THE BRIDGE BETWEEN PRECIPITATION AND TEMPERATURE – PRESSURE CHANGE EVENTS: MODELING FUTURE NON-STATIONARY PRECIPITATION

3 Ziwen Yu¹, Stephanie Miller¹, Franco Montalto¹, Upmanu Lall²

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Abstract

5 Anthropogenic warming may change precipitation patterns, impacting infrastructure performance and 6 reliability. Future precipitation statistics generated using General Circulation Models (GCM) are, 7 however, often biased and not easily applied to problems such as runoff estimation. Stochastic weather 8 generation is hence used as an alternative to GCMs in hydrology and hydraulic modelling. This paper 9 explores the dependence of fine temporal precipitation characteristics on air pressure and air temperature 10 using historic observations. The goal is to develop, based on the key causes of precipitation, a 11 climatological basis for a stochastic precipitation generator for non-stationary precipitation under climate 12 change conditions. The analysis focuses on precipitation in the urban Northeast United States and utilizes pooled observations from meteorological stations in New York City, Philadelphia, and Boston over 60 13 14years. A negative correlation between hourly Probability of Precipitation (POP) and air pressure is 15 observed. When the historical records are discretized using air Pressure Change Events (PCE), Decreasing 16 Pressure Change Events (DePCEs) had a higher POP and a higher Precipitation Depth (PD) than 17 Increasing Pressure Change Events (InPCEs). Temperature was more strongly associated with PD during 18 DePCEs than InPCEs; this association was more pronounced during high magnitude PCEs and extreme

¹ Civil, Architecture and Environmental Engineering Department, Drexel University, Curtis 251 3141 Chestnut Street, Philadelphia, PA 19104, USA

² Department of Earth & Environmental Engineering, Columbia University, 500 West 120th Street 918 Mudd, New York, NY, 10027, USA

- events. The potential for simulating future hourly precipitation by associating historic hourlyprecipitation patterns with PCE's and monthly temperature is assessed.
- 21 *Key words*: precipitation analysis, weather type categorization, GCM temperature, hourly precipitation,
- 22 average monthly temperature, pressure change event, probability of precipitation, extreme event

23 1. Introduction

Global climate variability and change is largely caused by modifications to the global energy and water 24 cycles. To improve our ability to adapt to precipitation changes under global warming (Trenberth, Dai et 25 26 al. 2003), research is necessary to characterize the relationship between precipitation and temperature 27 (Trenberth 1998, Trenberth, Dai et al. 2003, Allan and Soden 2007, Neiman., Ralph. et al. 2008, Lenderink 28 and van Meijgaard 2010). This relationship is complex, as it varies over space and time. Although 29 General Circulation Models (GCMs) can generally investigate coarser temporal scales (e.g. annual or decadal) in larger geographic areas (e.g. Northeast US, global), more uncertainties are observed at smaller 30 31 temporal and spatial scales, since local climate is also influenced by local geography, land cover, and 32 related circulation patterns (Mitchell, Johns et al. 1999, Räisänen 2001, Zveryaev and Allan 2005, 33 Sorteberg and KvamstØ 2006).

Researchers have tried to link these two factors using physical and atmospheric explanations. For 34 35 example, Trenberth, Dai et al. (2003) suggested that through convection, the moisture required for 36 precipitation is drawn from an area of atmosphere that is about four times the rainy area. A 7% increase in air moisture holding per degree of warming at the local level has been used to imply a similar rate of 37 38 global precipitation change, based on the Clausius-Clapeyron relation (Trenberth and Shea 2005, Sun, 39 Solomon et al. 2007). Other studies investigate this relationship at different time scales, from monthly 40 (Trenberth and Shea 2005, King, Klingaman et al. 2014) to daily (Sun, Solomon et al. 2007, Westra, 41 Alexander et al. 2013) and sub-daily (Lenderink and van Meijgaard 2008, Lenderink and van Meijgaard 42 2010); still others explore this relationship based on differences in precipitation patterns, looking at means 43 (Allen and Ingram 2002, Trenberth 2011), extremes (Groisman, Knight et al. 2005, Meehl, Arblaster et al. 442005, Shaw, Royem et al. 2011, Meehl, Washington et al. 2012, Kunkel, Karl et al. 2013), and events of varying durations (Panthou, Mailhot et al. 2014, Wasko, Sharma et al. 2015). 45

For example, Madden and Williams (1978) found a frequent negative correlation between precipitation and summer air temperature at time scales ranging from inter-annual to multi-decadal in the contiguous United States and Europe. Zhao and Khalil (1993) confirmed a similar negative correlation in the summer, after exploring monthly data of the contiguous United States from 1905 to 1984. However, on days with mean daily temperatures in excess of 12 °C, Lenderink and van Meijgaard (2008) found that the probability of one-hour precipitation extremes in De Bilt, Netherlands increased much faster than the Clausius–Clapeyron relation suggests, extending this finding to larger European simulations.

