Data assimilation in a coupled physical-biogeochemical model of the California Current System using an incremental lognormal 4-dimensional variational approach: Part 2, Joint physical and biological data assimilation twin experiments

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Abstract

Coupled physical and biological data assimilation is performed within the California Current System using model twin experiments. The initial condition of physical and biological variables is estimated using the four-dimensional variational (4DVar) method under the Gaussian and lognormal error distributions assumption, respectively. Errors are assumed to be independent, yet variables are coupled by assimilation through model dynamics. Using a nutrient-phytoplankton-zooplankton-detritus (NPZD) model coupled to an ocean circulation model (the Regional Ocean Modeling System, ROMS), the coupled data assimilation procedure is evaluated by comparing results to experiments with no assimilation and with assimilation of physical data and

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biological data separately. Independent assimilation of physical (biological) data reduces the root-mean-squared error (RMSE) of physical (biological) state variables by more than 56% (43%). However, the improvement in biological (physical) state variables is less than 7% (13%). In contrast, coupled data assimilation improves both physical and biological components by 57% and 49%, respectively. Coupled data assimilation shows robust performance with varied observational errors, resulting in significantly smaller RMSEs compared to the free run. It still produces the estimation of observed variables better than that from the free run even with the physical and biological model error, but leads to higher RMSEs for unobserved variables. A series of twin experiments illustrates that coupled physical and biological 4DVar assimilation is computationally efficient and practical, capable of providing the reliable estimation of the coupled system with the same and ready to be examined in a realistic configuration.

Keywords: Coupled data assimilation, Biogeochemical model, 4DVAR, California Current System Keyword

1 1. Introduction

Marine ecosystem and biogeochemical models coupled to realistic ocean circulation models are applied routinely today for an extensive range of studies, such as primary production (Franks and Chen, 2001), ecosystem phenology (Chenillat et al., 2013), biogeography (Follows et al., 2007, Goebel et al., 2010), nutrient cycling (Fennel, 2010), air-sea carbon exchange (Chai et al., 2009) and climate change (Cox et al., 2000, Behrenfeld et al., 2006, Stock et al., 2011). Despite real advances in the representation of complex biolog⁹ ical interactions and improvements in physical circulation modeling, many
¹⁰ factors still contribute to errors in model output, including imperfect param¹¹ eterization of biological and physical processes at both resolved and subgrid
¹² scales. In realistic applications in which ocean state estimates at particular
¹³ times are sought, for example as part of an ocean observing system, addi¹⁴ tional errors result from uncertainties in ocean model initial conditions and
¹⁵ applied forcing.

One approach to improving model fidelity for ocean state estimation is 16 through data assimilation in which model estimates are constrained through 17 adjustment of control variables to better match available observations. Devel-18 opments in data assimilation in physical oceanography for over two decades 19 now provide many estimates of the physical ocean state at global (Behringer 20 et al., 1998, Bell et al., 2000, Chassignet et al., 2007, Köhl et al., 2007, 21 Balmaseda et al., 2008, Carton and Giese, 2008) and regional (Oke et al., 22 2008, Cummings et al., 2009, Broquet et al., 2009, Shulman et al., 2009, Ku-23 rapov et al., 2011, Matthews et al., 2012, Sakov et al., 2012) scales. Data 24 assimilation techniques have been developed to a lesser extent in biological 25 oceanography, though their application has been used for both the determi-26 nation of poorly known model parameters (e.g., Matear, 1995, Spitz et al., 27 1998, Losa et al., 2004, Mattern et al., 2012, Roy et al., 2012, Doron et al., 28 2013, Simon et al., 2015) as well as quantitative improvement in modeled 29 biological fields (see Gregg (2008) and Edwards et al. (2015) for reviews). 30

Data assimilation in physical-biological coupled systems has focused generally on either physical or biological data assimilation in isolation. Better representation of the ocean circulation by physical data assimilation is ex-

pected to improve the distribution of biological variables. Studies focusing on 34 the impact of physical data assimilation on biological fields include Oschlies 35 and Garçon (1998), Miller et al. (2000), Berline et al. (2007) and Fiechter 36 et al. (2011). For example, Oschlies and Garçon (1998) assimilate satellite 37 estimates of sea surface height (SSH) over the North Atlantic to improve 38 the eddy representation in the physical model, which provides currents for a 39 coupled biological model. They report that the nitrate flux into the euphotic 40 zone is increased by improving the underestimated mesoscale eddy activity in 41 the free simulation. Raghukumar et al. (2015) present a counter example in 42 which physical data assimilation alone can drive spurious nutrient fluxes into 43 the euphotic zone degrading ecosystem model performance. Improvements in 44 biological fields have also resulted from assimilation of biological fields alone, 45 where physical fields have been assumed a priori to be sufficiently accurate or 46 already modified through physical data assimilation (e.g., Friedrichs, 2001, 47 Garcia-Gorriz et al., 2003, Natvik and Evensen, 2003, Hoteit et al., 2005, 48 Triantafyllou et al., 2007, Ciavatta et al., 2011, Rousseaux and Gregg, 2012, 40 Ford et al., 2012, Hu et al., 2012). For example, Garcia-Gorriz et al. (2003) 50 assimilate the Sea-viewing Wide Field-of-view Sensor (SeaWiFS) data into 51 an NPZ model coupled to a 3D ocean model over the Adriatic Sea, improving 52 ecosystem parameters to reduce misfits between observations and the model 53 output. Natvik and Evensen (2003) use SeaWiFS data to fit an 11-component 54 biochemical model coupled to a 3D ocean circulation model configured over 55 the North Atlantic. Using an ensemble Kalman filter approach, they adjust 56 state variables and show that multivariate biochemical data assimilation can 57 not only improve the representation of an observed variable but also reduce

⁵⁹ the variance of unobserved variables.

A few studies have addressed the assimilation of both physical and bi-60 ological data into coupled models and its advantages over the fit to either 61 physical or biological data alone. Using an optimal interpolation approach 62 applied to the Gulf Stream region, Anderson et al. (2000) find that dynam-63 ically consistent physical and biological fields created through joint physi-64 cal and biological assimilation are superior to those obtained through either 65 physical or biological data assimilation alone. In a sequential data assimila-66 tion study of the North Atlantic, Ourmières et al. (2009) find that ecosystem 67 state estimates are improved through assimilation of both physical (sea sur-68 face temperature (SST), SSH and climatological temperature (T) and salin-69 ity (S)) and biological (nitrate climatology) data more than through physical 70 data assimilation alone. Indeed in their results, physical data assimilation 71 alone may degrade ecosystem estimates, depending on the accuracy of the 72 nitrate background state. In a study of Monterey Bay, Shulman et al. (2013) 73 report that substantial improvement in biological estimates did not result 74 from physical assimilation alone but required assimilation of biological fields 75 or updates to biological fields (nitrate) through statistical relations. Simon 76 et al. (2015) perform two steps of assimilation using an ensemble Kalman 77 filter in coupled physical and biological state estimation. After fitting the 78 model to SST, along-track sea level anomalies and ice concentration obser-79 vations, they assimilate 8-day composite chlorophyll data to estimate the 80 biological states and parameters in log-transformed space. A stronger error 81 reduction results from assimilating all observations, but physical and biolog-82 ical components are independent during assimilation.

