error index, must be considered (Green and Stephenson, 1986; Coffey et  
113 al., 2004). Furthermore, the outputs of a hydrologic model suitable for the application should  
114 be used for evaluation. For example, a long-term complex hydrograph without separating  
115 single events should be avoided when evaluating a flood forecasting model as some period  
116 with no rain could play a role in generating noise that leads calculating inadequate error  
117 indices, for the purpose of hydrological assessment in flood forecasting (Ramirez, 2000). It is  
118 also important to consider the significance of the rising and recession limbs of a hydrograph  
119 as each limb represents a meaningful response of hydrological process. The rising limb is  
120 mainly formed by concentration of direct runoff which determines peak flow and time-to-  
121 peak. Since the recession limb is formed by all types of runoff, it is dominant over the rising  
122 limb in determining total runoff volume related to the water budget (Boyle et al., 2000).

123           Machine learning could be the alternative to overcome the shortcomings of a general  
124 evaluation method described above. Machine learning utilizes algorithms that detect patterns  
125 and relationships inherent to inputs and outputs, and is used across many areas with the  
126 development of various new algorithms and more powerful computers (Hong, 2008; Sahoo et  
127 al., 2017). Owing to an increase in the amount of data in hydrology, the use of machine  
128 learning is becoming increasingly important. More specifically, it is expected to serve as a  
129 supplementary solution in physics-based deterministic hydrology as many studies are being  
130 performed on physical factors such as surface runoff from rainfall, groundwater, and soil  
131 moisture (Coulibaly and Anctil, 1999; Tokar and Johnson, 1999; Shortridge et al., 2016).

132           Machine learning that can combine two or more methods for effective data analysis is  
133 referred to as Hybrid Machine Learning (HML). In general, the HML uses two machine

134 learning techniques suitable for most application and can complement the limitations of a  
135 single technique and deliver improved outcomes (Tsai and Chen, 2010). HML has been used  
136 widely in financial applications. Hsieh (2005) combined the K-means clustering technique  
137 and the neural network technique and developed a credit scoring model based on a hybrid  
138 mining approach. Huysmans et al. (2006) used a framework that combined an unsupervised  
139 self-organizing maps technique and supervised multi-layered perception technique to obtain a  
140 new credit scoring method. Tsai and Chen (2010) reviewed various combinations of  
141 clustering machine learning techniques and classification machine learning techniques, and  
142 demonstrated a high applicability of HML in developing credit rating systems. Tsai (2014)  
143 developed a novel hybrid financial distress model based on clustering and classification  
144 machine learning for supporting financial decisions. These studies that coupled clustering and  
145 classification machine learning techniques to establish a HML framework demonstrated  
146 better results than a single machine learning technique. The HML framework is considered an  
147 attractive approach for hydrological evaluation using various error indices. A HML  
148 framework could secure a stable performance assessment by employing a big data and has an  
149 advantage to determine a composite rating metric.

150         This study aims to develop a novel hydrological assessment tool (HAT) by adopting  
151 HML framework based on a combination of clustering and classification techniques and a  
152 composite of error indices. National Oceanic and Atmospheric Administration (NOAA)  
153 National Water Model (NWM) is used to develop the HAT since it has enough simulation  
154 data for over 5 years for training and testing the HAT. The NWM has been operated in real  
155 time since 2016 for the continental US (CONUS) (Han et al., 2019). The performance test is  
156 conducted on rising and recession limbs in a single hydrograph as well as the total  
157 hydrograph. To build, train, and validate the model, NWM simulated streamflow from  
158 October 2013 to February 2017 is applied at selected USGS streamflow sites across the San

159 Francisco Bay area. The performance of the HAT is then tested against the NWM simulated  
160 streamflow data.

161 The rest of this paper is organized as follows: Section 2 reviews the hydrological  
162 assessment framework in flood forecasting and introduces a HML framework and the HAT  
163 used in this study. Section 3 presents data descriptions for this study, the study area, and the  
164 HAT assessment results of simulated streamflow, which is estimated by the NWM from 2013  
165 to 2017. Section 4 compares the error-index-based results presented by previous studies for  
166 the performance test of a hydrologic model with the results of the new HAT and provides an  
167 overall discussion. Section 5 presents the conclusion of the study.

## 168 **2. Materials and Methods**

170

### 171 **2.1 Hydrological Assessment Framework in Flood Forecasting Aspect**

172

173 Various error indices are used for hydrological assessment. An error index is useful as  
174 it measures the simulated value against the reference value. Many cases where an error index  
175 was applied to hydrological assessment are noted in previous studies (Green and Stephenson,  
176 1986; Legates and McCabe, 1999; Moriasi et al., 2007; Yoo et al., 2016). Table 1 lists the  
177 error indices frequently used in hydrology.

178

|         |
|---------|
| Table 1 |
|---------|

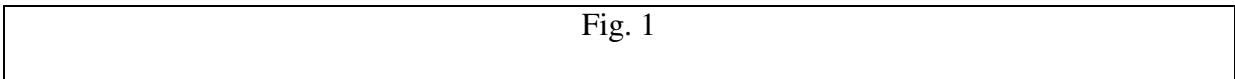
179

180 Error indices can be classified into two types based on their purpose. The first type of  
181 index is related to hydrograph characteristic values and includes errors of peak flow, peak  
182 time, and total runoff volume. Peak flow is calculated from complex interactions between  
183 precipitation, infiltration, and effective rainfall resultant at the watershed outlet or

184 measurement point. It is the maximum flow during the period in which direct runoff occurs  
185 intensively. Peak time refers to the time at which the peak flow occurs. As these error indices  
186 are determined by the rising limb of a hydrograph, they are very useful in assessing the  
187 performance for flood forecasting.

188         The second type of error index quantifies hydrograph characteristics. Most notably, it  
189 includes correlation coefficient (CC), Nash–Sutcliffe efficiency coefficient (NSE), bias and  
190 percent bias (PBIAS), and the RMSE-observations standard deviation ratio (RSR). These  
191 error indices have significance according to their development background. For instance, CC  
192 indicates a trend of simulated results against observations, whereas bias shows only average  
193 differences in ratio. As such, a single error index cannot fully represent the accuracy of a  
194 simulated hydrograph. Furthermore, even though various error indices are used together to  
195 assess a hydrograph, many individual analyses are required along with a wide range of data to  
196 reach a unified conclusion owing to the different features and scales of each indices. Fig. 1  
197 shows poor assessment results obtained from the use of a single error index.

198



199

200         Hydrological assessment should be based on an agile framework that can be applied  
201 in conditions appropriate for various purposes such as flood waves, low flows, and regulated  
202 flows in a river system. For the purpose of flood forecasting, an independent hydrograph is  
203 mainly assessed to test its performance in terms of surface runoff, which determines the peak  
204 value and flood risk level. Evaluation results may sharply diagnose the model performance  
205 and suggest a direction for calibration. Moreover, when a hydrological assessment is  
206 performed on a monthly or seasonal basis, it can assess the overall hydrological process but  
207 its results cannot represent the outperformance of a model in terms of flood forecasting. In



208 addition, as long duration simulated results contain multiple peak flows, repeated rising and  
209 recession limbs, and many low flows, they can become noise when estimating error indices.

210 An independent hydrograph can be separated into two limbs: rising and recession  
211 limbs. The rising limb is a part of a hydrograph ranging from the initial point of the direct  
212 runoff flow to the peak flow. Conceptually, the initial direct runoff flow starts when the  
213 precipitation rate exceeds initial losses in a watershed area. In terms of flood forecasting, the  
214 rising limb is very significant as it indicates a concentration time of discharge and as it  
215 provides the trend and magnitudes of the increasing flow and a peak flow. The recession limb  
216 is the part of a hydrograph ranging from the peak flow to the point where the decreasing flow  
217 is corresponds to the discharge immediately before the initial direct runoff. In terms of water  
218 management, the recession limb is very important as all hydrological runoff components  
219 (surface, subsurface, and groundwater) occur during this time. Finally, understandable  
220 terminology must be used to allow people across different disciplines to interpret assessment  
221 results.

222

## 223 **2.2 Hybrid Machine Learning Framework**

224

225 Machine learning uses the X dataset as an independent variable and the Y label as a  
226 dependent variable, and is divided into supervised learning (SL) and unsupervised learning  
227 (USL) based on whether it has the Y label (Bishop, 2006). Some of the most widely known  
228 SL approaches include the artificial neural network (McCulloch and Pitts, 1943), the random  
229 forest (Breiman, 2001). USL approaches include the self-organizing map (Kohonen, 1982)  
230 and K-means clustering (MacQueen, 1967). In the past, it was difficult to utilize machine  
231 learning owing to the limitations of computer technology; however, machine learning is  
232 garnering significant attention with the recent advances in high performance computing.

233 Many hydrological applications, which generate and handle large amounts of data and  
234 information, are also applying machine learning techniques (Shrestha and Solomatine, 2006;  
235 Demissie et al., 2009).

236

### 237 **2.2.1 Unsupervised Learning for Clustering**

238

239 USL is a type of machine learning that detects complex relationships between X  
240 datasets with no determined Y label. USL is mostly used for clustering, dimension reduction,  
241 and anomaly detection. Clustering is the most widely used technique in USL, and it aims to  
242 detect similarity between datasets and to cluster similar data points into one group. In  
243 addition, it can be used to identify similarity between data points in a cluster or differences  
244 with other objects in another cluster (Tsai and Chen, 2010). Some of the most widely known  
245 clustering techniques include K-means (MacQueen, 1967), DBSCAN (Ester et al., 1996), and  
246 hierarchical clustering (Johnson, 1967).

247

Fig. 2

248

249 K-means clustering, proposed by MacQueen (1967), is based on non-hierarchical  
250 clustering and is effective in detecting clusters from extensive large data sets (Hartigan and  
251 Wong, 1979; Everitt et al., 2001; Olden et al., 2012). Fig. 2 shows the conceptual diagram of  
252 a K-means clustering technique. K-means includes the number of clusters as a parameter, and  
253 uses it to begin clustering initial datasets. As many centroids as a set number of clusters are  
254 randomly chosen, and centroids are changed repeatedly until the sum of the distances  
255 between each centroid and data points reaches the minimum. Finally, a centroid that has the  
256 minimum sum of distances is detected to determine the set number of clusters. The

257 advantages of K-means are that its algorithms are simple and fast to calculate, it can obtain  
258 very reliable results, and it can be applied in various applications that involve a large amount  
259 of datasets.

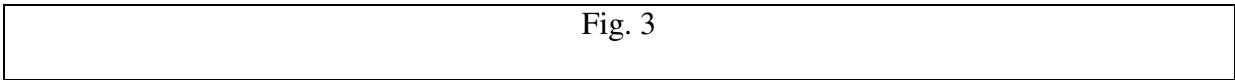
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### 261 **2.2.2 Supervised Learning for Classification**

262

263 SL is a type of machine learning that detects a pattern between the X dataset and the  
264 Y label and expresses the relationship in a function; it is used widely across disciplines that  
265 require data mining. SL can establish a model that estimates and predicts the Y label for a  
266 newly input X dataset by learning a training dataset consisting of an X dataset and Y label  
267 pair. SL is mainly used for regression and classification based on a causal relationship for  
268 datasets. The supervised classification technique is one of the most widely used techniques  
269 for statistics and engineering, and it classifies and predicts given X datasets into a suitable Y  
270 label. The dependent variable Y label serves as a category and is used for learning together  
271 with the independent variable X dataset. Classification techniques includes random forest  
272 (Breiman, 2001), support vector machine (Boser et al., 1992), and artificial neural networks  
273 (McCulloch and Pitts, 1943).

