

1 **Developing a 3D mechanistic model for examining factors contributing to harmful blooms**
2 **of *Margalefidinium polykrikoides* in a temperate estuary**

3 Qubin Qin^{1*}, Jian Shen¹, Kimberly S. Reece¹, Margaret R. Mulholland²

4 ¹Virginia Institute of Marine Science, William & Mary, Gloucester Point, VA 23062, USA

5 ²Department of Ocean, Earth and Atmospheric Sciences, Old Dominion University, 4600
6 Elkhorn Avenue, Norfolk, VA 23529-0276, USA

7

8 *Correspondence to:

9 Qubin Qin

10 Virginia Institute of Marine Science

11 William & Mary

12 Gloucester Point, VA 23062, USA

13 Email: qubin@vims.edu

14 Phone: +1 (804) 684-7670

15 Abstract

16 Blooms of *Margalefidinium* (previously *Cochlodinium*) *polykrikoides* occur almost
17 annually in summer in the lower Chesapeake Bay and its tributaries (e.g., the James and York
18 Rivers). The Lafayette River, a sub-tributary of the lower James River, has been recognized as an
19 initiation location for blooms in this region. The timing of bloom initiation varies interannually,
20 ranging from late June to early August. To fully understand critical environmental factors
21 controlling bloom initiation and interactions between physical and biological processes, a
22 numerical module simulating *M. polykrikoides* blooms was developed with a focus on the bloom
23 initiation. The module also includes life cycle and behavioral strategies such as mixotrophy,
24 vertical migration, cyst dynamics and grazing suppression. Parameterizations for these behaviors
25 were assigned based on published laboratory culture experiments. The module was coupled with
26 a 3D physical-biogeochemical model for the James River that examined the contribution of each
27 environmental factor and behavioral strategy to bloom initiation and development. Model
28 simulation results highlight the importance of mixotrophy in maintaining high growth rates for *M.*
29 *polykrikoides* in this region. Model results suggest that while many factors contribute to the
30 initiation process, temperature, physical transport processes, and cyst germination are the three
31 dominant factors controlling the interannual variability in the timing of bloom initiation.

32

33 Keywords: *Margalefidinium polykrikoides*; Mixotrophy; Estuary; Physical processes; Cyst
34 germination; Modeling

35 1. Introduction

36 Harmful algal blooms (HABs) have been observed in many estuarine and coastal systems,
37 and it has been suggested that anthropogenic nutrient enrichment is contributing to their
38 worldwide expansion (Anderson D.M. et al., 2002; Heisler et al., 2008). *Margalefidinium*
39 (previously *Cochlodinium*) *polykrikoides* is a dinoflagellate HAB species that blooms almost
40 annually in the lower Chesapeake Bay and its tributaries including the James and York Rivers
41 (Marshall 2009; Morse et al., 2013). *M. polykrikoides* blooms observed in the lower Chesapeake
42 Bay appear to initiate at localized “hot spots”, and the Lafayette River, a sub-tributary of the
43 lower James River is thought to be one such initiation site (Mulholland et al., 2009; Morse et al.,
44 2011, 2013; Qin and Shen, 2019). Blooms are then transported into adjacent and connected
45 waterways where they can flourish (Morse et al., 2011; 2013). This suggests that the initiation of
46 *M. polykrikoides* blooms is controlled by local conditions affecting cell growth and accumulation.

47 *Margalefidinium polykrikoides* blooms typically occur in the summer when warm
48 temperatures are thought to support their growth (Kudela and Gobler, 2012). In the James River,
49 long-term monitoring suggests that the time at which populations reach bloom density (> 1000
50 cells ml⁻¹, Virginia DEQ, 2019) varies interannually, ranging from late June to early August
51 (Mulholland et al., 2009, 2018; Morse et al., 2011; 2013). In addition, monitoring shows that the
52 duration of *M. polykrikoides* blooms also varies interannually, ranging from several days to
53 several months (Hofmann et al., in review). These fluctuations pose interesting and important
54 questions: How are the bloom dynamics regulated by environmental factors? And, what are the
55 key factors controlling the interannual variability in the timing of *M. polykrikoides* blooms?

56 Based on daily observational data, Morse et al. (2013) highlighted the important roles of
57 the temperature and localized nutrient inputs from storms for the initiation of the *M.*
58 *polykrikoides* blooms in the Lafayette River. However, due to the lack of robust local culture
59 isolates and the ephemeral nature of blooms, we still lack a quantitative understanding of many
60 of the factors thought to regulate the growth of *M. polykrikoides* such as their: 1) ecophysiology
61 (e.g., the effects of temperature, salinity, light and nutrient concentrations and their nonlinear
62 interactions); 2) ability to grow mixotrophically; 3) patterns of vertical migration; 4) food-web
63 interactions with other species including grazing suppression and allelopathic effects on
64 competitors; 5) transport processes; and 6) their ability to form temporary and resting cysts to
65 both avoid unfavorable environmental conditions and ensure that there are seed populations
66 available to germinate to vegetative cells when conditions become suitable (e.g., Kudela and
67 Gobler, 2012).

68 Process-based models with realistic forcings are one of the most powerful tools for
69 quantifying the relative contributions of various physical and biological factors to bloom
70 formation (Glibert et al., 2010; McGillicuddy, 2010; Anderson C.R. et al., 2015; Franks, 2018).
71 Three dimensional process-based models have been developed and widely used for
72 quantitatively examining biogeochemical processes (e.g., nutrient concentrations, oxygen, algal
73 biomass and productivity) in aquatic systems, but these have been much less used to model
74 HABs. While there are 3D mechanistic models developed for HABs in lakes, estuaries, and
75 coastal marine environments (e.g., McGillicuddy et al., 2005; Gentien et al., 2007; Milroy et al.
76 2008; Moore et al., 2015; Ralston et al., 2015; Aleynik et al., 2016; Gillibrand et al., 2016;
77 Zhang et al., 2021), the biogeochemical processes in those models are often simplified because it
78 is a challenge to accurately simulate the complex dynamics of HAB species that have multiple

79 behavioral and adaptive strategies (Anderson C.R. et al., 2015; Ralston et al., 2015; Ralston and
80 Moore, 2020). Nevertheless, these behavioral and life cycle strategies are needed to be suitably
81 simulated in HAB models for improving their modeling skills (Azanza et al., 2018; Flynn and
82 McGillicuddy, 2018; Wells et al., 2020). For example, for harmful mixotrophic species, properly
83 simulating the contribution of mixotrophy to population growth is important (Stoecker et al.,
84 2017; Flynn and McGillicuddy, 2018; Flynn et al., 2018). While approaches for using
85 mathematical models to simulate mixotrophy have been proposed (e.g., Flynn and Mitra, 2009;
86 Mitra and Flynn, 2010; Ghyoot e al., 2017a; Lin et al., 2018) and applied in some
87 biogeochemical models (e.g., Ghyoot et al., 2017b), the explicit modeling of mixotrophy is still
88 rare in large 3D mechanistic HAB models that couple physical and biogeochemical processes. In
89 shallow, estuarine systems, in addition to the construction of equations to describe the processes
90 related to mixotrophy, simulations must include the full nutrient dynamics with nonpoint- and
91 point-source loadings as well as internal nutrient cycles both in the water column and in the
92 bottom sediment.

93 In this study, a mechanistic model for simulating an *M. polykrikoides* bloom was
94 developed and applied to the lower James River. Values for most model parameters were
95 incorporated from laboratory culture experiments reported in the literature. The developed HAB
96 model was coupled with a 3D hydrodynamic-eutrophication model to fully simulate the
97 dynamics of *M. polykrikoides* under the influence of various estuarine biogeochemical processes.
98 The model was then used to quantitatively evaluate the contributions of various environmental
99 factors to the interannual variability in the initiation of *M. polykrikoides* blooms. Environmental
100 factors included: temperature, salinity, light, inorganic nutrient concentrations, bioavailable
101 organic matter and prey, grazing, retention, as well as behavioral strategies such as mixotrophy,

102 vertical migration, and cyst germination. The terminology used in this study is defined here: 1)
103 “present” refers to the entire period of time when the cell density of *M. polykrikoides* is greater
104 than 0 cell ml⁻¹ in the water column, including both bloom and non-bloom periods, 2) “bloom
105 event” refers to the period when cell densities are ≥ 1000 cells ml⁻¹, and 3) “initiation period” is
106 the period when the *M. polykrikoides* cell densities are > 0 but < 1000 cells ml⁻¹.

107 2. Methods

108 2.1. Site description

109 The Lafayette River is a sub-tributary of the lower James River near its confluence with
110 the lower Chesapeake Bay, USA, and is a site where *M. polykrikoides* blooms are thought to
111 initiate (Fig. 1; Mulholland et al., 2009; Morse et al., 2011, 2013; Qin and Shen, 2019). The
112 Lafayette River is a temperate estuary with a mean depth less than 5 m, and its hydrodynamics
113 are largely controlled by tidal forcing (the tidal range is about 1 m), runoff from the urban
114 watershed, and wind. Water temperatures in this estuary vary widely over annual cycles with
115 values in excess of 30°C observed in summer and below 10°C in winter. The primary sources of
116 freshwater to the estuary are rainfall and groundwater, and so in the absence of storms, salinity is
117 primarily controlled by tidal water transport from the lower James River; the average salinity
118 ranges from 15-25. However, when there is heavy rainfall, salinities in the upper Lafayette River
119 can decrease to less than 5.

120 Monthly environmental data including chlorophyll-a concentrations (chl-a) for 2007-
121 2013 were retrieved from the long-term Chesapeake Bay Program monitoring database
122 (<https://www.chesapeakebay.net/>) for stations LFB01 and LFA01 in the Lafayette River, and
123 stations LE5.6, and LE5.4 in the Lower James River. An additional station near the mouth of the

124 Lafayette River at the Norfolk Yacht and Country Club (NYCC) was included in this analysis, it
125 was established as a timeseries site for observing water quality impairments and bloom initiation
126 in 2012. Weekly surface dataflow cruises were conducted by the Hampton Roads Sanitation
127 District in the poly- and mesohaline James River, and in the Elizabeth and Lafayette Rivers to
128 map surface chl-a concentrations between March and October from 2008-2013. During dataflow
129 cruises surface water is pumped through a YSI datasonde equipped with a chl-a sensor. These
130 data are publicly available through the Virginia Estuarine and Coastal Observing System
131 (VECOS, <http://web2.vims.edu/vecos/>). For model comparison, dataflow chl-a concentrations
132 were spatially averaged over the areas (bounded by the corresponding grid cells) around Stations
133 LFB01, NYCC, LFA01, LE5.6, and LE5.4 to provide the mean values of surface chl-a at the five
134 stations.

135 *Margalefidinium polykrikoides* cell abundance in the Lafayette River was quantified
136 using light microscopy (Mulholland et al., 2009; Morse et al., 2011; 2013; 2014; Egerton et al.
137 2014). Algal cells were identified to the lowest taxonomic unit (usually to the genus or species
138 level) and densities were reported as cells ml⁻¹. Particularly, for better comparing the model
139 output with observational data, we used the data of *M. polykrikoides* cell abundance (cells ml⁻¹)
140 with relatively high frequency (daily) from a station near Station LFB01 in the summer of 2009
141 (Morse et al. 2013).

142 2.2. A model for *M. polykrikoides* blooms in the James River

143 A HAB module was first developed and built into the James River water quality model
144 (JRWQM). This module is carbon-based and consistent with the 3D hydrodynamic-
145 eutrophication model of Environmental Fluid Dynamics Code (EFDC, Park et al. 1995) used for
146 JRWQM, and the biomass of *M. polykrikoides* was simulated. Cell abundance was calculated

147 from carbon biomass using a conversion factor of 3437 pg C cell⁻¹ based on the average cell
 148 biovolume for *M. polykrikoides* (Smayda 1978). The results were compared to observational data
 149 of *M. polykrikoides* abundance, in units of cells ml⁻¹ in 2009. While this module focuses on
 150 vegetative cell growth, it includes behavioral and life cycle strategies employed by *M.*
 151 *polykrikoides*, such as vertical migration, mixotrophic growth, resting cyst formation, and cyst
 152 germination.

153 At a given location, the governing equation for *M. polykrikoides* dynamics can be
 154 described as:

$$\frac{\partial C}{\partial t} + u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} + w \frac{\partial C}{\partial z} - \left[\frac{\partial}{\partial x} \left(K_x \frac{\partial C}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_y \frac{\partial C}{\partial y} \right) + \frac{\partial}{\partial z} \left(K_z \frac{\partial C}{\partial z} \right) \right] =$$

$$155 \quad (G - R - M)C + w_c \frac{\partial C}{\partial z} + \text{germ} - \text{encyst} \quad (1)$$

156 where C is the density of the HAB species; x, y, z, and t denote the three-dimensional location
 157 and time, respectively, of C. The variables u, v, and w are the current velocities in x, y, z
 158 dimensions, respectively; and K_x , K_y , K_z are diffusivities in x, y, z dimensions, respectively, G is
 159 the gross growth rate, R is the respiration/excretion rate, and M is the mortality rate due to
 160 natural death, grazing, and parasitism. w_c denotes the vertical velocity/swimming speed of the
 161 algae, *germ* denotes the input rate of vegetative cells from the germination of resting cysts,
 162 *encyst* is a sink term denoting the loss rate of vegetative cells due to cyst formation. G is
 163 expressed as the product of the optimal gross growth rate and the growth-limiting functions for
 164 environmental factors, where each growth-limiting function ranges from 0 (most limiting) to 1
 165 (not limiting at all). The details of the module development are described in the Appendix, and
 166 the expressions for functions and critical parameters are listed in Table 1.

167 Detailed descriptions of the JRWQM model, model configuration, and boundary
168 conditions are described in Shen et al. (2016) and Shen and Qin (2019). The formation and
169 germination of temporary cysts can cause significant variability in the density of vegetative cells
170 over diurnal cycles (Shin et al., 2017). The transformation of vegetative cells into temporary
171 cysts is thought to be largely controlled by the light availability (Shin et al., 2017). Because the
172 formation and germination of temporary cysts do not represent a net source or loss term on the
173 time scale of bloom events, rather than adding to the complexity and uncertainty of the module,
174 the current module ignores temporary cyst dynamics.