To date biological assimilation efforts on adjusting state variables have 84 largely used sequential methods, based on optimal interpolation or Kalman 85 filter approaches. In particular, Bertino et al. (2003) applied Gaussian anamor-86 phosis to biogeochemical variables with the non-Gaussian distributions in 87 the ensemble Kalman filter. This transformation satisfies the assumption of 88 Gaussian error distribution and they show promising results in fitting 1-D 89 numerical ecosystem model to observations. Recently, a four-dimensional 90 variational assimilation method appropriate for ocean ecosystem variables 91 was studied in an idealized 1-dimensional context (Song et al., 2012). This 92 method accounts for the non-Gaussian statistics of ecosystem variables by as-93 suming lognormal statistics following Fletcher and Zupanski (2006). In Song 94 et al. (2016a), this approach is modified and implemented within a realis-95 tic ocean circulation model (ROMS; the Regional Ocean Modeling System). 96 The modification includes a linearization of the log-transformation function 97 to enable efficient searching for the cost function minimum. Although the lin-98 earization requires the exclusion of observations whose values substantially gc exceed the background state, the modified log-transformed 4DVar outper-100 forms the conventional 4DVar (which assumes Gaussian error distributions) 101 both in terms of RMSE and non-negativity in a series of model twin experi-102 ments configured for the California Current System (Song et al., 2016a). 103

In this study, we extend that work by developing the ability to jointly assimilate physical and biological data within ROMS. The four-dimensional variational (4DVar) method provides dynamically consistent state estimates within each assimilation cycle. Coupled dynamics within the tangent linear and adjoint models of the 4DVar system have the potential to enable both

physical data to improve biological fields and biological data to improve phys-109 ical fields. In most sequential data assimilation methods the latter is possible 110 only through statistical adjustments and not directly through model dynam-111 ics. We investigate the advantage of coupled data assimilation using both 112 physical and biological data by comparing results from multiple runs: no 113 data assimilation, physical data assimilation alone, biological data assimila-114 tion alone, and joint physical and biological assimilation. Using model twin 115 experiments, we fit the coupled model to pseudo observations of SST, SSH, 116 in situ temperature and salinity, and surface chlorophyll data. The statisti-117 cal analyses highlight the advantage of the coupled data assimilation in the 118 present model configuration. 119

The organization of this paper is as follows. A brief introduction to physical and biological variational data assimilation method is given in section 2. Section 3 describes the twin experiment design to evaluate the coupled data assimilation system and its performance is presented in section 4. We summarize results and provide a discussion in section 5 to end the paper.

¹²⁵ 2. Coupled variational data assimilation

It is desirable to perform physical and biological data assimilation simultaneously rather than independently because (a) it is computationally more efficient to carry out a single assimilation procedure with a larger model than to perform two sequential but smaller assimilation operations and (b) the physical and biological fields are coupled through model dynamics. This coupling enables biological observations to constrain physical fields and vice versa, in principle leading to improved state estimates over results from independent (i.e., uncoupled) physical and biological assimilation. In practice,
however, the beneficial results of coupled assimilation must be demonstrated,
and issues such as model error and observational uncertainty may limit the
ultimate improvements obtained through coupled state estimation.

Fundamentally, the basic error assumptions for physical and biological 137 data assimilation are different. Errors in physical variables are assumed to 138 be Gaussian distributed, whereas errors in biological variables are better 139 represented by lognormal distributions (Campbell, 1995, Simon and Bertino, 140 2009); as a result, the assumption of Gaussian-distributed errors is appro-141 priate for physical but not biological variables. Here, we present a method 142 for combining the two different 4DVar approaches by following Fletcher and 143 Zupanski (2006), Fletcher (2010) and Fletcher and Jones (2014). Although 144 the state vector could include initial conditions, boundary conditions, sur-145 face forcing fields, and biological parameters, we consider here for simplicity 146 a control vector consisting only of the initial state \mathbf{x}_0 . 147

We first adapt the incremental form of 4DVar following Song et al. (2016a). 148 If the posterior initial condition \mathbf{x}_0 is written as the sum of the background 149 state $\mathbf{x}_{b,0}$ and a (small) increment $\delta \mathbf{x}_0$, then $\mathbf{x}_i^o = \mathcal{H}_i(\mathcal{M}_{i,0}(\mathbf{x}_{b,0} + \delta \mathbf{x}_0)) \approx$ 150 $\mathcal{H}_i(\mathcal{M}_{i,0}(\mathbf{x}_{b,0})) + \mathbf{H}_i \mathbf{M}_{i,0} \delta \mathbf{x}_0$, where the nonlinear model $\mathcal{M}_{i,0}$ integrates the 151 state vector from $t = t_0$ to $t = t_i$, and the observation operator \mathcal{H}_i maps 152 model states to observation space and $\mathbf{x}_{b,0}$ is the background state vector. 153 The matrices \mathbf{H}_i and $\mathbf{M}_{i,0}$ are the tangent linear forms of \mathcal{H}_i and $\mathcal{M}_{i,0}$, respec-154 tively. In this case, the cost function J_G appropriate for Gaussian-distributed 155

156 variables becomes

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$$\mathcal{H}_{G}(\delta \mathbf{x}_{0}) = \frac{1}{2} \delta \mathbf{x}_{0}^{T} \mathbf{B}_{G}^{-1} \delta \mathbf{x}_{0}
 + \frac{1}{2} \sum_{i=1}^{N_{o}} (\mathbf{d}_{g,i} - \mathbf{H}_{i} \mathbf{M}_{i,0} \delta \mathbf{x}_{0})^{T} \mathbf{R}_{G,i}^{-1} (\mathbf{d}_{g,i} - \mathbf{H}_{i} \mathbf{M}_{i,0} \delta \mathbf{x}_{0}), \quad (1)$$

where $\mathbf{d}_{g,i} = \mathbf{y}_i - \mathbf{x}_{b,i}^o = \mathbf{y}_i - \mathcal{H}_i(\mathcal{M}_{i,0}(\mathbf{x}_{b,0}))$ define the innovations. Similarly, the cost function J_L for lognormally-distributed variables is

expressed in terms of increments $\delta \mathbf{g}_0 = \ln \mathbf{x}_0 - \ln \mathbf{x}_{b,0}$ as

$$J_{L}(\delta \mathbf{g}_{0}) = \frac{1}{2} \delta \mathbf{g}_{0}^{T} \mathbf{B}_{L}^{-1} \delta \mathbf{g}_{0}$$

