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This is the author manuscript accepted for publication and has undergone full peer review but has not been through the copyediting, typesetting, pagination and proofreading process, which may lead to differences between this version and the Version of Record. Please cite this article as doi: 10.1002/qj.3423

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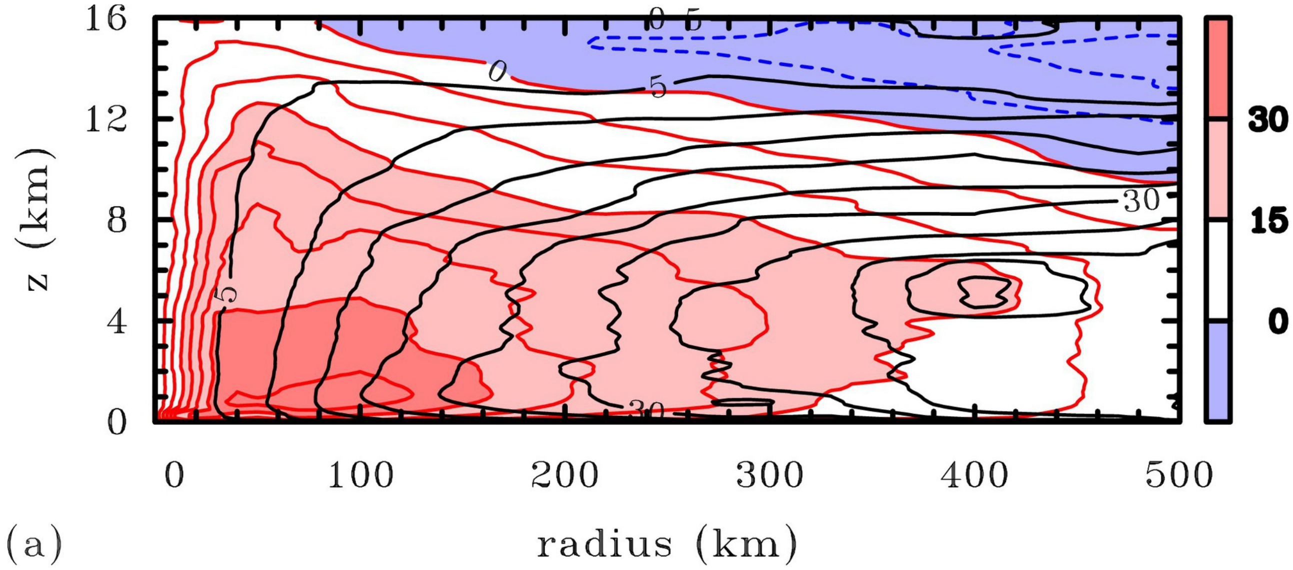

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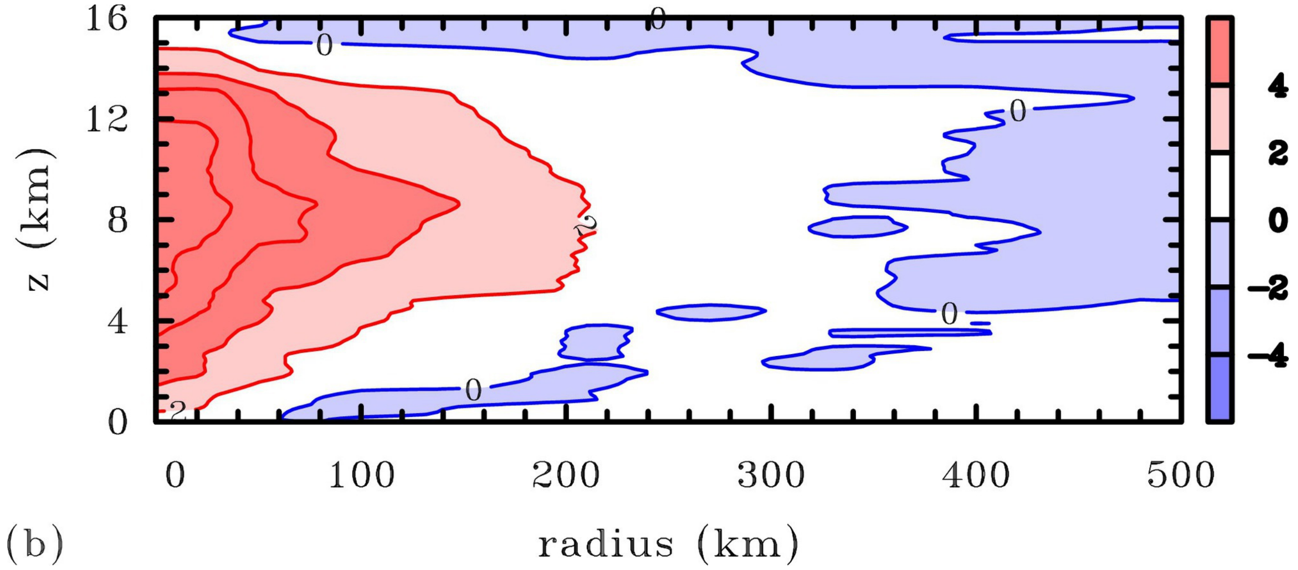

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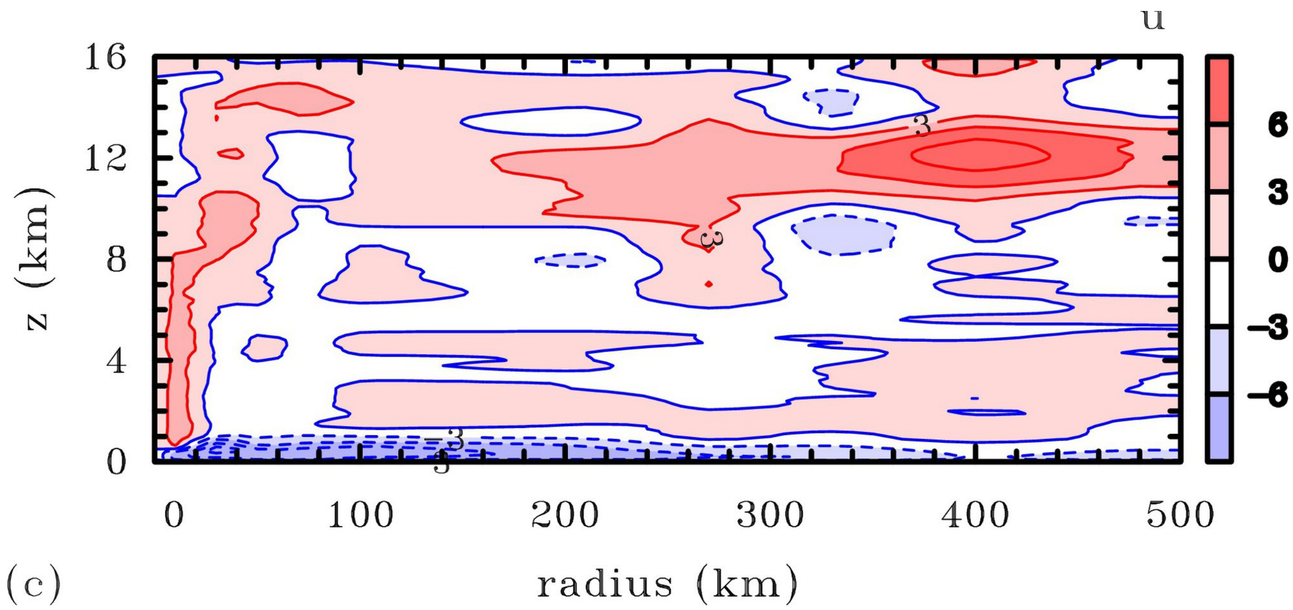

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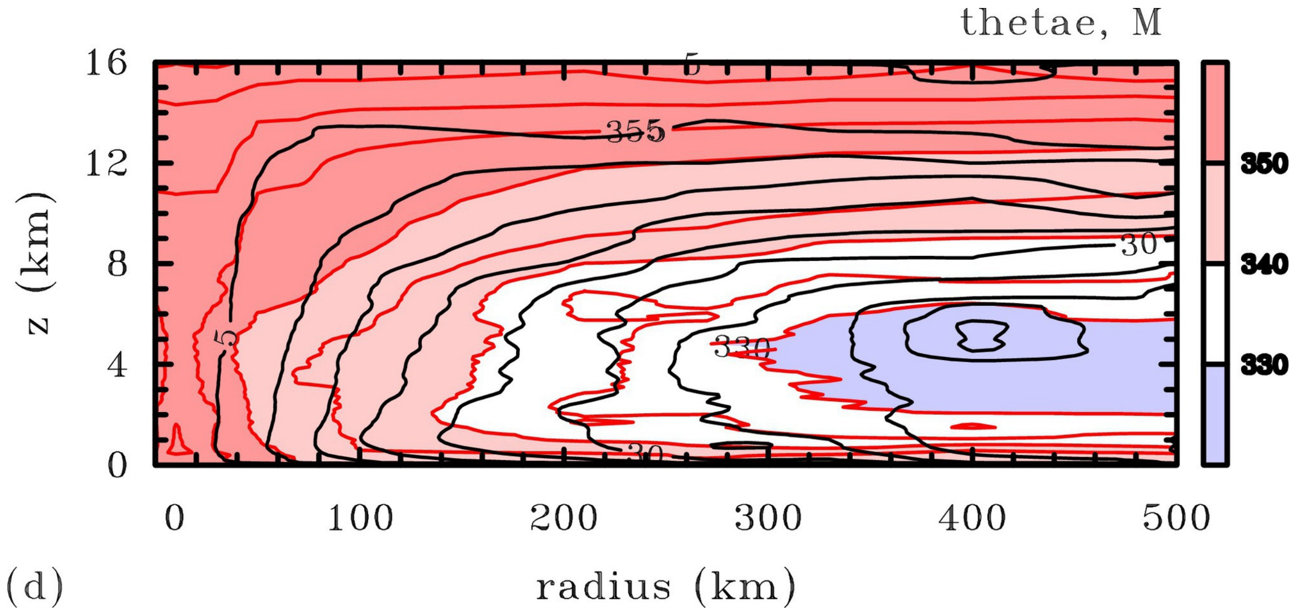

