

# **Space Weather**

# **RESEARCH ARTICLE**

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#### **Kev Points:**

- TEC and TEC changes during a storm predicted by ionosphere models were compared with ground-based GPS TEC measurements
- Skill scores (e.g., RMSE, NRMSE, and Yields) were calculated for five latitude regions in the selected eight longitude sectors
- Model performance strongly depends on the quantities considered, the type of metrics used, and the latitude considered

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# CEDAR-GEM Challenge for Systematic Assessment of Ionosphere/Thermosphere Models in Predicting TEC During the 2006 December Storm Event

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**Abstract** In order to assess current modeling capability of reproducing storm impacts on total electron content (TEC), we considered quantities such as TEC, TEC changes compared to quiet time values, and the maximum value of the TEC and TEC changes during a storm. We compared the quantities obtained from ionospheric models against ground-based GPS TEC measurements during the 2006 AGU storm event (14-15 December 2006) in the selected eight longitude sectors. We used 15 simulations obtained from eight ionospheric models, including empirical, physics-based, coupled ionosphere-thermosphere, and data assimilation models. To quantitatively evaluate performance of the models in TEC prediction during the storm, we calculated skill scores such as RMS error, Normalized RMS error (NRMSE), ratio of the modeled to observed maximum increase (Yield), and the difference between the modeled peak time and observed peak time. Furthermore, to investigate latitudinal dependence of the performance of the models, the skill scores were calculated for five latitude regions. Our study shows that RMSE of TEC and TEC changes of the model simulations range from about 3 TECU (total electron content unit, 1 TECU =  $10^{16}$  el m<sup>-2</sup>) (in high latitudes) to about 13 TECU (in low latitudes), which is larger than latitudinal average GPS TEC error of about 2 TECU. Most model simulations predict TEC better than TEC changes in terms of NRMSE and the difference in peak time, while the opposite holds true in terms of Yield. Model performance strongly depends on the quantities considered, the type of metrics used, and the latitude considered.

# 1. Introduction

Our daily lives are increasingly dependent on space-based technological infrastructure, such as satellites used for communications and navigations. Therefore, we are greatly affected by space weather. In mitigating any harmful effect, theory and modeling play a critical role in our quest to understand the connection between solar eruptive phenomena and their impacts in interplanetary space and in the near-Earth space environment, including the Earth's upper atmosphere. To evaluate the current state of space weather modeling capability and to track improvements of space weather models, it is important to assess model performance quantitatively. In an effort to address the needs and challenges of the quantitative assessment of modeling capabilities, the Community Coordinated Modeling Center (CCMC) initiated a series of community-wide model validation projects: Solar Heliospheric and INterplanetary Environment (SHINE), Geospace Environment Modeling (GEM) (Pulkkinen et al., 2010, 2011, 2013; Rastätter et al., 2011, 2013, 2016), Coupling, Energetics and Dynamics of Atmospheric Regions (CEDAR), and GEM-CEDAR Modeling Challenges. The CEDAR ETI (Electrodynamics Thermosphere Ionosphere) Challenge initiated in 2009 focused on the capability of ionosphere-thermosphere (IT) models to reproduce basic IT system parameters, such as electron and neutral densities,  $N_m F_2$ ,  $h_m F_2$ , and vertical drift (Shim et al., 2011, 2012, 2014). Model-data time series comparisons were performed for a set of selected events with different levels of geomagnetic activity (quiet, moderate, and storm conditions). Since 2011, the follow-on CEDAR-GEM Challenge aims to quantify

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models' performance in predicting geomagnetic storm impacts on the ionosphere-thermosphere system parameters, including Joule Heating (Rastätter et al., 2016), total electron content (TEC), and neutral density. TEC is one of the critical parameters in the description of ionospheric variability that affects heavily the accuracy of navigation and communication. There have been many validation studies to estimate the accuracy of TEC prediction of ionosphere models (e.g., Araujo-Pradere et al., 2007; Feltens et al., 2011; Orús et al., 2002, 2003; Zhu et al., 2006). However, for the first time we performed metric studies for various lonosphere/Thermosphere models, including empirical, physics-based, coupled and data assimilation models.

In this paper, we present results of the assessment of the models' performance for reproducing storm impacts on TEC during the 2006 AGU storm (14–15 December 2006) in eight 5° wide longitude sectors. Although this study has a few shortcomings, such as neglecting differences in TEC calculations among models (e.g., upper boundary), considering only one storm event, and using only 1 day TEC values as a quiet reference, the results of this systematic assessment of IT models in predicting TEC changes due to the geomagnetic storm along with our previous findings provide a baseline for future validation studies using new models and improved models.

The GPS TEC measurements and the model simulations used for this study are briefly described in sections 2 and 3, respectively. In section 4, the results of the analysis are presented with the details of the improvements introduced in different model simulations. Finally, the summary and conclusions are presented in section 5.

# 2. GPS Measurements

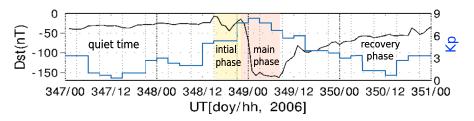
For this study, we selected eight 5° wide longitude sectors  $(25^\circ-30^\circ, 90^\circ-95^\circ, 140^\circ-145^\circ, 175^\circ-180^\circ, 200^\circ-205^\circ, 250^\circ-255^\circ, 285^\circ-290^\circ, and 345^\circ-350^\circ\text{E})$  distributed over the globe.

First, in these eight sectors during the time interval from 13 to 15 December 2006 (see Figure 1 for *Dst* and *Kp* values), we compared three GPS TEC data sets: MIT vertical TEC provided by MIT Haystack Observatory (http://cedar.openmadrigal.org/, http://cedar.openmadrigal.org/cgi-bin/gSimpleUIAccessData.py) (Rideout & Coster, 2006), JPL vertical TEC (Mannucci et al., 1998), and IGS (International GNSS service) vertical TEC map data (Hernandez-Pajares et al., 2009). Figure 2 (top) shows vertical TEC from the three data sets at 30°S in the 285°–290°E longitude sector. The similarity between JPL (denoted in blue) and IGS (green) TEC may be due in part to the fact that JPL TEC is part of the IGS product; IGS TEC is the weighted average of TEC values, which are obtained by using models that fill in the data gaps, from four analysis centers including Center for Orbit Determination in Europe (CODE), European Space Operations Centre of ESA (European Space Agency) (ESOC), Jet Propulsion Laboratory (JPL), and Polytechnical University of Catalonia (UPC). However, the difference between the MIT (red) and JPL/IGS TEC data is noticeable. The MIT TEC values appear to be smaller than JPL/IGS TEC in most cases (not shown here) for this study. The difference between the data sets likely resulted from different mapping functions that convert the line-of-sight TEC to vertical TEC, different pierce point altitudes, and/or different error processing schemes that account for instrument biases and multipath corrections (Hernandez-Pajares et al., 2009; Rideout & Coster, 2006).

However, it appears that the difference between MIT and JPL TEC data (Figure 2, middle) decreases after baseline subtraction by using their minimum value of a quiet day, which is 1 day prior to the storm in this study (13 December 2006, DOY 347) (dTEC\_m = TEC - TEC\_min). In addition, the two data sets show similar differences between TEC at a given UT after the storm occurs and TEC at the same UT on the quiet day (dTEC\_q = TEC - TEC\_quiet) as shown in Figure 2 (bottom). The IGS dTECs, which have a coarser time resolution (2 h) than the MIT and JPL dTECs (15 min), also match relatively well with the other two data sets most of the time.