+ $\frac{1}{2} \sum_{i=1}^{N_{o}} \left(\mathbf{d}_{l,i} - \mathbf{O}_{L,i} \mathbf{H}_{i} \mathbf{M}_{i,0} \mathbf{X}_{L} \delta \mathbf{g}_{0} \right)^{T} \mathbf{R}_{L,i}^{-1}$
 $\left(\mathbf{d}_{l,i} - \mathbf{O}_{L,i} \mathbf{H}_{i} \mathbf{M}_{i,0} \mathbf{X}_{L} \delta \mathbf{g}_{0} \right), \qquad (2)$

where $\mathbf{d}_{l,i} = \ln \mathbf{y}_i - \ln \mathbf{x}_{b,i}^o = \ln \mathbf{y}_i - \ln(\mathcal{H}_i(\mathcal{M}_{i,0}(\mathbf{x}_{b,0}))))$. The diagonal matrices $\mathbf{O}_{L,i}$ and \mathbf{X}_L are introduced during the linearization of \ln and exp function (Song et al., 2016a) where specifically, $\mathbf{O}_{L,i} = diag[(\mathbf{x}_{b,i}^o)_1, (\mathbf{x}_{b,i}^o)_2, \ldots, (\mathbf{x}_{b,i}^o)_{m_i}]^{-1}$ and $\mathbf{X}_L = diag[(\mathbf{x}_{b,0})_1, (\mathbf{x}_{b,0})_2, \ldots, (\mathbf{x}_{b,0})_{n_l}]$. A total of m_i lognormallydistributed observations exist at $t = t_i$, and a total of n_l lognormal variables exist within the model.

The state vector increment in the coupled, physical and biological system is defined as $\delta \mathbf{z} = [\delta \mathbf{x}_0^T \ \delta \mathbf{g}_0^T]^T$. The state vectors for physical and biological variables have dimensions $(n_g \times 1)$ and $(n_l \times 1)$, respectively. Hence the size of $\delta \mathbf{z}_0$ is simply $(n \times 1)$, where $n = n_g + n_l$. Then a compact form of the cost 170 function can be written as

$$J(\delta \mathbf{z}_{0}) = \frac{1}{2} \delta \mathbf{z}_{0}^{T} \mathbf{B}^{-1} \delta \mathbf{z}_{0}$$

+ $\frac{1}{2} \sum_{i=1}^{N_{o}} \left(\mathbf{d}_{i} - \mathbf{O}_{i}^{-1} \mathbf{H}_{i} \mathbf{M}_{i,0} \mathbf{X} \delta \mathbf{z}_{0} \right)^{T} \mathbf{R}_{i}^{-1}$
 $\left(\mathbf{d}_{i} - \mathbf{O}_{i}^{-1} \mathbf{H}_{i} \mathbf{M}_{i,0} \mathbf{X} \delta \mathbf{z}_{0} \right), \qquad (3)$

where $\mathbf{d}_{i}^{T} = [\mathbf{d}_{g,i}^{T} \ \mathbf{d}_{l,i}^{T}], \ \mathbf{O}_{i} = diag[1, 1, \ldots, 1, (\mathbf{x}_{b,i}^{o})_{1}, (\mathbf{x}_{b,i}^{o})_{2}, \ldots, (\mathbf{x}_{b,i}^{o})_{m_{i}}]$ and $\mathbf{X} = diag[1, 1, \ldots, 1, (\mathbf{x}_{b,0})_{1}, (\mathbf{x}_{b,0})_{2}, \ldots, (\mathbf{x}_{b,0})_{n_{l}}]$. Error covariances **B** and \mathbf{R}_{i} consist of error covariances for physical and biological components and their cross covariances.

The gradient of $J(\delta \mathbf{z}_0)$ with respect to $\delta \mathbf{z}_0$ is given by

$$\frac{\partial J}{\partial \delta \mathbf{z}_0} = \mathbf{B}^{-1} \delta \mathbf{z}_0 - \mathbf{X}^T \sum_{i=1}^{N_o} \mathbf{M}_{0,i}^T \mathbf{H}_i^T \mathbf{O}_i^{-T} \mathbf{R}_i^{-1} \left(\mathbf{d}_i - \mathbf{O}_i^{-1} \mathbf{H}_i \mathbf{M}_{i,0} \mathbf{X} \delta \mathbf{z}_0 \right), (4)$$

and we seek a solution $\delta \mathbf{z}_0$ that satisfies $\partial J/\partial \delta \mathbf{z}_0 = 0$. The optimal $\delta \mathbf{z}_0$ is identified iteratively by applying a conjugate gradient descent algorithm using the Lanczos formulation (Moore et al., 2011c).

179 3. Experiment design for the coupled data assimilation system 180 evaluation

We evaluate the performance of the new system by comparing results from multiple data assimilation experiments with a free run. For clarity of description, we distinguish between the coupled nonlinear model and the coupled data assimilation system by referring to the former as the forward model with no data assimilation. The free run results exclusively from the integration of the forward model.

We perform three data assimilation runs: the physical data assimilation 187 (PDA) run, the biological data assimilation (BDA) run and the coupled 188 data assimilation (PBDA) run. In the PDA run, physical data are used to 189 constrain both physical and biological variables in the forward model. In the 190 BDA run, only biological data are used to constrain physical and biological 191 variables in the forward model. Third, both physical and biological data are 192 used to constrain the physical and biological variables in the coupled model, 193 and is referred to as the PBDA run. The PDA (BDA) applies Gaussian 194 (Lognormal) 4DVar to fit the coupled model to the data. The PBDA fits 195 both physical and biological data into the coupled model using a hybrid 196 Gaussian and lognormal 4DVar approach. 197

Some additional experiments were performed to better evaluate the im-198 pact of model dynamics within the coupled assimilative system. Specifically, 199 we modify the BDA experiment by reducing the control vector to include 200 only biological variables alone (BDAb) or physical variables only (BDAp). 201 Similarly, we consider the PDA experiment, but with adjustments to only 202 the physical (PDAp) or biological (PDAb) variables. While physical state 203 variables in the forward model clearly influence biological variables (e.g., 204 through transport and mixing), biological variables generally do not alter 205 physical variables in the forward model. In nature, chlorophyll pigments 206 quantitatively impact light absorption and thus heat flux within the water 207 column (Morel, 1988, Lewis et al., 1990, Frouin and Iacobellis, 2002, Mur-208 tugudde et al., 2002, Park et al., 2015), but this feedback is not included in 209 the present model implementation. As a result, any misfit with respect to 210 physical data cannot be reduced by adjusting the initial conditions of biolog-211

ical variables. Therefore, the physical data misfit is identical for PDAp andPDA, and for PDAb and the free run.