53 In general, projections from GCMs are used to interpret the relationship between precipitation and temperature at coarser temporal scales (e.g. annual or decadal) under climate change scenarios when 54 considering larger geographic areas (e.g. Northeast US, global). Yet, precipitation datasets at fine time 55 56 scales (e.g. hourly or sub-hourly) are required to study the potential impacts of climate change on water resource management, urban hydrology, and agriculture. For example, one of the two primary causes of 57 runoff is Hortonian excess precipitation, whereby runoff is generated instantaneously whenever the 58 59 intensity of precipitation exceeds the infiltration capacity of the land surface. To assess whether 60 precipitation will be more intense under climate change, and possibly increase runoff generation, 61 precipitation sequences downscaled from GCM projections are needed at fine temporal scales. Despite 62 the dynamic methods used by Regional Climate Models (RCMs), stochastic precipitation generators, based on downscaled GCM projections, have been developed as an alternative (Fowler, Blenkinsop et al. 63 64 2007, Wilks 2010) and used extensively for flood risk management (Haberlandt, von Eschenbach et al. 65 2008), sizing reliable rainwater harvesting systems (Basinger, Montalto et al. 2010), and other water resource management tasks (Shamir, Megdal et al. 2015). Stochastic precipitation generators create long 66 67 continuous Markovian sequences of precipitation through a variety of methods (Wilks and Wilby 1999). One technique for sequence generation uses samples from parameterized statistical distributions of wet-68 69 day rain volume (Stern and Coe 1984, Wilks 1998), arrival and cell conditions intensity and duration (Rodriguez-Iturbe, Cox et al. 1987, Rodriguez-Iturbe, Cox et al. 1988, Wasko, Pui et al. 2015, Wasko and
Sharma 2017), and event characteristics (Heneker, Lambert et al. 2001); another relies on nonparametrically sampling historical observations (Lall, Rajagopalan et al. 1996, Lall and Sharma 1996,
Sharma and Lall 1999, Basinger, Montalto et al. 2010) with a moving window to preserve seasonality
(Rajagopalan, Lall et al. 1996).

The quality of downscaled GCM precipitation datasets is contingent upon accurate temperature predictions and a strategy for minimizing prediction bias (Johnson and Sharma 2009, Johnson and Sharma 2012). Researchers found that pressure and temperature have the most agreement across the GCMs (Johnson and Sharma 2009), while precipitation has the least consensus(Kendon, Rowell et al. 2008, Johnson and Sharma 2009) . A better understanding of the relationship between precipitation and temperature is necessary to increase confidence in precipitation projections derived from other GCM projections, such as monthly temperature.

This paper explores how fine temporal scale (e.g. hourly) precipitation patterns are related to coarser 82 83 temporal scale (e.g. average monthly) temperature. The physical causes of precipitation in a free 84 atmosphere system are discussed first. Next, an investigation into the relationship of air pressure and 85 precipitation is explored both at hourly time steps, and on an event basis. This analysis is then extended to examine how event based precipitation characteristics are impacted by Average Monthly Temperature 86 87 (AMT). The results are used to discuss the potential development of a new stochastic precipitation 88 generator that produces synthetic hourly precipitation time series by non-parametrically resampling 89 historical observations, informed by GCM projections of AMT, among other variables.

90 2. Mechanisms of Precipitation

91 One of the key causes of precipitation is the condensation of air that ascends as it moves laterally over 92 irregular terrain (orographic lifting) or is physically displaced by atmospheric phenomena (e.g. via frontal 93 lifting) (Bjerknes and Kristiania 1922). Condensed moisture then falls to the ground as precipitation after 94 drops coalesce enough to overcome the forces of drag (Ahrens, Jackson et al. 2012).