175 2.3. Model parameterizations and calibration

176 The HAB module for *M. polykrikoides* dynamics was applied to examine *M.*
177 *polykrikoides* blooms in the James River and its tributaries, for which there is a well-calibrated
178 JRWQM model (Shen et al., 2016; Shen and Qin, 2019). The model simulation, with realistic
179 forcings, was conducted from 2006-2013. The year 2006 was used for spinning up the
180 hydrodynamics of the model, and the dynamics of *M. polykrikoides* in the following 7 years
181 (2007-2013) were then simulated. In this study, three algal groups were simulated, *M.*
182 *polykrikoides* and two non-HAB assemblages, one dominated by diatoms, and the other
183 describing mixed phytoplankton communities including dinoflagellates, chlorophytes, and
184 cryptophytes. Each station was represented by one single grid cell. Statistical analyses were used
185 to evaluate the performance of the model, including the relative error (RE) and the correlation
186 coefficient (r) between the model output and observational chl-a data at the five stations.

187 Physiological parameterizations in the HAB module were estimated based on culture
188 experiments reported in the literature and adjusted during the calibration process based on both
189 chl-a and cell density data from the lower James River estuary. Model parameterizations used are

190 listed in Table 2 along with the data sources. As discussed in the Appendix, the mortality rate, M ,
191 was set to zero in the model. *M. polykrikoides* is assumed to swim upward when light is limiting
192 during daytime but no swimming activity at night. The swimming speed is set to be $w_c = 55 \text{ m d}^{-1}$.
193

194 The values for optimal gross growth rates for *M. polykrikoides* were estimated based on
195 the culture experiments conducted by Gobler et al. (2012). They reported maximum specific
196 growth rates of $0.43\text{-}0.44 \text{ d}^{-1}$ for growth on dissolved inorganic nitrogen (DIN) ($>25 \mu\text{M N}$) and
197 0.53 d^{-1} for growth on glutamic acid ($>25 \mu\text{M N}$) in cultures of *M. polykrikoides* isolated from
198 Long Island, NY, USA, and grown at $21 \text{ }^\circ\text{C}$ under a 14:10 light:dark cycle. These rates are
199 consistent with those reported for the *M. polykrikoides* Korean ribotype by Kim et al. (2004),
200 0.41 d^{-1} . These daily growth rates were used to obtain the phototrophic and heterotrophic gross
201 growth rates at the optimal condition (i.e., no limiting at all) and used at each time step in our
202 model experiments that are 1.06 d^{-1} and 0.62 d^{-1} , respectively (Table 2). Heterotrophic growth
203 was assumed to occur under both light and dark conditions. The values of parameters used to
204 compute growth-limiting functions for temperature, $f(T)$, and salinity, $f(Sal)$, were also
205 determined based on experimental results from cultures (Kim et al., 2004; Griffith and Gobler,
206 2016) using a least-squares fit. The parameter for the effect of light availability on phototrophic
207 growth, G^p , was based on values reported by Kim et al. (2004) and Oh et al. (2006).

208 *Margalefidinium polykrikoides* can take up various forms of nitrogen (Mulholland et al.,
209 2009; 2018). Because kinetic experiments demonstrated that the half-saturation coefficients for
210 nitrate and ammonium were similar to each other (Kim et al., 2001; Kudela et al., 2008; Gobler
211 et al., 2012; Hofmann et al., in review), only one half-saturation coefficient for dissolved
212 inorganic nitrogen (DIN) was used. The values of half-saturation coefficients for DIN and

213 dissolved inorganic phosphorus (DIP) used in the model were 0.028 g N m^{-3} ($2 \text{ }\mu\text{M}$) and 0.0177 g
214 P m^{-3} ($0.57 \text{ }\mu\text{M}$).

215 For heterotrophic growth, both phagotrophy (grazing on particulate organic matter, POM)
216 and osmotrophy (uptake of dissolved organic matter, DOM) are considered (Appendix). The
217 simulation allows *M. polykrikoides* to graze on POM smaller than $12 \text{ }\mu\text{m}$. This size cutoff is
218 consistent with the size of particles observed to be grazed by the Asian *M. polykrikoides*
219 ribotypes (Jeong et al., 2004; Kudela and Gobler, 2012). The corresponding growth-limiting
220 function for the heterotrophic growth depends on the concentrations of OM_{12} , the bioavailable
221 organic matter (DOM+POM) less than $12 \text{ }\mu\text{m}$ in size. By using a Monod-type equation, the half-
222 saturation coefficient for organic matter, OM_{12k} , was estimated to be $0.0263 \text{ g C m}^{-3}$ based on a
223 published culture experiment showing that the growth of *M. polykrikoides* increased with
224 increasing cryptophyte concentration (Jeong et al., 2004). In the lower James River, we assumed
225 that *M. polykrikoides* could not graze on larger co-occurring algae such as *Akashiwo sanguinea*
226 and *Scrippsiella trochoidea* (Morse et al., 2013) due to their size. Because concentrations of
227 cryptophytes in the Lafayette River is generally low in the summer ($5\text{-}40 \text{ cells ml}^{-1}$, Morse et al.,
228 2013), prey-sized algae are only a small fraction, less than 0.001, of the total biomass of co-
229 occurring algae, b (see the definitions in Appendix and Table 2). Simulations used a constant
230 value of 0.001 for the fraction of prey biomass, b . According to culture experiments by Jeong et
231 al. (2004), these low prey concentrations would not significantly increase the growth rates of *M.*
232 *polykrikoides* via phagotrophy. A sensitivity test setting $b = 0$ (i.e., no prey) versus 0.001 showed
233 negligible differences (the detailed comparison is not shown here). The fraction of POM that is
234 bioavailable for *M. polykrikoides* uptake that is not small algae, a (see the definitions in
235 Appendix and Table 2) was calibrated by trial and error. Briefly, with a series of a increasing in

236 value, we found the value leading to the best match of the model results against observational
237 chl-a data at the five stations (highest r and lowest RE). The parameters for respiration (R_0 , f^p ,
238 and θ_R) were also calibrated (Table 2) and their values are comparable to typical values used in
239 eutrophication or ecosystem models.

240 The condition for initiating the model corresponded to a cyst germination event. The
241 process was simplified as a one-time release of vegetative cells within one day (an initial loading
242 due to germination, $germ_{ini}$) from the bottom layer over the mesohaline and polyhaline zones of
243 the James River and its tributaries. Sediment samples show that the mean concentration of *M.*
244 *polykrikoides* cysts in wet sediment is 96 cysts g^{-1} in the lower James River (Seaborn and
245 Marshall, 2008). By using the wet sediment density of 2.65 $g\ cm^{-3}$ and assuming resting cysts in
246 the top 1 cm of the sediment can be germinated and released into the overlying water, the
247 potential concentration of cysts in the sediment is 2.54×10^6 cysts m^{-2} . However, not every cyst
248 can successfully germinate into vegetative cells. Five laboratory experiments by Tang and
249 Gobbler (2012) showed a range of 2-33% and a mean of 12% for the germination rate of *M.*
250 *polykrikoides* cysts in laboratory cultures. It is expected that the germination process in nature
251 may have a lower success rate and therefore, we assumed a germination rate of 1% in the model.
252 This resulted in an estimate of cell loading from cyst germination of about 25,000 cells $m^{-2}\ d^{-1}$.
253 The time when cells from cyst germination first enter the water column (referred to as “initial
254 time”) was an adjustable parameter, and it is typically that a later initial time corresponds to a
255 later beginning of the bloom; so we were able to calibrate the initial time for each year by trial
256 and error, based on chl-a and cell density data reported in previous studies (Morse et al., 2011,
257 2013; Mulholland et al., 2009). An additional requirement for the germination used for calibrating
258 the initial time is that the water temperature be above 18 °C, consistent with the germination

259 experiments conducted by Tang and Gobler (2012) (temperatures between 18-21 °C). These
260 temperatures are cooler than those observed during blooms in the lower Chesapeake Bay
261 (Mulholland et al., 2009; 2018).

262 2.4. Analysis of contributions of each factor

263 The calibrated model (Base Scenario) was used to analyze the contribution of each
264 environmental factor and behavior strategy to *M. polykrikoides* blooms in the James River and its
265 tributaries, with a focus on bloom initiation. Among all possible behavioral and life cycle
266 strategies of *M. polykrikoides*, the contributions of three, mixotrophic growth, vertical migration,
267 and cyst germination were considered.

268 For any algal species, the governing equation (1) can be rewritten mathematically into a
269 simplified form:

$$270 \quad \frac{\partial C}{\partial t} = r_g C \quad (2)$$

271 The relative growth rate, r_g , represents the net effects of all physical and biological processes on
272 algal dynamics (Qin and Shen, 2017 and 2019). The solution reads:

$$273 \quad C = C_{ini} \exp\left(\int_{t_{ini}}^{t_{bloom}} r_g dt\right) \quad (3)$$

274 where C_{ini} is the initial density at the “initial time” t_{ini} , and t_{bloom} is the day when the bloom
275 density is first reached (i.e., the beginning of the bloom event). Thus, the time required for bloom
276 initiation relative to the time cells are first observed in the water, t_B , is determined by both initial
277 cell density and relative growth rate which can be computed by:

$$278 \quad t_B = (t_{bloom} - t_{ini}) = \frac{1}{\langle r_g \rangle} \ln(C_{bloom}/C_{ini}) \quad (4)$$

279 where C_{bloom} is the bloom density, and $\langle r_g \rangle$ is the mean relative growth rate over the initiation
280 period. t_{bloom} is then calculated to be:

$$281 \quad t_{bloom} = t_{ini} + \frac{1}{\langle r_g \rangle} \ln(C_{bloom}/C_{ini}) \quad (5)$$

282 In the lower Chesapeake Bay and its tributaries, *M. polykrikoides* is considered to be at bloom
283 density when populations reach 1000 cells ml⁻¹ (Virginia DEQ, 2019), the interannual variability
284 in the beginning of an *M. polykrikoides* bloom event is controlled by initial time, t_{ini} , the initial
285 cell density, C_{ini} , and the relative growth rate of vegetative cells over the initiation period, $\langle r_g \rangle$.
286 Eq. (5) suggests that a higher C_{ini} , an earlier t_{ini} , or a higher $\langle r_g \rangle$ can all lead to an earlier start to
287 a bloom.

288 A variety of environmental factors can potentially change t_{ini} , C_{ini} , and $\langle r_g \rangle$ from year to
289 year and this can contribute to the interannual variability in the start of bloom events, but the
290 relative importance of each factor is different. Cyst germination determines the initial loading of
291 vegetative cells (or the “inoculum”) and therefore, the timing of the first appearance of active
292 cells in the water column, so it contributes to the bloom advent, t_{bloom} , by regulating t_{ini} and
293 C_{ini} . In this model study, the initiation of cell growth is set to begin at the time when vegetative
294 cells are first loaded to the water column from the sediment at a rate of 25000 cells m⁻² d⁻¹
295 ($germ_{ini}$) and this controls C_{ini} . Therefore, because the loading was constant, the contribution of
296 cyst germination to the interannual variability in bloom initiation in Base Scenario is mainly
297 through the variability in the timing of this event, t_{ini} , and can be estimated by comparing the
298 interannual variations in t_{ini} with the variations in the beginning of bloom event. To further
299 investigate the contribution of cyst germination to bloom initiation through C_{ini} , two additional
300 sensitivity tests were conducted in which germination rates, $germ_{ini}$, were increased or

301 decreased by a factor of 10 (Table 3). Presumably if a larger number of cysts can successfully
 302 germinate, a shorter time will be required for bloom initiation.

303 The contribution of each environmental factor to changes in algal biomass through their
 304 impact on relative growth rates $\langle r_g \rangle$ was investigated by examining the depth-integrated algal
 305 biomass over the water column using Eq. (1):

$$306 \quad \frac{\partial B}{\partial t} = (\bar{G} - \bar{R} - \bar{M})B - \bar{F}_B B + germ - encyst \quad (6)$$

307 where $B = \int_0^H C dz$ is the depth-integrated biomass, z is the vertical location, and H is the water
 308 depth. \bar{G} is the vertical mean gross growth rate that accounts for the growth of B, and $\bar{G} =$

309 $\frac{\int_0^H (GC) dz}{B}$, \bar{F}_B is the transport rate accounting for the effect of physical transport processes, which

310 is expressed as:

$$311 \quad \bar{F}_B = \frac{1}{B} \int_0^H \left[u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} + w \frac{\partial C}{\partial z} - \frac{\partial}{\partial x} \left(K \frac{\partial C}{\partial x} \right) - \frac{\partial}{\partial y} \left(K \frac{\partial C}{\partial y} \right) - \frac{\partial}{\partial z} \left(K \frac{\partial C}{\partial z} \right) \right] dz \quad (7)$$

312 \bar{F}_B at the given location describes the horizontal transport in or out of the estuary, a positive \bar{F}_B
 313 suggests that there is net transport out of the estuary that decreases local algal density while a
 314 negative \bar{F}_B corresponds to a net transport in to the estuary that increases local algal density (Qin
 315 and Shen, 2019; 2021). Note that the integration of the vertical migration/swimming term in Eq.

316 (1), $\int_0^H w_c \frac{\partial C}{\partial z} dz$, equals zero. Because the numerical experiments conducted here used a one-

317 time cyst germination event lasting one day to generate an initial loading of vegetative cells (i.e.,
 318 initial condition $germ = germ_{ini}$), it does not explicitly consider additional cell inputs from

319 germination over a longer time period and cell losses due to cyst formation; therefore, both $germ$

320 and $encyst$ are zero after the initial release. Without considering losses from grazing mortality

321 (i.e., $M = 0$), the rate equation for depth-integrated *M. polykrikoides* growth can be obtained by
322 dividing by B on both sides of Eq. (6):

$$323 \quad \bar{r}_g = \bar{G} - \bar{R} - \bar{F}_B \quad (8)$$

324 where $\bar{r}_g = \frac{\partial B}{B \partial t}$ is relative growth rate for the depth-integrated biomass and $\langle \bar{G} \rangle$, $\langle \bar{R} \rangle$, and $\langle \bar{F}_B \rangle$ are
325 the mean values of growth, respiration, and physical transport, respectively, over the time
326 increment examined (i.e., “Present Period”, “Initiation Period”). With the numerical model, the
327 relative contribution of each term in Eq. (8) was examined by comparing their values over each
328 period when *M. polykrikoides* was present and during its initiation period. Particularly, $\langle \bar{F}_B \rangle$ was
329 computed from the balance of the remaining terms. As shown by Eq. (8), for successful bloom
330 initiation, $\langle \bar{F}_B \rangle$ must be less than the net growth rate of *M. polykrikoides*, $\langle \bar{G} \rangle - \langle \bar{R} \rangle$, during the
331 initiation period. Since \bar{G}^p and \bar{G}^h are also computed in the model, the mean phototrophic
332 growth rate $\langle \bar{G}^p \rangle$ and mean heterotrophic growth rate $\langle \bar{G}^h \rangle$ were also computed. $\langle \bar{G}^h \rangle$ was
333 compared to $\langle \bar{G} \rangle$ to examine the importance of mixotrophic growth for initiating and developing
334 *M. polykrikoides* blooms. Additional numerical experiments were conducted to investigate the
335 model sensitivities to fractions of bioavailable particulate organic matter and mixotrophic
336 capability (Table 3). Sensitivity tests were also conducted for evaluating swimming speed in
337 contributing to bloom development.