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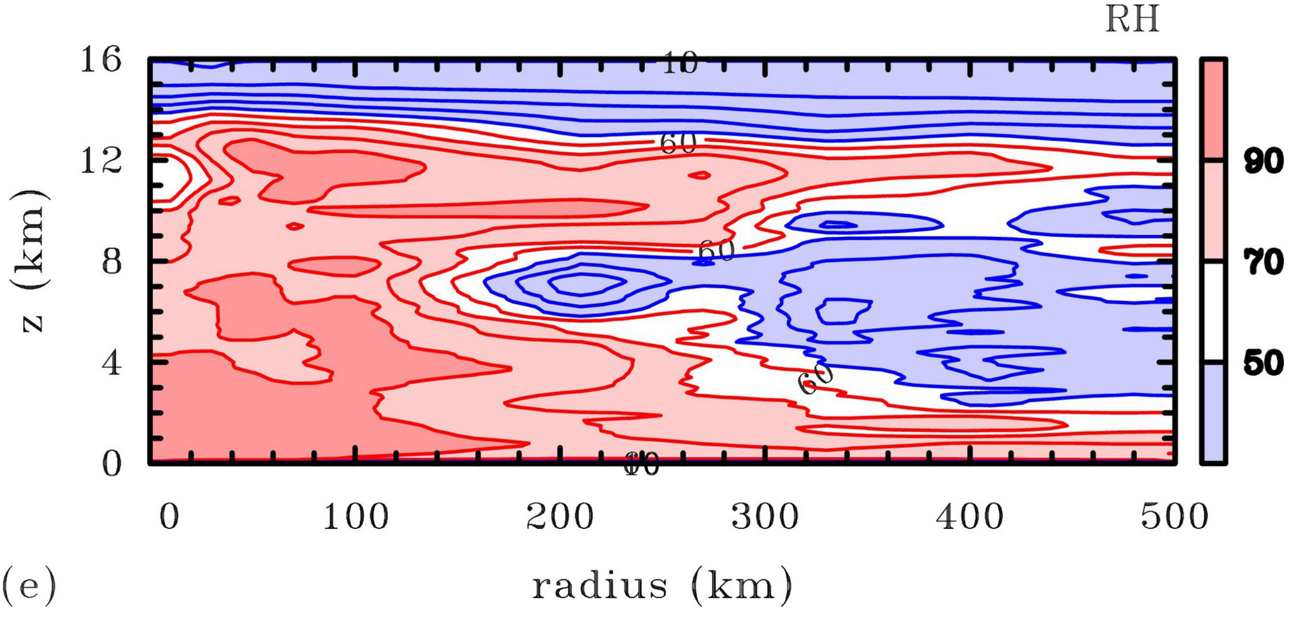

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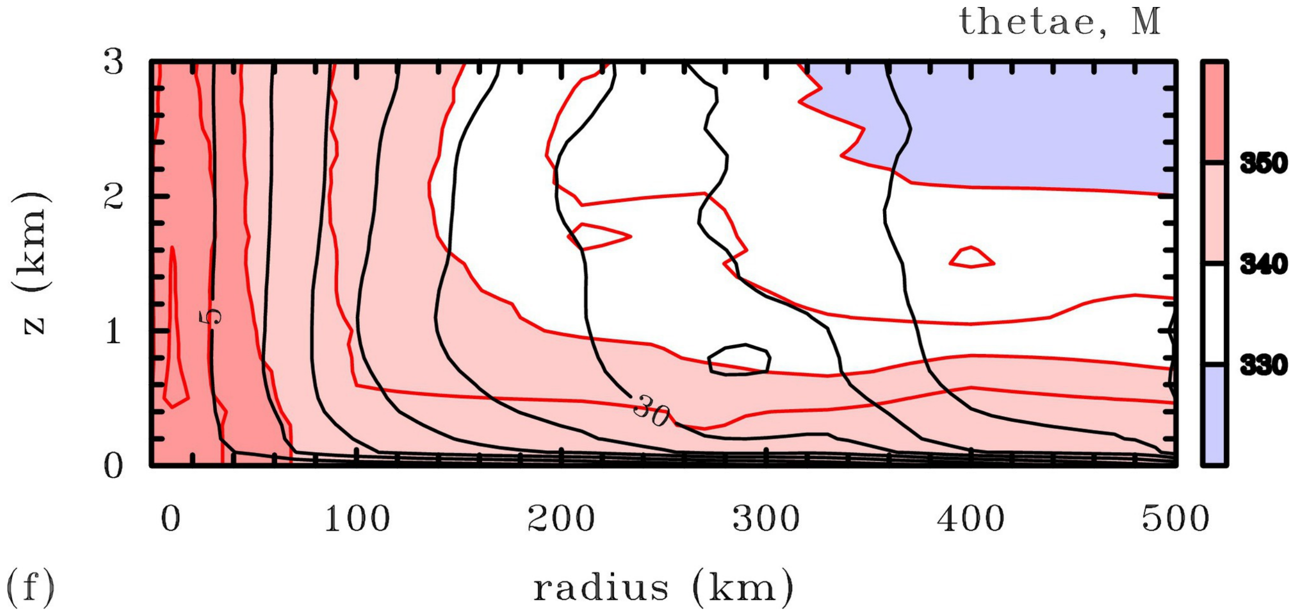

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Azimuthally-averaged structure of Hurricane Edouard (2014) just after peak intensity

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Analyses of dropsonde data just after the mature stage of Hurricane Edouard (2014) are presented. These data, which have unprecedentedly high spatial resolution, were obtained by the unmanned NASA Global Hawk during the Hurricane and Severe Storm Sentinel (HS3) field campaign. The analyses are related to theories of tropical cyclone structure and behaviour. In particular, the findings highlight the radial outflow above the boundary layer below about 8 km and between about 80 km and 220 km radius. This radial outflow would explain the observed spin down of the storm according to the classical mechanism. The findings highlight also a limitation of the assumed steadiness of the storm over the period of data collection.

Key Words: Tropical cyclone, hurricane, observed structure and behaviour

Received October 17, 2018; Revised ; Accepted

1. Introduction

In the past there have been few measurements of hurricane structure through the depth of the troposphere, the reason being that most aircraft reconnaisance flights have not been able to sample the upper troposphere. Some classic observational studies are those of La Seur and Hawkins (1963), Hawkins and Rubsam (1968) and Hawkins and Imbembo (1976) to whom *in situ* data from an instrumented high-flying jet aircraft were available. The situation changed recently through the deployment of the NASA* Global Hawk, an unmanned drone capable of releasing dropsondes in rapid succession from the lower stratosphere. During NASA's Hurricane and Severe Storm Sentinel (HS3; Braun *et al.* 2016) field campaign in 2014, comparatively high temporal and spatial resolution dropsonde observations were made over the Atlantic Ocean in Hurricane Edouard during four missions between 11 to 19 September 2014. A map showing the location of each dropsonde is contained in Figure 1 of Zawislak *et al.* (2016), while a description of the storm during its lifetime is given by Stewart (2014). Brief descriptions of the storm and the missions flown was given by Braun *et al.* (2016) and Munsell *et al.* (2018).

The structure of Edouard was particularly well sampled on 16-17 September while it was near peak intensity. On this mission, which lasted about 23 h, 87 dropsondes were deployed into the hurricane from a height of 18 km. The purpose of this paper is to present azimuthally averaged, radius-height cross sections of various quantities obtained from analyses of these unique data and to compare these analyses with theories of tropical cyclone behaviour.

2. Data

The 87 dropsondes were released into Edouard between 15:06 UTC 16 September and 08:28 UTC 17 September 2014 during which time the storm moved from about 32 N to 35 N (Stewart 2014, Table 1). The distribution of the dropsondes is shown in Abarca *et al.* (2016, Figure 2(a)). The sonde data were post-processed by NCAR using their Atmospheric Sounding Processing Environment (ASPEN) software (Young *et al.* 2016), see Wick *et al.* (2015). The original analyses of the dropsondes did not include a dry bias correction in the upper troposphere, but the present ones have used the correct humidity values. The analysis of these sondes is described briefly below.

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2.1. *Computation of azimuthal averages*

To calculate the azimuthal averages, the dropsonde data were first interpolated to 181 pressure levels with a spacing of 5 mb. The storm centre positions over the time period of the flight were used to determine the location of each dropsonde relative to the evolving centre position. The National Hurricane Center best track data were used also to estimate the mean storm motion over the flight period. The positions of the dropsonde data were shifted to a reference time of 00 UTC 17 September using the storm motion and the time difference between the sonde time and this reference time. Here, the sonde time is the time of the actual measurement at a particular level. Using these adjusted positions relative to the centre, radial and tangential velocities were calculated with the storm motion removed to obtain storm-relative flow. This analysis was done for all dropsondes during the flight. Bins were then created for averaging after all derived fields such as radial and tangential velocity were calculated.

The midpoints of the bins were at radial locations 10, 35, 70, 110, 170, 245, 320, 400, 480 and 560 km from the centre[†]. The number of soundings were distributed within each bin as follows: 0-20 km radius (10 sondes), 20-40 km (9), 40-60 km (7), 60-90 km (10), 90-120 km (8), 120-200 km (3), 200-280 km (14), 280-360 km (9), 360-440 km (8), 440-520 km (8), 520-600 km (7). No additional smoothing was applied to the individual dropsonde data. If, when computing the azimuthal mean, some values were missing from individual soundings, they were simply not included in the calculation of the mean. For the height-radius coordinate used in the plots to be shown, there were no missing azimuthal mean values.

2.2. *Steady-state composite data*

Although the storm was at peak intensity near the start of measurements, the intensity decreased by about 10 m s^{-1} during the period of measurements (see Abarca *et al.* 2016, Figure 1 and accompanying discussion of the various factors in this decay). Attempts were made to subdivide the data into two separate subsets, one in the first half of the flight and another in the second half. The number of soundings were distributed as follows over the course of the first half of the flight, and the second half of the flight: radius 0-20 km (first half 6, second half 4), 20-40 km (4, 5), 40-60 km (5, 3), 60-90 km (4, 7), 90-120 km (4, 4), 120-200 km (2, 1), 200-280 km (6, 8), 280-360 km (3, 6), 360-440 km (3, 5), 440-520 km (3, 5), 520-600 km (2, 5). Clearly, breaking up the soundings into two separate halves of the flight reduces the number of samples in each radial bin, although not necessarily by half since a good part of the first half of the flight was sampling storm outflow beyond 600 km radius. The biggest problem occurs in the 120-200 km radius bin, where the second half of the flight has only one sounding, and much of that data is missing, so contours cannot be drawn there. For these reasons, and because there was qualitative similarity between the derived structures from the two data sets in regions where there was data, we have based the analysis below on a composite for the whole period. Thus, all the storm-relative dropsonde data from the whole flight occurring within a particular bin were averaged. This procedure is tantamount to assuming the storm to be in a stready state for the duration of the flight. Some limitations of the steady state assumption will emerge later.

3. Storm structure

Figure 1 shows radius-height cross sections obtained from the dropsonde data as described in subsection 2.1 above. The data are slightly smoothed using a centred 1-4-1 box filter applied 10 times.

3.1. *Tangential wind and warm core structure*

The storm-relative composite tangential wind component (v, Figure 1a) and temperature perturbation (dT, panel (b)) show the classical structure of a warm-cored vortex with the maximum wind in the lower troposphere and the wind decreasing with height, becoming anticyclonic in the upper troposphere. The decrease in the tangential velocity component with height corresponds through balance considerations with the warm-core structure (see Figure 1b)

There is evidence of a secondary tangential wind maximum at a radius of about 100 km, the inner maximum being near 50 km radius. The formation of this secondary wind maximum was the focus of a separate study (Abarca *et al.* 2016, see below for more). The upper-level anticyclone begins at a radius of about 80 km, while the strength of the anticyclone increases with radius and the anticyclonic circulation deepens with increasing radius. The maximum anticyclonic flow is found at an altitude between 14 and 15 km.