274



275

276 Among the classification techniques, the random forest is highly applicable to  
277 applications that require the informed decision making based on numerous data, a high speed  
278 processing, and high accuracy. This technique also has an advantage that is easy to link with  
279 the USL based clustering technique for HML establishment. The random forest, which was  
280 introduced by Breiman (2001), is a type of ensemble learning based on multiple decision

281 trees. The random forest applies randomness to not only training sets but also each decision  
282 tree's variable to reduce the high probability of overfit of the traditional decision tree method  
283 (Chagas et al., 2016). Fig. 3 illustrates the conceptual diagram of the random forest technique.  
284 First,  $n$  sub-training sets are randomly selected from a given total training set. Here, a sub-  
285 training set refers to a single decision tree. While the sub-training set processing is the same  
286 as that of traditional decision tree processing, available variables are applied considering  
287 randomness. The final outcome is chosen based on majority voting determined from  $n$   
288 decision trees (Ließ et al., 2012; Chagas et al., 2016). As such, the random forest combines  
289 prediction results from multiple trees and makes a decision by using a bootstrap of samples  
290 similar to the conventional bootstrap aggregating method (i.e. bagging) and can achieve both  
291 predictability and stability (Cutler et al., 2007; Wang et al., 2015). In the random forest, a  
292 weight of variables is determined through measuring of contribution of the variables to the  
293 prediction accuracy and the node impurity used in training process. The descriptions of the  
294 detailed method are well documented elsewhere (Louppe et al., 2013).

295

### 296 **2.2.3 Hybrid Machine Learning Framework**

297

298 HML refers to a combination of two or more machine learning techniques (Tsai and  
299 Chen, 2010). In general, such techniques include a combination of: 1) USL techniques, 2) SL  
300 and USL techniques, or 3) a combination of SL techniques. Different HML frameworks can  
301 be established depending on the combination sequence and type of applied techniques. For a  
302 combination of SL and USL techniques, the pattern and characteristics of an X dataset can be  
303 defined by USL as a Y label, and the HML framework that shares it with SL can be  
304 established.

305

Fig. 4

306

307 Fig. 4 shows the conceptual diagram of a HML framework that combines the USL  
308 based clustering technique and the SL based classification technique. First, clustering creates  
309 groups (i.e. clusters) and provides them as a Y label to classification. The HML framework  
310 generates the Y label required for training in the SL technique from unsupervised clustering,  
311 and the SL technique takes charge of modeling, which is difficult in the USL technique. By  
312 doing so, the limitations of the two techniques can be mutually complemented. The Y label  
313 provided from clustering is applied to classification learning along with the X dataset, and the  
314 applicability of the model is confirmed through a verification process. The established model  
315 estimates and predicts the Y label for a new X dataset.

316

### 317 **2.3 A Framework for Hydrological Assessment Tool**

318

319 This study adopts a HML technique as described in section 2.2.3, and established a  
320 HAT that can assess the accuracy of simulated streamflow. The HML framework is  
321 configured through a combination of K-means and random forest. One of the key points in  
322 the applied HML framework is that the X dataset, an input, is clustered into multiple groups,  
323 and the group is used as the Y label required for classification. Accordingly, the  
324 representation of the Y label for the clustered X dataset group should be apparent. In the  
325 HML framework, the SL plays a role in establishing a practical model that can estimate the Y  
326 label for a new X dataset.

327 The HAT can evaluate rising and recession limbs for an independent hydrograph as  
328 well as the total hydrograph. The evaluation results are determined by four ratings: Very  
329 Good (VG), Good (G), Satisfactory (S), and Unsatisfactory (US), which are determined by

330 the unsupervised clustering technique. The HAT can evaluate all streamflow hydrographs  
331 estimated or predicted using various methodologies such as deterministic and stochastic  
332 approaches. Since this HML framework has a relatively simple structure, it could be applied  
333 not only for hydrologic modeling but also more broadly for analysis of other geophysical  
334 quantities. Fig. 5 is a schematic diagram of the structure and flow of the HAT.

335

Fig. 5

336

337 The HAT consists of three modules. The first module is for pre-processing. This  
338 module aims to separate an independent hydrograph, identify rising and recession limbs, and  
339 calculate error indices for the independent hydrograph and two limbs. The separation process  
340 has four steps as follows:

341 (1) Smoothing the hydrograph to eliminate the noise due to small fluctuation (i.e.  
342 hydrological responses) in observed hydrograph. The smoothed hydrograph is used to  
343 determine the beginning and end points. At a smoothing, three points (t-1, t and t+1)  
344 arithmetic mean is used.

345 (2) Eliminating very low flows below threshold value. The threshold value is defined  
346 as mean observed runoff over entire period.

347 (3) The rate of runoff increment is used to identify the rising and recession limbs of a  
348 single hydrograph. The rate of increment at each time is defined as  $(\text{runoff}(t+1) - \text{runoff}(t))$   
349  $/ \text{runoff}(t)$ . Parts of rising and recession limbs are defined by setting the threshold of the  
350 increment rate for each drainage area (small:  $<163 \text{ km}^2$ , medium:  $<1,010 \text{ km}^2$ , large:  $> 1,010$   
351  $\text{km}^2$ ). The threshold is determined by sensitivity analysis. For rising limb, the threshold  
352 values are 0.50 for small area, 0.30 for medium area and 0.25 for large area. For recession  
353 limb, the threshold values are -0.50 for small area, -0.40 for medium area and -0.20 for large

354 area. The beginning point at which the rising limb begins, the end point at which the  
355 recession limb ends, and the peak point at which the largest runoff occurs in the hydrograph.  
356 In the case of Recession limb, the N-days method is used to determine the point of the end  
357 point. For complex hydrographs with two or more peak flows, the largest runoff value is  
358 defined as the peak point of the hydrograph, and the rising and recession limbs are defined  
359 according to the processes previously described.

360 In this study, five indices to evaluate the performance of the NWM hydrologic model  
361 are used. Within the error indices shown in Table 1, this study used three (CC, NSE, PF) of  
362 them and modified two (modified PBIAS and TP) of them, to build the clustering module.  
363 The combination of the five error indices demonstrated better performance in the clustering  
364 module than the other combinations. For example, using NSE and RSR together was not as  
365 good as using only NSE as statistical meanings of the two error indices are similar (see Table  
366 1). Each error index used in this study has a different role in determining clusters. PF and the  
367 modified TP were used as hydrograph characteristic values, and CC, NSE, and Mod-PBIAS,  
368 which quantified the characteristics of a hydrograph from various aspects, were applied as  
369 error indices. The CC shows the trend of a hydrograph and NSE shows the variance of  
370 simulated errors against observations. Mod-PBIAS refers to modified PBIAS and aims to  
371 consider errors in runoff volume. Mod-PBIAS considers the cancellation effect of the runoff  
372 volume error, which cannot be reflected by the existing PBIAS, and overcomes the  
373 limitations of the conventional method, which estimates errors only based on the observed  
374 runoff volume (Eq. (1)). Furthermore, the modified TP (hereinafter referred to as Mod-TP)  
375 was used instead of the existing TP so that the peak times that have different error directions  
376 but the same scale can be clustered in the same group (Eq. (2)). These estimated error indices  
377 are used as the X dataset in the clustering and classification modules.

378

379 
$$\text{Mod-PBIAS} = \text{ABS}(\sum(Q_{obs} - Q_{sim})) \div \sum(Q_{obs} + Q_{sim}) \times 100 (\%) \quad (1)$$

380

381 
$$\text{Mod-TP} = \text{ABS}(T_{obs} - T_{sim}) \quad (2)$$

382

383 The second is the clustering module. This module determines ratings, which indicate  
384 the performance level of a hydrologic model, based on the error indices described above and  
385 provides the Y label required for training and testing in the classification module. CC, NSE,  
386 and Mod-PBIAS are applied to rising and recession limbs, and the PF (%) and the Mod-TP  
387 (hr) are used in addition to these three indices in the total hydrograph.

388 In the clustering process, it is necessary to determine the appropriate k as k (i.e. the  
389 number of clusters) of K-means is an important parameter that affects the reliability of the  
390 clustering result. This study implements sensitivity analysis using k values (from 4 to 30) and  
391 compares the observed and simulated hydrographs to verify clustering results in the four  
392 ratings. The sensitivity analysis consists of two steps to determine an initial k and final k. To  
393 determine the initial k, statistics (e.g. mean and variance) of error indices are used to rank in  
394 order of superiority. In order to confirm the final k, R-square value between the simulated  
395 and observed hydrographs was used as another statistics. In this study, the initial k is  
396 determined to 20. When more than 20 of k is used, it was difficult to distinguish clustered  
397 groups due to similar statistics of the groups. Conversely, when smaller than 20 of k is used,  
398 mean value of error indices was not representative of each group as variance of error indices  
399 was too wide. Final k was determined to 4 of the clustered groups referring to VG, G, S, and  
400 US.

401 The third module is the classification. This module is responsible for modeling,  
402 training, and testing the HAT. The range of the five error indices of clusters from the  
403 clustering module has a limitation to represent the relationship between the clusters and the



404 ranges since it indicates only a degree of distance between a centroid of clusters and error  
405 indices. To overcome this limitation, this study employs the third module, the classification.  
406 The classification module aims to model the range of the error indices and to help  
407 understanding of the clusters from the clustering module. The classification module identifies  
408 the algorithm between the clusters and the range of error indices and builds up the knowledge  
409 for modeling the range through training. In addition, the classification module provides  
410 weights of the error indices so that it is able to analyze the contribution of the indices to  
411 clustering. The error indices are used as the X dataset and four ratings determined in the  
412 clustering module are used as the Y label. The HAT training is performed using a large  
413 amount of streamflow data, and the performance of the trained HAT can be verified from the  
414 X dataset and Y label for verification. The verified HAT can be implemented by using  
415 observed and simulated time series streamflow data, and the four ratings can be determined  
416 for the rising and recession limbs and a total.

417

## 418 **2.4 National Water Model**

419

420 The NWM is a fully distributed hydrologic model that aims to enhance flood  
421 forecasting capability of the NOAA hydrologic prediction system (Han et al., 2019). The  
422 NWM simulates the water cycle with mathematical representations of different physical  
423 processes and their interactions. This complex representation of physical processes such as  
424 rainfall rate and spatial distribution, snowmelt and infiltration and movement of water  
425 through the soil layers varies significantly with the change in terrain, soils, vegetation types,  
426 and various other variables (Cosgrove et al., 2018). The NWM is based on the community  
427 WRF-Hydro modeling system, which produces various hydrological analysis and prediction  
428 products, including gridded fields of surface runoff, soil moisture, snowpack, shallow

429 groundwater levels, inundated area depths, and evapotranspiration; as well as estimates of  
430 river flow and velocity for approximately 2.7 million river reaches defined by the seamless  
431 National Hydrography Dataset (NHD) Plus v2.0 hydrography dataset.

432 The NWM ingests atmospheric forcings (e.g. temperature, humidity and precipitation  
433 rate) into a Noah-MP Land Surface Model (LSM) to simulate land surface processes at a 1-  
434 km resolution; then once exfiltration from the soil column is calculated, a diffusive wave  
435 overland routing scheme moves water horizontally across the landscape at 250 meters.  
436 Catchment aggregation occurs and distributes the water into the channel network at the end of  
437 each modeling time step, and flow is routed according to a modified Muskingum-Cunge  
438 scheme along a modified version of the NHDPlus, where waterbodies (lakes and reservoirs)  
439 are encountered on the network and store/release water according to a level pool routing  
440 scheme (<https://water.noaa.gov/about/nwm>).

441

## 442 **2.5 Data**

443

444 This study is performed in the nine county regions surrounding the San Francisco (SF)  
445 Bay area, California. The SF is an area of diverse topography with regions near sea level  
446 juxtaposed with mountains rising in excess of 1,000m. The SF Bay area is a flood-prone  
447 region owing to orographic rainfall occurring in steep terrain (Cifelli et al., 2018). The  
448 orographic rainfall is often produced from moisture plumes over the Pacific Ocean known as  
449 atmospheric rivers (ARs, Ralph et al., 2012). As an example, an AR event starting on  
450 December 29, 2005 brought more than 20 inches of rain across the SF Bay region. Urban  
451 areas such as the city of San Francisco recorded 24-hour rainfall totals of 5 inches on  
452 December 31 alone. There was major flooding in the Napa and Russian River basins, with 10  
453 counties declaring federal disaster areas. Over 1,000 homes were flooded in Napa, costing

454 over \$300 million in damages. The geographic diversity and resulting flooding events in the  
455 SF Bay area provides a challenging testbed to evaluate the performance of the NWM.