338 Since the interannual variability in bloom initiation is regulated by that in $\langle \bar{r}_g \rangle$, which
339 terms in Eq. (8) contributed most to the 7-year interannual variability in $\langle \bar{r}_g \rangle$ was evaluated
340 statistically by calculating and comparing the standard deviations of $\langle \bar{r}_g \rangle$, $\langle \bar{G} \rangle$, $\langle \bar{R} \rangle$, and $\langle \bar{F}_B \rangle$
341 during initiation periods.

342 The major contributions of environmental factors to the initiation and development of *M.*
343 *polykrikoides* blooms were also examined using the model. Note that the contribution of each
344 factor to bloom initiation is different from their contributions to the interannual variability in the
345 timing of bloom initiation. A factor may be important in supporting algal growth during bloom
346 initiation without being important in regulating the timing of bloom initiation because there is
347 interannual variability in most environmental factors. For temperature, salinity, light, *DIN*, *DIP*,
348 and bioavailable organic matter, growth-limiting functions that regulate the gross growth rate of
349 *M. polykrikoides* were compared with each other to examine which factor limited algal growth.
350 To examine the contribution of temperature and salinity to the interannual variability in the time
351 when bloom cell densities were reached, we calculated the coefficient of determination (r^2)
352 between the mean of the gross growth rate (G) during each initiation period (7 events over 7
353 years) and the mean of the growth-limiting functions ($f(T)f(Sal)$) for each of the two factors.
354 For the resources (light, inorganic nutrients, and bioavailable organic matter), as shown in
355 Appendix Eqs. (A1) (A2) and (A3), their effects on the growth rate, G, interact with each other.
356 By using a function $f(Res)$ describing the interaction effect of these resources makes $G =$
357 $G_{opt}f(T)f(Sal)f(Res)$, the total contribution of resources to the interannual variability in the
358 beginning of the bloom was examined by comparing r^2 between $f(Res)$ and G. Values of $f(Res)$
359 were directly output by the model. The contribution of each resource to G was weighted by its
360 significance in the total contribution, which was indicated by r^2 between $f(Res)$ and growth-
361 limiting function for each resource. The contribution of each factor to the intra-annual variability
362 in the growth was also examined by computing r^2 between G and the growth-limiting functions
363 for temperature, salinity, and the resource combination on daily timescales. The above analyses

364 were done for both the periods of bloom initiation and the periods when *M. polykrikoides* was
365 present (including both bloom and non-bloom periods).

366 3. Results

367 3.1. Model simulation results

368 Model results agree reasonably well with the observed chl-a concentrations at the five
369 long-term monitoring stations, for which there are monthly observations, and weekly dataflow
370 data for the Lafayette, Elizabeth and lower James Rivers (Fig. 2). The correlation coefficients, r ,
371 ranged from 0.56-0.90 and relative errors, RE, ranged from 0.25-0.36, indicating that the model
372 reasonably simulated the variability in *M. polykrikoides* cell density during each bloom year and
373 the interannual variability in the timing and magnitude of *M. polykrikoides* blooms in the lower
374 James River and its tributaries. When *M. polykrikoides* was not included in the model (i.e., only
375 the two non-HAB species were simulated), the summer *M. polykrikoides* bloom did not occur
376 within the model simulation period (Supplementary Fig. S1). There was good agreement
377 between simulated and observed *M. polykrikoides* cell densities in the Lafayette River under the
378 Base Scenario in 2009 (Fig. 3), considering the large variations among observations. The model
379 results also reproduced the interannual variability in the timing of bloom initiation (Table 4). The
380 bloom occurred as early as late June in 2009 and 2012, but did not develop until late July or even
381 early August in the other 5 study years.

382 There were also some discrepancies between the observations and the model results. In
383 the years when the bloom was first observed in late July or early August, the model shows a
384 second bloom and overestimates algal density (e.g., 2008, 2010, and 2011) while observations do
385 not corroborate this. Observations show that once bloom events were terminated, they generally

386 did not return. This suggests that the model is lacking some factors or mechanisms for bloom
387 termination. Statistics show there is generally higher r and lower RE between the model results
388 and observations if the termination periods are not included, indicating that the model performed
389 better for algal dynamics during initiation periods.

390 3.2. Interannual variability in t_{ini} , $\langle r_g \rangle$, and t_{bloom}

391 The importance of the effect of variance in t_{ini} and $\langle r_g \rangle$ on the interannual variability in
392 the start of the bloom, t_{bloom} , was evaluated using the model. Over the 7 years, t_{ini} varied from
393 April 15th to July 1st with a range of 77 d (Table 4), suggesting that the variations in t_{ini}
394 contributed disproportionately to the timing of bloom initiation. Variations in $\langle r_g \rangle$ during the
395 bloom initiation periods also showed large interannual shifts, and $\langle \bar{r}_g \rangle$ ranged from 0.24 to 1.08
396 d⁻¹ at LFB01 (Table S1). The difference in $\langle r_g \rangle$ suggests that each year *M. polykrikoides*
397 experienced very different environmental conditions during initiation periods, which contributed
398 to the interannual variability in the length of the initiation period, t_B . At LFB01, t_B varied from
399 17 to 69 d over the 7-year study period. The variability in t_{ini} and that in t_B resulted in the large
400 interannual variability in the beginning of the bloom event, t_{bloom} , which varied from June 22 in
401 2012 to July 24 in 2011 with a range of 32 d at Station LFB01 (Table 4).

402 3.3. Standard deviations of $\langle \bar{r}_g \rangle$, $\langle \bar{G} \rangle$, $\langle \bar{R} \rangle$, and $\langle \bar{F}_B \rangle$

403 During initiation periods, at the three stations (LFB01, NYCC, LFA01) in the Lafayette
404 River, the standard deviations for $\langle \bar{r}_g \rangle$ were 0.29 d⁻¹, 0.16 d⁻¹, and 0.10 d⁻¹, respectively, for $\langle \bar{F}_B \rangle$
405 they were 0.34 d⁻¹, 0.18 d⁻¹, and 0.09 d⁻¹, respectively; and for $\langle \bar{G} \rangle$ they were 0.11 d⁻¹, 0.08 d⁻¹,
406 and 0.07 d⁻¹, respectively. The standard deviations in $\langle \bar{F}_B \rangle$ and $\langle \bar{G} \rangle$ were much larger than those

407 for respiration rates, $\langle \bar{R} \rangle$ ($< 0.01 \text{ d}^{-1}$ at the three stations); this demonstrates that flushing and
408 factors affecting growth rates determined the interannual variability in $\langle \bar{r}_g \rangle$.

409 3.4. Contribution of behavioral strategies to bloom

410 The impacts of the three behavioral and life cycle strategies considered here (mixotrophic
411 growth, swimming, and cyst germination) were examined using Base Scenario and sensitivity
412 experiments. Model results in Base Scenario show that the overall contribution of heterotrophy
413 to growth rates of *M. polykrikoides*, \bar{G} , were about 0.18, 0.27, 0.30, 0.30, and 0.34 d^{-1} , at the
414 stations in the Lafayette (LFB01, NYCC, and LFA01), the Elizabeth (LE5.6), and the lower
415 James (LE5.4), respectively (Table 5). \bar{G} during the initiation periods in the model were much
416 higher, with about 0.31, 0.40, 0.42, 0.44, 0.48 d^{-1} , respectively, at the five stations. Heterotrophic
417 growth (osmotrophic + phagotrophic) was found to be as important as phototrophic growth, and
418 \bar{G}^h accounted for about 42-63% of the total growth, \bar{G} , when *M. polykrikoides* was present and
419 about 44-61% during the bloom initiation period over the 7 model years at the five stations.
420 When the heterotrophic growth rate was set to zero, i.e., *M. polykrikoides* growth was strictly
421 autotrophic, results showed that *M. polykrikoides* blooms were reduced in magnitude and their
422 initiation was delayed in 2008-2010 and suppressed entirely in other model years in the Lafayette
423 River. Further, even if they initiated, blooms did not propagate throughout the Elizabeth and the
424 lower James Rivers if the heterotrophic subsidy was not allowed (Fig. S2). This indicates that
425 mixotrophic growth is essential for blooms in this region to initiate, develop and proliferate.
426 Results suggest that both phagotrophy and osmotrophy contributed to the bloom magnitude and
427 duration. The observation-derived b of 0.001 and the calibrated a of 0.01 (see the definition in
428 Appendix and Table 2) suggest that only a very low fraction of living algae and other POM in
429 the water were bioavailable for phagotrophic growth. When there was a higher percentage of

430 bioavailable POM, e.g., $a = 0.1$ (Exp. 1), cell abundances of *M. polykrikoides* were higher than
431 the Base Scenario during the bloom events (Fig. 4A). On the other hand, in simulations where
432 heterotrophic growth of *M. polykrikoides* was only through osmotrophy (Exp. 2) (i.e., $a = b = 0$),
433 *M. polykrikoides* blooms were comparable to Base Scenario, with cell abundances slightly
434 smaller in magnitude, suggesting that osmotrophy is the quantitatively more important than
435 phagotrophy to the development of blooms. In Exp. 1 when there was a higher fraction of
436 bioavailable POM ($a = 0.1$) and in Exp. 2 in which only osmotrophy was allowed ($a = b = 0$), the
437 timing of *M. polykrikoides* achieving bloom concentrations shifted only slightly (by 0-1.3 d)
438 across years (Table 6), except for 2011 at LFA01. In 2011, modeled cell abundance at LFA01
439 first reached bloom densities ($1000 \text{ cells ml}^{-1}$) on Aug. 8 but was very close to the bloom density
440 on July 23 in Base Scenario (Fig. S3B). This shift in timing was due to the higher bioavailable
441 POM in Exp. 1 relative to the Base Scenario, which made the density on July 23 have reached
442 the bloom density and shifted the beginning of the bloom event more than 15 d earlier. This large
443 shift was not observed at LFB01 since cell abundance there was over the bloom density on July
444 24 in both Base Scenario and Exp. 1 (Fig. S3A).

445 When swimming speed was reduced, bloom timing (Table 6) and magnitude (Fig. 4B)
446 changed significantly. As shown above, the large interannual variation in t_{ini} in Base Scenario
447 suggests that the timing of cyst germination contributed largely to the interannual variability in
448 the start of the bloom event. In addition, a 10-fold increase or decrease in the initial loading of
449 vegetative cells, $germ_{ini}$, did not cause a large change in the overall magnitude of blooms after
450 the blooms initiated (Fig. 4C), but changes in cell loading did impact the timing of bloom
451 initiation (Table 6), suggesting the importance of the cyst abundance and the success of cyst
452 germination. However, the magnitude of the shift in bloom initiation varied interannually. For

453 example, with a 10-fold increase in cyst germination the start of the bloom event at LFB01 in
454 2007 advanced by 2.0 d but in 2009 it advanced by 13 d.

455 3.5. Contribution of environmental factors to blooms

456 Because the model assumes that *M. polykrikoides* are not grazed, the main factors
457 contributing to the dynamics of *M. polykrikoides* blooms were primarily through growth and
458 transport. In general, during the period when *M. polykrikoides* was present in the water column
459 the growth-limiting function for temperature, $f(T)$, and for salinity, $f(Sal)$, were about 0.59-0.87
460 and about 0.48-0.61 over the region, respectively (Table 7). The average value of $f(Sal)$ was
461 generally lower than $f(T)$. The average value of growth-limiting function for light, $f(I)$, was
462 about 0.97 during the daytime in the surface layer, suggesting that light did not limit
463 phototrophic growth of *M. polykrikoides*. Both DIP and DIN can be limiting factors for
464 phototrophic growth of phytoplankton in estuaries. Model results suggest that DIN limitation, in
465 general, was often the dominant limiting nutrient at station LFB01 in the upper Lafayette River
466 during intense blooms (Fig. 5), while DIP was the dominant limiting factor near the mouth of the
467 Lafayette (e.g., LFA01) and in the lower Elizabeth and the lower James Rivers. Bioavailable
468 organic matter was less limiting than either DIN or DIP in this region during simulated blooms,
469 especially during the initiation periods, when the function for bioavailable organic matter, f
470 (OM_{12}), had the values over 0.9. $f(OM_{12})$. However, bioavailable organic matter dropped to a
471 lower value during intense blooms (e.g., Figs. 5E and 5F). During those periods, nutrients
472 became severely limiting for both phototrophic and heterotrophic growth, and the gross growth
473 rate, G , was significantly lower than G_{TS} .

474 Among all the factors considered, temperature was the dominant factor driving both the
475 interannual and intra-annual variability in gross growth rates, G , in the region (Table 8). Overall,

476 $f(T)$ explained 67-75% of the interannual variability and 40-42% of the daily variability in G
477 during periods when *M. polykrikoides* was present in the water column at the Lafayette River
478 stations (LFB01, NYCC, and LFA01); and explained 61-95% of the interannual variability and
479 82-94% of the daily variability in G during bloom initiation. Temperature regulates the
480 interannual variability through both phototrophic and heterotrophic growths. As shown in
481 Appendix Eqs. (A1) and (A2), both growth rates are a function of temperature. For example, at
482 Station LFB01, the correlation between $f(T)$ and G is 0.67 for interannual variability for the
483 present period, and the corresponding correlations between $f(T)$ and G^p and $f(T)$ and G^h are
484 0.67 and 0.58, respectively. The correlation between $f(T)$ and G is 0.95 for interannual
485 variability for the initiation period, and the corresponding correlations between $f(T)$ and G^p and
486 $f(T)$ and G^h are 0.94 and 0.72, respectively. Other factors (light and nutrients), indicated by the
487 large values of $f(\text{Res})$, contributed less than temperature. In the lower Elizabeth River (LE5.6)
488 and the lower James River (LE5.4), resources contributed less than temperature to the
489 interannual variability in G but was as important as temperature to the intra-annual variabilities
490 in G.