To quantify storm impact and to reduce the dependence of model performance on a selection of measurement data set as a ground truth, we considered dTEC\_q, dTEC\_m, and maximum values of the dTECs during the storm. Note that throughout this paper dTEC\_m will be denoted as TEC\*, which is the shifted TEC after subtracting minimum of TEC values of DOY 347.

We used the MIT vertical TEC data set as a ground truth, because it is produced by using more GPS TEC data points (from more than 2,000 ground stations) than the others without any interpolation to fill in the data gaps. This guarantees that our results are purely data driven and not affected by the assumptions made in the interpolation schemes used in generating the IGS TEC Maps. Furthermore, the MIT vertical TEC data

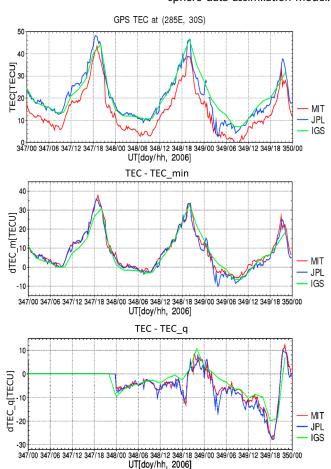


**Figure 1.** *Dst* (black) and *Kp* (blue) values for the 2006 December event.

were obtained by using a pierce point height of 350 km and a 7° elevation cutoff. For the eight longitude sectors, we used the data binned into 5° latitude  $\times$  5° longitude grid cells. The averaged error over all bins of the eight longitude sectors, for this selected time interval, is about 2 TECU (total electron content unit, 1 TECU =  $10^{16}$  el m<sup>-2</sup>). The average number of data points in a bin is about 15.

# 3. Models

A total of 15 model simulations were used for this study. The simulations were produced from eight models: IRI, empirical; SAMI3, USU-IFM, and physics-based ionosphere; CTIPe, GITM, TIE-GCM, Upper Atmosphere Model (UAM), and physics-based coupled ionosphere-thermosphere; and USU-GAIM, a physics-based ionosphere data assimilation model. The model outputs were either submitted by model developers through



**Figure 2.** Example of the observed vertical TEC from the three data sets (MIT GPS in red, JPL TEC in blue, and IGS TEC in green) at  $(285^{\circ}\text{E}, 30^{\circ}\text{S})$  during 13-15 December (DOY 347–349) 2006. The upper, middle and lower panels show vertical TEC, dTEC\_m (TEC — minimum TEC of DOY 347), and dTEC\_q (TEC — TEC on DOY 347), respectively.

the CCMC online submission interface, which was developed for this and other model validation studies, or generated by the CCMC using ionosphere-thermosphere (IT) models hosted at the CCMC (Webb et al., 2009). The submissions of the model outputs are listed in Table 1. Multiple output submissions from one model using different input drivers and/or different boundary conditions are distinguished by unique model setting identifiers. For example, 1\_IRI and 2\_IRI were simulated with different models for topside electron density; 1\_CTIPE and 2\_CTIPE were obtained from different version of the model and slightly different input values; three UAM simulations (1\_UAM-3\_UAM) used different high-latitude electric potential models to model the energy input from the magnetosphere; and 1\_TIE-GCM-4\_TIE-GCM were driven by different high-latitude electric potentials, different tides at the low boundary, and/or with different resolutions (see Table 1). The model setting identifier marked with "a" in Table 1 denotes that model results are submitted by the CCMC. Additional information on the models and the model submissions is available in Shim et al. (2011) (please refer to all references included) and at http://ccmc.gsfc.nasa.gov/challenges/GEM-CEDAR/tags\_list.php.

# 4. Results

Figure 3 shows an example of the observed and modeled vertical TEC in the 285°–290°E longitude sector, where the GPS TEC data coverage is better than in other longitude sectors (see Figure 4). The two topmost-left panels show dTEC\_m and dTEC\_q of the GPS TEC data as a function of geographic latitude and time for the 3 days (DOY 347–DOY 349) of the December 2006 event including one quiet day (DOY 347) prior to the storm.

From top to bottom, the modeled TEC\* (dTEC\_m) and TEC changes (dTEC\_q) obtained from empirical, physics-based ionosphere, coupled ionosphere-thermosphere, and data assimilation model simulations are shown. Figure 3 provides a comparative overview of the models' performance, showing qualitative differences in the TEC prediction

| Table 1         Models Submitted for This Study | r This Study  |   |   |   |
|---|---|---|---|---|
|   |   | Drivers   |   |   |
| Model setting ID                                | Model version   | Input data  | Models used for thermosphere,<br>tides from lower boundary, and<br>high-latitude electrodynamics  | Upper boundary for TEC calculation/<br>resolution |
| 1_IRl <sup>a</sup>                              | IRI-2007 (Bilitza, 1990, 2001;<br>Bilitza & Reinisch, 2008)   | Empirical model<br>F <sub>10.7</sub> , R12, IG12, and <i>ap</i>   | NeQuick model for topside Ne<br>(Coisson et al., 2006),MSIS-86  | ~2,000 km   |
| 2_IRl <sup>a</sup>                              | IRI-2012 (Bilitza et al., 2014)                               | :   | neutral composition (Hedin, 1987, 1991) IRI-corr model for topside Ne, NRLMSISE00 neutral composition (Picone et al., 2002)   |   |
| 1_SAMI3_HWM93 <sup>a</sup>                      | SAMI3 (Huba et al., 2000;<br>Huba et al., 2008)               | Physics-based ionosphere model NRLN HV HV   | model NRLMSISE00 neutral composition, HWM93 wind (Drob et al., 2008; Hedin et al., 1991), $E \times B$ drift  | ~20,000 km,1.5° lat × 4° lon                      |
| 1_USU-IFM <sup>a</sup>                          | IFM (Schunk et al., 2002,<br>1997)                            | F <sub>10.7</sub> , daily <i>Ap</i> , and <i>Kp</i>   | (Scrieness & Fight, 1997) MSIS-90 neutral composition (Hedin, 1991), HWM neutral wind (Hedin et al., 1991), Scherliess and Fejer E × B drift, high-latitude electric fields (Heppner & Maynard, 1987), Hardy aurora precipitation | ~1,600 km,3° lat × 7.5° lon                       |
|   |   | (nauy et al.,<br>Physics-based coupled ionosphere-thermosphere model<br>Tides   | mosphere model Tides High-latitude  | ~2,000 km,2° lat × 18° lon                        |
| 1_CTIPE <sup>a</sup>                            | CTIPe_2.0 (Codrescu et al.,<br>2000; Millward et al.,         | F <sub>10.7</sub> , ACE IMF data and solar wind speed and density, NOAA POES Hemispheric Power data   | Migrating Weimer-2005 high-latitude diurnal and electric potential cemidiirnal (Meimer 1995 2005)   |   |
| 2_CTIPE   | CTIPe_2.1 run at NOAA/<br>SWPC with Weimer-2005               | 1/2*(F <sub>10.7</sub> _81ave_current_day + F <sub>10.7</sub> _previous_day),<br>ACE IMF data and WIND solar wind speed and                         | ш.  |   |
| $^4$ _GITM $^a$                                 | GITM2.0 (Ridley et al., 2006)                                 | Jensity, NOAA FOES Hemispheric Fower data<br>F <sub>10,7</sub> , ACE IMF Data and Solar Wind Speed and<br>Density, NOAA POES Hemispheric Power Data | an Weim<br>99) El<br>ig Ro<br>nd  | ~600 km,2.5° lat × 5° lon                         |
| 1_TIE-GCM <sup>a</sup>                          | TIE-GCM1.93 (Richmond<br>et al., 1992; Roble et al.,<br>1988) | F <sub>10.7</sub> , Kp  | GSWM Heelis high-latitude electric migrating potential model (Heelis et diurnal and al., 1982),Roble and Ridley semidiurnal model.  | ~600 km,5° lat $\times$ 5° lon t                  |
| 2_TIE-GCM<br>3_TIE-GCM                          | TIE-GCM1.94<br>TIE-GCM1.94 with double<br>resolution          | $F_{10.7}$ , $\it Kp$ , OMNI IMF data<br>and solar wind speed and density   | Wein<br>el  | ~600 km,2.5° lat $\times$ 2.5° lon                |
| 4_TIE-GCM                                       | TIE-GCM1.94 with double<br>resolution                         |   | SABER/TIDI precipitation (1987)<br>migrating<br>diurnal and<br>semidiurnal  |   |