456

Fig. 6

457

458 Fig. 6 shows the locations of the SF Bay area and stream gages that are currently  
459 operated by the USGS. A total of 91 USGS gages were identified across the nine counties in  
460 the SF Bay area. Upon review on the USGS's observed data, a subset of 57 USGS gages  
461 were selected in this study, excluding those that observed low-quality streamflow data  
462 associated with reservoir operations and diversions. The watershed for these 57 gages varies  
463 from 11.5 to 3,425.3 km<sup>2</sup>. This study used the NWM to conduct a retrospective streamflow  
464 simulation using NLDAS forcing data (Cosgrove et al., 2003) as inputs. The HAT is  
465 developed and tested using long time period data from October 2013 to February 2017. The  
466 performance of HAT and NWM for the SF Bay area is assessed against the USGS  
467 streamflow data.

468

### 469 **3. Results**

470

#### 471 **3.1 Clustering of Rating Labels**

472 The ratings of the four clustered groups were categorized into VG, G, S, and US. As a  
473 part of the statistical method, the characteristics of error indices for each rating were  
474 examined. Fig. 7 illustrates the probability distribution of error indices for each rating group  
475 and each error index. The results are for individual rising and recession limbs and total  
476 hydrographs. According overall results, the trend of the probability distribution depending on  
477 rating group was obvious that all of average error index from VG to US moves toward the  
478 direction of negative meaning (i.e. negative infinity for NSE), and variance increases

479 gradually. It was also found that the percentage of a higher rating level was higher as the  
480 fraction of each rating approached the ideal error index (i.e. 1.0 for CC and NSE), whereas  
481 the percentage of a lower rating level was higher as it was further away. These results were  
482 observed in all error indices and in rising and recession limbs and total hydrographs.

483

Fig. 7

484

485 In addition, table 2 lists statistics of error indices depending on the performance rating  
486 for the total hydrograph case. From the table, it confirms the range features of error indices  
487 by the clustered rating level. It is found that the ranges (minimum to maximum) of the error  
488 indices were overlapped since the rating groups have clustered with a composite of the error  
489 indices. For example, a range of CC in very good rating level is from 0.74 to 1.00 and in  
490 good rating level is from 0.44 to 0.98. This result suggests that the clustered rating levels are  
491 very reasonable as there is no absolute range for performance rating. However, a range from  
492 Q1 to Q3 of the error indices was barely overlapped in the ratings. The characteristics of  
493 mean and variance statistics in the table were very obvious by each rating level, and it  
494 supports the results in Fig. 7.

495

Table 2

496

Fig. 8

497

498 It was confirmed that error indices for each rating were reasonably clustered.  
499 Subsequently, an assessment of the quality of simulated hydrologic model results for each  
500 rating was conducted. Fig. 8 shows scatter density plots between USGS observations and

501 simulated NWM values for each rating. To remove the variability of different streamflow  
502 scales by various watershed areas and rainfall events, the observed and simulated streamflow  
503 were normalized by a peak flow so that it did not exceed 1.0. The results showed that the  
504 distribution trend of the scatter plot of each rating was distinct, and the observed trend was  
505 consistent each rating's meaning. According to the results for the total hydrograph, VG's  
506 coefficient of determination was 0.86 and was the highest, and the data points tended to  
507 cluster around the X=Y line. G showed a similar distribution trend to that of VG, but its  
508 density for the X=Y line was relatively lower and more scattered. G's coefficient of  
509 determination was 0.66. S showed a more scattered distribution trend than G, and its  
510 coefficient of determination was 0.49. For US, most of the data points were located around  
511 the X or Y axis, indicating simulated values were largely underestimated or overestimated  
512 compared with observed ones. As a result, US's coefficient of determination was 0.01, which  
513 was the lowest. The scatter plot trend for each rating was observed to be identical in the  
514 results of rising and recession limbs. In addition, Fig. 9 shows samples of the comparison  
515 results between the observed and simulated hydrographs in the four ratings (clustered groups).  
516 Runoff (Y-axis) and duration time (X-axis) are normalized using a maximum value. The  
517 results present a degree of quality of hydrograph in accordance with each rating.

518

Fig. 9

519

520 The clustering module determined the ratings that were reliable both statistically and  
521 graphically. The determined ratings were then used as the Y label in the classification module  
522 and served as a link between two machine learning techniques.

523

524 **3.2 Classification and Verification**

525

526           The classification module was built based on the supervised random forest technique,  
527 and aims to detect the hidden pattern between error indices (X dataset) and ratings (Y label).  
528 Since the random forest technique includes the SL process for modeling the evaluation tool,  
529 the classification module in which all processes were completed became the HAT that can  
530 perform a hydrological assessment on new X datasets.

531

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| Table 3 |
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532

533           The trained classification module evaluates the performance of the model through a  
534 verification process. Table 3 lists the verification results for the trained classification module.  
535 Here, 80% of the training data was used for training whereas 20% was used for verification.  
536 The verification was performed by comparing the ratings previously determined by the  
537 clustering module and the ratings determined through the HAT. According to the results, the  
538 concordance rates of the HAT ratings were 98% (Rising), 99% (Recession), and 97% (Total),  
539 which confirms that the HAT could perform an accurate hydrograph assessment. The  
540 concordance rate for each rating was also observed to be similar to the above.

541

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| Table 4 |
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542

543           Table 4 lists a weight of error indices determined in the classification module. In  
544 overall, Mod-PBIAS is the most important error index to assign the ratings, and CC and NSE  
545 are the next higher in order. In the case of total hydrograph, the weights of TP and PB are  
546 similar to NSE. It is speculated that the accuracy of baseflow played a role in determining the  
547 weight as the evaluation subject of the HAT is total runoff flow consisting of baseflow and

548 direct runoff flow, not only for direct runoff flow. That could describe the main reason of  
549 why Mod-PBIAS is considered as the most important weight.

550

### 551 **3.3 Test to Evaluate the NWM**

552

553 The HAT tested the performance of the NWM for the SF Bay area through adopting a  
554 concept of leave-one-out-cross (LOOC) validation method (Efron, 1983) which is widely  
555 used in Machine Learning technique. The LOOC validation method leaves one set of total  
556 available data sets as a test set, trains the HAT using the remaining data sets except the one  
557 set and tests the NWM performance using the one set, and repeat this process as many times  
558 as needed. In this study, the entire simulation period (October 2013-February 2017) is equally  
559 divided into 10 sub-periods as the data sets by sequence of date, and the LOOC validation  
560 method is applied to each sub-period. The entire simulated results by the LOOC validation  
561 method are analyzed at various points of view. Table 5 shows the validation result of the  
562 LOOC validation method using a fraction of incorrect ratings. A range of the fractions is  
563 from 1.9 to 4.4 % on average, which confirms that the HAT is properly built and performs an  
564 accurate hydrograph assessment. However, ‘Overrated’ and ‘Underrated’ results did not show  
565 significant proportional differences.

566

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| Table 5 |
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567

568 First, the results by drainage size are presented in Fig. 10. Overall, the performance of  
569 the NWM for the SF Bay area was rated VG or G by the HAT for at least 46% of the  
570 simulated hydrographs regardless the limbs and total hydrograph. The occurrence of VG and  
571 G increased with drainage area. For the total hydrograph results, the ratings of small areas

572 VG and G accounted for 42% or more, medium areas 50% or more, and large areas 58% or  
573 more. Similar trends were identical across the limbs of the hydrograph.

574 In this study, training of the HAT was implemented for each hydrograph limb. Thus,  
575 the distribution of the four labels could be different depending on the hydrograph limbs (i.e.  
576 rising and recession). For example, a fraction of US in the rising limb is 5% on average while  
577 a fraction of US in the recession limb is 28% which is 5 times higher.

578

Fig. 10

579

580 Fig. 11 shows a map representing the average ratings of total hydrograph at USGS  
581 gages and the fraction of ratings for each county. From US to VG, the model performance  
582 score ranges from 0.0 to 3.0, and the arithmetically averaged score is indicated on the map.  
583 According to the results by county, Marin County scored 0.62 points on average and showed  
584 the lowest NWM performance among six other counties except three counties whose the  
585 observed data properly usable is not found. VG and G accounted for less than 18.5%.  
586 Following Marin County, Napa County showed the second lowest performance at 1.11 points.  
587 The best performance was shown in Santa Clara County, which scored 1.79 points on average.  
588 These VG and G ratings of the county accounted for 66.7% or more. In addition, the overall  
589 results demonstrated that the NWM performance for the Southern SF Bay area (San Mateo,  
590 Santa Clara, and Alameda) was better than that for the Northern SF Bay area (Marin, Sonoma,  
591 and Napa).

592

Fig. 11

593



594            Since the accuracy of simulated streamflows varies with various characteristics of  
595 rainfall and watershed, it is necessary to examine how the decision of performance ratings is  
596 affected by them. Fig. 12 shows the contribution of four impact factors, complexity of  
597 hydrograph with the numbers of peak, runoff duration, drainage size and whether regulated or  
598 not, to performance ratings. In the case of complexity of hydrograph, the ratings were  
599 assigned equally regardless of the numbers of peak. Multiple peaks case has a large fraction  
600 of VG, and it confirms that the performance of the NWM for complex storm events is reliable  
601 and comparable to simulation performance for single storm events. In the case of runoff  
602 duration, G, S, and US did not show significant proportional differences by a duration length.  
603 For VG, the long duration has the largest fraction.

604            In the case of drainage size, the higher ratings were assigned to a large drainage area.  
605 A fraction of a large drainage area was higher at the three ratings except the US, and the  
606 small area tended to be the opposite trend of the large drainage area. There are several  
607 reasons for that. The HAT assigns the performance ratings for total runoff flows consisting of  
608 baseflows and direct flows, and a large drainage area is affected by the accuracy of baseflow,  
609 different from small drainage areas commonly located in the upper river basin. Also, Mod-  
610 PBIAS among the error indices is highly influenced to determine the performance rating. In  
611 the case of whether regulated or not, G, S and US did not show significant proportional  
612 differences, and a fraction of unregulated was higher at VG.

613

Fig. 12

614

615

616 **4. Discussion**

617

618 One of the most notable hydrological evaluation framework studies was conducted by  
619 Moriasi et al. (2007) who suggested general hydrological assessment guidelines. Their study  
620 determined classification criteria for an error index through the basic framework of decision  
621 trees, and tested the performance of a hydrologic model based on the determined  
622 classification criteria. However, their evaluation method can only be used for single indices,  
623 and it is difficult to draw a comprehensive conclusion from various indices. Fig. 13 compares  
624 the results of the HAT and Moriasi et al. (2007). NSE, PBIAS, and RSR error indices were  
625 used for the results of Moriasi et al. (2007).

626

Fig. 13

627

628 The results using the Moriasi et al. (2007) methodology are difficult to interpret in  
629 terms of an overall performance rating result. Graphically, the scatter plot distributions of the  
630 top three ratings (VG, G, and S) are so similar that it was difficult to distinguish them. The  
631 US rating showed no trend in the scatter plot distribution. These results could be reaffirmed  
632 by the coefficient of determination. In particular, there were few differences in the coefficient  
633 of determination between VG, G, and S, and hence, it was difficult to determine which rating  
634 shows high accuracy. When PBIAS was applied, the coefficient of determination of the three  
635 ratings ranged from 0.75 to 0.77, and the coefficient of determination for the G rating was  
636 estimated to be higher than that of the VG rating. In NSE and RSR, the coefficient of  
637 determination for the three ratings ranged from 0.85 to 0.92 and from 0.84 to 0.92,  
638 respectively, which was similar to that in PBIAS. While the coefficient of determination of  
639 the US rating was estimated to be much lower than those of the top three ratings, it was  
640 difficult to conclude that US was assessed well, given that there was no trend in the scatter  
641 plot distribution. The advantage of the HAT is, that by objectively combining the indices into

642 an objective algorithm, an overall assessment of the model performance is easier to obtain. In  
643 addition, table 6 shows the comparison results of ranges of error indices derived from the  
644 HAT and Moriasi et al. (2007). It confirms that the absolute ranges of error indices used in  
645 the general evaluation may not reasonable to evaluate simulation results.