491 In addition to local factors affecting their growth, physical transport played a critical role
492 in controlling *M. polykrikoides* cell density during blooms. The effects of transport were
493 examined by including a function for transport rates, \overline{F}_B , which had mean values of up to 0.10 d^{-1}
494 during periods when *M. polykrikoides* was present in the water column and -0.15 to 0.14 d^{-1}
495 during the bloom initiation periods at the five stations (Table 5). These values are not trivial
496 compared to the mean gross growth rates, \overline{G} . The absolute values of mean $\overline{F}_B/\overline{G}$ were about 6-29%
497 during the periods when *M. polykrikoides* was present and 5-48% during bloom initiation. In
498 different years, \overline{F}_B was both positive and negative (Table S1), demonstrating that cell

499 abundances were controlled both by net “transport-in” and “transport-out” processes. During the
500 initiation periods, Stations LFB01 and NYCC show overall net “transport in” (Table 5). Over
501 multiple years these two stations more frequently “transported-in” (negative $\overline{F_B}$) cells than they
502 “transported-out” (positive $\overline{F_B}$) cells (Table S1) (i.e., a net transport of cells into the area around
503 the stations). All the other three stations had positive values of $\overline{F_B}$ for most years, indicating cells
504 there experienced “transport-out” processes more frequently.

505 4. Discussion

506 4.1. *The importance of mixotrophy*

507 Mixotrophy has now been shown to be common among dinoflagellates (Burkholder et al.,
508 2008; Joeng et al., 2015; Stoecker et al., 2017; Flynn et al., 2018), including the HAB species *M.*
509 *polykrikoides* (Joeng et al., 2004; Mulholland et al., 2009), and that there are different types of
510 mixotrophy among algal species (Jones, 1997; Stoecker, 1998; Mitra et al., 2016). For *M.*
511 *polykrikoides*, it is still unclear whether phototrophic or heterotrophic growth is preferred. In the
512 current model, *M. polykrikoides* is assumed to favor phototrophic growth, and heterotrophic
513 growth is performed to complement the total growth (Appendix Eq. A4). This parameterization
514 leads to a minimum amount of nutrient acquisition from heterotrophy. We also tested in the
515 model *M. polykrikoides* performing phototrophic and heterotrophic growth simultaneously, i.e.,
516 no preference on the growth mode (Appendix Eq. A5) and the model results showed that the
517 contribution of heterotrophic growth was about 7-10% higher than Base Scenario when
518 phototrophic growth was favored over the entire period when *M. polykrikoides* is present in the
519 water column and about 9-14% higher for the bloom initiation periods (Data not shown). This

520 indicates that the ability to employ heterotrophy to augment autotrophy is an important adaptive
521 strategy that promotes blooms of this organism.

522 Our model results show that heterotrophy contributes significantly to the growth of *M.*
523 *polykrikoides* in the lower Chesapeake Bay region. This is supported by model results showing *f*
524 (OM_{12}) above 0.70 in surface water during blooms (Table 7). During bloom initiation,
525 bioavailable organic matter was even more abundant with *f* (OM_{12}) found to be over 0.90.
526 Correspondingly, the model results of $\langle \bar{G}^h \rangle / \langle \bar{G} \rangle$ suggest that heterotrophic growth contributed
527 about half to the total growth rate of *M. polykrikoides* (Table 5). Note that uncertainties exist in
528 the model results, as the values of many parameters used in the model (e.g., gross growth rates,
529 swimming speed/vertical migration) are derived from laboratory measurements (Table 2) using
530 cultured isolates from other parts of the world where environmental conditions differ from those
531 observed in the lower Chesapeake Bay region. For example, across much of the globe, *M.*
532 *polykrikoides* blooms at higher salinities and lower temperatures than those found in the
533 Chesapeake Bay (Kudela and Gobler, 2012; Mulholland et al., 2018). Nevertheless, the model
534 results are reasonable and consistent with field observations where dissolved inorganic carbon
535 accounted for only a small fraction of the total carbon uptake during both bloom and non-bloom
536 periods in the Lafayette and Elizabeth Rivers (Mulholland et al. 2009, 2018). According to the
537 model, uptake of DOM via osmotrophy can support the heterotrophic growth of *M. polykrikoides*
538 and result in high cell densities blooms. The model calibration shows that bioavailable POM
539 only accounted for a very low fraction of the POM in the water column. If the fraction of
540 bioavailable POM were higher, results from Exp. 1 suggest that bloom cell densities would be
541 higher. But *M. polykrikoides* prey, e.g., cryptophytes, were not abundant during blooms (Morse
542 et al., 2013).

543 It should be noted that among the environmental factors regulating growth rate, the
544 uncertainty in heterotrophic growth may come from estimated nutrient concentrations. Overall
545 this has a limited effect that heterotrophy has on the total mixotrophic growth and the
546 contribution to a relatively high growth rate. Although the swimming behavior in the model may
547 also alter the heterotrophic growth due to changes in nutrient and flushing conditions at different
548 vertical locations, the overall ratio of dissolved inorganic nutrients to bioavailable organic
549 nutrients does not vary largely in the study region. Therefore, the uncertainty caused by the
550 choice of swimming behavior or speed will not change the important role of mixotrophy. This is
551 demonstrated in the two swimming experiments. $\langle \bar{G}^h \rangle / \langle \bar{G} \rangle$ at Station LFB01 are 0.56 and 0.61,
552 respectively, for the present period in Exp. 4 (reduced swimming speed) and Exp. 5 (no
553 swimming). These values are not largely different from the Base Scenario, 0.51 (Table 5). The
554 other stations also show similar results. This suggests that mixotrophy consistently plays a
555 central role in *M. polykrikoides* blooms with varying swimming speed.

556 4.2. *Dominant Factors controlling the interannual variability in the start of bloom* 557 *events*

558 Many factors contribute to bloom initiation (Morse et al., 2013), and model results and
559 observations suggest that the length of time required for blooms to initiate varies substantially
560 from year to year. In the model framework, the interannual variability in time *M. polykrikoides*
561 cells reach bloom density, t_{bloom} , is affected by cyst germination and by variations in
562 environmental factors that can regulate growth and by variations in physical transport.

563 4.2.1. Cyst germination

564 *Margalefidinium polykrikoides* produce resting cysts and cyst production and
565 germination are thought to contribute the near-annual recurrence of blooms and their initiation in

566 estuaries and coasts (Kudela and Gobler, 2012; Tang and Gobler, 2012). In the lower James
567 River and its tributaries, model results suggest that the timing and relative success of cyst
568 germination may contribute substantially to the interannual variability in the start of bloom
569 events, t_{bloom} , by determining t_{ini} and C_{ini} in Eq. (5). It is worth noting that the cyst
570 germination process for *M. polykrikoides* may also be temperature dependent, and this may
571 affect the interannual variability in t_{ini} . Tang and Gobbler (2012) showed that cyst germination
572 occurred over a shorter time period in the lab when it was cultured at a higher temperature.
573 Temperature may also impact on t_{ini} through other mechanisms such as the cyst chilling concept
574 (Fischer et al., 2018). The model does not consider this or the loss of vegetative cells due to
575 resting cyst formation during bloom initiation periods because cyst formation is to be minor until
576 populations reach high cell densities in late exponential or stationary phase of growth (Garcés et
577 al., 2004; Tang and Gobler, 2012; Brosnahan et al., 2017).

578 4.2.2. Temperature and salinity

579 As highlighted in Appendix Eqs. (A1) and (A2), temperature and salinity were two
580 factors regulating phototrophic and heterotrophic growth rates in the model. Previous studies
581 have shown that temperature plays an important role in the timing of blooms of *M. polykrikoides*
582 in the lower James River and its tributaries (Mulholland et al., 2009, 2018) as well as in other
583 systems (Kudela and Gobler, 2012). Culture studies using a Long Island isolate suggest that *M.*
584 *polykrikoides* grows optimally at temperatures ranging from 21-26 °C and salinities between 30
585 and 36 although Korean ribotypes grow at temperatures ranging from 15-30 °C and salinities
586 between 20-36 (Kim et al., 2004). Salinities are characteristically at the lower end and
587 temperatures at the higher end of these ranges in the lower James River estuary and the Lafayette
588 River (Morse et al., 2011, 2013, 2014; Mulholland et al., 2009, 2018). Model results show that

589 temperature is not a severe limiting factor during the initiation period in the Lafayette River but
590 it is the most important factor regulating both the intra-annual and interannual variabilities in
591 gross growth rates, G . The generally lower values of $f(Sal)$ than $f(T)$ suggest that the growth of
592 *M. polykrikoides* is more limited by salinity than temperature; but the role of salinity in driving
593 the interannual variability in the initiation of blooms events is far less important compared to
594 temperature, because the salinity typically varies less across years than the temperature in the
595 region.

596 4.2.3. Light, dissolved inorganic nutrients, and bioavailable organic matter

597 The gross growth rate, G , was not limited by light although light attenuation is generally
598 rapid during summer in this region (1% light level ranges from 2-3 m in depth; Echevarria et al.
599 unpublished data). The pattern of vertical migration of *M. polykrikoides*, however, suggests that
600 cells stay near the surface during daytime (Morse et al., 2013; Echevarria et al. unpublished data)
601 where they receive abundant light for growth, and migrate to the bottom at night where they can
602 evade predation or access nutrients present in bottom waters. This is supported by the model
603 result showing that $f(I)$ was over 0.97 at the three Lafayette River Stations.

604 In contrast, model simulations showed that concentrations of DIN and DIP limited
605 photoautotrophic growth of *M. polykrikoides* during the bloom initiation period. Model
606 simulations showed that the concentrations of DIN and DIP were low relative to half-saturation
607 constants for DIN (2-3 μM) and DIP (0.57 μM) during blooms (Gobler et al., 2012; Kim et al.,
608 2001). Based on the model results and observed DIN and DIP concentrations in the James and
609 Lafayette Rivers (Filippino et al., 2017; Morse et al., 2011, 2013, 2014; Mulholland et al., 2009,
610 2018), the supply of DIN may limit photoautotrophic growth by *M. polykrikoides* in the most
611 areas of the Lafayette during bloom initiation periods. Indeed, the model results show the

612 average value of growth-limiting function for DIN, $f(\text{DIN})$, was lower than that for DIP, $f(\text{DIP})$,
613 at LFB01 (Table 7). However, the model suggests that DIP is more limiting than DIN at LFA01,
614 a location near the mouth of the estuary where the loading of nutrients is largely influenced by
615 the water exchange between the mainstem James and the tributaries. The half-saturation
616 coefficient, P_k , used for the model was from a culture experiment reported in Kim et al. (2001)
617 for the Korean *M. polykrikoides* ribotype, and if the P_k for the local ribotype was lower,
618 phosphate limitation would be alleviated. In addition, bioavailable organic matter, which could
619 include nitrogen and phosphorus, was relatively abundant and contributed substantially to the
620 initiation process by supporting high mixotrophic growth rates. Analyses of model results show
621 that although these resources (light and nutrients) contributed greatly to the magnitude of G
622 during bloom initiation, their total contribution to the interannual variability in G or t_{bloom} was
623 not as important as temperature, suggested by the lower r^2 between G and the growth-limiting
624 functions for resources, $f(\text{Res})$ (Table 8). In addition, the above analysis of resource
625 contributions indicates that mixotrophy is not as essential as temperature in regulating the
626 interannual variability of G or t_{bloom} . This is because heterotrophic growth is determined by
627 bioavailable organic matter, which is relatively abundant and $f(\text{OM}_{12})$ varies little during
628 initiation periods from year to year (Table S2).

629 4.2.4. Flushing by physical transport

630 Successful bloom initiation requires a positive mean relative growth rate (Qin and Shen,
631 2019), and flushing regulates cell transport and residence time and determines whether cells can
632 accumulate and proliferate or whether they are “washed out” (Anderson D.M. and Stolzenbach,
633 1985; Ralston et al., 2015; Filippino et al., 2017; Philips et al., 2020). A large transport away
634 from initiation sites can delay initiation of *M. polykrikoides* blooms by reducing biomass

635 accumulation (Qin and Shen, 2019). At high flow rates, *M. polykrikoides* are transported out of
636 the estuary at greater rates than they can reproduce thereby preventing the accumulation of cell
637 biomass (Morse et al., 2013; Filippino et al., 2017). The large variability in transport rates during
638 the period when bloom initiation is favored suggests that transport processes can significantly
639 contribute to the interannual variability in the length of the initiation period and the time at which
640 bloom cell densities are achieved. The standard deviations in $\langle \overline{F_B} \rangle$ during initiation periods are
641 comparable to or even larger than those for gross growth rates, $\langle \overline{G} \rangle$. Consequently, transport
642 processes are an important regulator of interannual variability in the timing of the start of bloom
643 events, t_{bloom} .

644 As shown by the expression of F_B (Eq. 7), the flushing effects are determined by external
645 physical forcings through the hydrodynamic field and spatial gradients of algal density (Qin and
646 Shen, 2021). Since a successful initiation of *M. polykrikoides* bloom requires at least several
647 weeks, which is regulated mainly by the estuarine circulation and spring-neap tidal cycles. The
648 major physical forcings driving estuarine circulation include freshwater discharge, wind, and tide.
649 In the Lafayette River, the freshwater discharge is mainly caused by precipitation. Large runoff
650 induced by heavy precipitation or even storms can greatly increase flushing (e.g., Filippino et al.,
651 2017). Wind can alter horizontal transport in this area. Hong et al. (2018) showed that the
652 southerly wind increases the exchange between the lower James River and Elizabeth River and
653 enhances the transport of dissolved substances to the James River, whilst the northerly wind
654 reduces the exchange and inhibits the transport. On the subtidal timescale, spring tide may also
655 increase the exchange flow at the mouth of the Lafayette River and lead to an enhanced
656 transport-out effect.

657 The spatial gradients of algal density are mainly due to the spatial variability in the local
658 biological growth of *M. polykrikoides* under environmental conditions (temperature, salinity,
659 nutrients, and others). For a location, $F_B > 0$ if the incoming water has a lower density, and
660 $F_B < 0$ if the incoming water has a higher density (Qin and Shen, 2019; 2021).