95 In a free atmosphere, the primary cause of condensation is the displacement of air masses (Bjerknes and 96 Kristiania 1922). The earliest researcher describing precipitation generated from the frontal movement of 97 air masses was Bjerknes and Kristiania (1923), who studied atmospheric circulation patterns. There are 98 three main categories of frontal precipitation (Bjerknes and Kristiania 1922, Bjerknes and Kristiania 1923): 99 (1) A cold front forms when cold, dry stable air masses lift and replace relatively unstable, warm, moist air masses previously found near the land surface. Typically, the cold air moves from the northwest to 100 101 southeast direction in the northern hemisphere. The cold air forces its way under the warm air, which is 102 then convected upward, where it cools, condenses, and coalesces, often causing short-duration, highintensity precipitation. (2) By contrast, a warm front is formed by the advance of a warm moist air mass 103 104 and the simultaneous slow retreat of cold dry air. Most commonly, warm air moves from the southeast to 105 the northwest in the northern hemisphere. Since warm air has a lower density, it rolls up and over the 106 cold air and can cause light to moderate precipitation over a large geographic area. (3) Occludal fronts 107 occur when cold and warm fronts collide, causing a cyclone with low pressure in the joint area. Occludal 108 fronts typically move to the northeast, and cause synoptic (because both warm and cold fronts are 109 present) precipitation over large land areas. Figure 1 graphically illustrates the three types of fronts.





111Figure 1 Air mass front types (the numbers in plot indicate temperature in Fahrenheit) (a) Cold front,112blue arrows indicate the direction of movement, (b) Warm front, red semi-cycles indicate the direction113of movement, (c) Occludal front, purple arrows and semi-cycles show the direction of move, both cold114front and warm front move counter-clockwise and produce low pressure region in the joint area.115(Urbana-Champaign 2010)

116 Ahrens, Jackson et al. (2012) summarized general relationships between precipitation, temperature, and pressure for each of the three types of fronts (Table 1). Note that the trends in temperature changes are 117 118 not consistent for all front types, especially for the Occludal front, which makes it difficult to develop a 119 direct relationship between temperature and precipitation. However, when air is lifted by any of the three 120 different frontal mechanisms, air pressure at the ground surface is consistently reduced (Hughes and 121 Mayes 2014). This phenomenon is well-documented at the synoptic scale, as a result of frontal 122 precipitation (Urbana-Champaign 2010). At the local or meso-scale, Hoxit, Chappell et al. (1976) found 123 that surface pressure dropped due to the formation of convective clouds, triggering showery storms. The 124 magnitude of the pressure drop is associated with the type of air mass movement at the synoptic scale or with the extent of the surface heating imbalance at the meso-scale, suggesting that in both cases pressure 125 126 changes may provide a potential physical link between precipitation and seasonal variable frontal 127 movements, related to AMT and atmosphere stability.

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	Before Passing	While Passing	After Passing
Temperature	warm	sudden drop	steadily dropping
Pressure	falling steadily	minimum, then sharp rise	rising steadily
Precipitation	short period of showers	heavy rains, sometimes with hail, thunder and lightning	showers then clearing
(a)			
	Before Passing	While Passing	After Passing
Temperature	cool-cold, slow warming	steady rise	warmer, then steady
Pressure	usually falling	leveling off	slight rise, followed by fall
Precipitation	light-to-moderate rain, snow, sleet, or drizzle	drizzle or none	usually none, sometimes light rain or showers
(b)			
	Before Passing	While Passing	After Passing
Temperature •Cold occluded •Warm occluded	Cold or cool Cold	Dropping Rising	Colder Milder
Pressure	Usually falling	Low point	Usually rising
Precipitation	Light, moderate, or heavy precipitation	Light, moderate, or heavy continuous precipitation or showers	Light-to-moderate precipitation followed by general clearing

(c)

Table 1 Climate characteristic effect of three front types a) Cold front, b) Warm front, c) Occludal front (Urbana-Champaign 2010)

131 **3. Data and Methods**

132 **3.1 Data**

The analysis focuses on the northeastern coastal United States, a region extending from Philadelphia to 133 134 Boston, and characterized by plains with no high mountains. In this region, other than the general surface heating mechanism for local summer storms, the vertical movement of air masses is typically associated 135 with frontal precipitation, rather than orographic lifting. Studies describing the relationship between 136 137 precipitation and temperature (Lenderink and van Meijgaard 2010, Shaw, Royem et al. 2011, Panthou, Mailhot et al. 2014, Wasko and Sharma 2017) use data from many locations to prove the geographical 138 139 representative of their statistics. However, the physical mechanism of precipitation formation in this 140 study area has been observed in many other locations around the world (Hoxit, Chappell et al. 1976, Knupp and Cotton 1985, Neiman., Ralph. et al. 2008, Adams-Selin and Johnson 2010, Ahrens 2012, Dawn
and Mandal 2014, Houze, Rasmussen et al. 2015). The data used in this study includes hourly
observations of temperature, sea level air pressure, and precipitation from the international airports in
New York City, Philadelphia and Boston from 1948 to 2011.