214 3.1. Model

We use a Nutrient-Phytoplankton-Zooplankton-Detritus (NPZD) biolog-215 ical model coupled to ROMS, a 3-dimensional ocean circulation model, con-216 figured for the California Current System. This implementation has been 217 applied repeatedly as a useful testbed for various developments of the ROMS 218 4DVar system (Broquet et al., 2009, 2011, Moore et al., 2011b,a). The model 210 domain extends from the middle of the Baja Peninsula to the Washington 220 coast and offshore to 137W. The horizontal model resolution is 1/30 degree, 221 and it includes 30 terrain-following levels in the vertical. The configuration 222 used here is identical to that testing the lognormal 4DVar in isolation and 223 described in Song et al. (2016a), which provides additional details of the 224 configuration, including the parameters used for the NPZD model. 225

Model twin experiments are an excellent way to evaluate the performance 226 of data assimilation schemes because the true state is known exactly and the 227 error statistics can be controlled. A 4-year forward simulation, begun on 228 January 1^{st} , 2001, represents the "true" ocean state. A data assimilated run 229 described by Broquet et al. (2009) provides the physical initial conditions. 230 Biological initial conditions were obtained from the final state of a 45-year 231 forward spin-up run described in Song et al. (2016a). Surface forcing and 232 boundary conditions were derived from the output of the Coupled Ocean 233 Atmosphere Mesoscale Prediction System (COAMPS) (Doyle et al., 2009) 234 and the Simple Ocean Data Assimilation (SODA) (Carton and Giese, 2008) 235 product, respectively. 236

Although real data is not used in the present experiments, we present an 237 evaluation of the forward simulation using satellite derived estimates of sea 238 surface temperature (AVHRR Pathfinder V5 SST, 0.44 degree resolution) 239 and surface chlorophyll-a (SeaWiFS, 0.036 degree resolution) obtained from 240 http://las.pfeg.noaa.gov/oceanWatch. Model chlorophyll is estimated using 241 a constant carbon to chlorophyll ratio of 50 g C (g chl)⁻¹ and a Redfield 242 ratio to convert model units of nitrogen to carbon. The model yields phyto-243 plankton bloom-like patterns, intensity and spatial distribution comparable 244 to satellite data (Song et al., 2016a). Monthly average fields are used to cal-245 culate the bias (model minus data), normalized by the standard deviation, 246 and correlation coefficient (Figure 1). The standard deviation is estimated 247 at each grid cell using the output from the model spin-up. Although SST in 248 the simulation has a warm bias overall $(1 \, ^{\circ}C)$, the correlation coefficient (r)249 is very high ($\bar{r} = 0.92$), indicating a good representation of the annual cycle 250 in the model. Surface chlorophyll-a is biased low offshore and very near the 251 coast north of 44°N, and biased high along the northern and central Cali-252 fornia coast out into the coastal transition zone (Brink and Cowles, 1991). 253 On average, the model is biased low by approximately 0.5 mg m^{-3} . The 254 correlation coefficient for chlorophyll-a reveals generally positive values over 255 the whole domain. 256

257 3.2. Data

Physical and biological data are sampled from the true state. SSH and SST are observed at all grid points once per day (we assume no data dropouts due to cloud cover). In situ temperature and salinity profiles are obtained at times and locations based on the EN3 data set (Ingleby and Huddleston,

2007), which includes observations from the California Cooperative Fisheries 262 Investigations (CalCOFI) surveys, as well as Argo and glider data within 263 our model domain. For biological assimilation, only surface phytoplankton 264 is used, analogous to what might be obtained under cloud-free conditions 265 from satellite ocean color data. We note that our data collection for surface 266 fields is larger than occurs in nature (approximately 13% data coverage on 267 our model domain in the year 2000), but allows investigation of a best-case, 268 data-rich scenario. Assimilation of real data is performed in Song et al. 269 (2016b)270

Observation errors are added to the sampled data. Errors for physical 271 variables are drawn from normal random distributions ($\mathcal{N}(0, 0.1^2), \mathcal{N}(0, 0.01^2)$), 272 $\mathcal{N}(0, 0.02^2)$ and $\mathcal{N}(0, 0.1^2)$ for in situ temperature, salinity, SSH and SST, 273 respectively). The observational error levels for in situ temperature, salin-274 ity and sea surface height were adopted from Broquet et al. (2009), where 275 the same data assimilation system was used to fit the data in the same 276 domain. The observational error level for SST is close to the global stan-277 dard deviation of errors (0.13K for AVHRR) (O'Carroll et al., 2012). Errors 278 in phytoplankton biomass data were drawn randomly from $\mathcal{N}(0, 0.2^2)$ and 279 added in log-transformed space. This distribution approximately corresponds 280 to a 20% multiplicative error which is lower than uncertainty estimates for 281 global chlorophyll data (Gregg and Casey, 2004, Moore et al., 2009). We also 282 consider sensitivity experiments in which the observational error for SST is 283 elevated to 0.4° C and for phytoplankton is increased to 35% and 50%. 284

285 3.3. Assimilation setup

Following the method presented in Weaver and Courtier (2001), the back-286 ground error covariance is factorized as $\mathbf{B} = \Sigma \mathbf{C} \Sigma^T$, where Σ is a diagonal 287 matrix whose diagonal elements are model standard deviations and \mathbf{C} is 288 a correlation matrix. Standard deviations are computed from the 4-year 289 forward simulation. The background error covariance \mathbf{B}_L is for $\ln \mathbf{x}$, and 290 therefore biological variables should be log-transformed before computing 291 the standard deviation. The correlation matrix \mathbf{C} is obtained through so-292 lution of a diffusion equation (Weaver and Courtier, 2001), and we apply 293 horizontal and vertical length scales of 50 km and 30 m, respectively. It is 294 reasonable to expect that in general physical and biological variables have 295 different decorrelation length scales; for example, Lagrangian measurements 296 in offshore portions of the CCS reveal different decorrelation time-scales for 297 chlorophyll-a and temperature by Abbott and Letelier (1998). In this study, 298 we assume that the length scales are identical. Song et al. (2016b) discuss 299 the requirements of a smaller vertical decorrelation length scale for biological 300 variables than physical variables in the fully realistic assimilation scenario. 301

The set of experiments proceeds in sequences of 5-day assimilation cycles. Although Veneziani et al. (2009) has shown that the tangent linear assumption in the physical model is reasonable over a time-scale of 14 days, a shorter time-scale is required for biological models due to the inherent nonlinearities of the biological interactions. Song et al. (2016a) find that a time-scale of 5 days is reasonable for the NPZD model and the California Current System implementation.

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We examine the coupled assimilative system over the 4-year period 2001–

2004, divided into 48, 30-day experiments. Every 30-day experiment consists 310 of 6 sequential assimilation cycles, each extending for 5-days. The initial con-311 dition on the first day of each experiment is the 4-year mean state obtained 312 for that particular day obtained from the true run. Within each experiment, 313 the state estimate at the end of one cycle is used to initialize the background 314 estimate for the next 5-day cycle. In our analysis, the first cycle of each ex-315 periment is treated as a spin-up cycle when the linear approximation is the 316 least accurate (Song et al., 2016a) and not included in the statistical results. 317 Although we recognize that cross-covariances between model variables 318 exist, we calculate univariate correlations only, and we assume that obser-319 vation errors are independent and uncorrelated. These assumptions simplify 320 the construction of error covariances \mathbf{B} and \mathbf{R}_i , with 321

$$\mathbf{B} = \begin{bmatrix} \mathbf{B}_G & \mathbf{0} \\ \mathbf{0} & \mathbf{B}_L \end{bmatrix}$$
(5)

322 and

$$\mathbf{R}_{i} = \begin{bmatrix} \mathbf{R}_{G,i} & \mathbf{0} \\ \mathbf{0} & \mathbf{R}_{L,i} \end{bmatrix}.$$
(6)

For simplicity, we take this highly simplified approach but acknowledge that accurate cross-correlations between model variables should yield additional improvements in coupled biological and physical state estimation.