661 4.2.5. Vertical migration and stratification

662 Vertical migration, thought to be regulated by environmental conditions such as light
663 (Smayda, 2002), allows algal species to change their vertical position in the water column and is
664 common among dinoflagellates including *M. polykrikoides* (Sohn et al., 2011; Lim et al., 2014;
665 Jeong et al. 2015). Vertical migration can be beneficial for algae in many ways, including
666 facilitating their acquisition of nutrient resources and avoiding grazers (Jeong et al., 2015).
667 Migration of cells to the surface during daytime helps *M. polykrikoides* acquire light and
668 alleviate light limitation during the day (Morse et al., 2013); correspondingly, model results
669 show that the daily-averaged growth-limiting function for light, $f(I)$, was above 0.97.

670 *Margalefidinium polykrikoides* is the fastest phototrophic dinoflagellate with the
671 maximum swimming speed of about $1449 \mu\text{m s}^{-1}$ (Jeong et al., 1999; Jeong et al., 2015), so it
672 may only take them a few hours to migrate vertically from the bottom to the surface in the
673 shallow tidal system. Due to the superior swimming ability of *M. polykrikoides* and the shallow
674 depth of this tidal system, the impact of stratification on the settling of cells is also likely to be
675 unimportant.

676 Another effect of vertical migration on blooms is through its interaction with physical
677 transport (Anderson D.M. and Stolzenbach, 1985). Ralston et al. (2015) showed that different
678 swimming behaviors of mobile algae can alter the hydrodynamic forcing they encounter and
679 affect the retention of cells. Swimming speed can affect the vertical position of cells in the water

680 column and therefore the hydrodynamic forces and environmental conditions encountered. This
681 affects both the growing environments and flushing conditions for *M. polykrikoides*. Thus, the
682 nonlinear interaction between *M. polykrikoides* swimming speed, vertical position in the water
683 column, and the hydrodynamics can impact the algal growth and accumulation. The sensitivity
684 of the model to the swimming speed (Table 6 and Fig. 4B) suggests that it plays an important
685 role in regulating bloom initiation; different swimming speeds led to significantly different
686 trajectories for *M. polykrikoides* blooms in the model. Because a constant swimming speed was
687 applied over the years, swimming speed did not contribute substantially to the interannual
688 variability in the initiation of blooms in the current model framework. The variability in
689 swimming speeds in natural systems warrant further examination.

690 While many factors can contribute to the initiation of *M. polykrikoides* bloom events in
691 the Lafayette River, cyst germination and two environmental factors (temperature and estuarine
692 transport processes/flushing) are key factors contributing to the interannual variability in t_{bloom} .
693 The other environmental factors (salinity, light, dissolved inorganic nutrients) and nutrient
694 acquisition strategies (mixotrophy and swimming) may be less important in affecting the timing
695 of the start of the bloom, t_{bloom} , due to their small interannual variations, however they can
696 affect the length of bloom initiation.

697 4.3. *Model limitation and future work*

698 The model developed performs reasonably well in simulating the initiation of *M.*
699 *polykrikoides* blooms in the Lafayette River, and it was useful for improving our understanding
700 of how metabolic and behavioral strategies employed by *M. polykrikoides* contribute to bloom
701 initiation and development. However, the results of simulations show some discrepancies with
702 field observations. The inconsistencies between model results and observational data potentially

703 arose from a variety of sources. First, the model resolution (several hundred meters) may not be
704 fine enough to properly simulate the local patchiness in chl-a concentrations in the small
705 tributary. Because the model focuses on *M. polykrikoides* blooms originating locally within the
706 James River and its tributaries, bloom development outside of the James River was not
707 considered. Second, uncertainties exist in the applicability of values of physiological parameters
708 used as model input. Many parameterizations are from laboratory measurements (e.g., gross
709 growth rate, half-saturation for nutrients, the constant C:Chl, swimming speed, and the
710 conversion from density units to carbon units) using cultured isolates from Korea or Long Island,
711 NY where environmental, and thus culture, conditions are dissimilar to those found where *M.*
712 *polykrikoides* blooms in the lower Chesapeake Bay watershed. Third, the current structure of the
713 model may introduce biases in the simulation, both for *M. polykrikoides* and for other algal
714 assemblages. For example, only the dynamics of *M. polykrikoides* is modeled explicitly as a
715 water-quality state variable, other algal species are lumped into two assemblages simulated by
716 two state variables. Field observations conducted by Morse et al. (2013) indicate that the
717 dinoflagellates *Gymnodinium uncatenum*, *Scrippsiella trochoidea*, and *Akashiwo sanguinea* were
718 present in high abundance during the *M. polykrikoides* bloom initiation period in 2009. There are
719 commonly blooms of multiple dinoflagellate species during summer in the lower Chesapeake
720 Bay region (Morse et al., 2014, Mulholland et al., 2018). Different species have different
721 tolerances and physiological requirements, and these may not be well represented using the
722 method of aggregate models. Finally, the mechanisms responsible for the termination of *M.*
723 *polykrikoides* blooms are not fully understood, and the current model uses an artificial algorithm
724 to make the bloom collapse at a time consistent with field observations. As shown in Fig. 2, the
725 inability to simulate bloom termination accurately results in overestimates of algal cell density

726 during the late stages of blooms in some years. One possible mechanism whereby blooms
727 terminate is through the loss of vegetative cells by the formation of resting cysts. Some studies
728 have shown that after a bloom reaches a certain threshold, cyst-forming species may rapidly
729 convert to sexual stages and undergo mass gametogenesis events (e.g., Brosnahan et al., 2017
730 and 2020). This could result in the production of resting cysts and may cause a complete
731 termination of the bloom even if the environmental conditions still favor algal growth.
732 Alternatively, storms and frontal systems have been implicated in the rapid termination of *M.*
733 *polykrikoides* blooms (Filippino et al., 2017).

734 The current model does not simulate the complete life cycle of *M. polykrikoides*. The
735 contribution of cyst germination and the subsequent release and loading of vegetative cells,
736 $germ_{ini}$, into the water column is assumed to be completed within one day, and the release date in
737 each year is based on the model calibration. The real "initial time" may deviate from the
738 calibrated t_{ini} in the model, and the initial loading can also be different from the given $germ_{ini}$.
739 Because of the large tidal excursion that mixes algae within a few tidal cycles, the calibration is
740 to find a t_{ini} so that the modeled algal cell density with the given $germ_{ini}$ is close to the available
741 observations within a few tidal cycles. In natural systems, it is more likely that cyst germination
742 occurs over many days/weeks and the timing, varies among years due to differences in
743 environmental factors such as bottom water temperature, oxygen, and cyst resuspension (e.g.,
744 Kremp and Anderson, 2000; Anderson et al., 2005; Anderson and Rengefors, 2006; McGill et al.,
745 in revision). We currently lack a comprehensive understanding of cyst germination in nature and
746 this may require a comprehensive examination of environmental factors regulating germination.
747 Although cyst distributions in sediments may regulate the initial spatial loading of vegetative
748 cells, in the model the loading is the same over the entire area of the lower James and its

749 tributaries. Despite this, blooms still appeared to initiate in the Lafayette River because of how
750 physical transport processes redistribute the released cells within a few tidal cycles in the study
751 system with a relatively small area (Morse et al., 2013; Qin and Shen, 2019). The lack of
752 information on cyst distributions, germination rates, and the interaction between water residence
753 time and population development all hamper our ability to predict bloom initiation with certainty.

754 5. Conclusions

755 A numerical HAB module for *M. polykrikoides* bloom was developed, which includes
756 three behavioral and life cycle strategies (mixotrophic growth, swimming behavior, and cyst
757 germination). The HAB module was successfully incorporated into a 3D physical-
758 biogeochemical numerical model. The model results show that behavioral and life cycle
759 strategies contribute significantly to bloom development and dynamics in the lower James River
760 and its tributaries (the Elizabeth and Lafayette Rivers). Both during the initiation period and in
761 later stages, blooms are fueled by uptake of organic matter the heterotrophic growth rate is
762 higher than the phototrophic growth rate. The resultant mixotrophic growth (phototrophic +
763 heterotrophic) counterbalances the flushing and other unsuitable environmental conditions and
764 ensures that *M. polykrikoides* can accumulate to bloom densities and achieve high growth rates.
765 Swimming speed played a large role in *M. polykrikoides* bloom formation, altering the timing
766 and magnitude of blooms. Model results also showed that the interannual variability in the
767 timing of bloom initiation in the Lafayette River is regulated primarily by temperature, physical
768 transport processes, and the process of cyst germination, while other environmental factors and
769 behavioral strategies were less important.

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779 Appendix. HAB module development

780 *Gross growth rate*

781 *Margalefidinium polykrikoides* is considered a constitutive mixotroph (Mitra et al., 2016),
782 so its mixotrophic gross growth rate, G , can be contributed by both phototrophic growth and
783 heterotrophic growth. In this module, the components of the gross growth rate from each growth
784 mode (G^p for phototrophic and G^h for heterotrophic) are separately formulated and the
785 mixotrophic gross growth rate is calculated based on the two components. Among limiting
786 factors for *M. polykrikoides* growth, temperature, salinity, light irradiance, and nutrients were
787 included in the model. The current model does not explicitly simulate allelopathy effects of *M.*
788 *polykrikoides* on co-occurring algae, bacteria, and grazers (Tang and Gobler, 2010); or the effect
789 of Vitamin B, a possible limiting factor under natural conditions as suggested in the literature
790 (Tang et al., 2010; Koch et al., 2014).

791 Photoautotrophic growth

792 The gross growth rate for phototrophic growth is expressed as a function of temperature,
793 salinity, light irradiance, and dissolved nutrient concentrations:

794
$$G_o^p = G_{opt}^p f(T) f(Sal) \min[f(I), f(DIN), f(DIP)] \quad (A1)$$

795 Where G_o^p denotes G^p of *M. polykrikoides* if the growth is only through phototrophy, which can
796 be different from the finalized G^p in the model. G_{opt}^p is the phototrophic gross growth rate at the
797 optimal condition, $f(T)$, $f(Sal)$, $f(I)$, $f(DIN)$, $f(DIP)$ are the growth-limiting functions for
798 temperature (T), salinity (Sal), irradiance (I), dissolved inorganic nitrogen (DIN), and
799 dissolved inorganic phosphate (DIP), respectively, and their expressions are listed in Table 1.
800 The photosynthesis-irradiance relationship for *M. polykrikoides* suggests that the half saturation

801 constant for light is about $30 \mu\text{E m}^{-2} \text{s}^{-1}$ and photoinhibition does not occur at photon fluxes of
802 less than $300 \mu\text{E m}^{-2} \text{s}^{-1}$ (Kim et al., 2004; Oh et al., 2006). The Monod type equation was
803 adopted for both nutrients and light limitations.

804 Heterotrophic growth

805 *Margalefidinium polykrikoides* can take up organic matter (OM) to maintain a high
806 heterotrophic growth rate (Jeong et al., 2004), and the sources include DOM, a fraction of POM
807 and organisms with size smaller than $12 \mu\text{m}$, such as cryptophyte (Jeong et al., 2004) and
808 bacteria (Seong et al., 2006). Some studies have shown that the heterotrophic growth can be
809 affected by environmental conditions such as temperature, salinity, and light (e.g., Skovgaard,
810 1996; Hansen and Nielsen, 1997; Berge et al., 2008; Jeong et al., 2018; Lim et al., 2019; Ok et
811 al., 2019; You et al., 2020). Here, the heterotrophy is assumed to be a function of temperature
812 and salinity, as these two factors may regulate the activity of enzymes required for processes
813 involving heterotrophic growth. In this current model, because it is still unclear how light
814 influences the heterotrophic growth of *M. polykrikoides*, we did not consider the possible effect
815 of light and assumed heterotrophy can also occur in the dark. Nevertheless, the induced
816 uncertainty is minimized by using an optimal heterotrophic growth rate G_{opt}^h lower than G_{opt}^p to
817 make the daily-averaged value of G_{opt}^h equal the measured value in the laboratory (Table 2).

818 Thus, the formulation for G^h is

$$819 \quad G_o^h = G_{opt}^h f(T) f(Sal) f(OM_{12}), \quad (\text{A2})$$

820 where G_o^h denotes G^h of *M. polykrikoides* if the growth is only through heterotrophy, which can
821 be different from the finalized G^h in the model. G_{opt}^h is the heterotrophic gross growth rate at the
822 optimal condition, $f(T)$ and $f(Sal)$ are assumed to be the same for phototrophic gross growth

823 rate G_o^p in Eq. (A1), and the Monod type equation was adapted for $f(OM_{12})$ following the
 824 culture experiment in Jeong et al. (2004). *M. polykrikoides* can engulf particulate organic matter
 825 (POM) via phagotrophy and take up dissolved organic matter (DOM) via osmotrophy. In the
 826 numerical model, a fraction ($< 12 \mu m$) of the other two groups of algae besides *M. polykrikoides*
 827 and other POM contributes to the phagotrophic growth, while DOM contributes to the
 828 osmotrophic growth. Thus, the available organic matter, OM_{12} , is provided by the two groups of
 829 simulated algae, $\sum_i b_i C_i$, and also by the other organic matter (including both particulate and
 830 dissolved), OM_{dead} ; $OM_{12} = \sum_i b_i C_i + OM_{dead}$, where b is the fraction of organisms smaller
 831 than $12 \mu m$, with $i = 2$ or 3 indicating the index of algae group, and

$$832 \quad OM_{dead} = \min \left\{ \begin{array}{l} DOC + a_{1C}RPOC + a_{2C}LPOC, \\ (DON + a_{1N}RPON + a_{2N}LPON)/ANC, \\ (DOP + a_{1P}RPOP + a_{2P}LPOP)/APC \end{array} \right\},$$

833 where ANC and APC are nitrogen to carbon ratio and phosphate to carbon ratio, respectively.
 834 Correspondingly, the uptake of organic matter corresponding to mixotrophic growth is $G^h C$, and
 835 it contributes to kinetic equations for the other two simulated phytoplankton species, dissolved
 836 organic carbon (DOC), refractory particulate organic carbon (RPOC), labile particulate organic
 837 carbon (LPOC), dissolved organic nitrogen (DON), refractory particulate organic nitrogen
 838 (RPON), labile particulate organic nitrogen (LPON), dissolved organic phosphate (DOP),
 839 refractory particulate organic phosphate (RPOP), and labile particulate organic phosphate
 840 (LPOP), while coefficient a denotes the fraction of POM besides prey algae that is smaller than
 841 $12 \mu m$, and a_{1C} , a_{2C} , a_{1N} , a_{2N} , a_{1P} , and a_{2P} are the fraction for each component, respectively.
 842 Note that this model does not simulate bacteria explicitly, and bacteria is implicitly included in
 843 POM besides prey algae.