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|                                |  | Drivers  |  |   |
|--------------------------------|--|--|--|---|
| Model setting ID               | Model version  | Input data   | Models used for thermosphere,<br>tides from lower boundary, and<br>high-latitude electrodynamics | Upper boundary for TEC calculation/<br>resolution |
| -                              |  |  | - <del>(</del> 2   |   |
| N O AIM                        | Upper Atmosphere Model<br>(UAM) (Namgaladze<br>et al., 1988, 1991) | 710.7, Ap, Kp, AE, IMF data<br>and solar wind speed and density  | equal low FACS using Papitashvill et al. boundary model (2002) and the conditions Hardy model    | ~2,000 Km2* lat (irregular) × 7.5* Ion            |
| 2_UAM                          | UAM with AMIE  |  | with no AMIE electric potential tides model (Richmond, 1992). Hardy auroral precipitation        | ~2,000 km2° lat (irregular) × 15° lon             |
| 3_UAM                          | UAM with Weimer2005  | Physics-based data assimilation model  | Weimer-2005 high latitude electric potential,Hardy auroral precipitation                         |   |
| 1_USU-GAIM <sup>a</sup>        | USU-GAIM2.3 (Scherliess et al., 2004, 2006; Schunk et al., 2004)   | $F_{10.7}$ , daily $Ap_{\nu}$ and $Kp_{\nu}$ GPS TEC observations from more than 350 ground stations ( $-60^{\circ}$ < lat < $60^{\circ}$ )  | The IFM background physics-based ionosphere model, the same models used for IFM                  | ~1,400 km,3–5° lat<br>(irregular) × 15° lon       |
| <sup>a</sup> The model results | are submitted by the CCMC usi                                      | <sup>a</sup> The model results are submitted by the CCMC using the models hosted at the CCMC. Different mode setups are referred as different model setting identification number. | ups are referred as different model setting ide  | ıtification number.                               |

among the simulations. For example, IRIs, 1\_USU-IFM, 4\_GITM, and 1\_USU-GAIM, compared to other simulations, produce larger local daytime TEC\* (dTEC\_m) in southern low and middle latitudes during the initial and main phases of the storm and even during quiet time (see Figure 1). 1\_USU-IFM has also larger TEC\* in southern high latitudes most of the time. 2\_IRI (with NeQuick for topside electron density) has larger TEC\* than 1\_IRI (with IRI-corr) in southern low and middle latitudes. 2\_CTIPE with the improved version has larger TEC than 1\_CTIPe in low and northern high latitudes. Among TIE-GCMs, 1\_TIE-GCM (driven by Heelis high-latitude electric potential model) differs from the others, 2-4 TIE-GCM (driven by Weimer2005), and produces larger TEC\* in high latitudes during the main phase and in low latitudes during the recovery phase. 2\_UAM and 3\_UAM, driven by AMIE and Weimer2005 high-latitude electric potential model, respectively, produce similar TEC\* and dTEC\_q, while 1\_UAM, driven by FAC (field-aligned current), has larger TEC\* in northern high latitudes.

Most simulations, including 1\_SAMI3\_HWM93, which includes plasmasphere TEC, tend to underestimate TEC\* (dTEC\_m) and dTEC\_q as well, although 4\_GITM tends to overestimate TEC\* (dTEC\_m) and TEC changes from the quiet reference (dTEC\_q) especially in northern low latitudes during the recovery phase. 1\_USU-GAIM, obtained by assimilating GPS vertical TEC, tends to agree best with the observed GPS TEC. This is partially due to the fact that slant TEC values from about 350 of the 2,000 stations, which are used to produce the MIT TEC data set, were assimilated for 1\_USU-GAIM. One of possible causes of the tendency for the simulations to underestimate could be the difference between the height of the upper boundary for TEC calculation of the models (especially for the models with upper boundary of about 600 km, see Table 1) and the height of GPS satellites (20,200 km). However, the impact of differing upper boundaries (between the models and between models and observations) is likely reduced by using differential TEC (dTEC\_m and dTEC\_q).

For definite comparisons, we quantified the model performance using skill scores: including (1) root-mean-square error (RMSE =  $\sqrt{\frac{\Sigma(x_{\rm obs}-x_{\rm mod})^2}{N}}$ , where  $x_{\rm obs}$  and  $x_{\rm mod}$  are observed and modeled values), (2) RMSE normalized by the mean absolute value of the observed TEC (NRMSE =  $\frac{\rm RMSE}{\Sigma(x_{\rm obs})/N}$ ), (3) the ratio of the maximum modeled TEC to that of the observed TEC (Yield =  $\frac{(x_{\rm mod})_{\rm max}}{(x_{\rm obs})_{\rm max}}$ ), e.g., [maximum dTEC of the model simulations]/[maximum dTEC of GPS TEC] during 2 days of the storm (DOY 348–DOY 349), and (4) time difference between the modeled peak time and observed peak time (dt\_max = t\_max\_model - t\_max\_obs). In our Yield calculation, we focus on ionospheric positive storm effects (positive Yield) during the 2 days since the long-duration positive storm effects were reported for this storm event (Pedatella et al., 2009).