646

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| Table 6 |
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647

648 The HAT showed a high accuracy of over 98% in the verification results. To further  
649 improve the performance of the HAT, we believe that a model that uses more training data  
650 than those used in this study should be established. For 2%, the ratings were underestimated  
651 compared with the actual ratings in all cases. These results may be obtained owing to the use  
652 of the random forest, apart from whether the amount of data is simply large or small. The  
653 random forest is a machine learning technique that supplements flexibility, which decision  
654 trees do not have, and determines classification criteria between the given X dataset and Y  
655 label from various decision trees. This technique, however, cannot implement perfect  
656 classification criteria without infinite training data owing to the fundamental problem of  
657 decision trees-discontinuous classification criteria-even if the optimized classification criteria  
658 are determined based on multiple decision trees. Nevertheless, 98% accuracy achieved by the  
659 HAT can be considered acceptable, and we believe that the ratings for the hydrologic model  
660 determined via the HAT established based on such a performance are reliable.

661 Understanding uncertainties in the procedures needs for meaningful quantification of  
662 the results. In case of this study, uncertainties may arise from two parts: the hydrograph  
663 separation and the four ratings assignment. The hydrograph separation is the important  
664 process as it determines an independent hydrograph as well as two limbs (i.e. rising and  
665 recession) which is the source for evaluation criteria of the hydrologic model performance.

666 Thus, the results could be slightly varied with the separation methods, especially in  
667 determining the end point of a hydrograph. However, it is speculated that the uncertainties  
668 from the hydrograph separation are not big enough to change the results as the error indices  
669 were barely changed depending on the lengths of a hydrograph. On the other hands, since the  
670 rating assignment is a key to evaluate a hydrograph whether it is good or not, the parameter  $k$   
671 in the cluster module is very important. In this study,  $k$  is determined by the sensitivity  
672 analysis method so that the result may include a subjective point of view.

673

## 674 **5. Summary and Conclusions**

675

676 This study describes the HAT based on the HML technique. The HML technique was  
677 established by a combination of clustering and classification techniques, and ratings were  
678 reasonably determined from a composite of various error indices. The HAT was applied to  
679 retrospective simulations of the NWM in the SF Bay area. Conclusions from this study  
680 include:

- 681 1) A novel assessment tool, HAT, has been developed. Four ratings determined by  
682 the HAT accompanied apparent statistical and graphical characteristics and could  
683 accurately diagnose outputs for each rating. Accordingly, it could define the status  
684 of the model for each rating objectively, and the HAT is expected to be applied to  
685 determine the necessity, strategy, and extent of calibration.
- 686 2) Through the training and verification processes, we confirmed the reliability of the  
687 HAT, and showed that HAT could assess a single hydrograph from three aspects,  
688 the rising and recession limbs and total hydrograph. Moreover, easy-to-understand  
689 terms were used to define ratings and help understand the assessment results.

690 3) The HAT assessed the performance of the NWM for the SF Bay area using a  
691 limited training and verification data set. The NWM was shown to perform G-VG  
692 for at least 46% of the hydrographs examined during from October 2013 to  
693 February 2017, regardless of the watershed size.

694 The new evaluation framework is extensively applicable. The HAT is able to rate for  
695 additional performance levels (e.g. super-very-good and super-unsatisfactory) by adding new  
696 groups, as it is very flexible. If sub-hourly evaluation is needed like a flash flood, the HAT  
697 could implement that through training the HAT based on sub-hourly time step data. Also, the  
698 HAT can be applied to not only a flood forecasting model but also any geophysical data that  
699 are driven by physically pulsed phenomena. For instance, it can be applied to the indices that  
700 represent precipitation, soil moisture content, underground water, pollution load, and natural  
701 disasters.

702

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704

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708

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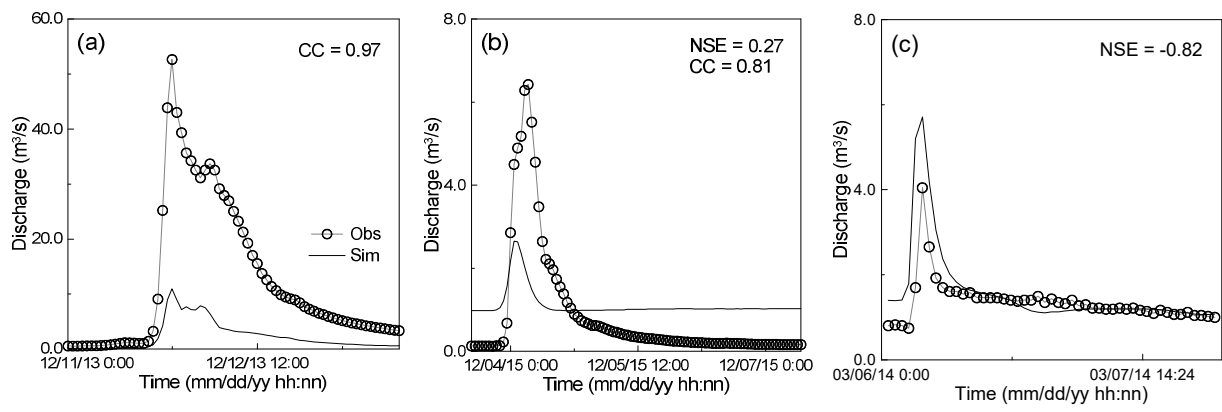