The reformulation of lognormal 4DVar to the quadratic cost function creates an additional linearization approximation. The logarithmic transformation of the model state in observation space is linearized using Taylor series whose necessary condition is that the difference between the model state and observations is small. In order to satisfy this condition, we filter observations ³³¹ such that those more than twice the modeled state are excluded from the as³³² similation procedure (Song et al., 2016a). While this procedure reduces the
³³³ total number of assimilated observations it helps ensure the stability of the
³³⁴ data assimilation calculations.

We also perform sensitivity experiments for the year 2001 to understand 335 how increased observational error and the ability of the model to represent 336 truth impact results. We consider experiments in which either or both SST 337 and phytoplankton observational error are increased from their original val-338 ues. In addition, the coupled data assimilation system is examined after 339 purposely introducing model error. Physical model error is introduced by 340 applying surface forcing from the year 2002, and biological model error is 341 obtained by applying different biological parameter values than the reference 342 run. Those parameters are listed in Table 1. Physical and biological model 343 errors are included in the assimilative runs either separately or jointly. 344

³⁴⁵ 4. Performance of the coupled data assimilation system

346 4.1. The improvement in the Root-mean-squared error

Performance is first evaluated using the root-mean-squared error (RMSE). 347 RMSEs for surface physical variables – zonal velocity (u), meridional veloc-348 ity (v), SST, and SSH – are significantly improved by coupled assimilation 349 of physical variables (PDA) (Figure 2). Using the forward model provides 350 better prediction skill than persistence, but assimilating physical observa-351 tions further decreases RMSE. The mean error reduction from the free run 352 for physical variables is approximately 56% with improvement in both ob-353 served variables (SST and SSH) and unobserved variables (u and v). RMSE 354

reduction is larger for observed variables than in unobserved variables, as ex-355 pected. Coupled assimilation of biological data (BDA) also decreases RMSE 356 for physical variables by about 13% from the free run on average, indicat-357 ing that surface phytoplankton observations can improve initial conditions 358 for current, SSH and SST entirely through the dynamics of the coupled sys-359 tem. Tracers are influenced by advection and diffusion, and because the 360 adjoint model includes these coupled dynamics, cost function reduction can 361 be achieved through alteration of physical as well as biological variables. 362

RMSE reduction is greatest, approximately 57% on average with respect 363 to the free run, when assimilating both physical and biological data (PBDA). 364 The modest improvement over PDA indicates that the physical fields are 365 most constrained by the physical data provided in this experiment. It is 366 noted that PBDA does not always lead to the improvement over PDA. The 367 RMSE of PDA for SSH is slightly lower than what PBDA offers, but within 368 the error bars $(0.980 \pm 0.017 \text{ cm} \text{ versus } 0.985 \pm 0.014 \text{ cm})$. In a case of SST, 360 PBDA has lower RMSE $(0.310 \pm 0.006 \text{ °C})$ than PDA $(0.314 \pm 0.006 \text{ °C})$, but 370 again within error bars. Although the improvement by PBDA over PDA is 371 statistically marginal for u and v, it is negligible compared with the RMSE 372 reduction from the free run to PDA. 373

PDA and PBDA reduce the RMSEs for the observed variables (SST and SSH) more than half almost everywhere (Figure 3(c,d,k,l)). Although the reduction of RMSE by BDA is less than 20%, BDA reduces the RMSE of SST and SSH over the entire region (Figure 3(g,h)). Surface currents are not assimilated, and RMSE reduction in those variables is smaller than for SST or SSH. There are regions even with the increased RMSE. For instance, PDA shows approximately 20% higher RMSE for u near the coast between 40°N and 45°N (Figure 3(a)). Although the RMSE reduction for u and v by BDA is smaller than for PDA, it occurs over the all model domain (Figure 3(e,f)). PBDA yields the best estimate of surface currents, resulting in the smallest RMSE. Interestingly, the increased RMSE for u by PDA in Figure 3(a) became less obvious when assimilating both physical and biological observations.

Forward simulation of the NPZD model improves the estimation of bi-387 ological variables as the RMSEs of the free run are smaller than the result 388 from one-month persistence. Assimilating data provides a better estimate 389 for biological variables, further reducing the RMSEs for biological variables 390 with respect to the free run. In BDA, incorporating surface phytoplank-391 ton data improves the estimate of not only phytoplankton but also other 392 unobserved biological variables. RMSE reduction of biological variables is 393 approximately 43% on average with respect to that by the free run. PDA 394 also improves the estimate of biological variables by approximately 7%, and 305 this improvement results not from the adjustment of biological initial con-396 ditions but from the improved representation of the circulation fields. As 397 described above, biological variables are passively coupled to the currents, 398 and therefore the sensitivity of the misfits in physical variables to variations 399 in the biological variables is zero. Improvements in T, S and SSH cannot be 400 reduced by changes in biological variables at the initial time. As in the eval-401 uation of physical variables, greatest RMSE reduction ($\sim 49\%$ on average) 402 for biological variables occurs through coupled assimilation of both physical 403 and biological data (PBDA), and this reduction is statistically significant. 404

Assimilating physical variables leads to mixed effects on the biological 405 state estimation at the surface. Figure 5(a-d) show that PDA has a pos-406 itive effect near the coastal regions but generally degrades the biological 407 estimation offshore. Changes in RMSEs by PDA are similar in overall mag-408 nitude for all four biological variables. BDA and PBDA result in comparable 409 RMSE reduction (Figure 5(e-l)). Largest RMSE improvement using these 410 two methods occurs for phytoplankton, the observed variable. The second 411 largest reduction in RMSE is seen in detritus. RMSE reduction for P and 412 D occurs throughout the model domain. The improvements in zooplankton 413 by BDA and PBDA occur mainly near the coast (Figure 5(f,j)). Least im-414 provement is found in the nutrient estimation, and it is visually similar to 415 the improvement by PDA (Figure 5(c,g,k)). 416

We note that although overall error decreases in all variables, there are 417 limited regions where the RMSE increases after assimilating surface phyto-418 plankton, even in PBDA. Such error increases occur most visibly in Z and 419 N, but also at one location in D (Figure 5(f,g,j,k)). The NPZD model is a 420 simple but highly nonlinear system, sometimes stretching the linear approx-421 imation used in 4DVar systems. In such cases, the increments can degrade 422 the posterior estimate. Although this is not limited to our assimilation sys-423 tem, it is possible that degrading increments can be amplified due to the 424 transformation back to the original space using the exponential function. 425 We note that the limited areas of degradation occur for unobserved vari-426 ables only, indicating that the system improves the phytoplankton estimates 427 through occasionally unrealistic changes to variables for which we have no 428 information other than background error statistics. Such performance is not 429

surprising in an estimation system, and generally could be improved through
observation of other ecosystem elements.