Figure 5 shows scatterplots of RMSE and NRMSE of the simulations for all eight longitude and five latitude sectors: RMSE in the left and NRMSE in the right panel for each simulation. In each plot, x and y axes correspond to skill scores for dTEC\_m and dTEC\_q predictions, respectively. To investigate latitudinal dependence of model performance, the skill scores were calculated for five latitude regions: low ( $||at|| < 25^\circ$ ; red circles), northern middle ( $25^\circ < |at| < 50^\circ$ ; green squares), southern middle (green

Table 1 (continued)

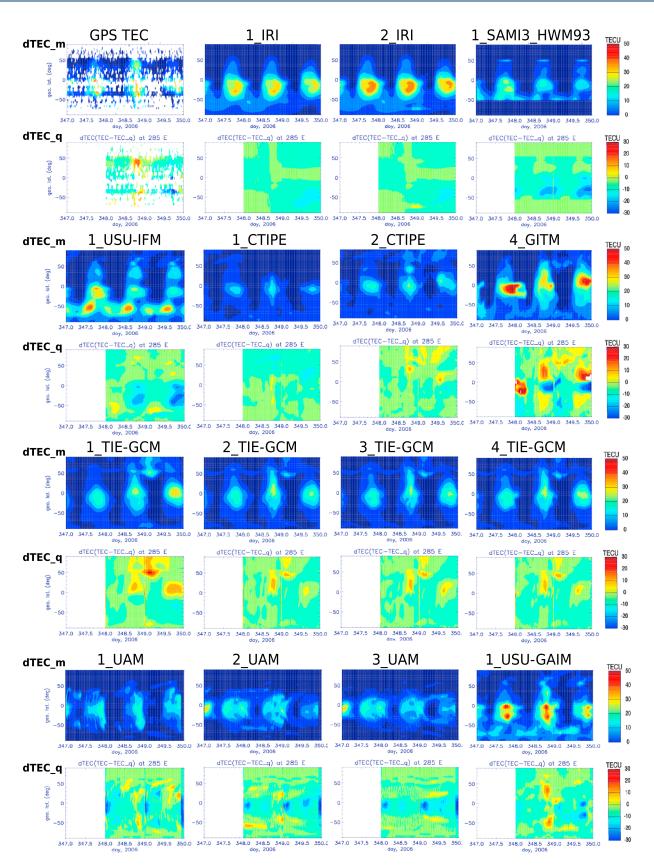
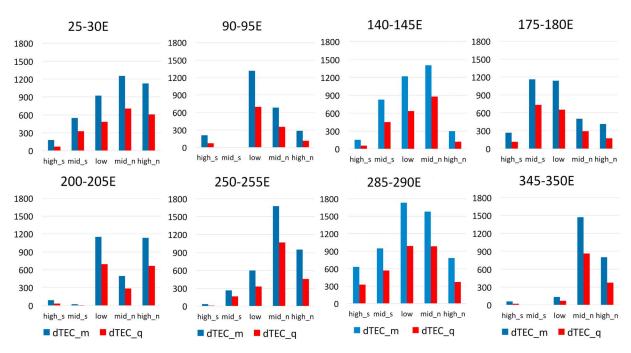


Figure 3. Example of the observed and modeled dTEC\_m (TEC − minimum TEC of DOY 347), and dTEC\_q (TEC − TEC on DOY 347) in 285°E as a function of geographic latitude and UT.



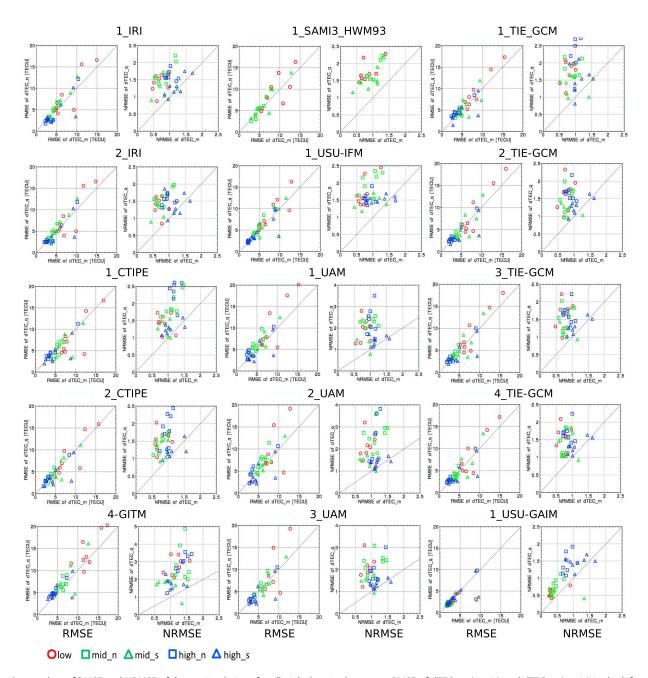
**Figure 4.** The total number of data points used for RMSE and NRMSE calculations for dTEC\_m (blue bars) and dTEC\_q (red bars) predictions in each of eight longitude and five latitude sectors: southern high (lat  $<-50^{\circ}$ ) and middle ( $-50^{\circ} < lat < -25^{\circ}$ ), low (|lat|  $<25^{\circ}$ ), and northern middle ( $25^{\circ} < lat < 50^{\circ}$ ) and high (lat  $>50^{\circ}$ ) latitudes (from left to right on the x axis).

triangles), northern high (lat  $> 50^\circ$ ; blue squares), and southern high (blue triangles) latitudes. It should be noted that data coverage varies with latitudes and longitude sectors (see Figure 4). In southern middle and high latitudes, there are fewer data points than in other latitude regions, and the data are not evenly distributed over the eight longitude sectors. Therefore, comparing the performance in the different latitude regions requires caution.

We found that using only the error values below 95th percentile for all cases, RMSE is reduced by a maximum of 40% and 10% on the average percentage. This indicates that RMSE is not severely affected by a few upper outliers in the distribution.

Most of the model simulations show similar RMSE for the dTEC\_m and dTEC\_ q predictions (close to the dotted line of slope 1). All simulations have the largest RMSE in the low-latitude region (especially in 175°–180°E, 200°–205°E longitude sectors) where TEC values are larger than in higher latitudes. However, NRMSE for the dTEC\_q is larger than NRMSE for dTEC\_m for most cases especially in low latitudes. Note that scale of y axis of NRMSE plots for UAMs and 4\_GITM is different than that of the plots for other simulations. NRMSE for dTEC\_m (TEC) prediction of most simulations ranges between about 0.5 and 1.5, while NRMSE for dTEC\_q (TEC changes) prediction ranges between about 1 and 2.5–3 (between 1 and 4–5 for UAMs and 4\_GITM). This indicates that in terms of NRMSE the models predict TEC\* better than TEC disturbances.

To investigate how the uneven data coverage mentioned above affects globally averaged model performance, we rank the model simulations using four different single values of RMSE in Tables 2a and 2b and NRMSE in Tables 2c and 2d. The four scores include two latitudinal average scores and two global scores. To obtain the two latitudinal average scores, we first calculated longitudinal means of RMSE and NRMSE, which are averages of the values shown in the same color and figures in Figure 5, in each latitude sector. The longitudinal means were averaged again over (1) only three (low and middle) latitude sectors (third column) and (2) all five latitude sectors (fifth column). The two global scores include (1) one global value (of RMSE and NRMSE) obtained by using errors of the simulations for only low and middle latitudes of all longitude sectors (seventh column) and (2) the other global value for all regions (ninth column). For both dTEC\_m and dTEC\_q predictions, all simulations produce the smallest RMSE average over all latitude sectors and the largest global RMSE for low and middle latitudes are larger



**Figure 5.** Scatterplots of RMSE and NRMSE of the 15 simulations for all eight longitude sectors: RMSE of dTEC\_m (*x* axis) and dTEC\_q (*y* axis) in the left panel, and NRMSE in the right panel. Red circles indicate low latitudes, green squares northern middle, green triangles southern middle, blue squares northern high, and blue triangles southern high.

than that for all latitude regions. On the contrary, for dTEC\_m predictions, NRMSE for low and middle latitudes are larger than that for all latitude regions. For dTEC\_q predictions, 2\_TIE-GCM (with Weimer2005) and 2\_UAM (with AMIE) show reduced NRMSE including high latitudes, while CTIPEs (with Weimer2005) and 3\_UAM (with AMIE) show the opposite and the others hardly show any changes. Ranking of the models appears not to depend heavily on the selection of any particular skill score among the four values.