Figure 1

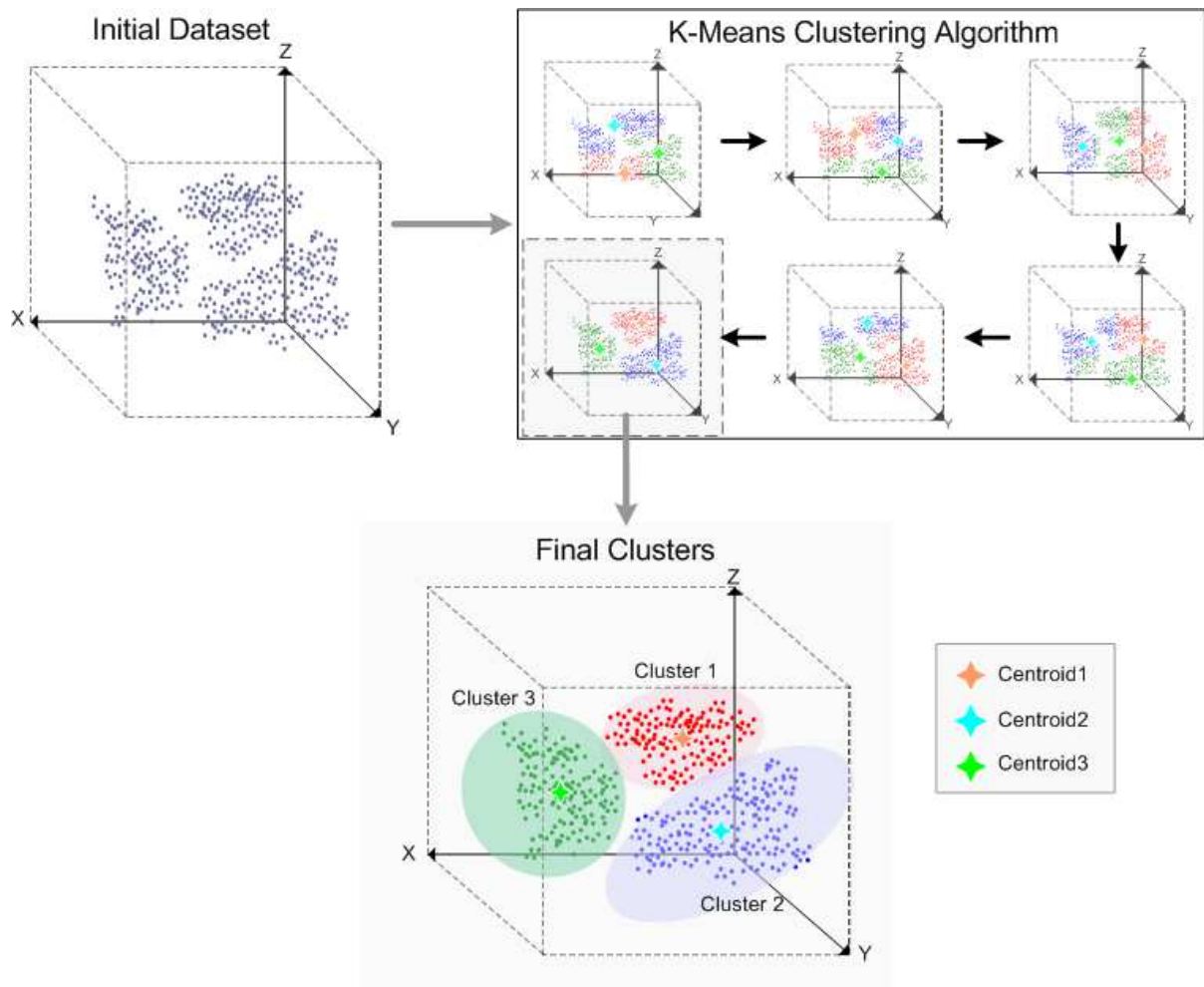


Figure 2

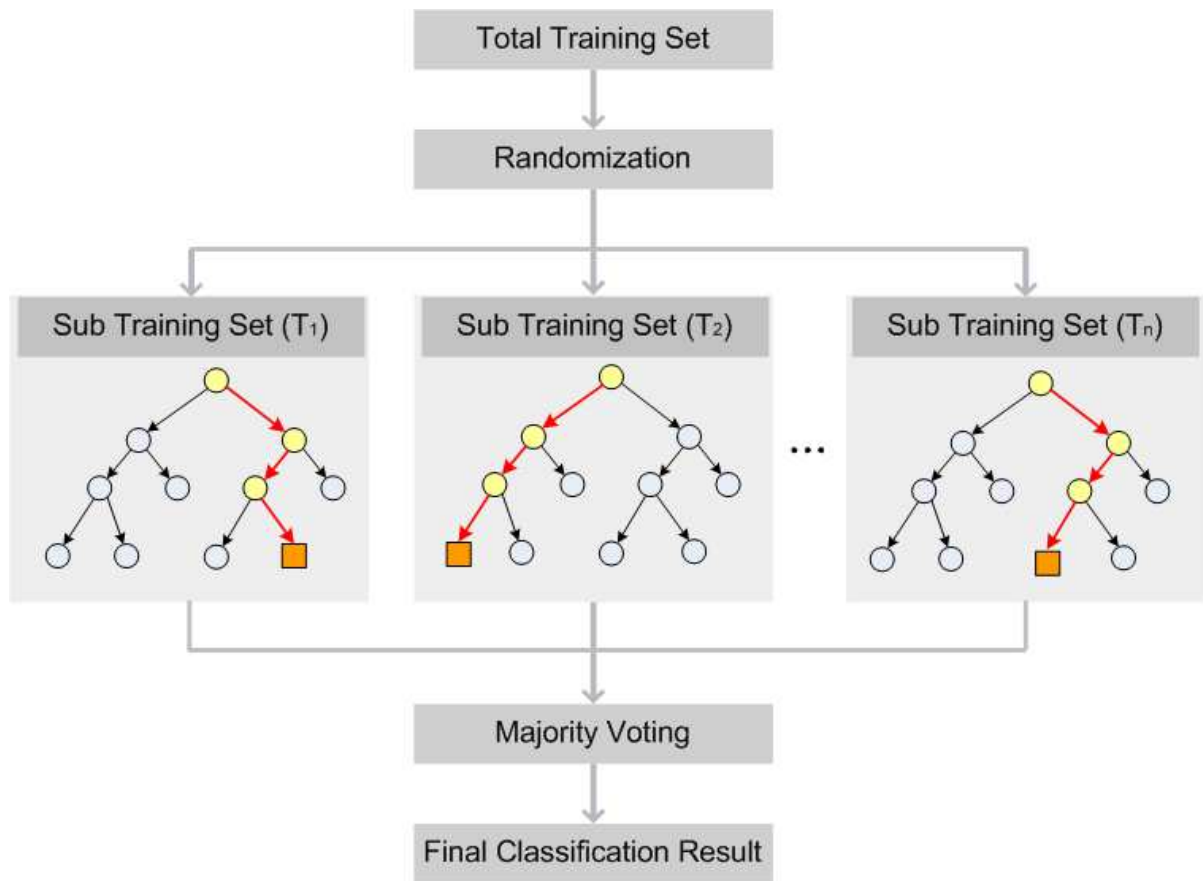


Figure 3

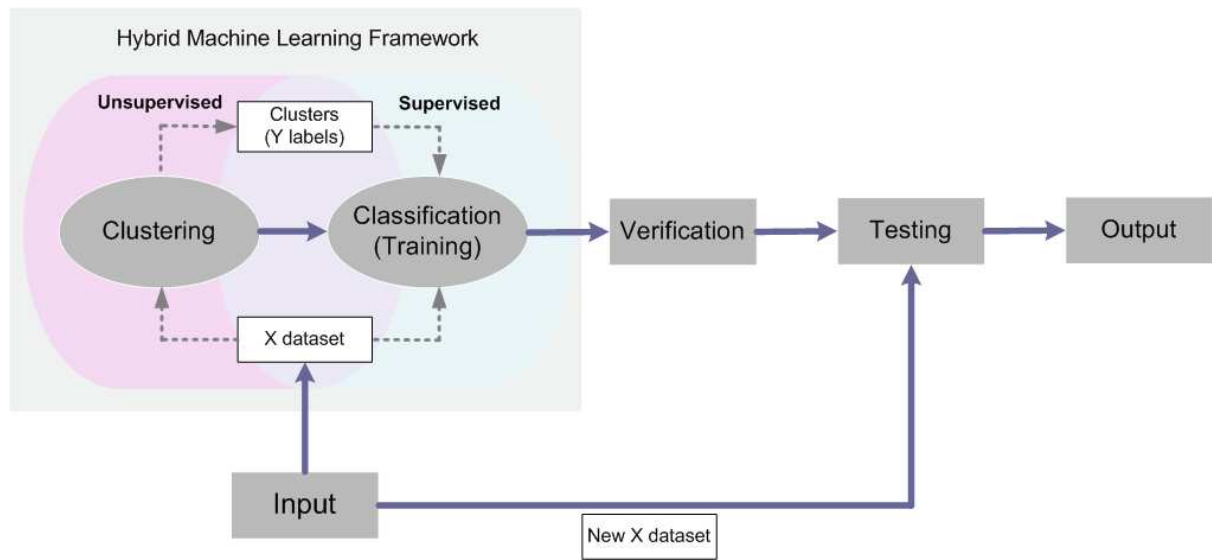


Figure 4

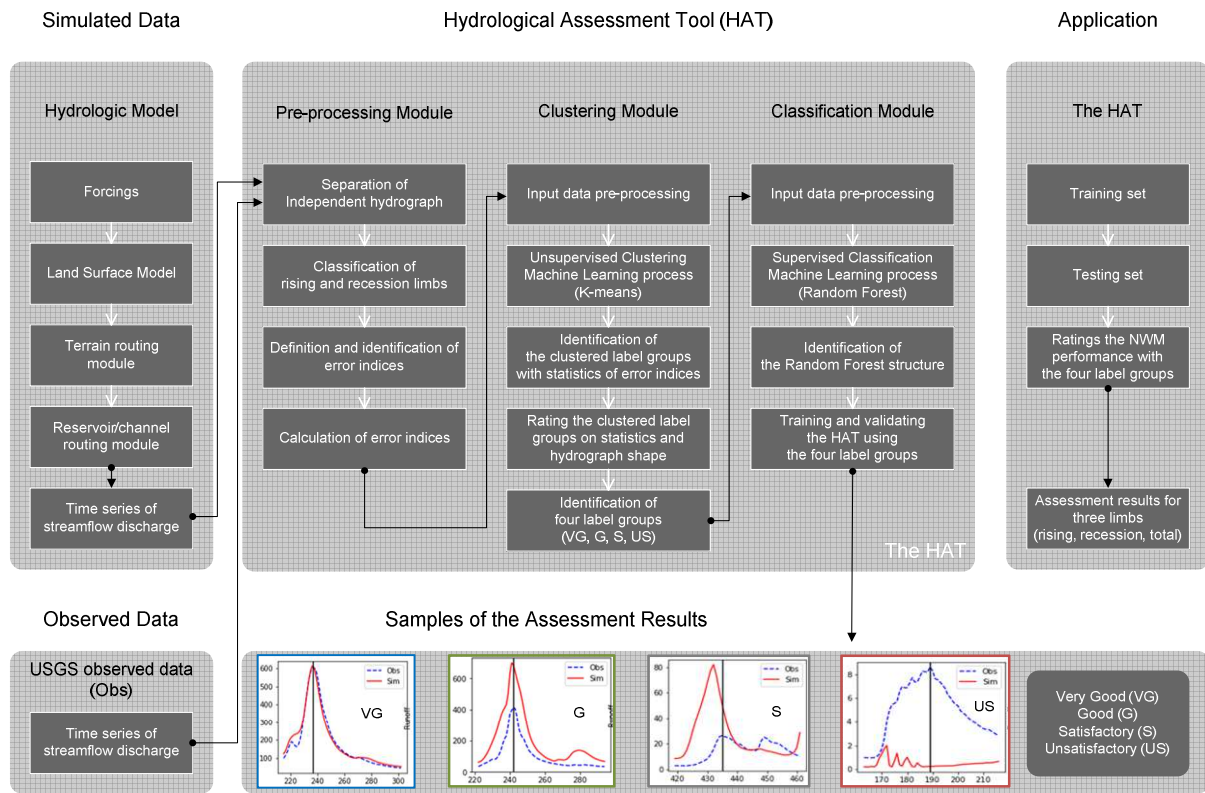


Figure 5