Figure 1(a) shows also the absolute angular momentum (or M-) surfaces corresponding with the tangential wind component. These are calculated using the formula $M = rv + \frac{1}{2}fr^2$, where r is the radius and f is the Coriolis parameter at the mean latitude of Edouard (33 N) during the period of dropsonde measurements. Consistent with theoretical expectations, the M-surfaces flare outwards with height, with M mostly increasing with radius and decreasing with height. There is an elevated local maximum of M located at a height of about 5.5 km and a radius of about 410 km and two additional maxima at larger radii. These maxima are accompanied by a negative radial gradient of M at radii beyond them, implying that the flow is inertially unstable. Since the dropsonde data at these radii are rather sparse (see Abarca *et al.* 2016, Figure 2(b)) and the period of collection spans an interval of more than 16 h, we do not attribute much significance to the implied regions of instability at these radii.

There is a marked positive temperature anomaly inside a radius varying between 100-150 km, depending on height (Figure 1(b)). (For the calculation of temperature perturbation, the "environmental temperature" was determined by averaging all dropsonde data at radii > 200 km. Specifically, there were 46 soundings used in calculation of the "environmental" mean temperature for the temperature perturbation plot.) The temperature anomaly has a maximum of nearly 10^{o}C at an altitude of about 8 km close to the axis of rotation. There is a weak cold temperature anomaly at low levels beyond about 50 km radius. The negative temperature anomalies beyond about 400 km are due to the way the ambient temperature has been defined (see section 2.1). Since the reference temperature is based on an average of all soundings beyond a radius of 200 km and if the temperature in this region decreases outwards, negative anomalies would be expected at large radii. The low-level negative anomaly between 100 and 300 km radius is presumably a result of the evaporation of falling raindrops.

[†]The data set is the same as that used by Abarca et al. (2016). However, the subdivision into bins is somewhat different. Even so, the tangential wind field in Abarca et al. (Figure 3(a)) is very similar to that shown in Figure 1(a). The pressure field is rather smooth and should be similar between the two analyses. Indeed, Abarca et al. did note that "the data were robust to different bin-length choices".

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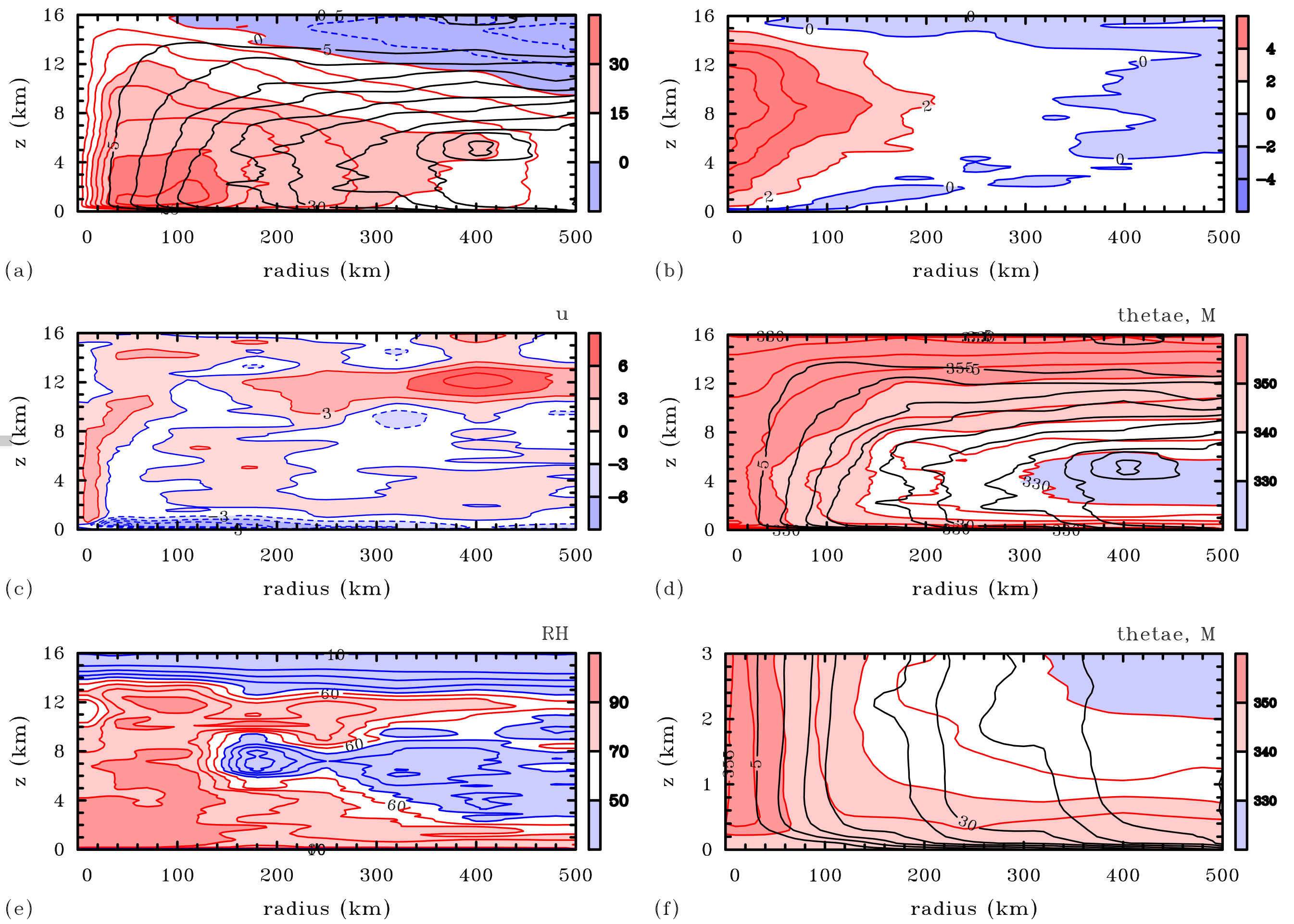

Figure 1. Radius-height cross sections of selected fields derived from the dropsonde data: (a) tangential velocity component, contour interval 5 m s^{-1}, shading indicated on the side bar in m s^{-1}, and absolute angular momentum, black lines, contour interval 5 $\times$ 10^5 m^2 s^{-1}; (b) temperature perturbation, contour interval 2 K (positive values), 1 K (negative values), shading indicated on the side bar in K; (c) radial velocity component, contour interval 3 m s^{-1}, shading indicated on the side bar in m s^{-1}; (d) equivalent potential temperature, contour interval 10 K, shading indicated on the side bar in K, and absolute angular momentum, black lines, contours as in (a); (e) relative humidity, contour interval 10%, shading indicated on the side bar in %; (f) a zoomed in version of panel (d) at heights below 3 km.

3.2. *Radial velocity component*

The storm-relative composite radial flow (u, Figure 1c) shows two features of the classical tropical cyclone structure with a layer of strong inflow below about 1 km extending to large radii as well as a layer of strong outflow in the upper troposphere between about 9 and 14 km depending on radius. The maximum low-level inflow is about 15 m s^{-1}. The layer of upper tropospheric outflow is a few km deep with a maximum of nearly 12 m s^{-1} at about 12 km altitude and 400 km radius.

Perhaps surprisingly, the layers of anticyclonic flow and outflow in the upper troposphere have only a small overlap and mainly at large radii. In particular, the level of maximum outflow does not coincide with that of the maximum anticyclonic flow, which is typically 2 km higher. A plausible explanation is that during the earlier part of the period of investigation, the outflow was higher than during the later part. This possibility is supported by the fact that the region of strong outflow begins beyond 100 km radius near where the secondary wind maximum and secondary eyewall have formed (cf. Abarca *et al.* 2016). In the region inside a radius of 100 km, there is a localized region of outflow with a maximum near 14 km height, presumably remnants of the previous outflow at a higher level. The foregoing difficulty in reconciling the radial and tangential structure of the storm highlights a potential limitation of assuming that the storm is in a quasi-steady state for the purpose of the analysis.

Another interesting feature of the radial flow is the broad region of outflow inside a radius of about 220 km in the lower half of the troposphere above the shallow surface-based boundary layer inflow. This outflow has two local maxima, the inner one associated in part with the inner eyewall and the outer one with the secondary eyewall and secondary wind maximum as documented in Abarca *et al.* (2016). This pattern of outflow would suggest that the flow in these regions is spinning down by the outward radial advection of the M-surfaces. However, this spin down effect would be countered by the vertical advection of air with high values of M from the boundary layer. It was shown by Abarca *et al.* (2016, see their Figure 4b), that the boundary layer flow was supergradient below both the primary and secondary eyewalls on the day prior to the present observations. The fact that the storm had just begun to weaken (see section 2.1) would indicate that the spin down tendency due to the outward radial advection of the M-surfaces would be dominant, at least for the primary eyewall. The role of the vertical advection of supergradient values of M from the boundary layer to spin up the primary eyewall was highlighted by the study of Schmidt and Smith (2016) using a minimal three-layer numerical model and was discussed in a more general context by Montgomery and Smith (2017: section 3.9).

Beyond the 220 km radius in Figure 1c, there are alternate layers of inflow and outflow with outflow being the dominant feature between about 1.5 km and up to 5 km in height.

Other interesting features of the radial flow are the layers of inflow in the upper troposphere, above and below the outflow layer. Such features are often seen in numerical model simulations, but to our knowledge are not well understood.

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3.3. Pseudo-equivalent potential temperature

The distribution of pseudo-equivalent potential temperature[‡], θ_e, (Figure 1d and 1f) shows the classical structure also. (Figure 1f is a zoomed in plot of Figure 1d in the lowest 3 km.) Principal features are: the mid-tropospheric minimum beyond a radius of about 100 km, increasing in prominence with radius; the tendency for the isopleths of θ_e to become close to vertical in the lower troposphere inside a radius of 100 km; and the tendency for the isopleths of θ_e to slope outwards and become close to horizontal in the upper tropospheric outflow layer. There is an approximate congruence between the θ_e- and M-surfaces in the inner core region and in the upper troposphere (the M-surfaces are shown also in Figure 1d and 1f). This approximate congruence in the inner-core region ($r < 200$ km) forms the cornerstone of the steady-state axisymmetric hurricane model by Emanuel (1986).

Throughout much of the troposphere, θ_e has a negative radial gradient. This is, in part, a reflection of the structure in the boundary layer. In this layer (below 1 km) the negative radial gradient of θ_e is apparent only inside a radius of about 100 km and is a result of the presumed increase in surface moisture flux with decreasing radius (Malkus and Riehl 1960, Ooyama 1969). Such a localized gradient was documented in the classical observational analysis of Hawkins and Imbembo (1976) and has been confirmed by more recent work (Montgomery *et al.* 2006, Marks *et al.* 2008, Bell and Montgomery 2008, Smith and Montgomery 2013). Maximum values of θ_e exceed 355 K in the low to mid troposphere near and inside the eyewall region. The surface value is approximately constant at 350 K outside of 100 km radius. The minimum value in the mid to low troposphere falls to values less than 320 K beyond about 300 km radius (the region highlighted in blue in Figure 1d).