Since the topography and climate across the region are known to be similar, data from the three cities, spanning over a distance of 480 km, are pooled for this analysis. More frequent extreme precipitation in the future has been projected for this region by other researchers (Hayhoe, Wake et al. 2008, Demaria, Palmer et al. 2016, USGCRP 2017). The pooling increases the number of data points that can be used in the analysis, especially for the extremes.

150 Because 1.04% of all time steps in the historical data contains some gaps, (i.e. missing data, cumulative 151 period with no detailed information, the time-interval of observation is longer than one hour for several 152 decades, etc.), an interpolation method is developed to fill in the missing data points for gaps less than 24 153 hours. A moving average method, with a window width of a single day, is used to smooth out gaps of 154 less than six hours (1.03%). For gaps between six hours and 24 hours (0.01%), a 2nd harmonic function is 155 fitted to the values of the dry days (all gaps are treated as dry), with a length of one week (adjustable) centered on the day of interest and adjusted to match the values of the gap's end points. Then, using this 156 adjusted harmonic function, the gaps were filled with values that mimic the general change pattern for 157 the neighboring days and which connect smoothly to the observed data. Figure 2 illustrates a sample of 158 159 such a case. This method is applied on both temperature and air pressure. Where longer gaps (greater 160 than 24 hours) were evident, data was eliminated from the analysis.



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- Curated Temperature · · · Houlry temperature change - - Raw data - Sinusoidal fit

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Figure 2 Sample of missing data filling

163 **3.2 Methods**

Because the movement of air masses is typically associated with pressure changes, the first step in the 164 165 analysis was to investigate the pressure changes associated with precipitation. For the purposes of this paper, both pressure change and precipitation were investigated on an event basis. Precipitation events 166 were defined by an Inter-Event Dry Period (IntEDP). Based on Restrepo-Posada and Eagleson (1982), 167 IntEDP follows an exponential distribution for which the mean equals the standard deviation, or 168 Coefficient of Variation (CV) of unity. However, the historic IntEDP is affected by extreme events, which 169 dramatically affect calculations of the CV. In Figure 3, the CV for each city is calculated and plotted based 170 171 on IntEDP quantile thresholds of 95%, 98%, 99%, 99.5% and 100%. An IntEDP beyond each threshold is 172 not included in the calculations. Based on the results, the CV is sensitive to the extreme events in the 173 distribution tail (e.g. the 100% results are far from 99.5% results, especially for the short IntEDPs). To avoid the influence of these low-frequency events (e.g. 0.5% for 99.5% quantile threshold), this paper uses 17499.5% as the quantile threshold to determine the minimum IntEDP, which is four hours for all cities 175 176 (Figure 3).





Figure 3 Analysis of IntEDP, black horizontal solid line (CV of unity), red vertical dash line (4 hour
 IntEDP)

180 A Pressure Change Event (PCE) is defined using de-seasonalized air pressure. De-seasonalized air
181 pressure is the change in air pressure over a 24-hour period, as shown in the following equation.

182
$$P'(t) = P(t) - P(t - 24)$$

183 Where P(t) is the actual air pressure on hour t, P'(t) is the de-seasonalized air pressure on hour t. Two 184 different types of PCEs are possible, as shown conceptually in Figure 4. The horizontal axis represents time, while vertical axis represents the change in air pressure over 24 hours, i.e. the de-seasonalized air 185 186 pressure series. The shaded areas above the horizontal axis are defined as an Increasing Pressure Change Events (InPCEs) because the air pressure increases over time. The shaded areas below the horizontal axis 187 are defined as Decreasing Pressure Change Events (DePCEs), because air pressure decreases with time. 188189 The local maxima and minima in the figure indicate the greatest positive and negative 24-hour changes in 190 pressure, respectively. As shown in Figure 4, each PCE, increasing or decreasing, is bracketed by time 191 points of stable pressure (e.g. no change over 24 hours). Using the data in this study, InPCEs correspond to Event Pressure Changes (EPC) from 0 to 1100 hPa; DePCE EPCs range from -1200 to 0 hPa. EPC is
defined as the cumulative air pressure change within a PCE. The sample sizes of PCEs for BOS, NYC and
PHL were, respectively, 11564, 7147 and 8511. Based on the meteorology finding described in Table 1,
precipitation is hypothesized to occur more frequently during DePCEs.