Figure 6 shows the longitudinal average RMSE (top) and NRMSE (bottom), for dTEC\_m (left) and dTEC\_q (right) in each of the five latitude sectors. Four groups of lines with figures correspond to empirical, physics-based ionosphere, coupled ionosphere-thermosphere, and data assimilation model simulations from the left to the right. Note that 1\_SAMI3\_HWM93 data at high latitudes were excluded due to lack of reliability,

**Table 2a** *Model Ranking With Respect to RMSE of dTEC\_m* 

|              |         | Average Ri | MSE (TECU)           |                   | Global RMSE (TECU) |        |           |      |  |
|--------------|---------|------------|----------------------|-------------------|--------------------|--------|-----------|------|--|
|              | Low and | middle     | All latit            | udes              | Low and            | middle | All latit | udes |  |
| TEC*(dTEC_m) | Ranking | RMSE       | Ranking              | RMSE              | Ranking            | RMSE   | Ranking   | RMSE |  |
|              |         |            |                      | Empirical         |                    |        |           |      |  |
| 1_IRI        | 1       | 6.0        | 1                    | 5.4               | 1                  | 6.3    | 1         | 6.1  |  |
| 2_IRI        | 2       | 6.2        | 2                    | 5.5               | 2                  | 6.5    | 2         | 6.3  |  |
|              |         |            | Physics-base         | ed ionosphere mo  | del                |        |           |      |  |
| 1_USU-IFM    | 1       | 6.7        |                      | 5.7               | 1                  | 6.5    |           | 6.2  |  |
| 1_SAMI3      | 2       | 7.0        |                      |                   | 2                  | 7.1    |           |      |  |
|              |         | Phy        | sics-based coupled i | onosphere-therm   | osphere model      |        |           |      |  |
| 4_TIE-GCM    | 1       | 6.3        | 1                    | 5.4               | 1                  | 6.6    | 1         | 6.1  |  |
| 3_TIE-GCM    | 1       | 6.3        | 1                    | 5.4               | 2                  | 6.8    | 2         | 6.3  |  |
| 2_TIE-GCM    | 3       | 6.4        | 1                    | 5.4               | 4                  | 6.9    | 3         | 6.4  |  |
| 2_CTIPE      | 3       | 6.4        | 4                    | 5.5               | 2                  | 6.8    | 3         | 6.4  |  |
| 1_TIE-GCM    | 5       | 6.6        | 5                    | 5.6               | 4                  | 6.9    | 3         | 6.4  |  |
| 1_UAM        | 6       | 7.0        | 6                    | 5.9               | 6                  | 7.4    | 6         | 6.9  |  |
| 3_UAM        | 7       | 7.5        | 7                    | 6.3               | 8                  | 7.9    | 7         | 7.3  |  |
| 2_UAM        | 8       | 7.6        | 8                    | 6.4               | 9                  | 8.0    | 8         | 7.4  |  |
| 1_CTIPE      | 8       | 7.6        | 8                    | 6.4               | 7                  | 7.9    | 8         | 7.4  |  |
| 4_GITM       | 10      | 8.8        | 10                   | 7.1               | 10                 | 9.5    | 10        | 8.6  |  |
|              |         |            | Physics-based o      | lata assimilation | model              |        |           |      |  |
| 1_USU-GAIM   |         | 3.3        | ·                    | 3.6               |                    | 2.8    |           | 3.5  |  |

since SAMI3 does not include high-latitude driving forces (e.g., the auroral precipitation and the convection electric field pattern). Therefore, in Figure 6, the performance of the simulations is ranked based on the average RMSE and NRMSE over three latitude (low and middle) sectors (see Tables 2a, 2b, 2c, 2d). The best performing simulation is located in the extreme left in each group.

Simulations using the empirical model IRI, 1\_IRI, and 2\_IRI perform similar to each other to predict TEC\* (dTEC\_m) and dTEC\_q for most cases, especially in middle latitudes. Note that different scales are used for dTEC\_m and dTEC\_q.

**Table 2b** *Model Ranking With Respect to RMSE of dTEC\_q* 

|            |         | Average RI | MSE (TECU)           |                   |                | Global RMSE (TECU) |           |       |  |
|------------|---------|------------|----------------------|-------------------|----------------|--------------------|-----------|-------|--|
|            | Low and | middle     | All latit            | udes              | Low and        | middle             | All latit | tudes |  |
| dTEC_q     | Ranking | RMSE       | Ranking              | RMSE              | Ranking        | RMSE               | Ranking   | RMSE  |  |
|            |         |            |                      | Empirical         |                |                    |           |       |  |
| 2_IRI      | 1       | 6.6        | 1                    | 5.5               | 1              | 7.4                | 1         | 7.2   |  |
| 1_IRI      | 2       | 6.7        | 2                    | 5.5               | 2              | 7.5                | 2         | 7.2   |  |
|            |         |            | Physics-bas          | sed ionosphere me | odel           |                    |           |       |  |
| 1_USU-IFM  | 1       | 7.4        | 1                    | 6.0               | 1              | 7.8                | 1         | 7.3   |  |
| 1_SAMI3    | 1       | 7.4        |                      |                   | 2              | 8.0                |           |       |  |
|            |         | P <i>l</i> | nysics-based coupled | ionosphere-thern  | nosphere model |                    |           |       |  |
| 2_CTIPE    | 1       | 6.3        | 1                    | 5.3               | 1              | 7.2                | 1         | 6.8   |  |
| 4_TIE-GCM  | 2       | 6.4        | 1                    | 5.3               | 2              | 7.4                | 2         | 6.9   |  |
| 2_TIE-GCM  | 3       | 6.6        | 3                    | 5.4               | 5              | 7.8                | 4         | 7.3   |  |
| 3_TIE-GCM  | 3       | 6.6        | 3                    | 5.4               | 4              | 7.7                | 3         | 7.2   |  |
| 1_CTIPE    | 5       | 6.7        | 5                    | 5.8               | 3              | 7.6                | 4         | 7.3   |  |
| 1_TIE-GCM  | 6       | 6.9        | 6                    | 6.0               | 6              | 7.8                | 6         | 7.4   |  |
| 1_UAM      | 7       | 8.1        | 8                    | 6.6               | 7              | 9.5                | 7         | 8.8   |  |
| 3_UAM      | 8       | 8.2        | 7                    | 6.5               | 8              | 9.9                | 8         | 9.1   |  |
| 2_UAM      | 9       | 8.6        | 9                    | 6.9               | 9              | 10.3               | 9         | 9.5   |  |
| 4_GITM     | 10      | 9.9        | 10                   | 8.0               | 10             | 11.3               | 10        | 10.3  |  |
|            |         |            | Physics-based        | data assimilation | model          |                    |           |       |  |
| 1_USU-GAIM | 2.6     | 2.6        | 3.1                  | 3.1               | 2.6            | 2.6                | 3.3       | 3.3   |  |