3.4. Relative humidity

Values of relative humidity[§], (RH, panel(d)), exceed 90% inside a radius of 200 km and below about 7 km altitude. At larger radii, values are high ($> 80\%$) in a shallow near-surface layer, but decrease markedly with height with values of less than 50% through much of the troposphere, especially beyond about 300 km in radius. These low values are an indication of drying in the subsiding branch of the secondary circulation. This plot does indicate a couple of features of interest. First, the RH starts to drop off beyond the secondary wind maximum, perhaps suggesting that this wind maximum either forms near the boundary with dry air or acts as a potential barrier to dry air. Second, very dry air is being drawn inwards just below the outflow layer.

4. Conclusions

In this paper we have used a dropsonde data set with unprecedentedly high spatial coverage from the NASA HS3 experiment to analyze the azimuthally-averaged structure of Hurricane Edouard (2014) just after its peak intensity. The dropsondes were deployed from above the tropopause and enable a sampling of the full troposphere. The analyses of these unique observations confirm many known structural features of a mature tropical cyclone, e.g. tangential wind structure, radial wind structure, warm core structure and equivalent potential temperature structure. In particular, they show radial outflow above the boundary layer in the lower half of the troposphere and inside about 220 km radius, which would explain the observed spin down of the storm as absolute angular momentum surfaces are advected outwards. Nevertheless, even with such an unprecedentedly high density of dropsondes to estimate the azimuthally-averaged structure, there remains an issue in reconciling the radial and tangential structure of the hurricane. This issue appears to arise from the analysis assumption of a quasi-steady state during the period of observations, an assumption that stands out as an important limitation of any analysis of dropsonde data over such an extended period of observations as the one in this case.

5. Acknowledgements

We thank Jun Zhang and two anonymous reviewers for their perceptive and constructive comments on the original manuscript. RKS acknowledges financial support for tropical cyclone research from the Office of Naval Research Global under Grant No. N62909-15-1-N021. MTM acknowledges the support of NSF grant AGS-1313948, NOAA HFIP grant N0017315WR00048, NASA (HS3) grant NNG11PK021, ONR grant N0001417WX00336, and the U. S. Naval Postgraduate School.

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[‡]The quantity θ_e is calculated using Bolton's formula (Bolton, 1980, Equation (43)).

[§]The relative humidity is calculated relative to water saturation.

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Azimuthally-averaged structure of Hurricane Edouard (2014) just after peak intensity

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Analyses of dropsonde data just after the mature stage of Hurricane Edouard (2014) are presented. These data, which have unprecedentedly high spatial resolution, were obtained by the unmanned NASA Global Hawk during the Hurricane and Severe Storm Sentinel (HS3) field campaign. The analyses are related to theories of tropical cyclone structure and behaviour. In particular, the findings highlight the radial outflow above the boundary layer below about 8 km and between about 80 km and 220 km radius. This radial outflow would explain the observed spin down of the storm according to the classical mechanism. The findings highlight also a limitation of the assumed steadiness of the storm over the period of data collection.

Key Words: Tropical cyclone, hurricane, observed structure and behaviour

Received October 17, 2018; Revised ; Accepted

1. Introduction

In the past there have been few measurements of hurricane structure through the depth of the troposphere, the reason being that most aircraft reconnaisance flights have not been able to sample the upper troposphere. Some classic observational studies are those of La Seur and Hawkins (1963), Hawkins and Rubsam (1968) and Hawkins and Imbembo (1976) to whom *in situ* data from an instrumented high-flying jet aircraft were available. The situation changed recently through the deployment of the NASA* Global Hawk, an unmanned drone capable of releasing dropsondes in rapid succession from the lower stratosphere. During NASA's Hurricane and Severe Storm Sentinel (HS3; Braun *et al.* 2016) field campaign in 2014, comparatively high temporal and spatial resolution dropsonde observations were made over the Atlantic Ocean in Hurricane Edouard during four missions between 11 to 19 September 2014. A map showing the location of each dropsonde is contained in Figure 1 of Zawislak *et al.* (2016), while a description of the storm during its lifetime is given by Stewart (2014). Brief descriptions of the storm and the missions flown was given by Braun *et al.* (2016) and Munsell *et al.* (2018).

The structure of Edouard was particularly well sampled on 16-17 September while it was near peak intensity. On this mission, which lasted about 23 h, 87 dropsondes were deployed into the hurricane from a height of 18 km. The purpose of this paper is to present azimuthally averaged, radius-height cross sections of various quantities obtained from analyses of these unique data and to compare these analyses with theories of tropical cyclone behaviour.

2. Data

The 87 dropsondes were released into Edouard between 15:06 UTC 16 September and 08:28 UTC 17 September 2014 during which time the storm moved from about 32 N to 35 N (Stewart 2014, Table 1). The distribution of the dropsondes is shown in Abarca *et al.* (2016, Figure 2(a)). The sonde data were post-processed by NCAR using their Atmospheric Sounding Processing Environment (ASPEN) software (Young *et al.* 2016), see Wick *et al.* (2015). The original analyses of the dropsondes did not include a dry bias correction in the upper troposphere, but the present ones have used the correct humidity values. The analysis of these sondes is described briefly below.

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2.1. *Computation of azimuthal averages*

To calculate the azimuthal averages, the dropsonde data were first interpolated to 181 pressure levels with a spacing of 5 mb. The storm centre positions over the time period of the flight were used to determine the location of each dropsonde relative to the evolving centre position. The National Hurricane Center best track data were used also to estimate the mean storm motion over the flight period. The positions of the dropsonde data were shifted to a reference time of 00 UTC 17 September using the storm motion and the time difference between the sonde time and this reference time. Here, the sonde time is the time of the actual measurement at a particular level. Using these adjusted positions relative to the centre, radial and tangential velocities were calculated with the storm motion removed to obtain storm-relative flow. This analysis was done for all dropsondes during the flight. Bins were then created for averaging after all derived fields such as radial and tangential velocity were calculated.

The midpoints of the bins were at radial locations 10, 35, 70, 110, 170, 245, 320, 400, 480 and 560 km from the centre[†]. The number of soundings were distributed within each bin as follows: 0-20 km radius (10 sondes), 20-40 km (9), 40-60 km (7), 60-90 km (10), 90-120 km (8), 120-200 km (3), 200-280 km (14), 280-360 km (9), 360-440 km (8), 440-520 km (8), 520-600 km (7). No additional smoothing was applied to the individual dropsonde data. If, when computing the azimuthal mean, some values were missing from individual soundings, they were simply not included in the calculation of the mean. For the height-radius coordinate used in the plots to be shown, there were no missing azimuthal mean values.

2.2. *Steady-state composite data*

Although the storm was at peak intensity near the start of measurements, the intensity decreased by about 10 m s^{-1} during the period of measurements (see Abarca *et al.* 2016, Figure 1 and accompanying discussion of the various factors in this decay). Attempts were made to subdivide the data into two separate subsets, one in the first half of the flight and another in the second half. The number of soundings were distributed as follows over the course of the first half of the flight, and the second half of the flight: radius 0-20 km (first half 6, second half 4), 20-40 km (4, 5), 40-60 km (5, 3), 60-90 km (4, 7), 90-120 km (4, 4), 120-200 km (2, 1), 200-280 km (6, 8), 280-360 km (3, 6), 360-440 km (3, 5), 440-520 km (3, 5), 520-600 km (2, 5). Clearly, breaking up the soundings into two separate halves of the flight reduces the number of samples in each radial bin, although not necessarily by half since a good part of the first half of the flight was sampling storm outflow beyond 600 km radius. The biggest problem occurs in the 120-200 km radius bin, where the second half of the flight has only one sounding, and much of that data is missing, so contours cannot be drawn there. For these reasons, and because there was qualitative similarity between the derived structures from the two data sets in regions where there was data, we have based the analysis below on a composite for the whole period. Thus, all the storm-relative dropsonde data from the whole flight occurring within a particular bin were averaged. This procedure is tantamount to assuming the storm to be in a stready state for the duration of the flight. Some limitations of the steady state assumption will emerge later.

3. Storm structure

Figure 1 shows radius-height cross sections obtained from the dropsonde data as described in subsection 2.1 above. The data are slightly smoothed using a centred 1-4-1 box filter applied 10 times.

3.1. *Tangential wind and warm core structure*

The storm-relative composite tangential wind component (v, Figure 1a) and temperature perturbation (dT, panel (b)) show the classical structure of a warm-cored vortex with the maximum wind in the lower troposphere and the wind decreasing with height, becoming anticyclonic in the upper troposphere. The decrease in the tangential velocity component with height corresponds through balance considerations with the warm-core structure (see Figure 1b)

There is evidence of a secondary tangential wind maximum at a radius of about 100 km, the inner maximum being near 50 km radius. The formation of this secondary wind maximum was the focus of a separate study (Abarca *et al.* 2016, see below for more). The upper-level anticyclone begins at a radius of about 80 km, while the strength of the anticyclone increases with radius and the anticyclonic circulation deepens with increasing radius. The maximum anticyclonic flow is found at an altitude between 14 and 15 km.

Figure 1(a) shows also the absolute angular momentum (or M-) surfaces corresponding with the tangential wind component. These are calculated using the formula $M = rv + \frac{1}{2}fr^2$, where r is the radius and f is the Coriolis parameter at the mean latitude of Edouard (33 N) during the period of dropsonde measurements. Consistent with theoretical expectations, the M-surfaces flare outwards with height, with M mostly increasing with radius and decreasing with height. There is an elevated local maximum of M located at a height of about 5.5 km and a radius of about 410 km and two additional maxima at larger radii. These maxima are accompanied by a negative radial gradient of M at radii beyond them, implying that the flow is inertially unstable. Since the dropsonde data at these radii are rather sparse (see Abarca *et al.* 2016, Figure 2(b)) and the period of collection spans an interval of more than 16 h, we do not attribute much significance to the implied regions of instability at these radii.

There is a marked positive temperature anomaly inside a radius varying between 100-150 km, depending on height (Figure 1(b)). (For the calculation of temperature perturbation, the "environmental temperature" was determined by averaging all dropsonde data at radii $>$ 200 km. Specifically, there were 46 soundings used in calculation of the "environmental" mean temperature for the temperature perturbation plot.) The temperature anomaly has a maximum of nearly 10^{o}C at an altitude of about 8 km close to the axis of rotation. There is a weak cold temperature anomaly at low levels beyond about 50 km radius. The negative temperature anomalies beyond about 400 km are due to the way the ambient temperature has been defined (see section 2.1). Since the reference temperature is based on an average of all soundings beyond a radius of 200 km and if the temperature in this region decreases outwards, negative anomalies would be expected at large radii. The low-level negative anomaly between 100 and 300 km radius is presumably a result of the evaporation of falling raindrops.

[†]The data set is the same as that used by Abarca et al. (2016). However, the subdivision into bins is somewhat different. Even so, the tangential wind field in Abarca et al. (Figure 3(a)) is very similar to that shown in Figure 1(a). The pressure field is rather smooth and should be similar between the two analyses. Indeed, Abarca et al. did note that "the data were robust to different bin-length choices".