Two additional experiments outlined above better illustrate how modeled 432 dynamics in coupled data assimilation influence the final state estimate. In 433 BDAb, biological data is assimilated but only biological variables are ad-434 justed. In this case, RMSE in biological fields is reduced by approximately 435 35% on average (not shown), less than the reduction by BDA with adjust-436 ments to all variables. In BDA, the coupled data assimilation system parti-437 tions improvements to both physical and biological variables. Adjusting only 438 biological fields limits the quantitative improvement in biological fields over 439 the full assimilation cycle relative to what can be achieved through adjust-440 ment also of physical fields. RMSE reduction in physical variables is zero in 441 BDAb because adjusted biological variables do not affect the physical fields. 442 In BDAp physical variables only are adjusted, and misfits in biological 443 variables can be reduced only through improvement in circulation and mix-444 ing. Although the phytoplankton biomass RMSE is reduced in this case. 445 assimilation generally degrades the estimates of other variables (not shown). 44F In particular, physical variables are adjusted such that their RMSEs are 447 larger than in the free run. While the misfit in observed variables can be re-448 duced through modification of various fields through coupled dynamics, not 449 all adjustments result in a better overall estimate of the unobserved variables. 450

451 4.2. The improvement in the statistical states

⁴⁵² Model performance can be visualized also through a Taylor diagram which ⁴⁵³ summarizes the model variability relative to the truth, specifically the corre-⁴⁵⁴ lation coefficient and standard deviation (Taylor, 2001). PDA (square termi-

nator) and PBDA (circular terminator) show substantial improvements in all 455 three statistics relative to the prior, especially in observed variables (SST and 456 SSH) (Figure 6). Unobserved u and v are also statistically improved when 457 physical data are assimilated. For both PDA and PBDA, physical variables 458 show about the same amount of variability as the true state, and posterior 459 correlation coefficients are greater than 0.8. Statistically, the improvements 460 realized by the PDA and PBDA are comparable, implying that physical ob-461 servations in this case provide sufficient information for the optimal physical 462 solution. In BDA (triangular terminator), the statistics of the physical vari-463 ables are also improved, with the posterior located closer to the reference 464 point than the line origins for u, v and SSH, although the improvements 465 are not as large as for PDA and PBDA. Chlorophyll and ocean currents are 466 strongly coupled in the advection/diffusion equation while temperature does 467 not appear in the equations for NPZD model. Hence, chlorophyll observa-468 tions have a more substantial impact on u, v and SSH. 460

In the right panel in Figure 6, results from BDA and PBDA indicate im-470 provements in the statistics for all biological variables. As expected, phyto-471 plankton, the observed variable, exhibits the greatest improvement, showing 472 a normalized standard deviation close to 1 and correlation coefficient greater 473 than 0.9. The statistics of the unobserved variables are also improved, al-474 though not as much as for P. Improvements in the biological error statistics 475 from BPDA are greater than those for BDA, and more so than improvements 476 in the physical error statistics by PBDA over PDA; this result indicates again 477 the significant role that the physical state has on biological fields but not the 478 reverse. Results from PDA show the least improvement in biological vari-479

480 ables.

481 4.3. Sensitivity to observational errors

The performance of data assimilation is dependent on the error levels. We 482 conduct a sensitivity test with varied observational error levels for SST and 483 phytoplankton. When observational error for SST is increased from 0.1°C 484 to 0.4° C, the RMSE for SST is elevated by approximately 50% (PDA(0.1, 485 N/A) versus PDA(0.4, N/A) in Figure 7). Higher SST observational error 486 also influences the estimation of surface currents and SSH, increasing RM-487 SEs more than 20%. The RMSEs for physical variable are less sensitive to 488 the phytoplankton observational error (BDA(N/A, 20%)) versus BDA(N/A, 20%)) 489 35%) versus BDA(N/A, 50%) in Figure 7). BDA reduces the RMSEs for 490 physical variables with respect to the free run even when the phytoplankton 491 observational error level is 50%. The sensitivity of PBDA to the observa-492 tional error can be considered as the mixed response of PDA and BDA to 493 the changes in observational error for SST and phytoplankton, respectively 494 (PBDA(0.1, 20%) versus PBDA(0.4, 35%) versus PBDA(0.4, 50%) in Figure 495 7). 496

Changing observational error for SST does not provide a statistically 497 significant impact on the RMESs for biological variables (PDA(0.1, N/A)) 498 versus PDA(0.4, N/A) in Figure 8). Higher phytoplankton observational 499 error degrades the estimation of phytoplankton by elevating the RMSE by 500 more than 15%, which is statistically significant (BDA(N/A, 20\%)) versus 501 BDA(N/A, 35%) versus BDA(N/A, 50%) in Figure 8). Other biological 502 variables do not have the influence of higher phytoplankton observational 503 error as much as phytoplankton, showing less than 10% RMSE increase. As 504

for physical variables, the sensitivity of PBDA to the observational error 505 can also be viewed as the mixed response of PDA and BDA to the changes 506 in observational error for SST and phytoplankton (PBDA(0.1, 20%)) versus 507 PBDA(0.4, 35%) versus PBDA(0.4, 50%) in Figure 8). It is noted that higher 508 phytoplankton observational error does not always degrade the estimation for 509 the biological variables. For instance, BDA(N/A, 50%) shows smaller RMSE 510 for P than BDA(N/A, 35%). We attribute this to the observation filtering 511 process discussed in subsection 3.3. More outlying observations are rejected 512 in BDA(N/A, 50%) than in BDA(N/A, 35%), and eventually the filter helps 513 the data assimilation run fit observations better, leading to smaller RMSE. 514

515 4.4. Sensitivity to the model errors

The performance of coupled physical and biological data assimilation is 516 also evaluated under the presence of model errors. In this sensitivity test, 517 the control run is PBDA with 0.4° C and 35% observational errors for SST 518 and phytoplankton, respectively. We refer to EF as error free, EP as error in 519 physics (in which the wrong year's surface forcing has been introduced), EB 520 as error in biology (with different NPZD model parameters than the reference 521 run), and EPB as error in physics and biology. PBDA results in higher 522 RMSEs in the observed variables, SST and SSH, when the surface forcing of 523 the year 2002 is used in the assimilative run for the year 2001, but RMSEs 524 are still considerably lower than that of the free run in which no model 525 error is included (PBDA, EF versus PBDA, EP in Figure 9). However, the 526 introduced physical model error degrades the estimation of surface currents: 527 RMSEs of PBDA, EP for u and v are greater than that of the free run with 528 no model error. The impact of biological model error to physical variables 529

is not statistically significant. Using incorrect biological parameter values in
PBDA does not change RMSEs for all physical variables (PBDA, EP versus
PBDA, EPB in Figure 9).