844 In the model, the contribution (recycle) to the nutrient pool is calculated by adding a sink
 845 term ($-G^h C\chi$) for each kinetic equation, where χ denotes the fractions of each component
 846 resembling OM_{12} , respectively. Specifically, the corresponding sink term for the dynamics of the
 847 other two phytoplankton species is expressed as:

$$\text{Phytoplankton } i: \chi_i = \frac{b_i C_i}{OM_{12}}, i = 2 \text{ or } 3$$

848 For carbon cycle:

$$\text{DOC: } \chi_{1C} = \frac{OM_{dead}}{OM_{12}} \frac{DOC}{DOC + a_{1C}RPOC + a_{2C}LPOC}$$

$$\text{RPOC: } \chi_{2C} = \frac{OM_{dead}}{OM_{12}} \frac{a_{1C}RPOC}{DOC + a_{1C}RPOC + a_{2C}LPOC}$$

$$\text{LPOC: } \chi_{3C} = \frac{OM_{dead}}{OM_{12}} \frac{a_{2C}LPOC}{DOC + a_{1C}RPOC + a_{2C}LPOC}$$

849 nitrogen cycle:

$$\text{DON: } \chi_{1N} = \frac{OM_{dead}}{OM_{12}} \frac{DON}{DON + a_{1N}RPON + a_{2N}LPON} \text{ANC}$$

$$\text{RPON: } \chi_{2N} = \frac{OM_{dead}}{OM_{12}} \frac{a_{1N}RPON}{DON + a_{1N}RPON + a_{2N}LPON} \text{ANC}$$

$$\text{LPON: } \chi_{3N} = \frac{OM_{dead}}{OM_{12}} \frac{a_{2N}LPON}{DON + a_{1N}RPON + a_{2N}LPON} \text{ANC}$$

850 and phosphate cycle:

$$\text{DOP: } \chi_{1P} = \frac{OM_{dead}}{OM_{12}} \frac{DOP}{DOP + a_{1P}RPOP + a_{2P}LPOP} \text{APC}$$

$$RPOP: \chi_{2P} = \frac{OM_{dead}}{OM_{12}} \frac{a_{1P}RPOP}{DOP + a_{1P}RPOP + a_{2P}LPOP} APC$$

$$LPOP: \chi_{3P} = \frac{OM_{dead}}{OM_{12}} \frac{a_{2P}LPOP}{DOP + a_{1P}RPOP + a_{2P}LPOP} APC$$

851 Mixotrophic growth (photoautotrophic + heterotrophic growths)

852 Without considering interactions between phototrophic growth and heterotrophic growth,
 853 the gross growth rate for mixotrophic growth can be expressed as a combination of phototrophic
 854 growth and heterotrophic growth ($G_o^p + G_o^h$). It is apparent that the mixotrophic rate, G, equals
 855 the heterotrophic rate, G_o^h , during the nighttime. During the daytime, however, G cannot exceed
 856 the maximum growth rate that *M. polykrikoides* can reach under the given environmental
 857 condition (Ghyoot et al., 2017a), which at a certain temperature and salinity is $G_{opt}^p f(T) f(Sal)$.

858 Thus, G has the formula:

$$\begin{aligned} 859 \quad G &= \min[G_o^p + G_o^h, G_{opt}^p f(T) f(Sal)] \quad (Daytime) \\ G &= G_o^h \quad (Nighttime) \end{aligned} \quad (A3)$$

860 During the nighttime, only heterotrophic growth exists, and the finalized G^h resulted in the
 861 model equals G_o^h . During the daytime, two options of computing the finalized G^p and the
 862 finalized G^h are included in the module for the case $(G_o^p + G_o^h) > G_{opt}^p f(T) f(Sal)$, based on the
 863 preference of which growth mode this algal species uses primarily. If phototrophy is favored and
 864 the heterotrophy only complements the total growth, the finalized G^p and the finalized G^h equal:

$$\begin{aligned} 865 \quad G^p &= G_o^p \quad (Daytime) \\ G^h &= [G_{opt}^p f(T) f(Sal) - G_o^p] \quad (Daytime) \\ G^h &= G_o^h \quad (Nighttime) \end{aligned} \quad (A4)$$

866 If there is no preference of using the growth modes, then the finalized G^p and the finalized G^h
867 are calculated, respectively:

$$\begin{aligned} G^p &= G_{opt}^p f(T) f(Sal) \cdot G_o^p / (G_o^p + G_o^h) \quad (\text{Daytime}) \\ G^h &= G_{opt}^p f(T) f(Sal) \cdot G_o^h / (G_o^p + G_o^h) \quad (\text{Daytime}) \\ G^h &= G_o^h \quad (\text{Nighttime}) \end{aligned} \quad (\text{A5})$$

869 Currently in the module, favoring phototrophy is defaulted for *M. polykrikoides* growth.

870 In addition, for the convenience, the mixotrophic growth rate, G , at any time is simply
871 notated in the study as:

$$G = G_{opt} f(T) f(Sal) f(Res) \quad (\text{A6})$$

873 where $f(Res)$ denotes the total contribution of resource species (light, inorganic nutrients, and
874 bioavailable organic matter) to G . Clearly, G_{opt} equals G_{opt}^p during the daytime and G_{opt}^h during
875 the nighttime. The notation $G_{TS} = G_{opt} f(T) f(Sal)$ was also used, which describes the potential
876 highest gross growth rate limited by temperature and salinity (i.e., resources are not limited).

877 *Carbon to chl-a ratio*

878 For *M. polykrikoides*, Noh et al. (2018) reported that the chl-a content of the cultured
879 strain is 30 pg chl-a cell⁻¹, i.e., 30 μg chl-a l⁻¹ per 1000 cells ml⁻¹. In the numerical model, a
880 constant carbon to chl-a ratio (C:Chl) was used. The chl-a content is assumed to be 30 pg chl-a
881 cell⁻¹ that was obtained from a laboratory measurement (Noh et al., 2018), and the corresponding
882 C:Chl is 60.6 g C / g chl-a.

883 *Loss terms*

884 The sink of *M. polykrikoides* biomass may include the respiration/excretion, grazing,
885 degradation by bacteria (e.g., Park et al., 2015), and resting cysts germination.

886 In the model, the basic metabolism (respiration/excretion) is a function of temperature.
887 The respiratory loss due to photosynthesis is an additional metabolism to respiration/excretion,
888 and the ratio to phototrophic growth rate, f^P , is estimated from the curve between specific
889 growth rate and light irradiance. The degradation by bacteria is not explicitly considered, which
890 is implicitly included in the metabolism in the model. The loss to grazers is assumed to be
891 suppressed for simplicity. According to literature, the harmful effects of *M. polykrikoides* to
892 organisms become significant when their density reaches a threshold level, e.g., 330 cells ml⁻¹
893 (Tang and Gobler, 2009; Gobler et al., 2012). Thus, a mortality rate, M , was assumed to equal
894 zero in the model for the James River.

895 The resting cysts are generally produced in the intense phase of a HAB event, but the
896 mechanisms of forming resting cysts are still not clear (Brosnahan et al., 2020). Some studies
897 suggest that the resting cyst formation occurs when the environmental conditions are not suitable,
898 such as scarcity of macronutrients. Other studies suggest that the formation of resting cysts is
899 endogenous or ‘clock’-regulated (e.g., Anderson and Keafer, 1987). In the model, the loss due to
900 the formation of resting cysts is not included.

901 For the termination of *M. polykrikoides* blooms, observations show that the bloom
902 usually declines after September of the year and eventually disappears. Data analysis shows that
903 within one year, the temperature is suitable for *M. polykrikoides* growth from May to June in this
904 region, and it can be a significant limiting factor during the high-temperature period (e.g.,
905 August). However, it becomes suitable again from late September through October. If vegetative

906 cells of *M. polykrikoides* could survive to the second suitable period for temperature, they could
907 grow again with a high growth rate and cause a bloom. This suggests that there must be some
908 unknown mechanisms causing the decline of *M. polykrikoides* blooms and prevent their return.
909 While a mandatory dormancy for resting cysts may prevent the re-initiation of the bloom (Kremp
910 and Anderson, 2000), the mechanisms for the collapse still remain unknown, and hypotheses
911 may include the unsuitable environmental conditions (e.g., shortage of nutrients), resting cyst
912 formation, parasitism, and aggregation. In numerical modeling, the collapse is implicitly
913 considered. To be consistent with observations, the gross growth rate is assumed to be zero after
914 mid-September every year, and *M. polykrikoides* cells are entirely removed from the water
915 column by September 26.

916 *Swimming*

917 The swimming ability of dinoflagellates allows the cells to change their vertical position
918 in the water column, and studies suggest that in the daytime, *M. polykrikoides* can swim up to the
919 near surface where the potential to receive high light irradiance is better (Kudela and Gobler,
920 2012). The maximum swimming speed of *M. polykrikoides* is reported to be $1449 \mu\text{m s}^{-1}$ (Jeong
921 et al., 2015). The swimming behavior is modeled with the measured values of speed in Sohn et al.
922 (2011), where they observed in laboratory that the mean swimming speeds at 22 °C for single
923 cell, two-, four-, and eight-cell chain are 391, 599, 800, $856 \mu\text{m s}^{-1}$, respectively. Chain-
924 formation provides them a more competitive advantage in receiving light (Kudela and Gobler,
925 2012). The corresponding velocities are 34–74 m d^{-1} , respectively. In the module, the swimming
926 speed is set to be $w_c = 55 \text{ m d}^{-1}$, and the cells are only allowed to swim upward. In addition, it is
927 possible that the upward swimming can stop at those layers where the light irradiance is not a
928 limiting factor. At night there may not be a specific swimming direction for swimming, and

929 therefore the vertical swimming speed is set to be zero in the model. The vertical mixing,
930 nevertheless, can transport surface cells to the lower layers.

931 *Cyst germination*

932 The external source of vegetative *M. polykrikoides* is from the germination of resting
933 cysts (input from the germination of temporary cyst is omitted). In reality, the loading rate of
934 vegetative cells by cyst germination depends on the cyst density in sediment and the germination
935 process that are influenced by environmental conditions such as temperature.

936 In this model, this process is incorporated implicitly by assuming an initial loading of
937 vegetative cells ($germ_{ini} = 25000 \text{ cells m}^{-2} \text{ d}^{-1}$ in this study) into the bottom layer for one day on a
938 chosen date of the year. This assumption avoids the uncertainties in the temporal variability in
939 the germination rate.

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1185

1186 Table 1. The *M. polykrikoides* model structure.

Abbreviation	Description	Expression
G^p	Phototrophic gross growth rate	See Eqs. A1, A4, and A5
G^h	Heterotrophic gross growth rate	See Eq. A2, A4, and A5
G	(Mixotrophic) gross growth rate	$G = G^p + G^h$; see Eqs. A3 and A6
$f(T)$	Growth-limiting function for temperature	$f(T) = e^{-k_{T1}(T-T_{opt})^2}, T \leq T_{opt}$ $f(T) = e^{-k_{T2}(T-T_{opt})^2}, T > T_{opt}$
$f(Sal)$	Growth-limiting function for salinity	$f(Sal) = e^{-k_{Sal1}(Sal-Sal_{opt})^2}, Sal \leq Sal_{opt}$ $f(Sal) = e^{-k_{Sal2}(Sal-Sal_{opt})^2}, Sal > Sal_{opt}$
$f(DIN)$	Growth-limiting function for DIN	$f(DIN) = \frac{DIN}{DIN+N_k}$
$f(DIP)$	Growth-limiting function for DIP	$f(DIP) = \frac{DIP}{DIP+P_k}$
$f(I)$	Growth-limiting function for light irradiance	$f(I) = \frac{I}{I+I_k}$
$f(OM_{12})$	Growth-limiting function for organic matter smaller than 12 μm	$f(OM_{12}) = \frac{OM_{12}}{OM_{12}+OM_{12k}}$
R	Respiration/excretion rate	$R = R_0\theta_R^{T-20} + f^p G^p$

1187

1188

1189 Table 2. The *M. polykrikoides* model parameters and the values used in the experimental
 1190 treatments. Most values were estimated based on the reported results from published laboratory
 1191 experiments, the others are calibrated numerically. The optimal condition means the growth is
 1192 not limiting by any environmental factor at all.

Abbr.	Description	Unit	Value	Reference
G_{opt}^p	Phototrophic gross growth rate at the optimal condition	d^{-1}	1.06	Gobler et al. (2012)
G_{opt}^h	Heterotrophic gross growth rate at the optimal condition	d^{-1}	0.62	Gobler et al. (2012)
f^p	respiratory losses associated with photosynthesis as a ratio to G^p		0.16	Gobler et al. (2012)
R_0	Basic metabolism rate at 20 °C	d^{-1}	0.025	Calibrated
w_c	Swimming velocity of <i>M. polykrikoides</i>	$m d^{-1}$	55	Sohn et al. (2011)
T_{opt}	Optimal temperature for growth	°C	25.1	Kim et al. (2004); Griffith and Gobler (2016)
k_{T1}	Temperature effect on growth below T_{opt}	°C ⁻²	0.0230	Kim et al. (2004); Griffith and Gobler (2016)
k_{T2}	Temperature effect on growth above T_{opt}	°C ⁻²	0.0277	Kim et al. (2004); Griffith and Gobler (2016)
Sal_{opt}	Optimal salinity for growth		34	Kim et al. (2004)
k_{Sal1}	Salinity effect on growth below Sal_{opt}		0.0024	Kim et al. (2004)
k_{Sal2}	Salinity effect on growth below Sal_{opt}		0.0222	Kim et al. (2004)
I_{opt}	Half-saturation coefficient for light irradiance	$\mu E m^{-2} s^{-1}$	30	Kim et al. (2004) and Oh et al. (2006)
N_k	Half-saturation coefficient for DIN	$g N m^{-3}$	0.028	Kim et al. (2001) and Gobler et al. (2012)
P_k	Half-saturation coefficient for DIP	$g P m^{-3}$	0.0177	Kim et al. (2001)
θ_R	Constant for quantifying the temperature effect on respiration rate		1.07	Calibrated
OM_{12k}	Half saturation coefficient for organic matter smaller than 12 μm	$g C m^{-3}$	0.0263	Jeong et al. (2004)
a (a_{1C} , a_{1N} , a_{1P} , a_{2C} , a_{2N} , a_{2P})	Fraction of refractory and labile particulate organic matter smaller than 12 μm , excluding prey algae		0.01	Calibrated
b (b_2 , b_3)	Fraction of co-occurring algae that are prey to <i>M. polykrikoides</i>		0.001	Derived from observations

1193 Table 3. Sensitivity tests for examining the effects of mixotrophic growth, swimming, and cyst
 1194 germination on the initiation and development of *M. polykrikoides* blooms. Significant
 1195 differences between experimental and the Base treatment are shown in bold.