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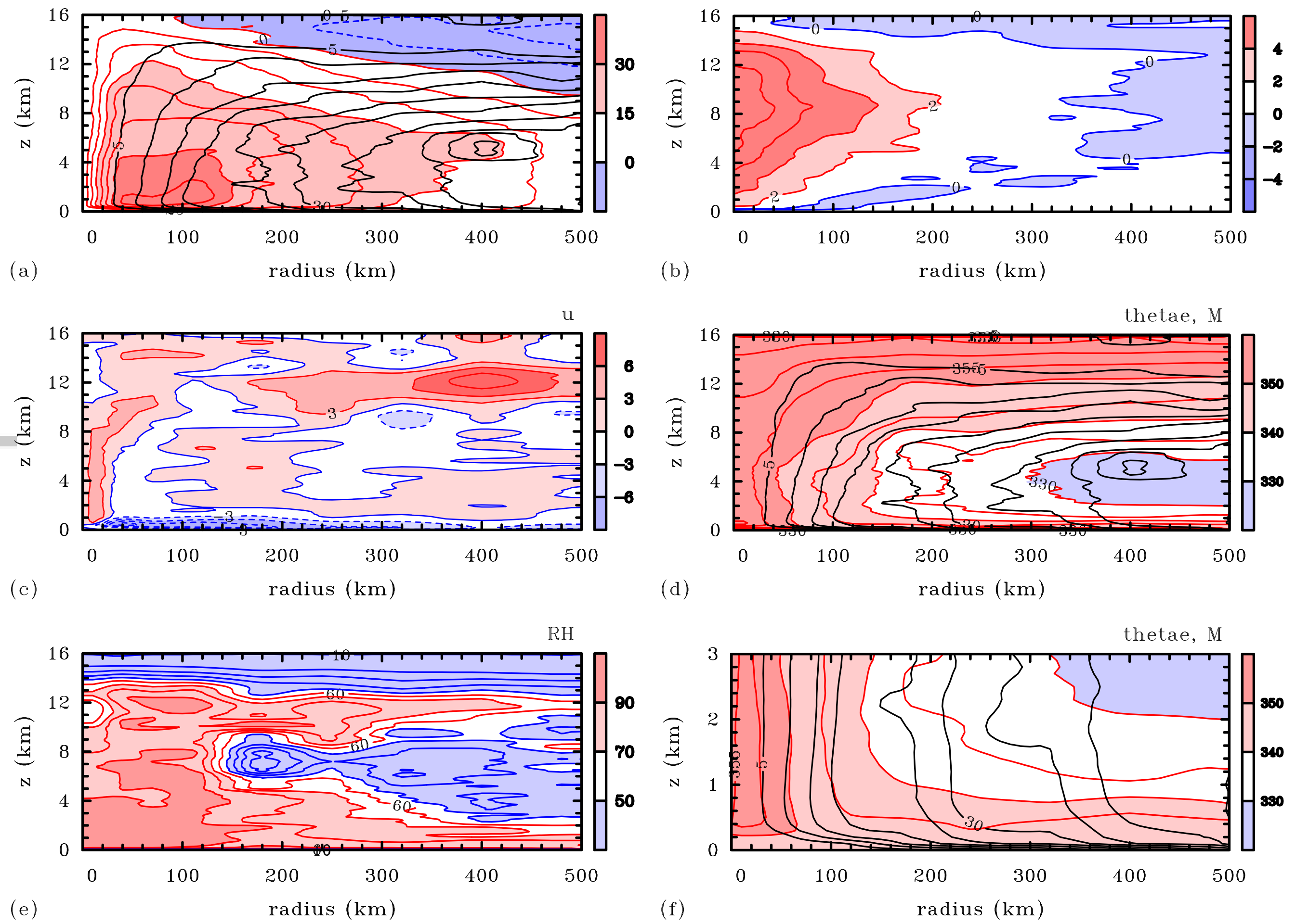

Figure 1. Radius-height cross sections of selected fields derived from the dropsonde data: (a) tangential velocity component, contour interval 5 m s^{-1}, shading indicated on the side bar in m s^{-1}, and absolute angular momentum, black lines, contour interval 5 × 10^5 m^2 s^{-1}; (b) temperature perturbation, contour interval 2 K (positive values), 1 K (negative values), shading indicated on the side bar in K; (c) radial velocity component, contour interval 3 m s^{-1}, shading indicated on the side bar in m s^{-1}; (d) equivalent potential temperature, contour interval 10 K, shading indicated on the side bar in K, and absolute angular momentum, black lines, contours as in (a); (e) relative humidity, contour interval 10%, shading indicated on the side bar in %; (f) a zoomed in version of panel (d) at heights below 3 km.

3.2. Radial velocity component

The storm-relative composite radial flow (u, Figure 1c) shows two features of the classical tropical cyclone structure with a layer of strong inflow below about 1 km extending to large radii as well as a layer of strong outflow in the upper troposphere between about 9 and 14 km depending on radius. The maximum low-level inflow is about 15 m s^{-1}. The layer of upper tropospheric outflow is a few km deep with a maximum of nearly 12 m s^{-1} at about 12 km altitude and 400 km radius.

Perhaps surprisingly, the layers of anticyclonic flow and outflow in the upper troposphere have only a small overlap and mainly at large radii. In particular, the level of maximum outflow does not coincide with that of the maximum anticyclonic flow, which is typically 2 km higher. A plausible explanation is that during the earlier part of the period of investigation, the outflow was higher than during the later part. This possibility is supported by the fact that the region of strong outflow begins beyond 100 km radius near where the secondary wind maximum and secondary eyewall have formed (cf. Abarca *et al.* 2016). In the region inside a radius of 100 km, there is a localized region of outflow with a maximum near 14 km height, presumably remnants of the previous outflow at a higher level. The foregoing difficulty in reconciling the radial and tangential structure of the storm highlights a potential limitation of assuming that the storm is in a quasi-steady state for the purpose of the analysis.

Another interesting feature of the radial flow is the broad region of outflow inside a radius of about 220 km in the lower half of the troposphere above the shallow surface-based boundary layer inflow. This outflow has two local maxima, the inner one associated in part with the inner eyewall and the outer one with the secondary eyewall and secondary wind maximum as documented in Abarca *et al.* (2016). This pattern of outflow would suggest that the flow in these regions is spinning down by the outward radial advection of the M-surfaces. However, this spin down effect would be countered by the vertical advection of air with high values of M from the boundary layer. It was shown by Abarca *et al.* (2016, see their Figure 4b), that the boundary layer flow was supergradient below both the primary and secondary eyewalls on the day prior to the present observations. The fact that the storm had just begun to weaken (see section 2.1) would indicate that the spin down tendency due to the outward radial advection of the M-surfaces would be dominant, at least for the primary eyewall. The role of the vertical advection of supergradient values of M from the boundary layer to spin up the primary eyewall was highlighted by the study of Schmidt and Smith (2016) using a minimal three-layer numerical model and was discussed in a more general context by Montgomery and Smith (2017: section 3.9).

Beyond the 220 km radius in Figure 1c, there are alternate layers of inflow and outflow with outflow being the dominant feature between about 1.5 km and up to 5 km in height.

Other interesting features of the radial flow are the layers of inflow in the upper troposphere, above and below the outflow layer. Such features are often seen in numerical model simulations, but to our knowledge are not well understood.

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3.3. Pseudo-equivalent potential temperature

The distribution of pseudo-equivalent potential temperature[‡], θ_e, (Figure 1d and 1f) shows the classical structure also. (Figure 1f is a zoomed in plot of Figure 1d in the lowest 3 km.) Principal features are: the mid-tropospheric minimum beyond a radius of about 100 km, increasing in prominence with radius; the tendency for the isopleths of θ_e to become close to vertical in the lower troposphere inside a radius of 100 km; and the tendency for the isopleths of θ_e to slope outwards and become close to horizontal in the upper tropospheric outflow layer. There is an approximate congruence between the θ_e- and M-surfaces in the inner core region and in the upper troposphere (the M-surfaces are shown also in Figure 1d and 1f). This approximate congruence in the inner-core region ($r < 200$ km) forms the cornerstone of the steady-state axisymmetric hurricane model by Emanuel (1986).

Throughout much of the troposphere, θ_e has a negative radial gradient. This is, in part, a reflection of the structure in the boundary layer. In this layer (below 1 km) the negative radial gradient of θ_e is apparent only inside a radius of about 100 km and is a result of the presumed increase in surface moisture flux with decreasing radius (Malkus and Riehl 1960, Ooyama 1969). Such a localized gradient was documented in the classical observational analysis of Hawkins and Imbembo (1976) and has been confirmed by more recent work (Montgomery *et al.* 2006, Marks *et al.* 2008, Bell and Montgomery 2008, Smith and Montgomery 2013). Maximum values of θ_e exceed 355 K in the low to mid troposphere near and inside the eyewall region. The surface value is approximately constant at 350 K outside of 100 km radius. The minimum value in the mid to low troposphere falls to values less than 320 K beyond about 300 km radius (the region highlighted in blue in Figure 1d).

3.4. Relative humidity

Values of relative humidity[§], (RH, panel(d)), exceed 90% inside a radius of 200 km and below about 7 km altitude. At larger radii, values are high ($> 80\%$) in a shallow near-surface layer, but decrease markedly with height with values of less than 50% through much of the troposphere, especially beyond about 300 km in radius. These low values are an indication of drying in the subsiding branch of the secondary circulation. This plot does indicate a couple of features of interest. First, the RH starts to drop off beyond the secondary wind maximum, perhaps suggesting that this wind maximum either forms near the boundary with dry air or acts as a potential barrier to dry air. Second, very dry air is being drawn inwards just below the outflow layer.

4. Conclusions

In this paper we have used a dropsonde data set with unprecedentedly high spatial coverage from the NASA HS3 experiment to analyze the azimuthally-averaged structure of Hurricane Edouard (2014) just after its peak intensity. The dropsondes were deployed from above the tropopause and enable a sampling of the full troposphere. The analyses of these unique observations confirm many known structural features of a mature tropical cyclone, e.g. tangential wind structure, radial wind structure, warm core structure and equivalent potential temperature structure. In particular, they show radial outflow above the boundary layer in the lower half of the troposphere and inside about 220 km radius, which would explain the observed spin down of the storm as absolute angular momentum surfaces are advected outwards. Nevertheless, even with such an unprecedentedly high density of dropsondes to estimate the azimuthally-averaged structure, there remains an issue in reconciling the radial and tangential structure of the hurricane. This issue appears to arise from the analysis assumption of a quasi-steady state during the period of observations, an assumption that stands out as an important limitation of any analysis of dropsonde data over such an extended period of observations as the one in this case.

5. Acknowledgements

We thank Jun Zhang and two anonymous reviewers for their perceptive and constructive comments on the original manuscript. RKS acknowledges financial support for tropical cyclone research from the Office of Naval Research Global under Grant No. N62909-15-1-N021. MTM acknowledges the support of NSF grant AGS-1313948, NOAA HFIP grant N0017315WR00048, NASA (HS3) grant NNG11PK021, ONR grant N0001417WX00336, and the U. S. Naval Postgraduate School.

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[‡] The quantity θ_e is calculated using Bolton's formula (Bolton, 1980, Equation (43)).

[§] The relative humidity is calculated relative to water saturation.