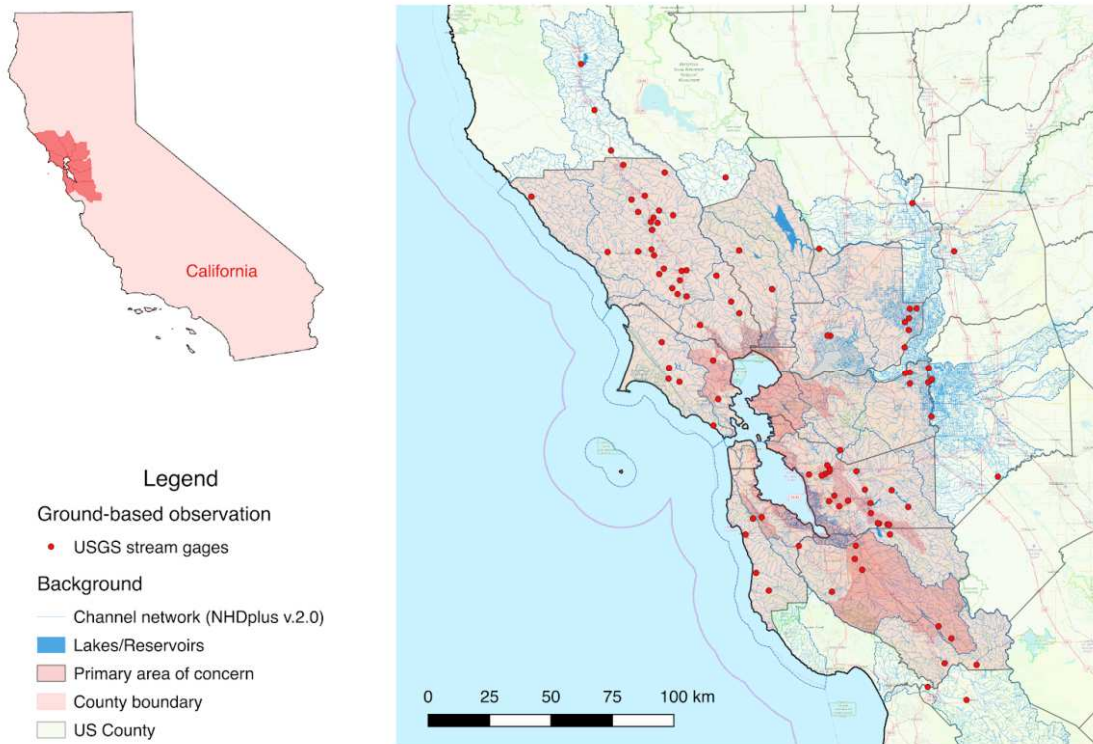


Figure 6

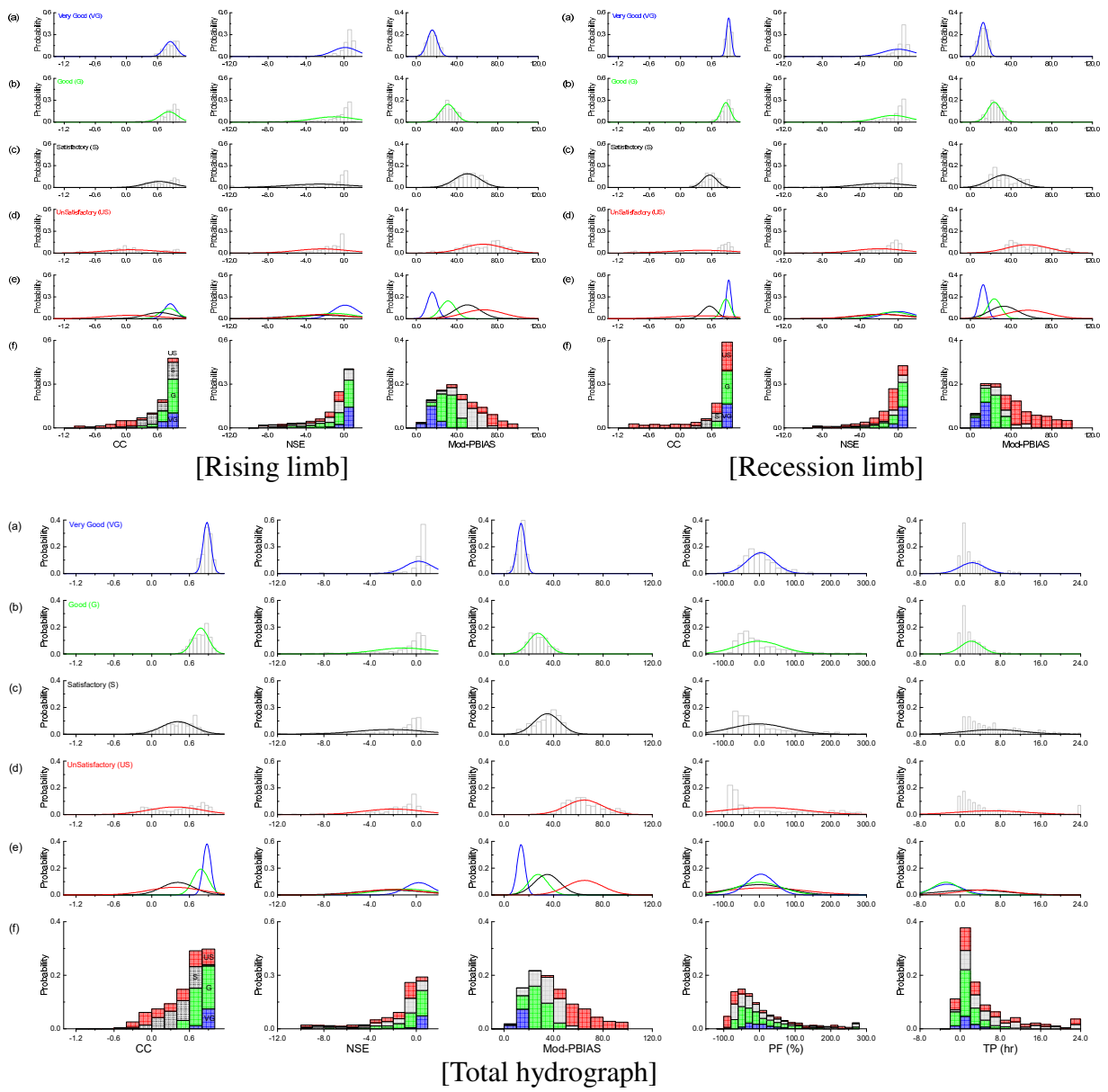


Figure 7



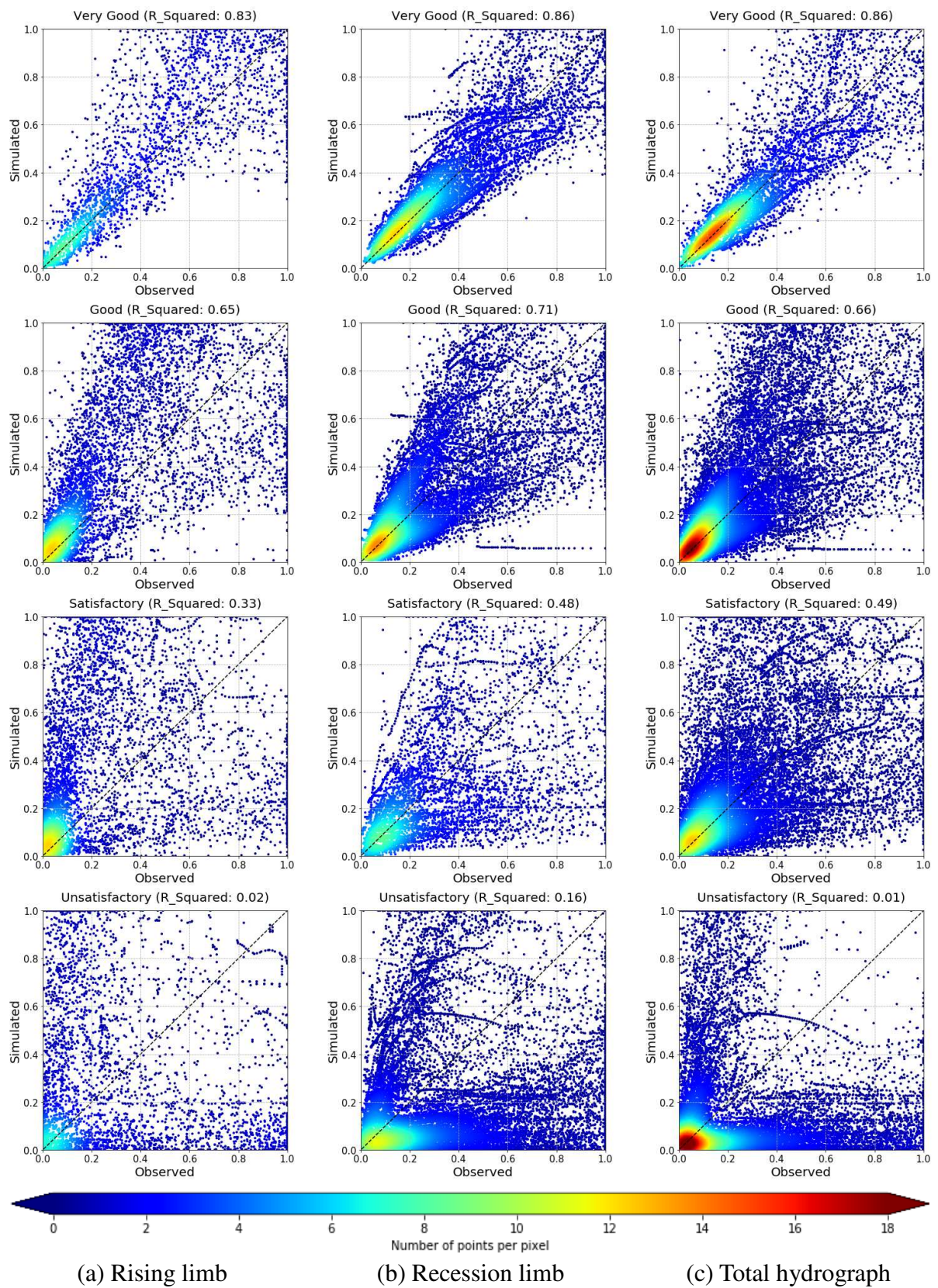
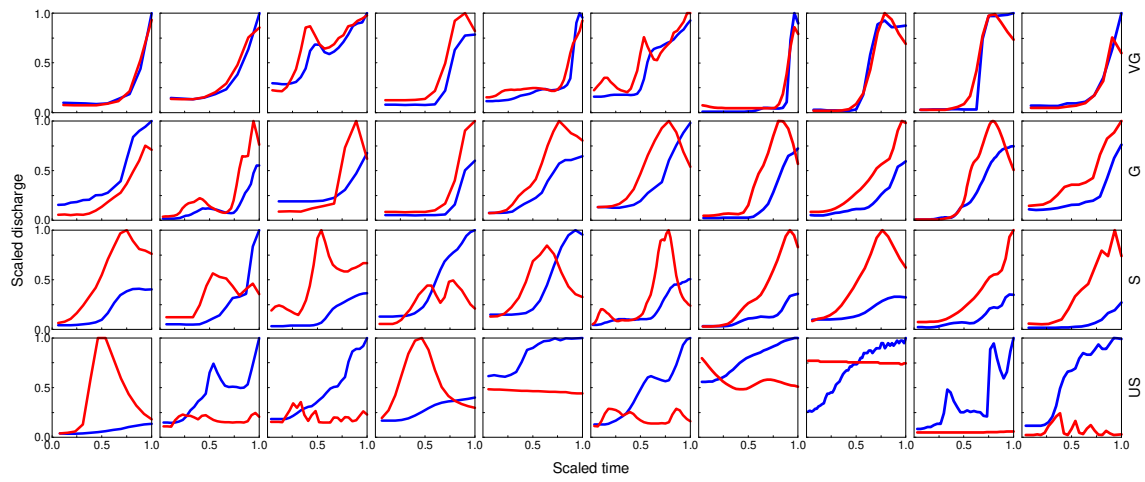
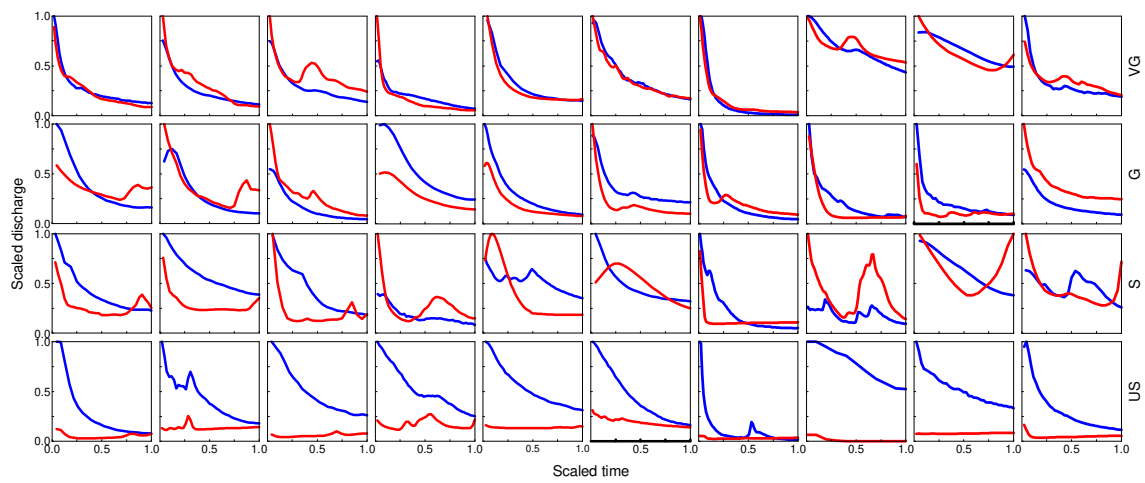