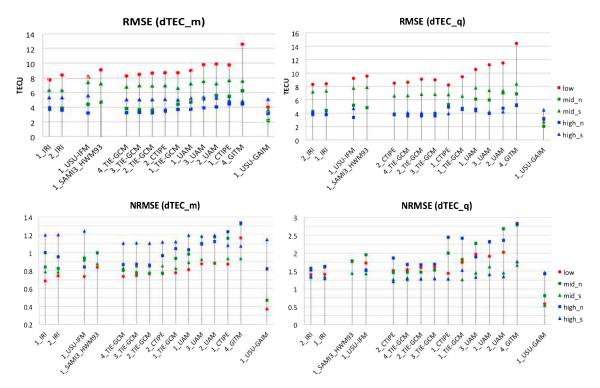
**Table 2c** *Model Ranking With Respect to NRMSE of dTEC\_m* 

|               |         | Average | e NRMSE               |                   | Global NRMSE  |        |           |      |  |
|---------------|---------|---------|-----------------------|-------------------|---------------|--------|-----------|------|--|
|               | Low and | middle  | All latit             | udes              | Low and       | middle | All latit | udes |  |
| TEC* (dTEC_m) | Ranking | RMSE    | Ranking               | RMSE              | Ranking       | RMSE   | Ranking   | RMSE |  |
|               |         |         | I                     | mpirical          |               |        |           |      |  |
| 1_IRI         | 1       | 0.77    | 1                     | 0.91              | 1             | 0.80   | 1         | 0.88 |  |
| 2_IRI         | 2       | 0.79    | 1                     | 0.91              | 2             | 0.83   | 2         | 0.90 |  |
|               |         |         | Physics-base          | ed ionosphere mo  | del           |        |           |      |  |
| 1_USU-IFM     | 1       | 0.87    |                       | 0.94              | 1             | 0.82   |           | 0.89 |  |
| 1_SAMI3       | 2       | 0.91    |                       |                   | 2             | 0.90   |           |      |  |
|               |         | Phy     | rsics-based coupled i | onosphere-therm   | osphere model |        |           |      |  |
| 4_TIE-GCM     | 1       | 0.79    | 1                     | 0.87              | 1             | 0.83   | 1         | 0.89 |  |
| 3_TIE-GCM     | 1       | 0.79    | 1                     | 0.87              | 2             | 0.86   | 2         | 0.91 |  |
| 2_TIE-GCM     | 3       | 0.80    | 1                     | 0.87              | 4             | 0.87   | 3         | 0.92 |  |
| 2_CTIPE       | 3       | 0.80    | 4                     | 0.90              | 2             | 0.86   | 3         | 0.92 |  |
| 1_TIE-GCM     | 5       | 0.85    | 5                     | 0.95              | 4             | 0.87   | 5         | 0.93 |  |
| 1_UAM         | 6       | 0.90    | 6                     | 0.99              | 6             | 0.94   | 6         | 0.99 |  |
| 3_UAM         | 7       | 0.97    | 7                     | 1.05              | 7             | 1.00   | 8         | 1.06 |  |
| 2_UAM         | 8       | 0.98    | 8                     | 1.06              | 7             | 1.00   | 8         | 1.06 |  |
| 1_CTIPE       | 9       | 0.99    | 9                     | 1.07              | 7             | 1.00   | 7         | 1.05 |  |
| 4_GITM        | 10      | 1.14    | 10                    | 1.18              | 10            | 1.21   | 10        | 1.24 |  |
|               |         |         | Physics-based a       | lata assimilation | model         |        |           |      |  |
| 1_USU-GAIM    |         | 0.44    | 0.67                  | 0.67              | 0.36          | 0.36   | 0.50      | 0.50 |  |

Two physics-based ionospheric model simulations, 1\_USU-IFM and 1\_SAMI3\_HWM93, also show similar scores when considering scores available from both simulations (e.g., low and middle latitudes). 1\_USU-IFM performs slightly better than 1\_SAMI3\_HWM93 in low and northern middle latitudes for dTEC\_m, while the opposite is true in northern middle latitudes for dTEC\_q. However, the differences in averaged RMSE and NRMSE of the two simulations for low and middle latitudes do not exceed 0.5 TECU and 0.04, respectively (see Tables 2a, 2b, 2c, 2d). Both models use the same empirical models for the thermosphere wind and

**Table 2d**Model Ranking With Respect to NRMSE of dTEC\_q

|            |         | Average | e NRMSE              | Global NRMSE      |                |        |           |       |
|------------|---------|---------|----------------------|-------------------|----------------|--------|-----------|-------|
|            | Low and | middle  | All latit            | udes              | Low and        | middle | All latit | tudes |
| dTEC_q     | Ranking | RMSE    | Ranking              | RMSE              | Ranking        | RMSE   | Ranking   | RMSE  |
|            |         |         |                      | Empirical         |                |        |           |       |
| 2_IRI      | 1       | 1.44    | 1                    | 1.45              | 1              | 1.71   | 1         | 1.74  |
| 1_IRI      | 2       | 1.46    | 2                    | 1.47              | 2              | 1.72   | 2         | 1.75  |
|            |         |         | Physics-bas          | sed ionosphere me | odel           |        |           |       |
| 1_SAMI3    | 1       | 1.66    |                      |                   | 2              | 1.91   |           |       |
| 1_USU-IFM  | 2       | 1.70    | 1                    | 1.65              | 1              | 1.86   | 1         | 1.88  |
|            |         | Pł      | nysics-based coupled | ionosphere-thern  | nosphere model |        |           |       |
| 2_CTIPE    | 1       | 1.42    | 2                    | 1.47              | 1              | 1.73   | 4         | 1.87  |
| 4_TIE-GCM  | 1       | 1.42    | 1                    | 1.46              | 2              | 1.76   | 2         | 1.78  |
| 2_TIE-GCM  | 3       | 1.45    | 3                    | 1.47              | 5              | 1.87   | 1         | 1.75  |
| 3_TIE-GCM  | 4       | 1.48    | 4                    | 1.49              | 4              | 1.84   | 3         | 1.85  |
| 1_CTIPE    | 5       | 1.57    | 5                    | 1.71              | 3              | 1.82   | 8         | 2.33  |
| 1_TIE-GCM  | 6       | 1.61    | 6                    | 1.78              | 5              | 1.87   | 6         | 1.89  |
| 3_UAM      | 7       | 1.90    | 7                    | 1.80              | 8              | 2.36   | 9         | 2.45  |
| 1_UAM      | 8       | 1.95    | 8                    | 1.93              | 7              | 2.28   | 7         | 2.26  |
| 2_UAM      | 9       | 2.06    | 9                    | 2.00              | 9              | 2.47   | 5         | 1.88  |
| 4_GITM     | 10      | 2.42    | 10                   | 2.41              | 10             | 2.69   | 10        | 2.64  |
|            |         |         | Physics-based        | data assimilation | model          |        |           |       |
| 1_USU-GAIM |         | 0.64    | 0.99                 | 0.99              | 0.63           | 0.63   | 0.85      | 0.85  |



**Figure 6.** Model ranking for predicting dTEC\_m (left) and dTEC\_q (right) based on RMS error (top), and NRMS error (bottom). Red circles denote the average values of eight longitude sectors for low latitudes ( $|\text{lat}| < 25^\circ$ ), green squares and triangles indicate the average of those for middle latitudes ( $25^\circ < |\text{lat}| < 50^\circ$ ) in Northern and Southern Hemispheres, blue squares and triangles indicate the average for high geographic latitudes ( $|\text{lat}| > 50^\circ$ ) in Northern and Southern Hemispheres, respectively. The ranking of the models performance among the same types of the models is arranged by the average values of three latitude sectors (low and middle latitudes ( $|\text{mid}_n|$  and  $|\text{mid}_s|$ ) in each group of the models. The best performing model is located in the extreme left in each group.

compositions, and low-latitude electric fields. After including scores for high latitudes of 1\_USU-IFM, the differences in averaged RMSE become larger (~1.4 TECU). Although the averaged NRMSE differences remain similar (~0.03), the rank of the two simulations for dTEC\_m is reversed; 1\_SAMI3\_HWM93 shows slightly better performance than 1\_USU-IFM.