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Figure 4 PCE definition

198 Next, the relationships between historical hourly precipitation and air pressure were explored. An 199 exploratory analysis was performed to determine whether air pressure is related to precipitation across 200 the study area. Hourly Probabilities of Precipitation (POPs) over the full air pressure range for a year and 201 each month were explored graphically. Then, the association between precipitation occurrence and 202 pressure change was qualitatively investigated on an event basis. Historical observations were 203 specifically inspected for coincidences of DePCEs and precipitation. An EPC histogram of both rainy and 204 non-rainy PCEs was plotted to explore whether precipitation is more frequently triggered during DePCEs. 205 The association between precipitation and EPC was then further analyzed and quantified in terms of PCE Precipitation Depth (PD) and PCE POP, with both computed from the total number of rainy PCEs. 206

For the association between precipitation and PCE to be applicable under climate change conditions, it is hypothesized that atmosphere stability, PCE POP, and PCE PD must be dependents of AMT. To test this theory, the frequency of PCEs is graphically inspected to interpret the stability of atmospheric system under different AMT conditions. By importing AMT information, the seasonality, corresponding PD, and POP of different PCE types is explored. To bridge precipitation and AMT, heatmaps and contours of PCE POP were overlaid with AMT for different half-years (Jan – June and July – Dec); different PCE PD percentiles were also investigated against AMT under different EPC magnitudes and seasons.

214 4. Results and Discussion

215 Figure 5 displays POP associated with different air pressures for LaGuardia International Airport (NYC) 216 at an hourly time scale. POP in this chart refers to the probability of any form of precipitation. At the top 217 of the chart is the POP versus hourly air pressure for the full data set. Below, POP is broken down by 218 month. The figure indicates that POP is negatively correlated to the hourly air pressure, irrespective of 219 month. However, during July, August, and September, this trend is less pronounced than during other 220 months. This trend is likely because 1) the air system is relatively stable in summer, with less variability 221 in air pressure, and 2) summertime convection storms are often highly localized and may not pass over 222 the climate station, even it is in the tributary area of the storm's convection. The same trends and 223 phenomena were also found in Boston and Philadelphia (Figures not shown).



 224
 Air Pressure (hPa)

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 Figure 5 POP on hourly air pressure in NYC LaGuardia International Airport (the local regressions are

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 indicated by the blue lines)

Figure 6 shows a sample sequence of alternating PCEs (shaded area) and the associated hyetographs (red bars) and 24-hour-smoothed temperature (green line). This graph illustrates that precipitation is generally associated with the DePCEs, which supports the trends illustrated in Table 1 (i.e. that frontal precipitation is successive to pressure fall).

231 Histograms describing all pooled PCEs (red) and all rain-triggering PCEs (green) are shown in Figure 7. 232 The rain-triggering PCEs are defined as those PCEs whose durations overlap with the beginning of a 233 precipitation event. The histogram of the full sample of all PCEs is similar to a normal distribution, with a 234 mean near zero. The distribution of rain-triggering PCEs is, however, skewed to the left and is 235 discontinuous at the vertical axis (in the negative range). The left-skewness is consistent with the meteorological interpretation that as air masses are vertically lifted, negative changes in pressure are 236 237 associated with precipitation events. The discontinuity in the distribution could indicate the presence of 238 two different types of fronts. Cold fronts lift warm air rapidly, generating precipitation over relatively 239 small geographic areas very soon after the pressure drops. Because POP in the negative region of Figure 7 240 is higher, it may be that these events correspond to cold-front storms. Alternatively, the smaller POP under positive EPC may correspond to warm-front storms, since warm-front storms usually affect a large 241 242 region ahead of the front. For this reason, precipitation correlated with InPCE has a lower POP.