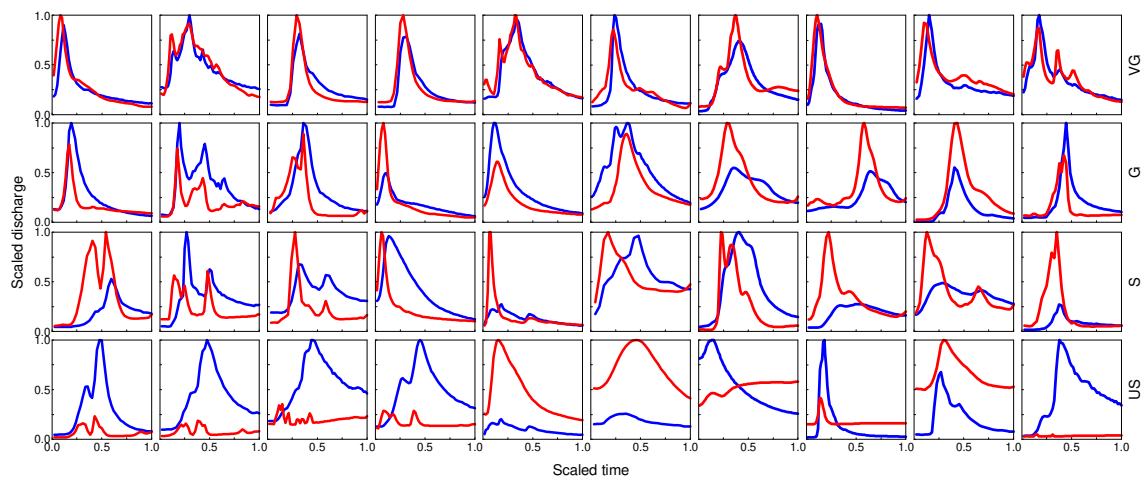
Figure 8



(a) Rising limb



(b) Recession limb



(c) Total hydrograph

Figure 9

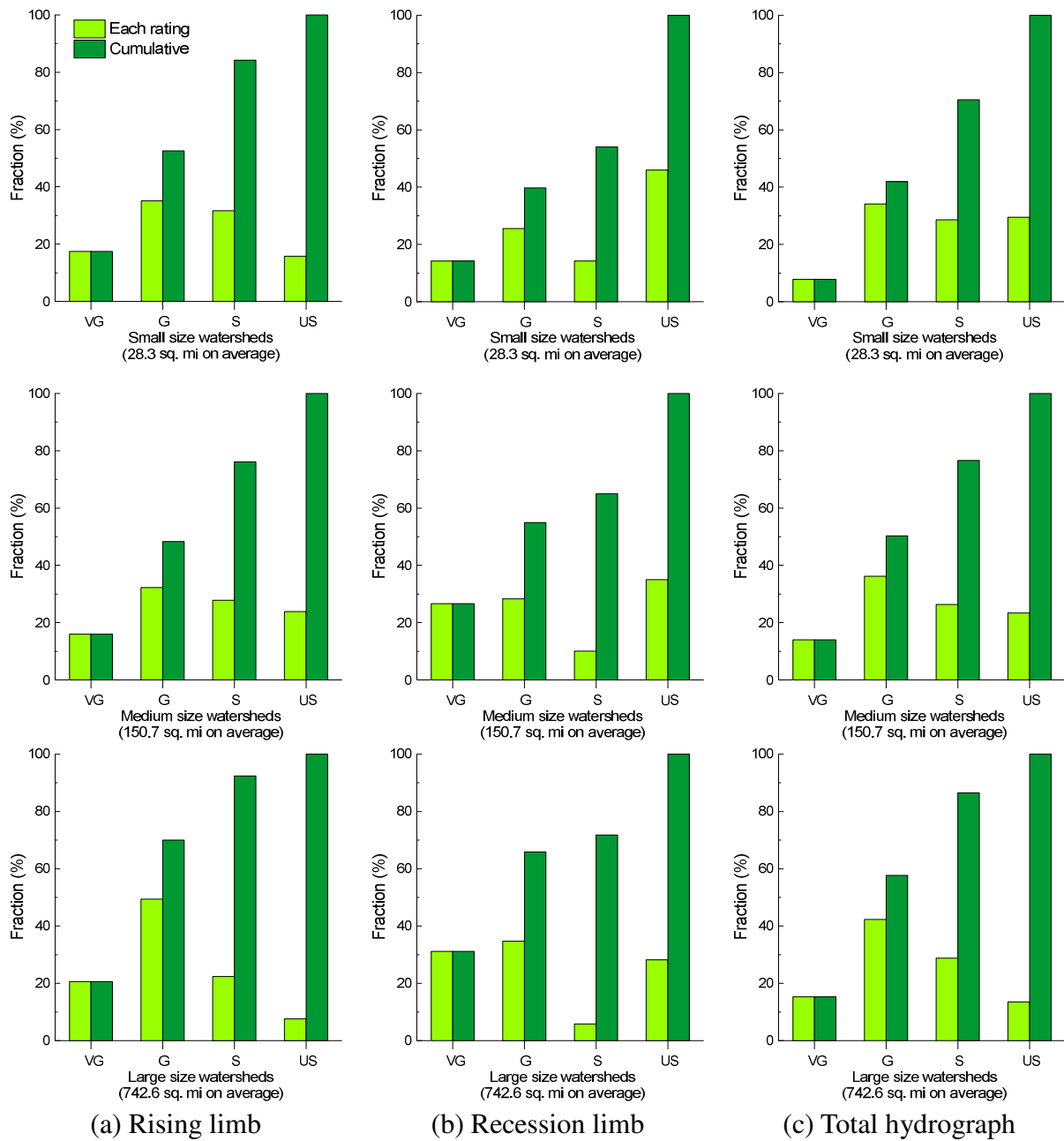


Figure 10

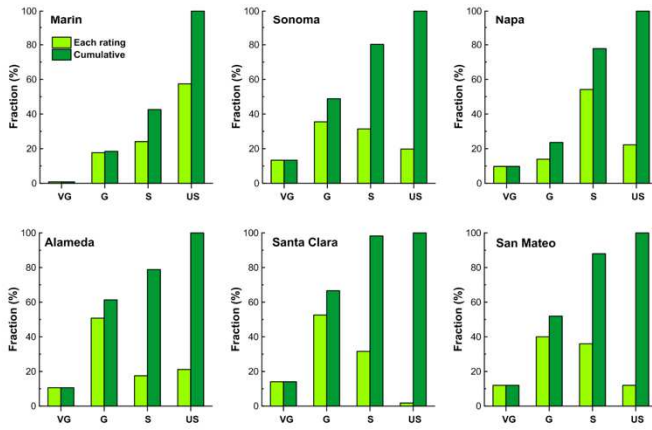
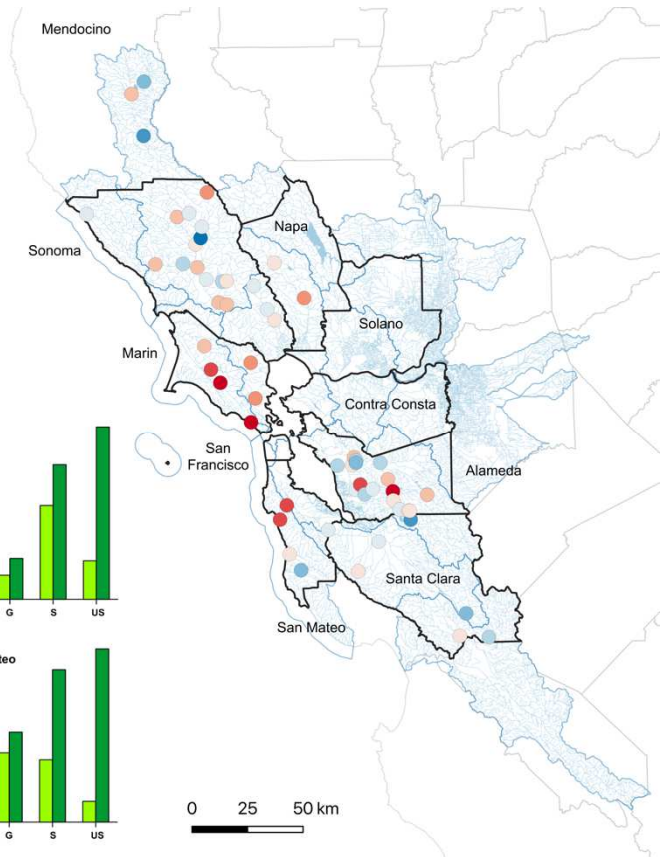


Figure 11

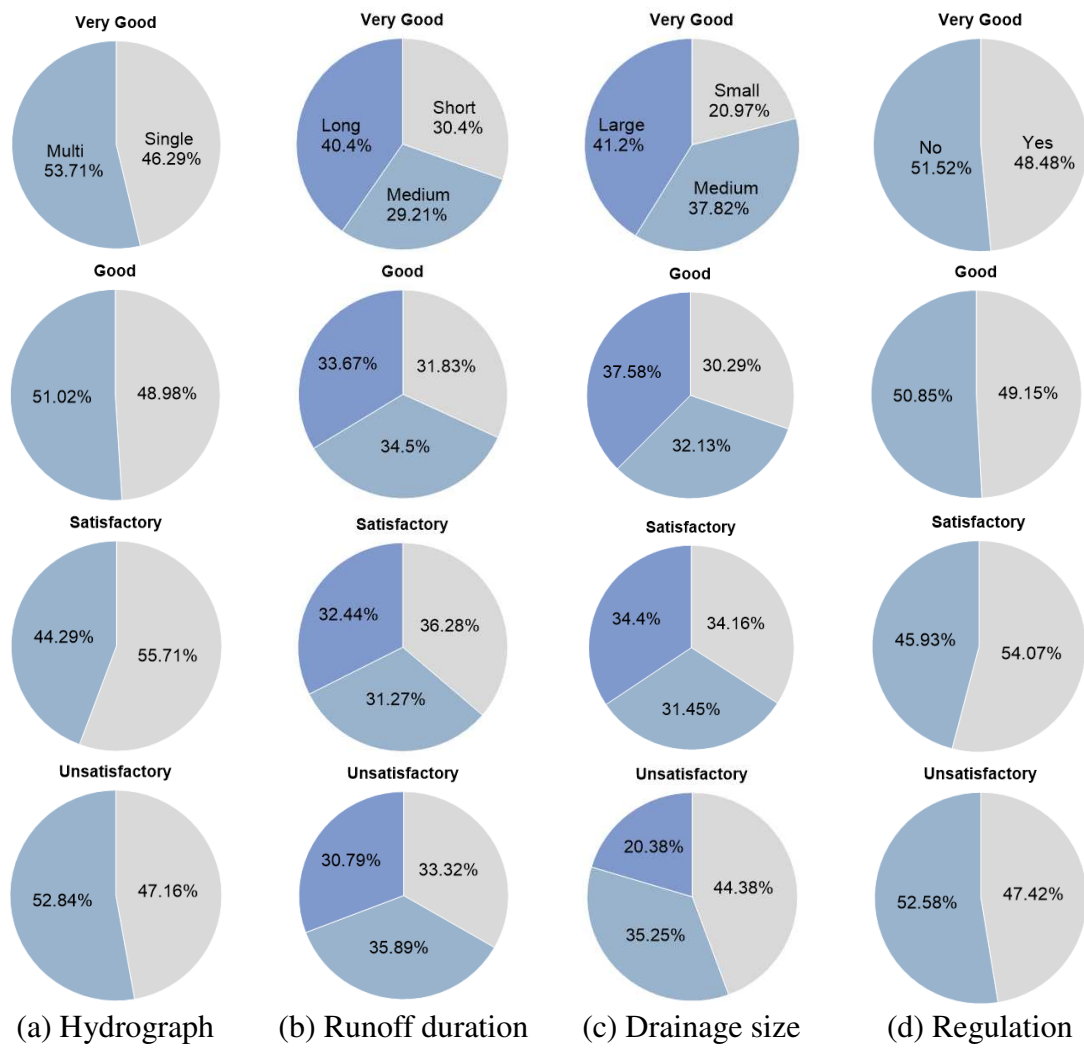


Figure 12

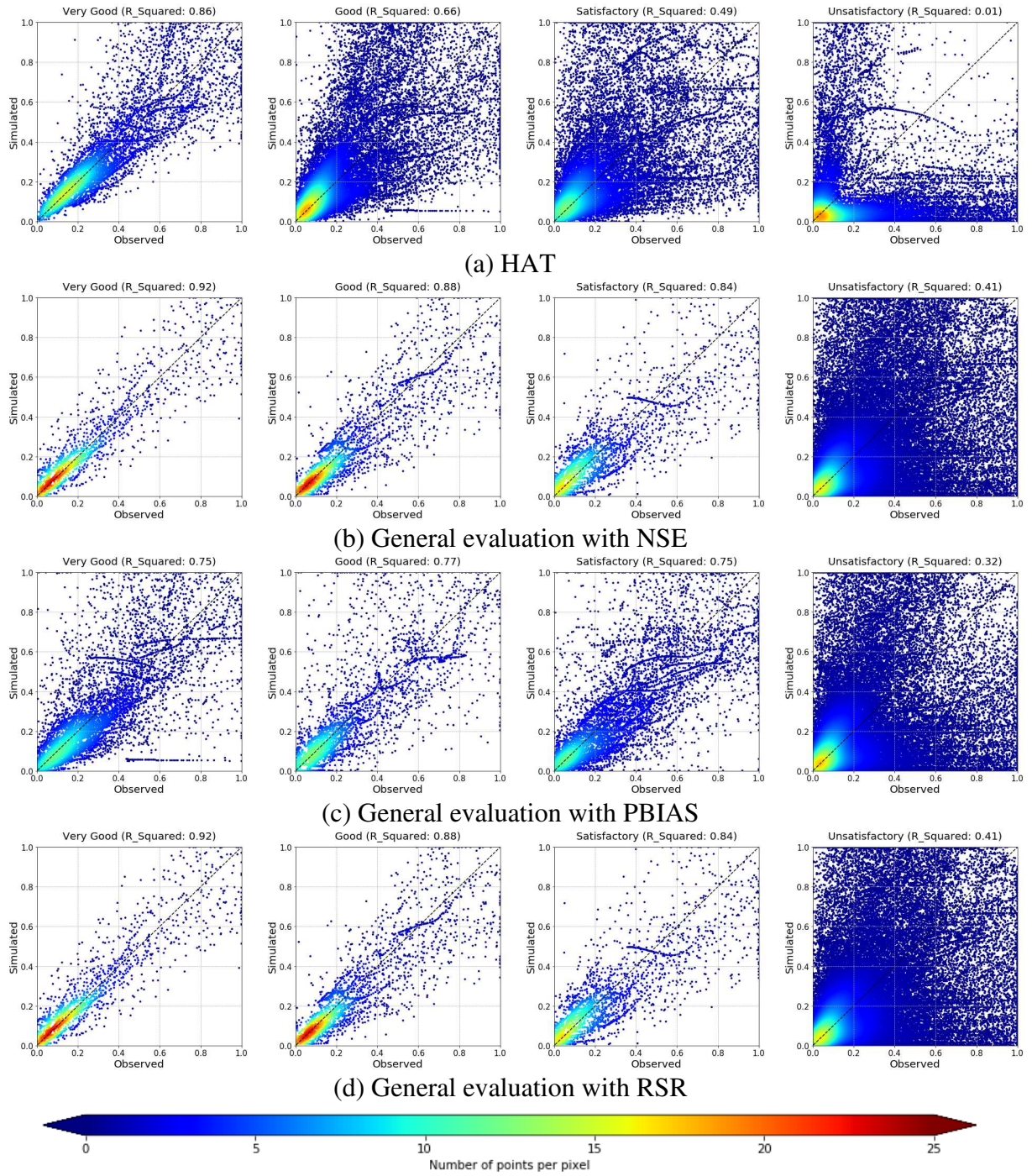


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Table 6 Comparison of statistics of error indices (RSR, NSE, and PBIAS) determined by the HAT and the general evaluation approach.