<i>Experiment</i>		<i>Osmotrophy</i>	<i>Phagotrophy</i>		w_c (m d ⁻¹)	$germ_{ini}$ (cells m ⁻² d ⁻¹)
			<i>a</i>	<i>b</i>		
Base		on	0.01	0.001	55	25000
1	Higher bioavailable POM	on	0.1	0.001	55	25000
2	Osmotrophy only	on	0	0	55	25000
3	photoautotrophy only	off	0	0	55	25000
4	Reduced swimming speed	on	0.01	0.001	30	25000
5	No swimming	on	0.01	0.001	0	25000
6	Higher initial cell loading	on	0.01	0.001	55	250000
7	Lower initial cell loading	on	0.01	0.001	55	2500

1196

1197 Table 4. The initial time (t_{ini}), when *M. polykrikoides* was first observed in water samples, the
 1198 date at which *M. polykrikoides* reached bloom densities (t_{bloom} , 1000 cells ml⁻¹), the duration of
 1199 bloom initiation period (t_B), the duration of the bloom events (density > t_{bloom}), maximum
 1200 surface cell densities, and mean surface cell densities for each modeled year from 2007-2013
 1201 (Base Scenario). Note that the initial time is the same for each station, and only days with a
 1202 density over 1000 cells ml⁻¹ are included for computing duration of the bloom and mean surface
 1203 cell densities during each bloom.

Year	Station	Initial time (t_{ini})	Beginning of bloom event (t_{bloom})	Duration of initiation period (t_B , d)	Duration of bloom event (weeks)	Maximum surface cell density (cells ml ⁻¹)	Mean surface cell density during bloom event (cells ml ⁻¹)
2007	LFB01	6/29/2007	7/15/2007	17	10.4	6335	1052
	NYCC		7/23/2007	25	7.4	6038	735
	LFA01		8/4/2007	37	5.5	4190	742
	LE5.6		8/13/2007	46	3.9	3877	1263
	LE5.4		8/11/2007	44	4.5	4328	925
2008	LFB01	7/1/2008	7/22/2008	22	8.6	8840	1464
	NYCC		8/2/2008	33	6.0	6145	863
	LFA01		8/3/2008	34	5.8	4558	792
	LE5.6		8/13/2008	44	4.1	3915	1230
	LE5.4		8/13/2008	44	4.1	5180	1097
2009	LFB01	5/20/2009	6/26/2009	38	8.8	10290	1662
	NYCC		7/3/2009	45	7.8	6634	1031
	LFA01		7/3/2009	45	7.8	4539	982
	LE5.6		7/9/2009	51	6.9	4436	1180
	LE5.4		7/16/2009	58	5.9	3850	976
2010	LFB01	6/8/2010	7/20/2010	43	9.6	7195	1171
	NYCC		7/19/2010	42	7.9	3050	769
	LFA01		7/19/2010	42	7.3	4978	791
	LE5.6		7/26/2010	49	7.2	4731	1327
	LE5.4		7/29/2010	52	5.6	4849	1154
2011	LFB01	5/27/2011	7/24/2011	59	5.6	1920	584
	NYCC		8/8/2011	74	4.1	4554	708
	LFA01		8/8/2011	74	4.0	6408	813
	LE5.6		8/11/2011	77	3.3	4393	1283
	LE5.4		8/6/2011	72	4.9	4172	1114
2012	LFB01	4/15/2012	6/22/2012	69	12.8	7469	1198
	NYCC		7/3/2012	80	7.1	4640	850
	LFA01		7/1/2012	78	7.2	5824	845
	LE5.6		7/2/2012	79	7.6	2698	982
	LE5.4		7/7/2012	84	7.1	2232	866
2013	LFB01	6/16/2013	7/22/2013	37	9.3	8466	1251
	NYCC		7/25/2013	40	7.0	11666	1199
	LFA01		8/16/2013	62	3.8	10776	1083

LE5.6	8/19/2013	65	3.0	3445	1130
LE5.4	8/24/2013	70	2.0	1936	725

1204 Table 5. The 7-year mean of growth rates, metabolism rate, and transport rate during the
 1205 modeled blooms in 2007-2013, in units of d^{-1} . We include relative growth rate, $\overline{r_g}$, mixotrophic
 1206 gross growth rate, \overline{G} , phototrophic growth rate, $\overline{G^p}$, heterotrophic growth rate, $\overline{G^h}$, total
 1207 metabolism rate, \overline{R} , and transport rate, $\overline{F_B}$. Values presented are for depth-integrated biomass
 1208 described in Eq. (8) while the bracket “ $\langle \ \rangle$ ” denotes the mean values over the given periods.
 1209 Note that *M. polykrikoides* reached bloom densities ($1000 \text{ cells ml}^{-1}$) at different times at each
 1210 station.

Station	Period	$\langle \overline{r_g} \rangle$	$\langle \overline{G} \rangle$	$\langle \overline{G^p} \rangle$	$\langle \overline{G^h} \rangle$	$-\langle \overline{R} \rangle$	$-\langle \overline{F_B} \rangle$	$\frac{\langle \overline{G^h} \rangle}{\langle \overline{G} \rangle}$	$\frac{\langle \overline{F_B} \rangle}{\langle \overline{G} \rangle}$
LFB01	Present	0.13	0.18	0.09	0.09	-0.06	0.01	0.51	-0.06
	Initiation	0.39	0.31	0.15	0.16	-0.07	0.15	0.52	-0.48
NYCC	Present	0.18	0.27	0.15	0.12	-0.07	-0.02	0.43	0.08
	Initiation	0.34	0.40	0.22	0.18	-0.08	0.02	0.46	-0.05
LFA01	Present	0.18	0.30	0.17	0.12	-0.07	-0.05	0.42	0.17
	Initiation	0.31	0.42	0.24	0.19	-0.08	-0.03	0.44	0.08
LE5.6	Present	0.19	0.30	0.15	0.14	-0.06	-0.04	0.48	0.14
	Initiation	0.29	0.44	0.22	0.22	-0.07	-0.07	0.49	0.17
LE5.4	Present	0.19	0.34	0.13	0.21	-0.06	-0.10	0.63	0.29
	Initiation	0.28	0.48	0.19	0.29	-0.07	-0.14	0.61	0.28

1211 Footnote: “Present Period”: refers to the entire period of time when the cell density of *M.*
 1212 *polykrikoides* is greater than 0 cell ml^{-1} in the water column, including both bloom and non-
 1213 bloom periods; “Initiation Period”: refers to the period between the time when the initial cell
 1214 density was greater than 0 (i.e., t_{ini}) and the time when the density of *M. polykrikoides* reached
 1215 $1000 \text{ cells ml}^{-1}$, t_{bloom} .

1216

1217 Table 6. The shifts in timing of the beginning of the bloom event, t_{bloom} , (Experiment – Base
 1218 Scenario) in units of d at two Lafayette River stations, LFB01 and LFA01, due to simulated
 1219 changes in the fraction of bioavailable particulate organic matter or mixotrophic ability (Exps. 1-
 1220 3), changes of swimming speed of *M. polykrikoides* (Exps. 4-5), and changes of the magnitude of
 1221 initial cell loading, $germ_{ini}$ (Exps. 6-7). Positive and negative values indicate that t_{bloom} in the
 1222 experiments are advanced and delayed, respectively, compared with Base Scenario. The cases
 1223 when bloom density cannot be reached is denoted by “—”.

	Exp. 1	Exp. 2	Exp. 3	Exp. 4	Exp. 5	Exp. 6	Exp. 7
<u>LFB01</u>							
2007	0.0	0.0	0.0	—	—	-2.0	18.2
2008	0.0	0.0	12.0	37.8	45.0	-2.0	11.3
2009	0.0	0.0	54.3	19.5	29.0	-13.0	6.8
2010	0.0	0.0	—	5.3	22.8	-2.0	4.3
2011	0.0	0.0	—	21.8	34.3	-7.2	37.8
2012	-0.8	0.0	—	56.0	35.5	-8.5	14.2
2013	0.0	0.0	—	35.5	—	-11.8	2.8
<u>LFA01</u>							
2007	-1.3	0.0	—	—	—	-12.5	12.2
2008	0.0	0.0	—	29.8	—	-2.3	5.8
2009	0.0	0.0	—	11.5	39.7	-10.5	7.5
2010	0.0	0.0	—	6.5	—	-2.0	10.0
2011	-15.3	0.0	—	0.3	21.5	-29.5	13.3
2012	0.0	0.0	—	45.5	—	-15.2	10.8
2013	0.0	0.0	—	9.0	—	-22.8	4.0

1224

1225 Table 7. The 7-year mean of the modeled daily-averaged growth-limiting function for each
 1226 environmental factor, including temperature (T), salinity (Sal), irradiance (I), dissolved
 1227 inorganic nitrogen (DIN), dissolved inorganic phosphate (DIP), and bioavailable organic matter
 1228 that is smaller than $12 \mu m$ (OM_{12}), during the simulated blooms in 2007-2013. The mean of
 1229 $f(Res)$ that represents the overall contribution of resources (I , DIN , DIP , and OM_{12}) is also
 1230 presented. Note that the values are for the surface layer only, $f(I)$ equals zero at night and the
 1231 means for $f(I)$ during the photic period between 6:00 to 18:00 are listed in parentheses.

Station	Period	$f(T)$	$f(Sal)$	$f(Res)$	$f(I)$	$f(DIN)$	$f(DIP)$	$f(OM_{12})$
LFB01	Present	0.59	0.48	0.82	0.53 (0.97)	0.40	0.70	0.74
	Initiation	0.64	0.46	0.97	0.54 (0.97)	0.55	0.68	0.95
NYCC	Present	0.72	0.54	0.85	0.53 (0.97)	0.60	0.58	0.70
	Initiation	0.73	0.51	0.98	0.54 (0.98)	0.72	0.58	0.91
LFA01	Present	0.76	0.55	0.86	0.53 (0.97)	0.65	0.57	0.71
	Initiation	0.76	0.52	0.97	0.54 (0.97)	0.75	0.58	0.91
LE5.6	Present	0.82	0.56	0.84	0.53 (0.97)	0.66	0.56	0.70
	Initiation	0.82	0.54	0.97	0.54 (0.97)	0.77	0.58	0.90
LE5.4	Present	0.87	0.61	0.89	0.53 (0.97)	0.60	0.53	0.80
	Initiation	0.87	0.59	0.98	0.53 (0.97)	0.72	0.53	0.92

1232 Footnote: “Present Period”: refers to the entire period of time when the cell density of $M.$
 1233 $polykrikoides$ is greater than 0 cell ml^{-1} in the water column, including both bloom and non-
 1234 bloom periods; “Initiation Period”: refers to the period between the time when initial density was
 1235 larger than 0 (i.e., t_{ini}) and the time when the density of $M. polykrikoides$ reached $1000 \text{ cells ml}^{-1}$,
 1236 t_{bloom} .

1237

1238 Table 8. r^2 between the modeled gross growth rate, G , and the modeled daily-averaged growth-
1239 limiting function for temperature (T), salinity (Sal), and $f(Res)$ that represents the overall
1240 contribution of resources (I , DIN , DIP , and OM_{12}) to the variability in G ; and r^2 between $f(Res)$
1241 and daily-averaged growth-limiting function for irradiance (I), dissolved inorganic nitrogen
1242 (DIN), dissolved inorganic phosphate (DIP), and organic matter smaller than $12 \mu m$ (OM_{12}).
1243 Statistics are reported for interannual variability and daily variability, respectively for the
1244 modeled 7-year dataset encompassing the years 2007-2013. Note that the values are for the
1245 surface layer only and that *M. polykrikoides* cell abundances at each station reached bloom
1246 densities at different times. Significant values with p-values less than 0.05 are shown in bold.

Station	Period	$f(T) \sim G$	$f(Sal) \sim G$	$f(Res) \sim G$	$f(I) \sim f(Res)$	$f(DIN) \sim f(Res)$	$f(DIP) \sim f(Res)$	$f(OM_{12}) \sim f(Res)$
<i>Interannual</i>								
LFB01	Present	0.67	0.07	0.02	0.14	0.46	<0.01	0.98
	Initiation	0.95	0.03	0.01	0.55	0.58	0.32	0.13
NYCC	Present	0.75	0.08	0.31	0.18	0.65	0.01	0.91
	Initiation	0.77	<0.01	0.43	0.09	0.13	0.34	0.03
LFA01	Present	0.69	0.03	0.48	0.20	0.71	0.02	0.87
	Initiation	0.61	<0.01	0.51	0.01	0.31	0.08	0.03
LE5.6	Present	0.66	0.06	0.42	0.21	0.78	0.04	0.88
	Initiation	0.39	0.02	0.16	0.40	0.02	0.20	0.01
LE5.4	Present	0.56	<0.01	0.23	0.18	0.73	<0.01	0.88
	Initiation	0.54	0.05	0.04	0.26	0.05	0.34	0.09
<i>Daily</i>								
LFB01	Present	0.42	0.04	0.22	0.22	0.30	0.01	0.96
	Initiation	0.94	0.02	0.02	0.07	0.10	0.02	<0.01
NYCC	Present	0.42	0.07	0.29	0.33	0.50	<0.01	0.93
	Initiation	0.89	0.01	0.03	<0.01	0.03	<0.01	<0.01
LFA01	Present	0.40	0.05	0.31	0.32	0.55	0.01	0.92
	Initiation	0.82	0.01	0.06	<0.01	0.10	<0.01	<0.01
LE5.6	Present	0.25	0.06	0.47	0.33	0.72	0.04	0.93
	Initiation	0.75	0.01	0.05	0.04	0.03	0.01	0.36
LE5.4	Present	0.33	<0.01	0.36	0.25	0.60	0.01	0.90
	Initiation	0.76	0.04	0.05	<0.01	0.01	<0.01	0.09

1247 Footnote: “Present Period”: refers to the entire period of time when the cell density of *M.*
1248 *polykrikoides* is greater than 0 cell ml^{-1} in the water column, including both bloom and non-
1249 bloom periods; “Initiation Period”: refers to the period between the time when initial density was
1250 larger than 0 (i.e., t_{ini}) and the time when the density of *M. polykrikoides* reached $1000 \text{ cells ml}^{-1}$,
1251 t_{bloom} .