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Figure 7 Kernel density of EPC for rain triggered PCEs (green) and all PCEs (red)

The POP and PD associated with EPCs are depicted graphically in Figure 8. A local fit line using loess 248 249 method (Cleveland, Grosse et al. 1992) is used to highlight the correlation between POP and EPC. Note, the density plot in the lower chart reflects only the distribution of the rainy PCEs, as all dry PCEs are all 250 251 laying atop the x axis (PD = 0 mm). Two distinct PCEs are divided by EPC = 0 hPa. As the absolute value 252 of an EPC increases, the POP of DePCEs increases from 15% to 100% within 0 ~ -300 hPa, while InPCE 253 POP increases only from 15% to about 40% within 0 ~ 820 hPa. Given that the sample size of intensive 254 InPCEs is limited (n = 79 when EPC > 820 hPa), less confidence is associated with the POP beyond 820 255 hPa. Falling pressure appears to be a better indicator of precipitation than increasing pressure. The 256 highest PCE occurrence occurs at EPC values of approximately -250 hPa and PD of 20 mm. These ranges 257 are consistent with the histogram shown in Figure 7. Similar to POP, the trend of PD versus EPC can also be divided by PCE types. For DePCEs, the PD increases along with the EPC magnitude, while for InPCEs, 258 259 EPC magnitude reduces PD. Physically, InPCE appears in a stable atmosphere, which does not benefit air 260 mass lifting and so lacks the moisture supply necessary to intensify the precipitation process as DePCE 261 does.



Bjerknes and Kristiania (1923) reported that the average lifetime of an air circulation system was 5.5 days, a period that was similar in duration to the average 5.7 days of precipitation events reported in 1909 by Defant (1921). It suggests that occurrence of air circulation and its corresponding air pressure change could be treated as an indicator of atmosphere stability, especially for moderate and intensive events. Since precipitation is formed due to atmospheric instability, it is important to evaluate the impact of temperature on the atmospheric system. The monthly frequency of moderate and intensive PCEs

262 263 270 (absolute value of EPC > 90 hPa) is plotted in two half-years against AMT in Figure 9, with a local 271 regression line in blue. An obvious negative relationship when $AMT > 0^{\circ}C$ can be seen for both half-years. Atmospheric systems are more stable when the weather gets cold (AMT < 0° C). This illustrates that the 272 273 atmospheric system stability, indicated by monthly frequency of moderate and intensive PCEs, is a 274 function of AMT, one of the GCM outputs. It should be noted that even though the occurrence becomes low, individually PCE in high temperature is generally more intensive than low temperature. 275





Figure 9 Association between monthly PCE frequency and AMT with local regression line (blue) To further investigate the impact of AMT on PCE and its associated precipitation characteristics, Figure 278 279 10 and 10 present the PD and POP for two halves of the year, indexed by AMT.

280 The relationship between PD and AMT is contoured by frequency in Figure 10 for both InPCEs and DePCEs. Two seasonal systems (centroids), winter and summer, are visible for both PCE types. The 281

summer system is concentrated around 8 mm for DePCEs and 6 mm for InPCEs (both centroids near 282 283 22°C). The difference of PD between DePCE and InPCE in summer is not pronounced since precipitation 284 tends to be localized in the relatively stable atmospheric system, as implied by the narrow variance of air 285 pressure. However, the opposite is true for winter system. The winter system is centered around 17.5 mm 286 for DePCEs and 2.5 mm for InPCEs (both centroids near 2.2°C). This indicates that DePCE has a larger 287 geographical scale effect on winter storms. The magnitude of this difference fades out as the AMT grows 288 from winter to summer. The change in PD between winter and summer is +3.5 mm for InPCEs and -8.5 289 for DePCEs. These differences are largely due to the seasonality of precipitation formation, with large-290 scale, frontal mechanisms dominating in winter, and local air convection dominating in summer.

291 Figure 11 illustrates the POP of both PCE types under different AMT conditions. The POP of DePCEs is 292 generally higher than of InPCEs which is coincided with Figure 7 and Figure 8. For DePCEs, during both halves of a year, POP is roughly level, oscillating between 55% and 65% with some small differences in 293 294 the tail regions (e.g. high and low end of AMT range). The small POP during low temperatures in the second half of the year (Jul~Dec) is not reliable, due to a limited sample size (n = 9 for both InPCEs and 295 296 DePCEs). However, during high temperatures, the POP decreases about 10%. This could be another 297 impact of meso-scale summer convection storms, which generally have a tributary area much larger than 298 the area of precipitation (Hoxit, Chappell et al. 1976, Hoxit, Chappell et al. 1976). Given that the data in the study is only from three airports, it is very likely these areas contribute to convections forming storms 299 300 elsewhere. For InPCEs, during both year halves, the POP indicated is approximately 25% at the lowest 301 temperatures and 35% at the highest. Between Jan and Jun, POP gradually rises to 35% between 4°C and 10°C, while during Jul and Dec, the increase in POP is delayed until the temperature increases from 20°C 302 to 26°C. This observation suggests that the precipitation / pressure dynamics in the fall and spring differ 303 304 somewhat from one another, although both have a similar temperature range (6°C).