Among 10 physics-based coupled ionosphere-thermosphere simulations, 2\_CTIPE and three TIE-GCM runs (2\_TIE-GCM through 4\_TIE-GCM, referred to as 2-4\_TIEGCMs) perform better than the other six simulations. 2\_CTIPE tends to perform better than 2-4\_TIE-GCMs for the dTEC\_q prediction. The opposite holds true for the dTEC m prediction. The four TIE-GCM simulations show similar RMSE and NRMSE in southern middle latitudes. However, in the other latitude sectors, the dTECs prediction of 1\_TIE-GCM, which is driven by the Heelis electric potential with constant critical crossover latitudes, is less satisfactory than that of the other three TIE-GCM simulations, which are driven by the Weimer-2005 electric potential with dynamic critical crossover latitudes. This is caused mainly by a poorer performance in high latitudes. Among the three simulations, 2-4\_TIE-GCMs, which show similar accuracy predicting dTECs, 4\_TIE-GCM (driven by SABER/TIDI lower boundary conditions) does better reproducing low-latitude TEC. With regard to the two CTIPE simulations, 2\_CTIPE performs better than 1\_CTIPE for all cases, although 1\_CTIPE shows better scores for dTEC\_q prediction at low latitudes. Differences between the two CTIPE simulations are caused by different input data sets for the solar wind parameters and different values for the solar flux (see Table 1). 2\_CTIPE shows better performance than 1\_CTIPE, especially at high latitudes. The model version used in 1\_CTIPE simulation is an older version of 2\_CTIPE, and required the use of trimmed IMF (interplanetary magnetic field) values. For example, the magnitude of IMF has a saturated value of about 12 nT when  $B_z$  is less than -10 nT. 4\_GITM shows similar performance in predicting middle- and high-latitude TEC, but it performs worse for low-latitude TEC prediction than the other simulations. Three UAM simulations driven by different high-latitude electric potential models also show similar skill scores. However, 1 and 3\_UAM perform better than 2\_UAM for most cases; 1\_UAM and 3\_UAM appear to be better for low-latitude dTECs and high-latitude dTEC\_q prediction, respectively.

The only simulation using a data assimilation model, 1\_USU-GAIM, outperforms other models for all cases excluding high-latitude TEC prediction. The average RMSE of 1\_USU-GAIM for TEC\* (dTEC\_m) prediction is about 4 TECU, which is twice the average GPS TEC error of 2 TECU.

The RMSE of TEC\* (dTEC\_m) for all simulations and all cases ranges from about 3 TECU in northern high latitudes to about 13 TECU in low latitudes. Even the lowest RMSE of the simulations is larger than average GPS TEC error of about 2 TECU.

In Figure 7, we present Yield (ratio of modeled to observed maximum difference) and differences in time  $(dt_max = t_max_model - t_max_obs)$ , considering only the maximum of dTECs that occurs during the storm time, between the simulations and observation. Yield and  $dt_max$  are shown in left and right columns, respectively, in each simulation group. The x and y axes corresponds to the values of dTEC\_m and dTEC\_q, respectively. Colors and figures indicate different latitudes, as the same in Figure 5.

The largest maximum increase in GPS TEC due to the storm occurs in low-latitude regions in the 200°–205°E longitude sector during the main phase; dTEC\_q reaches up to about 70 TECU (not shown here), which is about 5 times the quiet time TEC. The largest maximum percentage increase in TEC occurs in the 175°–180°E longitude sector in low-latitude regions during the main phase; dTEC\_q of 50 TECU is about 7 times larger than the quiet time TEC. These facts possibly explain why most model simulations have the largest RMSE in the low-latitude region in 175°–180°E and 200°–205°E longitude sectors due to the tendency of the models to underestimate TEC (as described above), while RMSEs in the other longitude sectors are relatively similar to each other.

Most models have the tendency to underestimate the peak of dTECs. However,  $4\_GITM$  and TIE-GCMs appear to overestimate dTECs' peak in more cases in comparison to the other model simulations. Two simulations,  $1\_IRI$  and  $2\_IRI$ , of the empirical model, which represents average ionospheric conditions, produce the smallest Yield of dTEC $_q$  (<0.5 for most cases), even though the performance of the model in terms of the RMSE and/or NRMSE is comparable to that of the physics-based models.

1\_USU-GAIM has a smaller spread of data points of time difference, dt\_max, compared to other models. 2\_IRI and 1\_USU-IFM have smaller spread of data points of time difference than 1\_IRI and 1\_SAMI3\_HWM93, respectively. TIE-GCM runs have more data points closer to the line dt\_max = 1 than other coupled physics-based model simulations. 1\_IRI, 2\_UAM, and CTIPE runs tend to reach the maximum values of both dTEC\_m and dTEC\_q more often before the observed maximum occurs.

Tables 3a and 3b show global ranking of the simulations in terms of two averages (as the same as in Tables 2a, 2b, 2c, 2d) of Yield and dt\_max: over (1) low and middle latitudes and (2) all five latitudes. With high latitudes included, the following results are observed: 1\_IRI and 2\_IRI produce worse Yield and dt\_max for dTEC\_m prediction, but they produce better or similar scores for dTEC\_q prediction; I\_USU-IFM shows better Yield and dt\_max for both dTECs' predictions; 4\_GITM does not much change in the scores but produces better Yield for dTEC\_q and dt\_max for dTEC\_m; 1-3\_UAM produce worse scores for most cases; however, 2\_UAM and 3\_UAM show better dt\_max for dTEC\_q; 2\_CTIPE has better Yield and dt\_max for dTEC\_q, while 1\_CTIPE has worse scores for both dTECs; four TIE-GCMs produce better Yield and dt\_max, especially dt\_max for dTEC\_m, it caused noticeable ranking changes for dt\_max prediction. However, with respect to Yield and dt\_max, the global ranking of the simulations seems not to be affected strongly by including high latitudes in other cases.

Figure 8 (top) shows the longitudinal average Yield (modeled dTEC\_max/observed dTEC\_max) of dTEC\_m (left) and dTEC\_q (right) sectors, and Figure 8 (bottom) shows the longitudinal average time differences (average of |dt\_max|) in the five latitudes. The longitudinal average scores were obtained from the values shown in the same color and figures in Figure 7. The results of the simulations are grouped according to the type of the models, and the best simulation is located at the leftmost in each group as the same as in Figure 6. The performance of the simulations is ranked based on the average scores over three latitude (low and middle) sectors (see Tables 3a and 3b). All simulations tend to underestimate dTECs for all cases with the exceptions of 4\_GITM and 1\_TIE-GCM, which are ranked first and second place in their group based on the average Yield for dTEC\_q over low and middle latitudes. 4\_GITM produces best Yield among all simulations, while 1\_USU-GAIM predicts best the time at which the maximum dTECs occur for most cases (about 5 h difference on the average). Most models tend to produce larger dt\_max for low latitudes (red circles).