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Analyses of dropsonde data collected in Hurricane Edouard (2014) just after its mature stage are presented. These data, have unprecedentedly high spatial resolution, based on 87 dropsondes released by the unmanned NASA Global Hawk from an altitude of 18 km during the Hurricane and Severe Storm Sentinel (HS3) field campaign. Attempts are made to relate the analyses of the data to theories of tropical cyclone structure and behaviour. The tangential wind and thermal fields show the classical structure of a warm core vortex, in this case with a secondary eyewall feature. The equivalent potential temperature (θ_e) field shows also the expected structure with a mid-tropospheric minimum at outer radii and contours of θ_e flaring upwards and outwards at inner radii and, with some imagination, roughly congruent to the surfaces of absolute angular momentum. However, details of the analysed radial velocity field are somewhat sensitive to the way in which the sonde data are partitioned to produce an azimuthal average. This sensitivity is compounded by an apparent limitation of the assumed steadiness of the storm over the period of data collection.

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1. Introduction

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Figure 1(a) shows also the absolute angular momentum (or M-) surfaces corresponding with the tangential wind component. These are calculated using the formula $M = rv + \frac{1}{2}fr^2$, where r is the radius and f is the Coriolis parameter at the mean latitude of Edouard (33°N) during the period of dropsonde measurements. Consistent with theoretical expectations, the M-surfaces flare outwards with height, with M mostly increasing with radius and decreasing with height. There is a local maximum of M, located at a height of about 6 km and a radius of just over 400 km. This maximum is accompanied by a negative radial gradient of M at radii beyond it, implying that, according to linear theory, the flow would be centrifugally unstable locally (Rayleigh, 1916). Since the dropsonde data at these radii are rather sparse (see Abarca *et al.* 2016, Figure 3(b)) and the period of collection spans an interval of more than 16 h, we do not attribute much significance to the implied regions of instability at these radii.

[†]The data set is the same as that used by Abarca *et al.* (2016). However, the subdivision into bins is somewhat different. Even so, the tangential wind field in Abarca et al. (Figure 3(a)) is very similar to that shown in Figure 1(a). The pressure field is rather smooth and should be similar between the two analyses. Indeed, Abarca et al. did note that "the data were robust to different bin-length choices".

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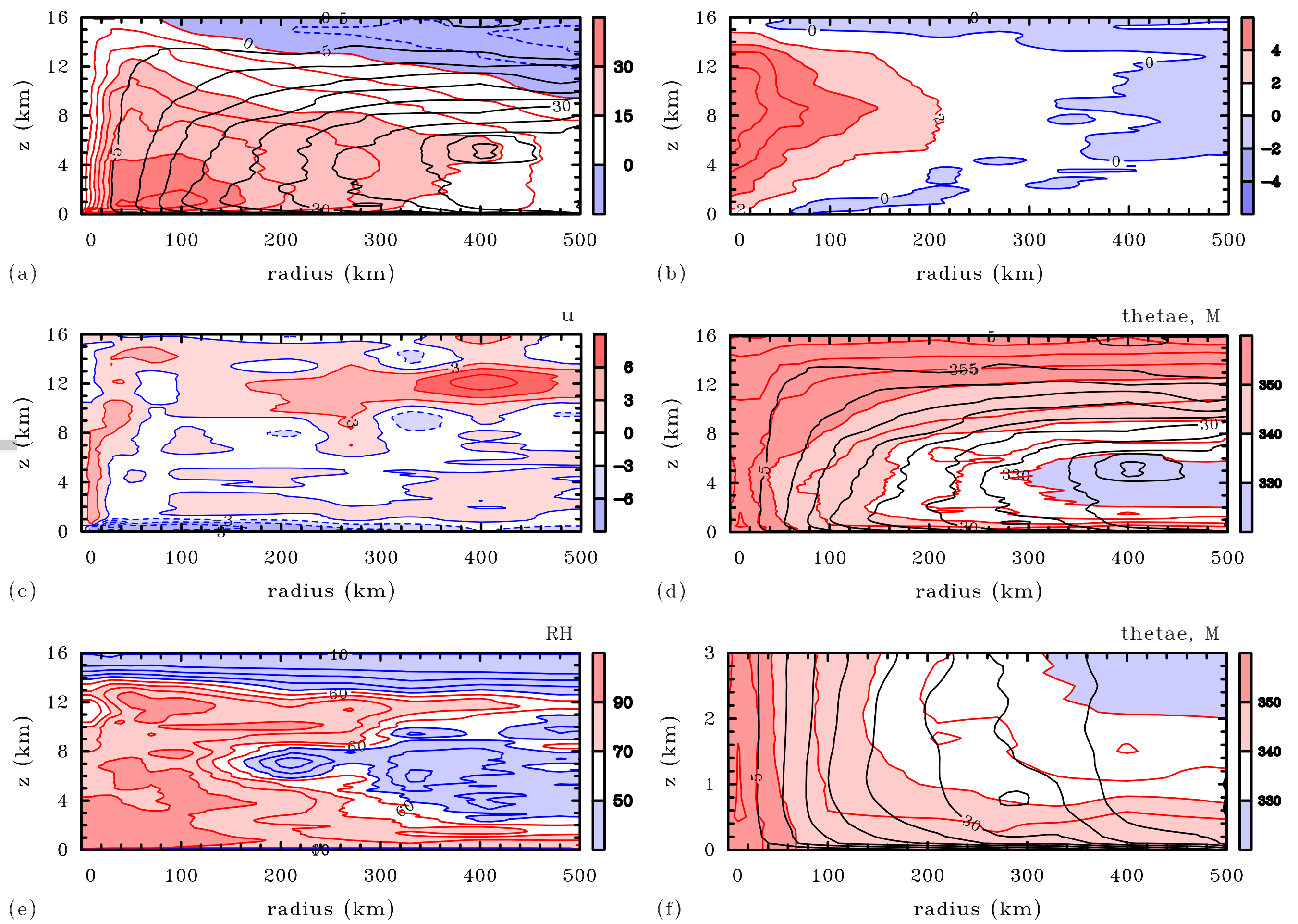

Figure 1. Radius-height cross sections of selected fields derived from the dropsonde data: (a) tangential velocity component, contour interval 5 m s^{-1}, shading indicated on the side bar in m s^{-1}, and absolute angular momentum, black lines, contour interval 5 $\times$ 10^5 m^2 s^{-1}; (b) temperature perturbation, contour interval 2 K (positive values), 1 K (negative values), shading indicated on the side bar in K; (c) radial velocity component, contour interval 3 m s^{-1}, shading indicated on the side bar in m s^{-1}; (d) equivalent potential temperature, contour interval 10 K, shading indicated on the side bar in K, and absolute angular momentum, black lines, contours as in (a); (e) relative humidity, contour interval 10%, shading indicated on the side bar in %; (f) a zoomed in version of panel (d) at heights below 3 km.

There is a marked ($> 2^o$C) positive temperature anomaly inside a radius of about 200 km (Figure 1(b)). This anomaly has a maximum of nearly 10^{o}C on the axis of rotation at an altitude of about 8 km. (For the calculation of temperature perturbation, the "environmental temperature" was determined by averaging all dropsonde data at radii $>$ 200 km. Specifically, there were 46 soundings used in calculation of the "environmental" mean temperature for the temperature perturbation plot.) There is a weak cold temperature anomaly at low levels beyond about 60 km radius. The negative temperature anomalies beyond about 400 km radius and those above 13 km are due to the way the ambient temperature has been defined and are presumably not significant. Since the reference temperature is based on an average of all soundings beyond a radius of 200 km and if the temperature in this region decreases outwards, negative anomalies would be expected at large radii. The low-level negative anomaly between 60 and 240 km radius is plausibly a result of the evaporation of falling raindrops.

3.2. *Radial velocity component*

The storm-relative composite radial flow (u, Figure 1c) shows two features of the classical tropical cyclone structure with a layer of strong inflow below about 1 km extending to large radii as well as a layer of strong outflow in the upper troposphere between about 9 and 14 km depending on radius. The maximum low-level inflow is about 15 m s^{-1}. The layer of upper tropospheric outflow is a few km deep with a maximum of nearly 12 m s^{-1} at about 12 km altitude and 400 km radius.

Perhaps surprisingly, the level of maximum outflow in the upper troposphere does not coincide with that of the maximum anticyclonic flow, which is typically 2 km higher. A plausible explanation for this finding is that during the earlier period of measurement, the outflow was higher than during the later part. This possibility is supported by the fact that there are two layers of outflow, one centred around 14 km height, emanating from the inner eyewall and another, centred around 12 km height, emanating from the outer eyewall (see Abarca *et al.* 2016 for further details of the double eyewall structure). The upper layer has its maximum well within a radius of 100 km, whereas the lower maximum, which is much stronger, occurs at a radius of 400 km. The foregoing issue in reconciling the radial and tangential wind structure in the upper troposphere highlights a potential limitation of assuming that the storm is in a quasi-steady state for the purpose of the analysis.

In the lower troposphere there are significant regions of outflow above the shallow surface-based boundary layer inflow. This outflow has a local maximum in the inner eyewall (near 20 km radius) and has a layered structure beyond a radius of about 90 km starting near outer eyewall. This pattern of outflow would suggest that the flow in these regions is spinning down by the outward radial advection of the M-surfaces. However, this spin down effect would be countered by the vertical advection of air with high values of M from the boundary layer, at least in the inner core region. In this context, it was shown by Abarca *et al.* (2016, see their Figure 4b), that the

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boundary layer flow was supergradient below both the primary and secondary eyewalls on the day prior to the present observations. The fact that the storm had just begun to weaken (see section 2.1) would indicate that the spin down tendency due to the outward radial advection of the M-surfaces would be dominant, at least for the inner eyewall. The role of the vertical advection of supergradient values of M from the boundary layer to spin up the inner eyewall was highlighted by the study of Schmidt and Smith (2016) using a minimal three-layer numerical model and was discussed in a more general context by Montgomery and Smith (2017: section 3.9).

Beyond about 300 km radius in Figure 1c, where the boundary layer flow is typically subgradient, there is mostly outflow in the lower troposphere above the boundary layer. At such radii, this outflow would carry the M surfaces outwards leading to a spin-down of the tangential winds and therefore a contracting in the storm size (see Kilroy *et al.* 2016 for a discussion of the factors influencing storm size).

Other interesting features of the radial flow are the layers of inflow in the upper troposphere, above and below the two outflow layers. Such features are often seen in numerical model simulations (e.g. Rotunno and Emanuel 1987, Figure 5c; Persing *et al.* 2013, Figures 10a, 11a, 15a; Montgomery *et al.* 2018, Figures 7b, 8b), but to our knowledge are not well understood.

It should be pointed out that while the broad features of the analyzed radial flow field are robust (e.g. the strong inflow in the boundary layer, the upper-level outflow and the outflow in the inner and outer eyewalls), the details of this field are somewhat sensitive to the way in which the sonde data are binned to produce an azimuthal average (not shown). This sensitivity is compounded by an apparent limitation of the assumed steadiness of the storm over the period of data collection discussed above.