The PD of spring and fall are difficult to differentiate in Figure 10, since their AMTs overlap. Similar POP values are shown in Figure 11 for DePCEs, though the temperatures at which POP increases for InPCEs are slightly different. The increase in POP could be caused by warm-front frequency under different AMTs. Since warm air masses generally move to the north in spring, it is reasonable to expect stronger warm-front storms in spring than in the fall.

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Figure 10 PD of different PCE types on AMT (red: DePCE, green: InPCE)





Figure 11 POP of different PCE types on AMT in different half years (red: DePCE, green: InPCE)

This analysis suggests that high POP in this geographical region is associated both with low absolute 315 pressure and with DePCEs. It also indicates that PCE could serve as a potential link between AMT and 316 POP. This relationship is plotted in Figure 12 in terms of POP and PCE against AMT, with break points in 317 318 the middle of a year. POP ranges from 0% (tan) to 100% (light blue). Generally, POP is higher in DePCEs 319 for the entire year. As indicated by the contours of the local regression, POP for DePCEs is highest when EPC is near -800 hPa, regardless of the time of year. Between July and December, POP increases as 320 temperatures decrease. For InPCEs, EPC magnitude is positively correlated to POP, though this 321 322 correlation is more pronounced for DePCEs.



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Figure 12 PCE POP over AMT by EPC

As a further investigation, we explored PD quantiles against EPC and AMT in different seasons (Figure 325 13). Three PD percentiles, 50%, 75% and 95%, are included. The relationships represented by the local 326 regression lines are colored by season. Vertically, similar to the results presented in Figure 8, PD 327 percentiles increases as the EPC drops, especially in DePCE regions. This generally holds for all PD 328 percentiles and seasons. Horizontally, PD seems to vary greatly depending on the AMT, with an 329 amplified magnitude on high percentile categories (75% and 95% quantiles). For intensive 330 (500hPa~2000hPa) and non-intensive (0hPa~500hPa) InPCEs, the all-season dash lines reflect the overall 331 relationship between PD and AMT since seasonality is not significant. When AMT is lower than 10°C, PD 332

stays small. At temperatures above 10°C, non-intensive InPCE PD starts to increase slightly with AMT in the PD percentiles of 95%. This increase is amplified in intensive InPCEs for all PD quantiles, as shown in Figure 13, but delayed to 22°C, which almost exclusively represents summertime events. It should be noted that this amplification could be caused by the limited sample size (n = 40 for 23°C~26°C) at the corresponding AMT range and thus may not be reliable.

338 For DePCE, seasonality is more pronounced in high PD percentiles (75% and 95%) and under intensive 339 EPC conditions. When combined with the density graph from Figure 8, non-intensive (-500hPa~0hPa) 340 DePCEs occur more frequently than other EPC categories and thus are more important in the investigation of how PD responds to PCEs and AMT. Although not all pronounced, non-intensive 341 DePCEs generate more precipitation when AMT is higher, obvious for PD in the 95th percentile. This 342 343 trend for non-intensive DePCEs is stronger than for non-intensive InPCE in a similar AMT range. The trends for all seasons have a dropping tail for high AMTs, which could be due to shrinking sample sizes. 344 It could also imply that extreme events (95%) are more influenced by temperature and will likely be more 345 affected by climate change than regular events, a finding that is supported by other researchers (Allen 346 and Ingram 2002, Trenberth, Dai et al. 2003, Allan and Soden 2008, Giorgi, Im et al. 2011). 347

Since PD is negatively associated with EPC, intensive (-2000hPa~-500hPa) DePCEs contain many extreme events. Seasonality is also more differentiable for intensive DePCEs. A monotonic positive trend between PD and AMT can be observed in fall. In winter, PD increases when the AMT is less than 0°C, and decreases for warmer temperatures. In spring, PD (except in the 95% percentile) does not obviously change until AMT is greater than 10°C. Summer shows a general monotonic decrease in PD as AMT increases. This is consistent with Shaw, Royem et al. (2011)'s findings in the NE, USA, suggesting that extreme precipitation events show a decrease in PD after 25°C during the summer. The relationship between PD and AMT is important in the context of downscaling precipitation based on GCM temperature projections, the motivation for this study. AMT could generally indicate the moisture holding capacity and associated non-extreme PD trend of the CC relationship. However, at finer temporal scale or for a specific precipitation event, precipitation should be more physically related to hourly temperature (Panthou, Mailhot et al. 2014, Peleg, Marra et al. 2018). Moreover, pressure change, as a driver of precipitation investigated in this study, could impact on PD more directly than temperature and is worth to further explored.