1252

1253 Figure Captions

1254 Figure 1. Map of the lower James River and the Elizabeth and Lafayette River sub-tributaries,
1255 Virginia, USA. The hollow squares denote the locations of long-term monitoring stations LE5.4
1256 (polyhaline James River), LE5.6 (lower Elizabeth River), LFA01 (Lafayette River mouth), and
1257 LFB01 (Lafayette River headwaters), and the filled circle denotes the location of Station NYCC.

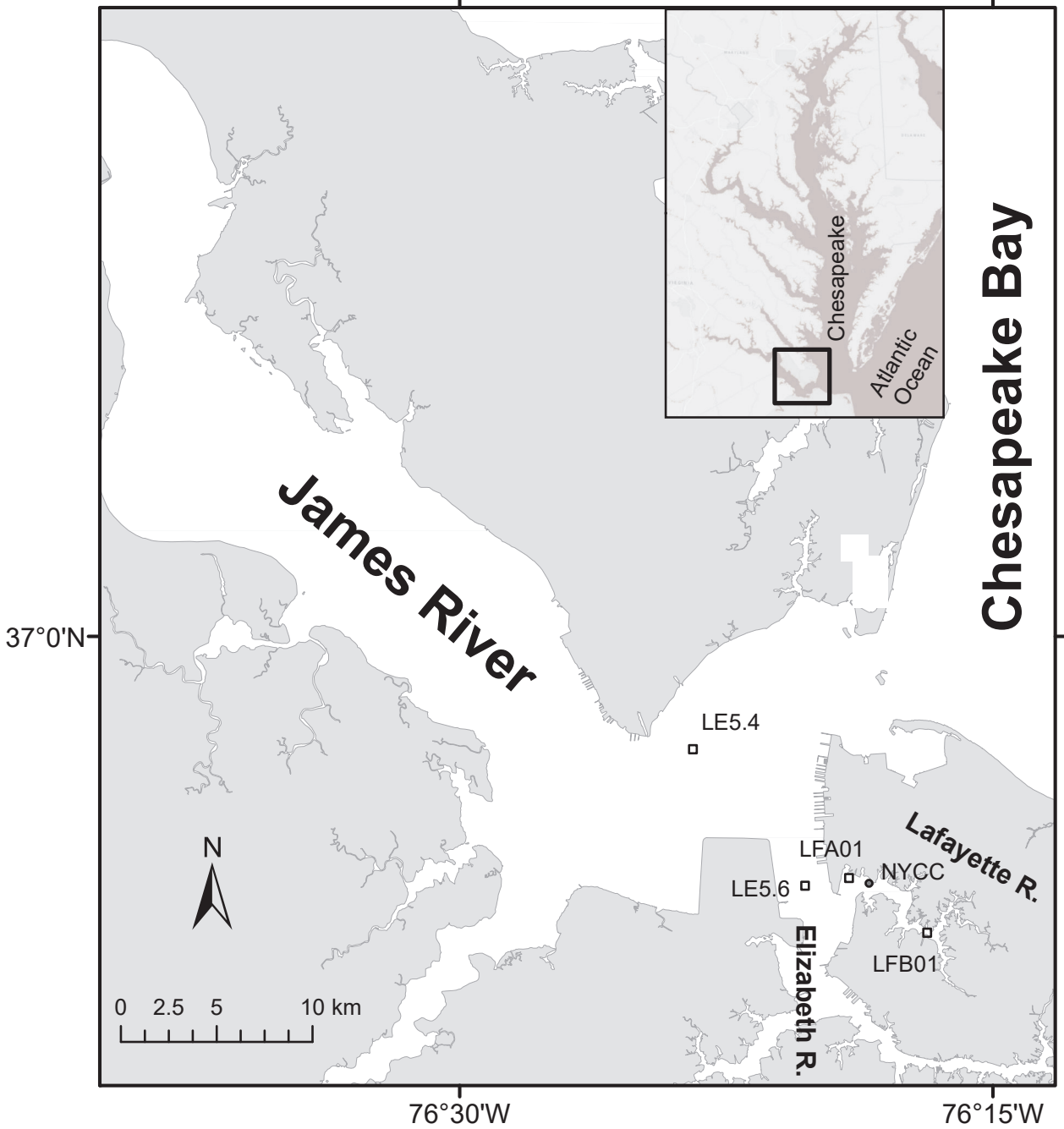
1258
1259 Figure 2. Comparison of modeled daily surface chl-a from 2007-2013 at monitoring stations in
1260 the Lafayette River (LFB01, NYCC, and LFA01), the Elizabeth River (LE5.6), and the mainstem
1261 James River (LE5.4). The blue area represents the area between the minimum and the maximum
1262 chl-a, the monthly chl-a data from the Chesapeake Bay Program data are indicated by the dots
1263 and the weekly dataflow chl-a data are indicated by the diamonds. The correlation coefficients (r)
1264 between the model output and observational data of surface chl-a at the five stations and the
1265 relative errors (RE) are listed. The grey area represents the initiation periods that are bounded by
1266 the time of initial cell loading, t_{ini} , and the time when bloom cell densities were reached, t_{bloom} .

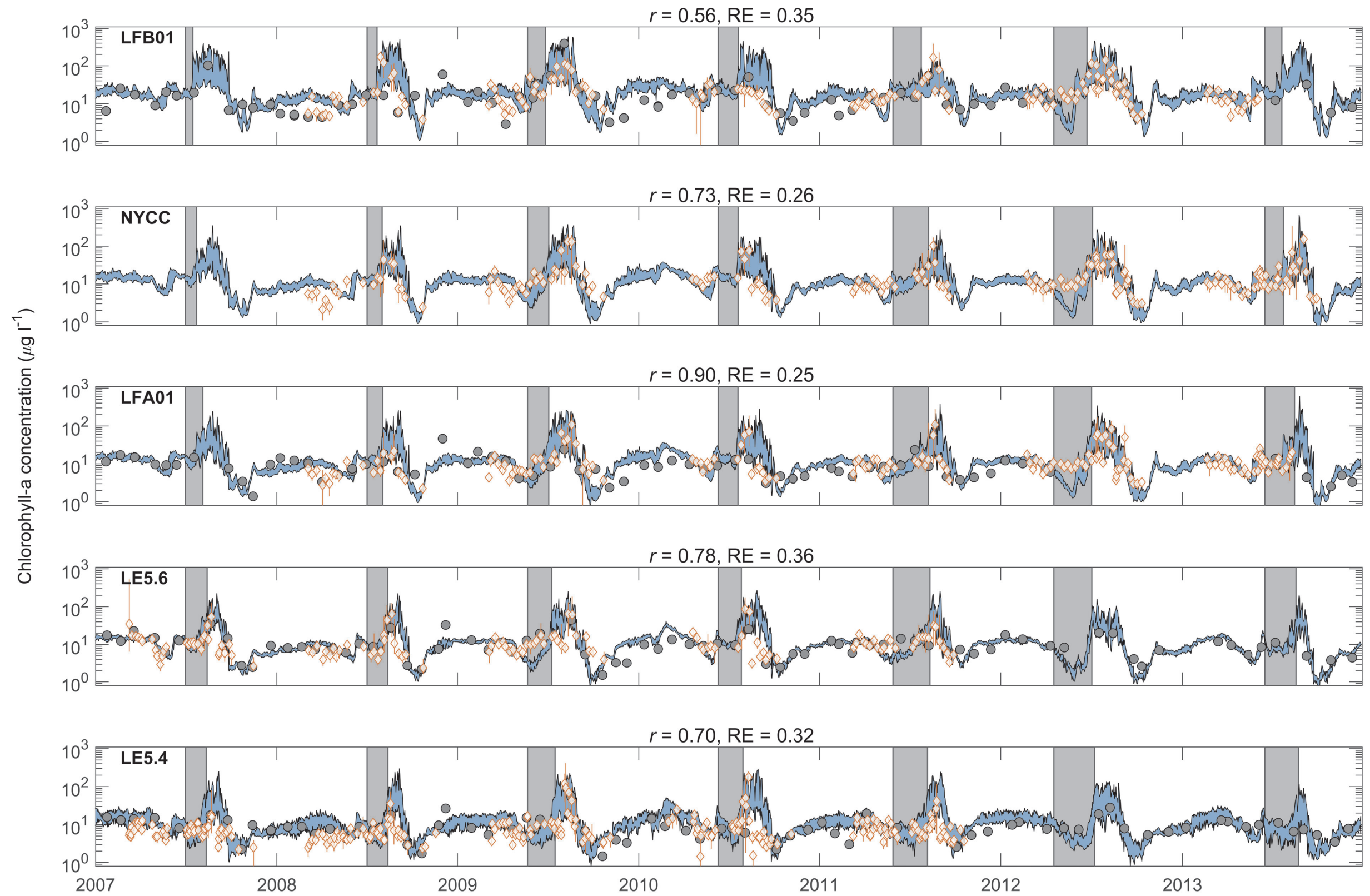
1267
1268 Figure 3. Comparison of model results of *M. polykrikoides* cell densities at station LFB01 (Base
1269 Scenario) to the observational density data (red circles) in the Lafayette River in 2009. The thick
1270 blue line is the daily-averaged modeled *M. polykrikoides* cell density, and the blue area
1271 represents the area bounded by the daily minimum and the daily maximum of the modeled cell
1272 density in the grid cell representing the station, and the black dashed line indicates the cell
1273 density considered to be a bloom (e.g., 1000 cells ml⁻¹).

1274
1275 Figure 4. Daily maximum surface cell densities of *M. polykrikoides* at Station LFB01 during
1276 2009 for each experiment compared with the Base Scenario (black lines), resulting from (A)
1277 different fractions of bioavailable particulate organic matter or different mixotrophic capability;
1278 Base: $a = 0.01$, $b = 0.001$; Exp. 1: $a = 0.1$, $b = 0.001$; Exp. 2: osmotrophy only ($a = b = 0$); Exp.
1279 3: photoautotrophy only (heterotrophy off); (B) different swimming speeds, w_c , Base: $w_c = 55$ m
1280 d⁻¹, Exp. 4: $w_c = 30$ m d⁻¹, Exp. 5: $w_c = 0$ m d⁻¹; and (C) different magnitudes of initial cell
1281 loadings, $germ_{ini}$; Base: $germ_{ini} = 25,000$ cells m⁻² d⁻¹, Exp. 6: $germ_{ini} = 250,000$ cells m⁻² d⁻¹,
1282 Exp. 7: $germ_{ini} = 2,500$ cells m⁻² d⁻¹. The red dotted lines indicate the time when bloom cell
1283 densities were reached in Base Scenario, t_{bloom} .

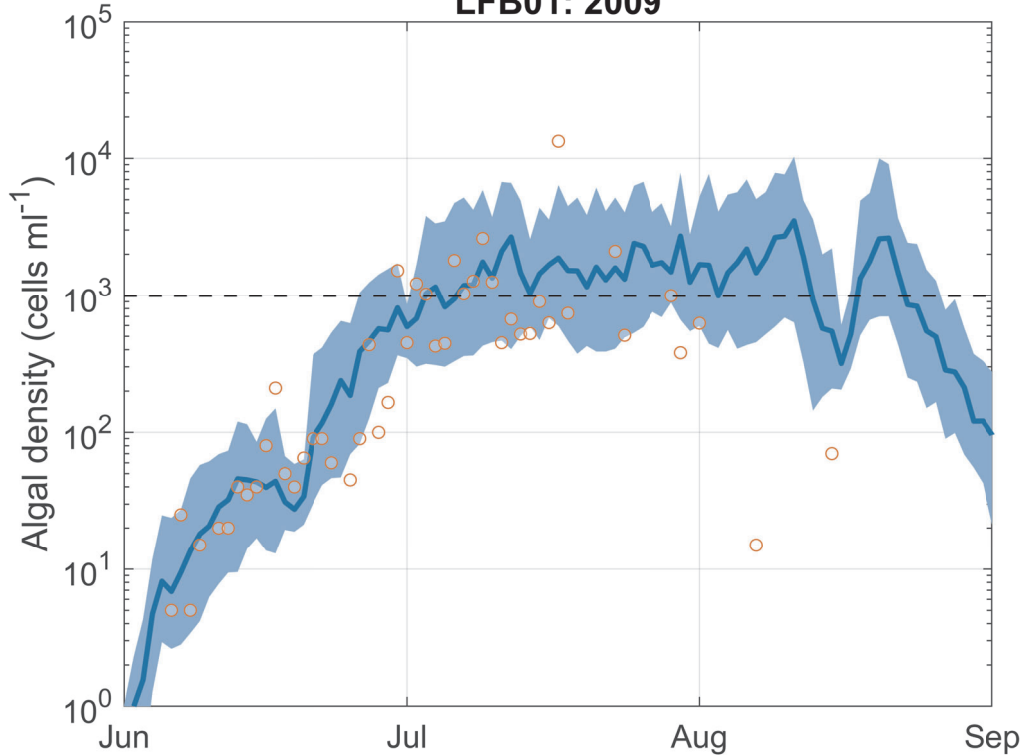
1284
1285 Figure 5. The daily-averaged gross growth rate, G , phototrophic growth rate, G^p , heterotrophic
1286 growth rate, G^h , growth-limiting functions for temperature, $f(T)$, salinity, $f(Sal)$,
1287 irradiance, $f(I)$, dissolved inorganic nitrogen, $f(DIN)$, dissolved inorganic phosphate, $f(DIP)$,
1288 and organic matter smaller than 12 μm , $f(OM_{12})$, at Station LFB01 in 2012 (left panels) and
1289 2013 (right panels). G_{TS} is also plotted, $G_{TS} = G_{opt}f(T)f(Sal)$, which is the highest potential

1290 growth rate based on temperature and salinity limitation (i.e., other resources are not limited).
1291 The initiation periods are bounded by the black dotted lines indicating the time of initial cell
1292 loading, t_{ini} , and the red dotted lines indicate the time when bloom cell densities were reached,
1293 t_{bloom} .





LFB01: 2009



LFB01: 2009