3.3. Pseudo-equivalent potential temperature

The distribution of pseudo-equivalent potential temperature‡, θ_e, (Figure 1d and 1f) shows the classical structure also. (Figure 1f is a zoomed in plot of Figure 1d in the lowest 3 km.) Principal features are: the mid-tropospheric minimum beyond a radius of about 100 km, increasing in prominence with radius; the tendency for the isopleths of θ_e to become close to vertical in the lower troposphere inside a radius of 100 km; and the tendency for the isopleths of θ_e to slope outwards and become close to horizontal in the upper tropospheric outflow layer. With a little imagination, there is an approximate congruence between the θ_e- and M-surfaces in the inner core region and in the upper troposphere, at least out to 250 km radius (the M-surfaces are shown also in Figure 1d and 1f). This approximate congruence forms the cornerstone of the steady-state axisymmetric hurricane model by Emanuel (1986).

Throughout much of the troposphere, θ_e has a negative radial gradient. This is, in part, a reflection of the structure in the boundary layer. Below about 600 m, the negative radial gradient of θ_e is apparent only inside a radius of about 100 km and is a result of the presumed increase in surface moisture flux with decreasing radius (Malkus and Riehl 1960, Ooyama 1969). Such a localized gradient was documented in the classical observational analysis of Hawkins and Imbembo (1976) and has been confirmed by more recent work (Montgomery *et al.* 2006, Marks *et al.* 2008, Bell and Montgomery 2008, Smith and Montgomery 2013). Maximum values of θ_e exceed 355 K in the low to mid troposphere near and inside the inner eyewall region. The near surface value is approximately constant at 350 K outside of 100 km radius. The minimum value in the mid to low troposphere falls to values less than 320 K beyond about 300 km radius (the region highlighted in blue in Figure 1d).

3.4. Relative humidity

Values of relative humidity§, (RH, panel (d)), exceed 90% inside a radius of 200 km and below about 7 km altitude. At larger radii, values remain relatively high ($> 80\%$) in a shallow near-surface layer, but decrease markedly with height with values of less than 50% through much of the troposphere, especially beyond a radius of about 300 km. These low values are an indication of drying in the subsiding branch of the secondary circulation. The RH starts to drop off beyond the outer wind maximum, perhaps suggesting that this wind maximum either forms near the boundary with dry air or acts as a potential barrier to dry air. Comparison with Figure 1c shows that relatively dry air is being drawn inwards just below the outflow layer.

4. Conclusions

In this paper we have used a dropsonde data set with unprecedentedly high spatial coverage from the NASA HS3 experiment to analyze the azimuthally-averaged structure of Hurricane Edouard (2014) just after its peak intensity. The dropsondes were deployed from above the tropopause and enable a sampling of the full troposphere. The analyses of these unique observations confirm many known structural features of a mature tropical cyclone, e.g. tangential wind structure, radial wind structure (low-level inflow in a shallow boundary layer, outflow in the upper troposphere), warm core temperature structure, relative humidity structure and equivalent potential temperature structure.

Nevertheless, even with such an unprecedentedly high density of dropsondes to estimate the azimuthally averaged structure, there remain issues in reconciling the radial and tangential structure of the hurricane in the upper troposphere. One issue appears to arise from the analysis assumption of a quasi-steady state during the period of observations, an assumption that stands out as an important limitation of any analysis of dropsonde data over such an extended period of observations as the one in this case. Another issue is that details of the analyzed radial velocity field are somewhat sensitive to the way in which the dropsonde data are partitioned to produce an azimuthal average.

5. Acknowledgements

We thank Jun Zhang and two anonymous reviewers for their perceptive and constructive comments on the original manuscript. RKS acknowledges financial support for tropical cyclone research from the Office of Naval Research Global under Grant No. N62909-15-1-N021. MTM acknowledges the support of NSF grant AGS-1313948, NOAA HFIP grant N0017315WR00048, NASA (HS3) grant NNG11PK021, ONR grant N0001417WX00336, and the U. S. Naval Postgraduate School.

‡The quantity θ_e is calculated using Bolton's formula (Bolton, 1980, Equation (43)).
§The relative humidity is calculated relative to water saturation.

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Azimuthally-averaged structure of Hurricane Edouard (2014) just after peak intensity

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Analyses of dropsonde data collected in Hurricane Edouard (2014) just after its mature stage are presented. These data, have unprecedentedly high spatial resolution, based on 87 dropsondes released by the unmanned NASA Global Hawk from an altitude of 18 km during the Hurricane and Severe Storm Sentinel (HS3) field campaign. Attempts are made to relate the analyses of the data to theories of tropical cyclone structure and behaviour. The tangential wind and thermal fields show the classical structure of a warm core vortex, in this case with a secondary eyewall feature. The equivalent potential temperature (θ_e) field shows also the expected structure with a mid-tropospheric minimum at outer radii and contours of θ_e flaring upwards and outwards at inner radii and, with some imagination, roughly congruent to the surfaces of absolute angular momentum. However, details of the analysed radial velocity field are somewhat sensitive to the way in which the sonde data are partitioned to produce an azimuthal average. This sensitivity is compounded by an apparent limitation of the assumed steadiness of the storm over the period of data collection.

Key Words: Tropical cyclone, hurricane, observed structure and behaviour

Received November 9, 2018; Revised ; Accepted

1. Introduction

In the past there have been few measurements of hurricane structure through the depth of the troposphere, the reason being that most aircraft reconnaisance flights have not been able to sample the upper troposphere. Some classic observational studies are those of La Seur and Hawkins (1963), Hawkins and Rubsam (1968) and Hawkins and Imbembo (1976) to whom *in situ* data from an instrumented high-flying jet aircraft were available. The situation changed recently through the deployment of the NASA* Global Hawk, an unmanned drone capable of releasing dropsondes in rapid succession from the lower stratosphere. During NASA's Hurricane and Severe Storm Sentinel (HS3; Braun *et al.* 2016) field campaign in 2014, comparatively high temporal and spatial resolution dropsonde observations were made over the Atlantic Ocean in Hurricane Edouard during four missions between 11 to 19 September 2014. A map showing the location of each dropsonde is contained in Figure 1 of Zawislak *et al.* (2016), while a description of the storm during its lifetime is given by Stewart (2014). Brief descriptions of the storm and the missions flown was given by Braun *et al.* (2016) and Munsell *et al.* (2018).

The structure of Edouard was particularly well sampled on 16-17 September while it was near peak intensity. On this mission, which lasted about 23 h, 87 dropsondes were deployed into the hurricane from a height of 18 km. The purpose of this paper is to present azimuthally averaged, radius-height cross sections of various quantities obtained from analyses of these unique data and to compare these analyses with theories of tropical cyclone behaviour.

2. Data

The 87 dropsondes were released into Edouard between 15:06 UTC 16 September and 08:28 UTC 17 September 2014 during which time the storm moved from about 32 N to 35 N (Stewart 2014, Table 1). The distribution of the dropsondes is shown in Abarca *et al.*

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(2016, Figure 2(a)). The sonde data were post-processed by NCAR (see Wick *et al.* 2015) using their Atmospheric Sounding Processing Environment (ASPEN) software (Young *et al.* 2016). The original analyses of the dropsondes did not include a dry bias correction in the upper troposphere, but the present ones have used the correct humidity values. The analysis of these sondes is described briefly below.

2.1. *Computation of azimuthal averages*

To calculate the azimuthal averages, the dropsonde data were first interpolated to 181 pressure levels with a spacing of 5 mb. The storm centre positions over the time period of the flight were used to determine the location of each dropsonde relative to the evolving centre position. The National Hurricane Center best track data were used also to estimate the mean storm motion over the flight period. The positions of the dropsonde data were shifted to a reference time of 00 UTC 17 September using the storm motion and the time difference between the sonde time and this reference time. Here, the sonde time is the time of the actual measurement at a particular level. Using these adjusted positions relative to the centre, radial and tangential velocities were calculated with the storm motion removed to obtain storm-relative flow. This analysis was done for all dropsondes during the flight. Bins were then created for averaging after all derived fields such as radial and tangential velocity were calculated.

The midpoints of the bins were at radial locations 10, 30, 50, 70, 100, 150, 210, 270, 330, 400, 480, and 560 km from the centre†. The number of soundings were distributed within each bin as follows: 0-20 km radius (11 sondes), 20-40 km (9), 40-60 km (6), 60-80 km (7), 80-120 km (10), 120-180 km (0), 180-240 km (9), 240-300 km (8), 300-360 km (8), 360-440 km (4), 440-520 km (8), 520-600 (7). No additional smoothing was applied to the individual dropsonde data. If, when computing the azimuthal mean, some values were missing from individual soundings, they were simply not included in the calculation of the mean. Because there were no dropsonde data at radii between 120 km and 200 km and therefore in the radial bin 120-180 km, the azimuthal values for 150 km radius were determined by linear interpolation between the bin midpoints at 100 km and 210 km.

2.2. *Steady-state composite data*

Although the storm was at peak intensity near the start of measurements, the intensity decreased by about 10 m s^{-1} during the period of measurements (see Abarca *et al.* 2016, Figure 1 and accompanying discussion of the various factors in this decay). Because of the relatively long period of data collection, attempts were made to subdivide the data into two separate subsets, one in the first half of the flight and another in the second half. In this subdivision the number of soundings were distributed as follows over the course of the first half of the flight, and the second half of the flight: radius 0-20 km (first half 6, second half 5), 20-40 km (4, 5), 40-60 km (3, 3), 60-80 km (3, 4), 80-120 km (5, 5), 120-180 km (0, 0), 180-240 km (4, 5), 240-300 km (4,4), 300-360 km (3, 5), 360-440 km (1, 3), 440-520 km (3, 5), 520-600 km (2,5). Clearly, breaking up the soundings into two separate halves of the flight reduces the number of samples in each radial bin, although not necessarily by half since a good part of the first half of the flight was sampling storm outflow beyond 600 km radius. As mentioned earlier, the biggest problem occurs between 120-180 km, where there are no soundings for either time. For these reasons, and because there was qualitative similarity between the derived structures from the two data sets in regions where there was data, we have based the analysis below on a composite for the whole period. Thus, all the storm-relative dropsonde data from the whole flight occurring within a particular bin were averaged. This procedure is tantamount to assuming the storm to be in a quasi-steady state for the duration of the flight. Some limitations of the quasi-steady state assumption will emerge later.

3. Storm structure

Figure 1 shows radius-height cross sections obtained from the dropsonde data as described in subsection 2.1 above. The wind data are smoothed using a centred 1-4-1 box filter applied 10 times.

3.1. *Tangential wind and warm core structure*

The storm-relative composite tangential wind component (v, Figure 1a) and temperature perturbation (dT, panel (b)) show the classical structure of a warm-cored vortex with the maximum wind in the lower troposphere and the wind decreasing with height, becoming anticyclonic in the upper troposphere. The decrease in the tangential velocity component with height corresponds through balance considerations with the warm-core structure (see Figure 1b).

There is evidence of a weak inner tangential wind maximum near 40 km and an outer maximum at a radius of about 100 km. The formation of the outer wind maximum was the focus of a separate study by Abarca *et al.* (2016). The upper-level anticyclone begins at a radius of about 80 km, while the strength of the anticyclone increases with radius and the anticyclonic circulation deepens with increasing radius. The maximum anticyclonic flow is found at an altitude between 14 and 15 km at 500 km radius and is clearly increasing beyond this radius.