Estimating the biological state can be influenced by both physical and 533 biological model errors. Using the wrong forcing degrades the estimate of 534 biological variables, leading higher RMSEs (PBDA, EF versus PBDA, EP in 535 Figure 10). The degradation is particularly strong for N and D, resulting in 536 higher RMSEs than those from the free run. The introduced biological model 537 error also has statistically significant impact on the estimation of biological 538 variables. Using wrong parameter values and surface forcing increased the 539 RMSE for phytoplankton, although it is still slightly smaller than that from 540 the free run with no model error (PBDA, EF versus PBDA, EP versus PBDA, 541 EPB in Figure 10). However, our model errors result in higher RMSEs for 542 unobserved biological variables. Including both physical and biological errors 543 makes the RMSEs for Z, N and D greater with respect to the free run. The 544 most substantial impact is observed in Z and is perhaps results from the fact 545 that two of four modified parameters are associated with the zooplankton 546 dynamics. 547

The incremental form of 4DVar used here does not allow easily for the accurate computation of posterior error estimates. The posterior error covariance is equivalent to the inverse of Hessian matrix (Moore et al., 2012). Here, the inverse of Hessian matrix is estimated as $\mathbf{VT}^{-1}\mathbf{V}^{T}$, where \mathbf{V} is the orthogonal matrix with Lanczos vectors, and \mathbf{T} is the symmetric tridiagonal matrix that contains coefficients in Lanczos recurrence relation (Song et al., 2016a). The Hessian matrix is approximated by a tridiagonal factorization

using the Lanczos vectors, and represents a reduced approximation. The 555 leading eigenvectors of the Hessian matrix can be estimated from the Lanc-556 zos vectors but these would represent the smallest eigenvectors of the analysis 557 error covariance. Therefore, this calculation provides a poor representation of 558 the analysis error covariance matrix. One can consider other effective meth-559 ods (e.g. Daescu and Navon, 2007, a reduced second order adjoint model) 560 for the estimation of Hessian, but the inverse of the Hessian matrix is still 561 approximated with the least important orthogonal vectors. We note that 562 that ROMS does provide options to estimate the posterior error covariance 563 in dual form (Moore et al., 2012), but that is not the form used in this study. 564

565 5. Summary and Discussion

We have developed and investigated combined physical and biological 4-566 dimensional variational data assimilation in an ocean model. Biological data 567 assimilation benefits from a unique approach because of the non-Gaussian 568 statistics of biological variables and their errors. We have assumed lognor-560 mal statistics for these variables and applied the quadratic formulation of the 570 incremental approximation developed by Song et al. (2016a). Assimilation 571 of variables having different error statistics is required for combined physi-572 cal and biological assimilation and proceeds here following the approach of 573 Fletcher (2010) and Fletcher and Jones (2014). 574

In model twin experiments using ROMS and a 4-component, NPZD ecosystem model configured for the realistic California Current System, we investigated how coupled biological and physical data assimilation improves overall estimates of the combined physical and biological ocean state. Ob-

servations were drawn from a forward model run which represented the true 579 ocean state with errors drawn from distributions with known statistics added. 580 Three observation sampling strategies were chosen: (1) biological observa-581 tions, (2) physical observations, and (3) both biological and physical ob-582 servations. Then we altered the model state through adjustment of initial 583 conditions in physical and/or biological variables using those observations. 584 Statistics of RMSE, correlation coefficients, state variability were analyzed 585 from a total of 48 sequences of six 5-day assimilation cycles. 586

We found that assimilation of physical data (PDA) improves model-data 587 misfit of physical variables, and assimilation of biological data (BDA) re-588 duces model error for biological variables. Such results should be expected. 589 In addition, PDA resulted in biological error reduction, and BDA yielded 590 improvements in the physical variable misfit. Even though PDA has no ef-591 fect on biological initial conditions, it does influence biological variables over 592 the entire assimilation cycle through improvements to the physical fields 593 which then feed back on biological variables through tangent linear (and 594 forward) model advection and diffusion. In contrast, a change in biological 595 initial conditions, for example resulting from BDA, has no influence on phys-596 ical variables through the forward model directly. However, BDA influences 597 physical variable initial conditions through coupled dynamics included in the 598 adjoint model. The coupled data assimilation system partitions changes to 590 all control vector elements that can reduce error in the biological data misfit, 600 and this partitioning extends to both biological and physical variables. This 601 conceptual division of influence is drawn schematically in Figure 11. 602

603

Overall, the greatest performance in both physical and biological fields

as quantified by various measures resulted from the combined assimilation of 604 physical and biological data (PBDA), further supporting the interpretation 605 of the PDA and BDA results. While physical observations provide the most 606 effective constraint for physical variables, and biological observations most 607 constrain biological variables, additional improvement in physical variables 608 derived from biological information through model adjoint dynamics and bi-609 ological errors can be reduced through physical observations via the tangent 610 linear (and forward) model. Higher observational errors in SST and phyto-611 plankton increase the RMSEs of PBDA, but the increase is smaller than the 612 combined increments in RMSE of PDA with higher SST observational er-613 ror and of BDA with higher phytoplankton observational error. Introducing 614 model errors (through the application of incorrect surface forcing or altered 615 biological parameters) also degrades the performance of PBDA, but its im-616 pact on PBDA is not particularly different from that for PDA and BDA on 617 a monthly time scale. 618

More generally, variables in a coupled 4DVar system can be influenced 619 in two ways, dynamically through the adjoint and tangent linear models 620 and statistically through covariances of the background error covariance ma-621 trix. In this study, univariate spatial correlations in fields were assumed 622 through the integration of a diffusion equation; however, no multivariate 623 correlations were represented, and therefore all improvements resulting from 624 observations of coupled variables resulted exclusively from adjoint and tan-625 gent linear model dynamics. These coupling dynamics are not included in 626 alternate data assimilation approaches based on statistical estimation alone, 627 and statistical correlations between physical and biological variables provide 628

the only way to transfer this critical information. These correlations are not 629 well-known in nature, though some groups have reported such information 630 (Behrenfeld et al., 2006), and estimates that are consistent with the ocean 631 circulation and in principle ecosystem models can be calculated from forward 632 model calculations (Shulman et al., 2013). Ensemble-based data assimilation 633 approaches use the ensemble to estimate time-dependent correlations (Simon 634 et al., 2015), usually with an inflation factor and localization to compensate 635 the effects of having a small ensemble. We would expect that the present 636 4DVar assimilation approach would further benefit from better background 637 error covariance estimates, a subject for future study. 638

The variational approach to coupled dynamics with mixed statistics pre-639 sented here is conceptually straightforward to implement within any existing 640 coupled system equipped with tangent and adjoint models and assuming no 641 multivariate correlations between physical and biological variables. The com-642 putational cost of the combined physical and biological system is comparable 643 to the cost of either the physical or biological system in isolation. Results 644 from this study suggest that coupled assimilation using 4DVar is practical 645 and realizable. However, the twin experiment framework used here repre-646 sents an idealized setting in which the data is unencumbered by cloud cover 647 and the model surface forcing and boundary conditions are error free. 648

Our conclusions are drawn based on the ensemble of 30-day assimilation (6 cycles). It is possible that the model may drift from the truth if biases are introduced by assimilation and accumulate over time scales longer than one month. In our ideal twin experiment, error is introduced in the initial conditions only and estimating accurate initial conditions always improves the model bias. Indeed, the model bias does not increase for more than 6 months when we tested the data assimilation system using 48 cycles (not shown). However, in realistic scenarios in which errors in surface forcing, boundary forcing, and model construction exist, it is possible that model bias develops more rapidly. Such an issue does not appear in Song et al. (2016b), but further studies of model bias in realistic scenarios over long periods of time is warranted.