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- All Season - Fall (SON) - Spring (MAM) - Summer (JJA) - Winter (DJF)



The impacts of both AMT and EPC on precipitation characteristics (POP, PD and percentiles) in Figure 12 and 13 quantify the precipitation change with climate. Ban, Schmidli et al. (2015) suggest future climate may not be represented by the statistics derived from present using CC-related results. In this study, it might be true for the trends of precipitation characteristics in the extreme situation (e.g. an AMT or an EPC not seen in the historical data, or a local scale summer convection system only shown in the point

source data in terms of pressure changes but not precipitation). However, the analysis in this study is not 369 370 statistical based. Although the intensity of different precipitation types may vary due to divergent 371 thermodynamic conditions across different areal, seasonal and climate conditions (Panthou, Mailhot et al. 372 2014, Peleg, Marra et al. 2018), pressure change as a physical requirement of precipitation formation, 373 described in this study, is independent of global warming. Thus, qualitatively, the dependences between 374 EPC, PD and AMT will be generally held. Meanwhile, the analysis results, for observed climate, may 375 have lower confidence under climate change, especially for local convection events, because a) the sample size of such events is underestimated in the historical data collected by point sources, such as climate 376 377 stations in this study; b) the trajectory and effective area of precipitation events could change in future 378 climate (Peleg, Marra et al. 2018).

379 **5.** Conclusion

We investigated the possibility of associating hourly precipitation / pressure data with AMT data as a preliminary analysis for generating a non-stationary, non-parametric, stochastic precipitation generator conditioning GCM monthly temperature output. Specifically, the results of this analysis answer the following two questions: 1) how PD and POP change with EPC during different types of PCE and 2) how the PD and POP of specific PCEs respond to AMT.

Precipitation is formed by the cooling of moist air, typically due to vertical lifting. Physically, this lifting results in reduced sea-level air pressure prior to precipitation events. This research reveals that both POP and PD are highly correlated to PCEs. It provides a more physically reliable strategy by importing pressure change for stochastic precipitation generation, either parameterized statistical type or nonparametric resampling type, to model precipitation. The dependence of precipitation characteristics (POP, PD and percentiles) on AMT and EPC (Figure 12 and 13) could also enable stochastic precipitation 391 generations to incorporate more reliable GCM AMT projections in generating non-stationary situations.
392 For this reason, we propose a stochastic precipitation generator for generating PCE sequences
393 conditionally, using the corresponding precipitation as an output.

394 Since the relationship between PCE and precipitation is derived from the physical precipitation formation 395 mechanism, this kind of stochastic precipitation generator represents a much stronger and more reliable 396 conceptual basis on which to build a model, as compared to those models barely relying on statistical 397 assumptions. Moreover, because PCE is more strongly related to precipitation formation than coarser 398 temporal scale temperature (e.g. monthly), it could be a reliable method for downscaling precipitation 399 from GCM AMT projections, which are currently more trustworthy than GCM precipitation projections. Such a stochastic precipitation generator could be built by sampling PCE-associated hourly precipitation 400 401 series from historical observations, and by adjusting for GCM predicted monthly temperatures. 402 Specifically, by employing non-parametric method (Lall, Rajagopalan et al. 1996, Lall and Sharma 1996, 403 Rajagopalan and Lall 1999), AMT projections from GCMs would be used as a reference to determine a pool of candidate PCEs under similar AMTs (i.e. a range of 6°C within which POP seasonal changes occur, 404 405 as shown in Figure 11), similar to the moving window method (Rajagopalan, Lall et al. 1996). A 406 secondary paper, specifically describing such a non-stationary non-parametric stochastic precipitation 407 generator, will be published.

In all, this paper suggests a means of generating long, continuous, synthetic precipitation series from scaled-down GCM AMT projections. These series could then be used for a variety of climate change model applications, such as hydrologic and hydraulic modeling, water resource modeling, agriculture modeling.

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