Figure 1(a) shows also the absolute angular momentum (or M-) surfaces corresponding with the tangential wind component. These are calculated using the formula $M = rv + \frac{1}{2}fr^2$, where r is the radius and f is the Coriolis parameter at the mean latitude of Edouard (33°N) during the period of dropsonde measurements. Consistent with theoretical expectations, the M-surfaces flare outwards with height, with M mostly increasing with radius and decreasing with height. There is a local maximum of M, located at a height of about 6 km and a radius of just over 400 km. This maximum is accompanied by a negative radial gradient of M at radii beyond it, implying that, according to linear theory, the flow would be centrifugally unstable locally (Rayleigh, 1916). Since the dropsonde data at these radii are rather sparse (see Abarca *et al.* 2016, Figure 3(b)) and the period of collection spans an interval of more than 16 h, we do not attribute much significance to the implied regions of instability at these radii.

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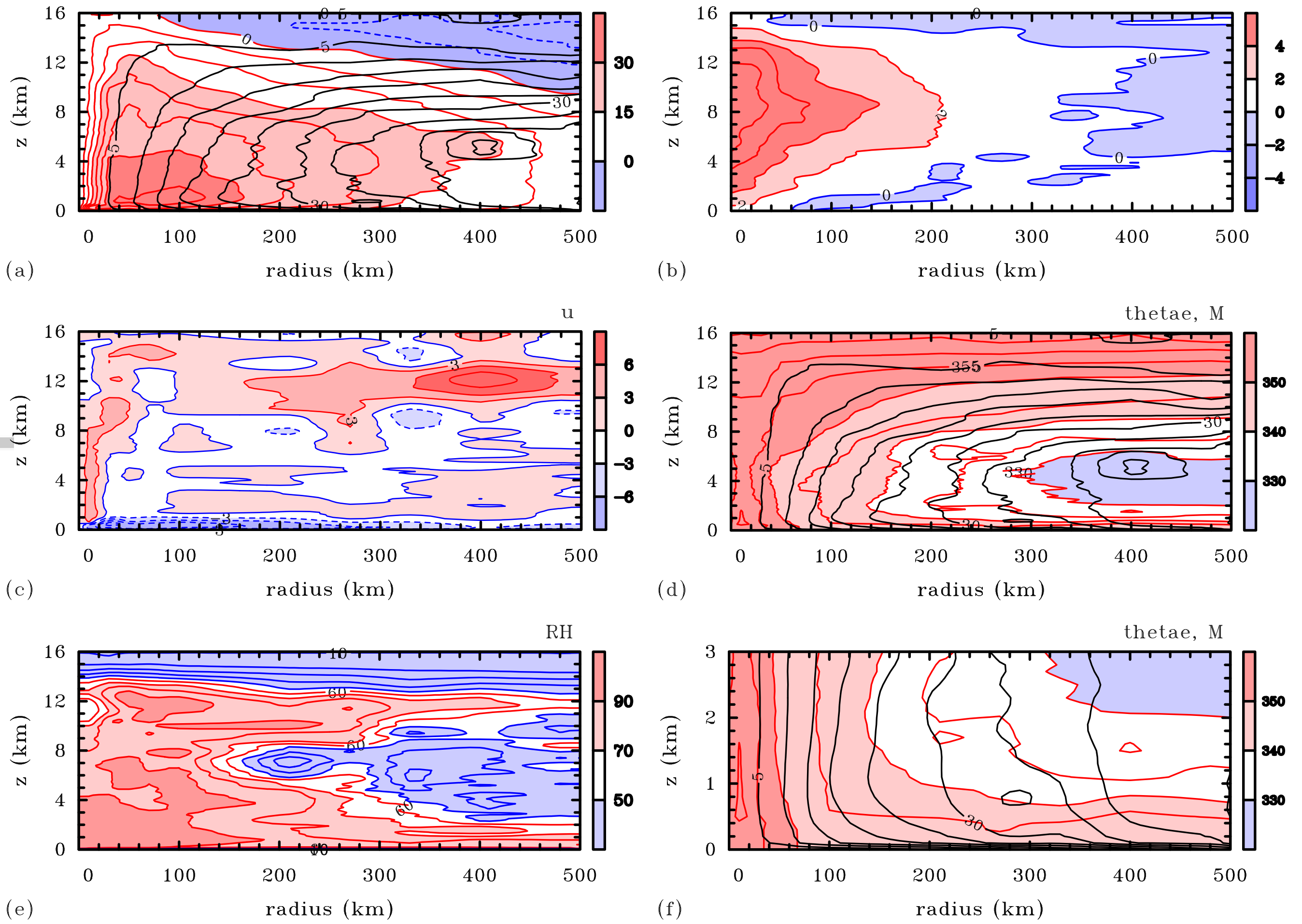

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There is a marked (> 2^{o}C) positive temperature anomaly inside a radius of about 200 km (Figure 1(b)). This anomaly has a maximum of nearly 10^{o}C on the axis of rotation at an altitude of about 8 km. (For the calculation of temperature perturbation, the "environmental temperature" was determined by averaging all dropsonde data at radii > 200 km. Specifically, there were 46 soundings used in calculation of the "environmental" mean temperature for the temperature perturbation plot.) There is a weak cold temperature anomaly at low levels beyond about 60 km radius. The negative temperature anomalies beyond about 400 km radius and those above 13 km are due to the way the ambient temperature has been defined and are presumably not significant. Since the reference temperature is based on an average of all soundings beyond a radius of 200 km and if the temperature in this region decreases outwards, negative anomalies would be expected at large radii. The low-level negative anomaly between 60 and 240 km radius is plausibly a result of the evaporation of falling raindrops.

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boundary layer flow was supergradient below both the primary and secondary eyewalls on the day prior to the present observations. The fact that the storm had just begun to weaken (see section 2.1) would indicate that the spin down tendency due to the outward radial advection of the M-surfaces would be dominant, at least for the inner eyewall. The role of the vertical advection of supergradient values of M from the boundary layer to spin up the inner eyewall was highlighted by the study of Schmidt and Smith (2016) using a minimal three-layer numerical model and was discussed in a more general context by Montgomery and Smith (2017: section 3.9).

Beyond about 300 km radius in Figure 1c, where the boundary layer flow is typically subgradient, there is mostly outflow in the lower troposphere above the boundary layer. At such radii, this outflow would carry the M surfaces outwards leading to a spin-down of the tangential winds and therefore a contracting in the storm size (see Kilroy *et al.* 2016 for a discussion of the factors influencing storm size).

Other interesting features of the radial flow are the layers of inflow in the upper troposphere, above and below the two outflow layers. Such features are often seen in numerical model simulations (e.g. Rotunno and Emanuel 1987, Figure 5c; Persing *et al.* 2013, Figures 10a, 11a, 15a; Montgomery *et al.* 2018, Figures 7b, 8b), but to our knowledge are not well understood.

It should be pointed out that while the broad features of the analyzed radial flow field are robust (e.g. the strong inflow in the boundary layer, the upper-level outflow and the outflow in the inner and outer eyewalls), the details of this field are somewhat sensitive to the way in which the sonde data are binned to produce an azimuthal average (not shown). This sensitivity is compounded by an apparent limitation of the assumed steadiness of the storm over the period of data collection discussed above.

3.3. Pseudo-equivalent potential temperature

The distribution of pseudo-equivalent potential temperature[‡], θ_e, (Figure 1d and 1f) shows the classical structure also. (Figure 1f is a zoomed in plot of Figure 1d in the lowest 3 km.) Principal features are: the mid-tropospheric minimum beyond a radius of about 100 km, increasing in prominence with radius; the tendency for the isopleths of θ_e to become close to vertical in the lower troposphere inside a radius of 100 km; and the tendency for the isopleths of θ_e to slope outwards and become close to horizontal in the upper tropospheric outflow layer. With a little imagination, there is an approximate congruence between the θ_e- and M-surfaces in the inner core region and in the upper troposphere, at least out to 250 km radius (the M-surfaces are shown also in Figure 1d and 1f). This approximate congruence forms the cornerstone of the steady-state axisymmetric hurricane model by Emanuel (1986).

Throughout much of the troposphere, θ_e has a negative radial gradient. This is, in part, a reflection of the structure in the boundary layer. Below about 600 m, the negative radial gradient of θ_e is apparent only inside a radius of about 100 km and is a result of the presumed increase in surface moisture flux with decreasing radius (Malkus and Riehl 1960, Ooyama 1969). Such a localized gradient was documented in the classical observational analysis of Hawkins and Imbembo (1976) and has been confirmed by more recent work (Montgomery *et al.* 2006, Marks *et al.* 2008, Bell and Montgomery 2008, Smith and Montgomery 2013). Maximum values of θ_e exceed 355 K in the low to mid troposphere near and inside the inner eyewall region. The near surface value is approximately constant at 350 K outside of 100 km radius. The minimum value in the mid to low troposphere falls to values less than 320 K beyond about 300 km radius (the region highlighted in blue in Figure 1d).

3.4. Relative humidity

Values of relative humidity[§], (RH, panel (d)), exceed 90% inside a radius of 200 km and below about 7 km altitude. At larger radii, values remain relatively high ($> 80\%$) in a shallow near-surface layer, but decrease markedly with height with values of less than 50% through much of the troposphere, especially beyond a radius of about 300 km. These low values are an indication of drying in the subsiding branch of the secondary circulation. The RH starts to drop off beyond the outer wind maximum, perhaps suggesting that this wind maximum either forms near the boundary with dry air or acts as a potential barrier to dry air. Comparison with Figure 1c shows that relatively dry air is being drawn inwards just below the outflow layer.

4. Conclusions

In this paper we have used a dropsonde data set with unprecedentedly high spatial coverage from the NASA HS3 experiment to analyze the azimuthally-averaged structure of Hurricane Edouard (2014) just after its peak intensity. The dropsondes were deployed from above the tropopause and enable a sampling of the full troposphere. The analyses of these unique observations confirm many known structural features of a mature tropical cyclone, e.g. tangential wind structure, radial wind structure (low-level inflow in a shallow boundary layer, outflow in the upper troposphere), warm core temperature structure, relative humidity structure and equivalent potential temperature structure.

Nevertheless, even with such an unprecedentedly high density of dropsondes to estimate the azimuthally averaged structure, there remain issues in reconciling the radial and tangential structure of the hurricane in the upper troposphere. One issue appears to arise from the analysis assumption of a quasi-steady state during the period of observations, an assumption that stands out as an important limitation of any analysis of dropsonde data over such an extended period of observations as the one in this case. Another issue is that details of the analyzed radial velocity field are somewhat sensitive to the way in which the dropsonde data are partitioned to produce an azimuthal average.

5. Acknowledgements

We thank Jun Zhang and two anonymous reviewers for their perceptive and constructive comments on the original manuscript. RKS acknowledges financial support for tropical cyclone research from the Office of Naval Research Global under Grant No. N62909-15-1-N021. MTM acknowledges the support of NSF grant AGS-1313948, NOAA HFIP grant N0017315WR00048, NASA (HS3) grant NNG11PK021, ONR grant N0001417WX00336, and the U. S. Naval Postgraduate School.

[‡]The quantity θ_e is calculated using Bolton's formula (Bolton, 1980, Equation (43)).
[§]The relative humidity is calculated relative to water saturation.

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