When assimilating real observations, the presented assimilation system 661 may encounter obstacles. For instance, the model dynamics inevitably mis-662 represent or entirely miss important processes in nature. Under these circum-663 stances, adjustments to the initial conditions determined by model dynamics 664 are of limited value in matching observations. Large differences between the 665 observed and prior state can also create an issue because they violate the 666 linearization of log-transformation function and may prevent solution con-667 vergence. In order to prevent this outcome, the coupled assimilation system 668 requires a filtering process that excludes observations far from the prior. The 660 filtering process may reduce the number of observations, but it stabilizes the 670 assimilation system and may lead to a better posterior solution as shown 671 in subsection 4.3. We note that the filtering procedure is reevaluated during 672 each outer loop of the assimilation system, and observations that are rejected 673 initially may be included in the final outer loop. 674

In a companion paper Song et al. (2016b), we investigate the assimilation system's performance in a more realistic system in which real remotely sensed and in situ physical and ecosystem data are assimilated. In that realistic setting, improvements to RMSE for physical variables is not improved

by assimilating real chlorophyll observations. Several factors may account 679 for this result that stands in contrast to that offered by the twin experi-680 ments here. Data availability is reduced relative to this study as frequent 681 cloud cover prevents collection of SST and chlorophyll data over much of our 682 domain. In addition, physical and biological model error are likely greater 683 than that considered in the present study. Even though the real assimila-684 tion experiment is carried out on a higher resolution grid that better resolves 685 the CCS mesoscale circulation, the physical model is still imperfect relative 686 to nature. The NPZD ecosystem model used is advantageous for its rela-687 tive simplicity, and has been applied to multiple realistic studies of ocean 688 biogeochemistry, including in the CCS (Powell et al., 2006). However, with 689 only one phytoplankton functional group, it is less than ideal in representing 690 the multiple phytoplankton communities in different geographical regions of 691 the CCS. Assimilation improvements may result from application of a more 692 complex biogeochemical model. At this time, we do not know which of 693 these elements is responsible for the differences between the two studies, but 694 the present study shows that under excellent conditions in which a model 695 is nearly able to represent truth and observations are abundant, the lowest 696 RMSE for physical and biological variables results from assimilation of both 697 biological and physical variables into the coupled system. 698

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Table 1: A list of parameters for the NPZD model that is chosen differently in the assimilation runs to include the biological model error. The columns from the left to the right represent names, units, values in the true run and values for biological model error, respectively. The parameter values for the biological model error are from the study for Gulf of Alaska in Fiechter et al. (2011).

Parameter name	unit	Value, True	Value, EB
Uptake rate for nitrate	day^{-1}	1.0	0.8
Zooplankton grazing rate	day^{-1}	0.65	0.4
Ivlev constant	Dimensionless	0.4	0.84
Detritus remineralization rate	Dimensionless	0.1	0.2

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Figure 1: Normalized bias of the simulated (a) SST and (c) surface chlorophyll that are assumed as the truth in a twin experiment, and their correlation coefficients (b, d). Monthly mean values from the model and the satellite observation AVHRR (SeaWiFS), as the reference states for SST (surface chlorophyll), are considered in the calculation.



Figure 2: Root-mean-squared error (RMSE) of u, v, SST and SSH at the surface in the four different simulation: Free run (blue), analysis by the PDA (light blue), analysis by the BDA (white), analysis by the PBDA (light red). Red bar represents the one-month persistence RMSE. Error bars represent standard error from 1200 days (25 days \times 12 months \times 4 years).



Figure 3: The ratio of the physical variables' RMSEs between data assimilation runs and free run. Smaller than 1 (cold colors) represents the reduction of the RMSE while larger than 1 (warm colors) corresponds to the increased RMSE. White areas with the value 1 mean no change in the RMSE. Top, middle and bottom rows are for PDA, BDA and PBDA, respectively, and the columns represent u, v, SST and SSH from the left to the right.



Figure 4: Same as Figure 2, but RMSE of P, Z, N and D at the surface.



Figure 5: Same as Figure 3, but RMSE of P, Z, N and D at the surface.



Figure 6: Taylor diagram showing the improvements of three statistical values in (left) physical and (right) biological variables. Each line shows the statistical improvement by data assimilation. The dots represent the statistical states of the prior solution, and square, triangular and circular terminators represent the statistical states of the posterior solution from PDA, BDA and PBDA, respectively. Physical variables on the right panel include u (blue), v (cyan), SST (dark green) and SSH (red). On the right panel, lines represent P (blue), Z (cyan), N (dark green) and D (red). Black dots represent the reference or true states.



Figure 7: The RMSEs for u, v, SST and SSH (from the left to the right) in the year 2001. The RMSEs at the bottom are from the free run, overlaid by RMSEs from data assimilation runs whose observational errors for SST and phytoplankton are indicated in the parenthesis. For example, PBDA(0.4, 50%) is the data assimilation run where the SST and phytoplankton observational errors are 0.4°C and 50%, respectively. 'N/A' indicates that the corresponding observation is not assimilated.



Figure 8: Same as Figure 7, but for P, Z, N and D.



Figure 9: The RMSEs for u, v, SST and SSH (from the left to the right) in the year 2001. The RMSEs at the bottom are from the free run with no model error, overlaid by RMSEs from data assimilation runs whose observational errors for SST, phytoplankton and the label associated with the model error are indicated in the parenthesis. The labels 'EF', 'EP' and 'EPB' represent 'Error Free', 'Error in Physics' and 'Error in Physics and Biology', respectively. The physical model error is introduced by using surface forcing of the year 2002, and the biological model error comes from different biological parameter values in the assimilation runs (Table 1).



Figure 10: Same as Figure 9, but for P, Z, N and D.



Figure 11: Diagram that shows the flow of the information from observations. Physical observations (Obs.) provide the information to adjust the physical initial condition (IC). This information is spread to biological variables through advection and diffusion. Biological observations provide the information to adjust both physical and biological initial condition. This is because the dynamics in the adjoint model pass the information only from biological component to physical component in the coupled system used in this study.