Table 1

| Error Indices                              | Acronym<br>(Range)   | Equation   |
|--|----------------------|--|
| Correlation coefficient                    | CC<br>[-1, 1]        | $\frac{\sum(Q_{sim} - \overline{Q_{sim}})(Q_{obs} - \overline{Q_{obs}})}{\sqrt{\sum(Q_{sim} - \overline{Q_{sim}})^2} \sqrt{\sum(Q_{obs} - \overline{Q_{obs}})^2}}$ |
| Nash-Sutcliffe efficiency                  | NSE<br>(-inf, 1]     | $1 - \frac{\sum(Q_{sim} - Q_{obs})^2}{\sum(Q_{obs} - \overline{Q_{obs}})^2}$   |
| Percent bias                               | PBIAS<br>(-inf, inf) | $\left( \sum(Q_{obs} - Q_{sim}) \right) \div \sum Q_{obs} \times 100 (\%)$   |
| RMSE-observations standard deviation ratio | RSR<br>[0, inf)      | $\frac{\sqrt{\sum(Q_{obs} - Q_{sim})^2}}{\sqrt{\sum(Q_{obs} - \overline{Q_{obs}})^2}}$   |
| Time to peak error                         | TP<br>(-inf, inf)    | $T_{obs} - T_{sim}$  |
| Peak flow error                            | PF<br>(-inf, inf)    | $(\text{Max}(Q_{obs}) - \text{Max}(Q_{sim})) \div \text{Max}(Q_{obs}) \times 100 (\%)$   |



Table 2

| Rating         | Statistic                            | Error index   |                   |                       |
|----------------|--------------------------------------|---------------|-------------------|-----------------------|
|                |                                      | CC            | NSE               | Mod PBIAS<br>(MPBIAS) |
| Very good      | min <sub>≤</sub> , ≤max              | 0.74≤CC≤1.00  | -8.16≤NSE≤1.00    | 0.00≤MPBIAS≤18.50     |
|                | Q1 <sup>a</sup> ≤ , ≤Q3 <sup>a</sup> | 0.84≤CC≤0.92  | 0.25≤NSE≤0.72     | 11.31≤MPBIAS≤15.74    |
|                | mean (variance)                      | 0.88 (0.004)  | 0.22 (1.342)      | 13.63 (10.148)        |
| Good           | min <sub>≤</sub> , ≤max              | 0.44≤CC≤0.98  | -54.34≤NSE≤0.87   | 5.64≤MPBIAS≤45.44     |
|                | Q1 <sup>a</sup> ≤ , ≤Q3 <sup>a</sup> | 0.68≤CC≤0.88  | -1.79≤NSE≤0.34    | 21.81≤MPBIAS≤32.89    |
|                | mean (variance)                      | 0.78 (0.015)  | -2.23 (33.984)    | 27.36 (60.616)        |
| Satisfactory   | min <sub>≤</sub> , ≤max              | -0.41≤CC≤0.89 | -165.40≤NSE≤0.72  | 8.63≤MPBIAS≤55.72     |
|                | Q1 <sup>a</sup> ≤ , ≤Q3 <sup>a</sup> | 0.24≤CC≤0.65  | -5.62≤NSE≤-0.13   | 27.69≤MPBIAS≤42.26    |
|                | mean (variance)                      | 0.41 (0.065)  | -5.13 (161.571)   | 34.78 (108.115)       |
| Unsatisfactory | min <sub>≤</sub> , ≤max              | -0.92≤CC≤0.98 | -534.44≤NSE≤0.60  | 25.36≤MPBIAS≤99.38    |
|                | Q1 <sup>a</sup> ≤ , ≤Q3 <sup>a</sup> | 0.01≤CC≤0.76  | -13.22≤NSE≤-0.44  | 53.92≤MPBIAS≤74.89    |
|                | mean (variance)                      | 0.37 (0.176)  | -21.74 (3713.448) | 64.89 (214.739)       |

<sup>a</sup> Q1 and Q3 indicate the lower (25%) and upper (75%) quartiles.

Table 3

| Ratings | Hydrograph              |           |                            |           |                        |           | (d) Entire <sup>a</sup> |           |
|---------|-------------------------|-----------|----------------------------|-----------|------------------------|-----------|-------------------------|-----------|
|         | (a) Rising <sup>a</sup> |           | (b) Recession <sup>a</sup> |           | (c) Total <sup>a</sup> |           | Correct                 | Incorrect |
|         | Correct                 | Incorrect | Correct                    | Incorrect | Correct                | Incorrect |                         |           |
| VG      | 96.8                    | 3.2       | 100.0                      | 0.0       | 100.0                  | 0.0       | 98.8                    | 1.2       |
| G       | 97.7                    | 2.3       | 96.7                       | 3.3       | 96.8                   | 3.2       | 97.1                    | 2.9       |
| S       | 98.4                    | 1.6       | 100.0                      | 0.0       | 92.8                   | 7.2       | 96.1                    | 3.9       |
| US      | 97.8                    | 2.2       | 100.0                      | 0.0       | 100.0                  | 0.0       | 99.6                    | 0.4       |
| Mean    | 97.7                    | 2.3       | 99.2                       | 0.8       | 97.4                   | 2.6       | 97.9                    | 2.1       |

<sup>a</sup> (a)-(c) represent each limb and total hydrograph results, and (d) indicates correct and incorrect percentages for entire results regardless limbs.

Table 4

| Error Index | Hydrograph |               |           |
|-------------|------------|---------------|-----------|
|             | (a) Rising | (b) Recession | (c) Total |
| Mod PBIAS   | 0.55       | 0.56          | 0.52      |
| CC          | 0.30       | 0.29          | 0.26      |
| NSE         | 0.15       | 0.15          | 0.07      |
| TP          | -          | -             | 0.08      |
| PF          | -          | -             | 0.07      |
| Sum         | 1.00       | 1.00          | 1.00      |

Table 5

| Set  | Incorrect (%) |           |       | Overrated (%) |           |       | Underrated (%) |           |       |
|------|---------------|-----------|-------|---------------|-----------|-------|----------------|-----------|-------|
|      | Rising        | Recession | Total | Rising        | Recession | Total | Rising         | Recession | Total |
| 1    | 5.7           | 3.6       | 6.4   | 3.6           | 2.1       | 2.1   | 2.1            | 1.4       | 4.3   |
| 2    | 1.4           | 0.7       | 3.6   | 0.0           | 0.0       | 2.1   | 1.4            | 0.7       | 1.4   |
| 3    | 1.4           | 2.9       | 5.0   | 1.4           | 1.4       | 2.9   | 0.0            | 1.4       | 2.1   |
| 4    | 2.1           | 2.1       | 0.7   | 0.7           | 0.7       | 0.0   | 1.4            | 1.4       | 0.7   |
| 5    | 0.7           | 3.6       | 6.4   | 0.7           | 0.7       | 2.9   | 0.0            | 2.9       | 3.6   |
| 6    | 2.9           | 0.7       | 1.4   | 0.7           | 0.7       | 1.4   | 2.1            | 0.0       | 0.0   |
| 7    | 0.7           | 1.4       | 2.1   | 0.0           | 0.7       | 0.0   | 0.7            | 0.7       | 2.1   |
| 8    | 1.4           | 2.1       | 7.1   | 0.7           | 0.0       | 5.0   | 0.7            | 2.1       | 2.1   |
| 9    | 3.6           | 1.4       | 5.7   | 1.4           | 1.4       | 2.1   | 2.1            | 0.0       | 3.6   |
| 10   | 4.0           | 0.7       | 5.3   | 2.6           | 0.0       | 1.3   | 1.3            | 0.7       | 4.0   |
| Mean | 2.4           | 1.9       | 4.4   | 1.2           | 0.8       | 2.0   | 1.2            | 1.1       | 2.4   |

Table 6

| Rating         | Method               | Statistic               | Error index    |                   |                      |
|----------------|----------------------|-------------------------|----------------|-------------------|----------------------|
|                |                      |                         | RSR            | NSE               | PBIAS                |
| Very good      | HAT                  | min <sub>≤</sub> , ≤max | 0.00≤RSR≤3.03  | -8.16≤NSE≤1.00    | -38.33≤PBIAS≤28.49   |
|                |                      | Q1 <sub>≤</sub> , ≤Q3   | 0.53≤RSR≤0.86  | 0.25≤NSE≤0.72     | -18.70≤PBIAS≤10.52   |
|                |                      | mean<br>(variance)      | 0.78 (0.181)   | 0.22 (1.342)      | -2.99 (333.921)      |
|                | General <sup>a</sup> | min <sub>≤</sub> , ≤max | 0.00≤RSR≤0.50  | 0.75<NSE≤1.00     | PBIAS≤±10            |
| Good           | HAT                  | min <sub>≤</sub> , ≤max | 0.36≤RSR≤7.44  | -54.34≤NSE≤0.87   | -166.54≤PBIAS≤62.48  |
|                |                      | Q1 <sub>≤</sub> , ≤Q3   | 0.81≤RSR≤1.37  | -1.79≤NSE≤0.34    | -56.17≤PBIAS≤23.39   |
|                |                      | mean<br>(variance)      | 1.46 (1.112)   | -2.23 (36.984)    | -22.52 (2726.906)    |
|                | General <sup>a</sup> | min <sub>≤</sub> , ≤max | 0.50<RSR≤0.60  | 0.65<NSE≤0.75     | ±10<PBIAS<±15        |
| Satisfactory   | HAT                  | min <sub>≤</sub> , ≤max | 0.53≤RSR≤12.90 | -165.40≤NSE≤0.72  | -189.11≤PBIAS≤71.17  |
|                |                      | Q1 <sub>≤</sub> , ≤Q3   | 1.06≤RSR≤2.57  | -5.62≤NSE≤-0.13   | -55.33≤PBIAS≤32.84   |
|                |                      | mean<br>(variance)      | 2.01 (2.083)   | -5.13 (161.571)   | -19.25 (4010.565)    |
|                | General <sup>a</sup> | min <sub>≤</sub> , ≤max | 0.60<RSR≤0.70  | 0.50<NSE≤0.65     | ±15<PBIAS<±25        |
| Unsatisfactory | HAT                  | min <sub>≤</sub> , ≤max | 0.63≤RSR≤23.14 | -534.44≤NSE≤0.60  | -1409.10≤PBIAS≤99.52 |
|                |                      | Q1 <sub>≤</sub> , ≤Q3   | 1.20≤RSR≤3.77  | -13.22≤NSE≤-0.44  | -154.89≤PBIAS≤80.40  |
|                |                      | mean<br>(variance)      | 3.20 (12.469)  | -21.74 (3713.448) | -43.37 (40543.580)   |
|                | General <sup>a</sup> | min <sub>≤</sub> , ≤max | RSR>0.70       | NSE≤0.50          | PBIAS≥±25            |

<sup>a</sup> general evaluation approach by Moriasi et al. (2007).