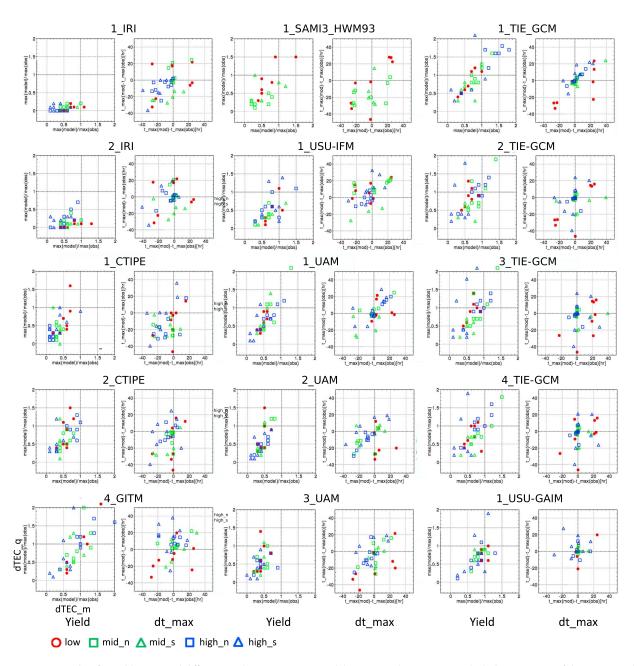


Figure 7. Same as Figure 5 but for Yield (ratio) and differences (dt\_max = t\_max\_model - t\_max\_obs) in time (at which the maximum of dTECs occurs during the storm time) between a simulation and observation.

The two IRI runs produce similar scores of Yield and dt\_max, but 2\_IRI slightly outperforms 1\_IRI for all cases. The IRI runs perform worse in predicting Yield of dTEC\_q than that of TEC (dTEC\_m) with one exception (2\_IRI in southern high latitudes), although there is relatively small difference in average dt\_max between dTEC\_m and dTEC\_q predictions of the two simulations (see Tables 3a and 3b).

1\_USU-IFM shows better Yield and dt\_max of dTEC\_m than 1\_SAMI3\_HWM93, which shows better Yield of dTEC\_q. 1\_SAMI3\_HWM93 appears to predict better Yield for low latitudes than 1\_USU-IFM, but the opposite holds true for dt\_max. The two simulations produce similar Yield and dt\_max in northern middle latitudes.

The physics-based coupled models make better prediction of peak values of dTECs in middle and high latitudes of the Northern Hemisphere than in the Southern Hemisphere. They perform better in predicting Yield of dTEC\_q than that of dTEC\_m for most cases, which is opposite to the empirical and data

**Table 3a**Model Ranking With Respect to Yield and dt\_max of dTEC\_m

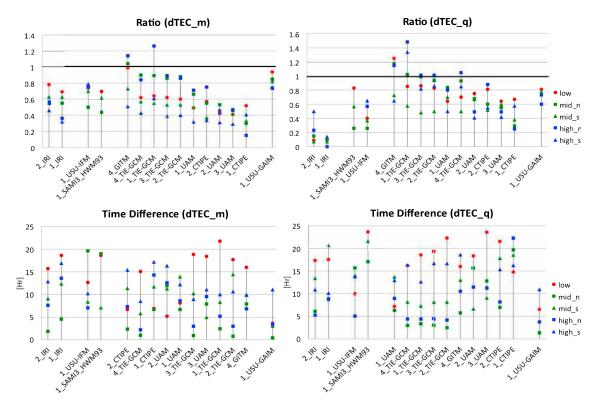
|               | Average yield |        |                     |                  |                 | Average  | Average  dt_max  (h) |        |  |
|---------------|---------------|--------|---------------------|------------------|-----------------|----------|----------------------|--------|--|
|               | Low and       | middle | All latit           | udes             | Low and         | l middle | All lat              | tudes  |  |
| TEC* (dTEC_m) | Ranking       | Yield  | Ranking             | Yield            | Ranking         | dt_max   | Ranking              | dt_max |  |
|               |               |        |                     | Empirical        |                 |          |                      |        |  |
| 2_IRI         | 1             | 0.66   | 1                   | 0.60             | 1               | 8.9      | 1                    | 9.4    |  |
| 1_IRI         | 2             | 0.62   | 2                   | 0.51             | 2               | 11.9     | 2                    | 13.2   |  |
|               |               |        | Physics-ba          | sed ionosphere i | model           |          |                      |        |  |
| 1_USU-IFM     | 1             | 0.65   |                     | 0.70             | 1               | 13.6     |                      | 11.6   |  |
| 1_SAMI3       | 2             | 0.58   |                     |                  | 2               | 14.9     |                      |        |  |
|               |               | Ph     | ysics-based coupled | l ionosphere-the | rmosphere model |          |                      |        |  |
| 4_GITM        | 1             | 0.92   | 1                   | 0.88             | 10              | 11.3     | 7                    | 10.1   |  |
| 4_TIE-GCM     | 2             | 0.70   | 2                   | 0.67             | 2               | 7.3      | 1                    | 6.5    |  |
| 1_TIE-GCM     | 3             | 0.69   | 2                   | 0.79             | 8               | 10.8     | 5                    | 9.5    |  |
| 3_TIE-GCM     | 4             | 0.67   | 4                   | 0.66             | 6               | 10.0     | 2                    | 8.4    |  |
| 2_TIE-GCM     | 4             | 0.67   | 5                   | 0.65             | 9               | 11.0     | 4                    | 9.3    |  |
| 1_UAM         | 6             | 0.55   | 6                   | 0.54             | 5               | 9.6      | 6                    | 9.9    |  |
| 2_CTIPE       | 7             | 0.50   | 7                   | 0.52             | 1               | 6.8      | 3                    | 8.6    |  |
| 2_UAM         | 8             | 0.48   | 8                   | 0.44             | 4               | 9.5      | 10                   | 11.5   |  |
| 3_UAM         | 9             | 0.43   | 9                   | 0.41             | 7               | 10.4     | 8                    | 10.4   |  |
| 1_CTIPE       | 10            | 0.39   | 10                  | 0.34             | 3               | 8.4      | 9                    | 11.4   |  |
|               |               |        | Physics-based       | data assimilatio | on model        |          |                      |        |  |
| 1_USU-GAIM    |               | 0.87   | · ·                 | 0.82             |                 | 2.3      |                      | 4.3    |  |

assimilation model simulations. It indicates that the physics-based coupled model simulations tend to predict TEC increases (dTEC\_q) somewhat better than TEC itself (dTEC\_m). However, in most of the simulations, dt\_max values of dTEC\_q are larger than or similar to those of dTEC\_m.

The average values of Yield of 4\_GITM and 1\_TIE-GCM are closer to 1, with a larger spread of Yield around the mean compared to other simulations. Four TIE-GCM runs, 1–4\_TIE-GCM, rank higher for predicting both Yield and dt\_max, while 4\_GITM ranks first for Yield but ranks lower for predicting dt\_max.

**Table 3b**Model Ranking With Respect to Yield and dt\_max of dTEC\_q

|            |         | Average yield Average  dt_ |                      |                   |                  | It_max  (hrs) |         |        |
|------------|---------|----------------------------|----------------------|-------------------|------------------|---------------|---------|--------|
|            | Low and | middle                     | All latit            | udes              | Low and          | l middle      | All lat | itudes |
| dTEC_q     | Ranking | Yield                      | Ranking              | Yield             | Ranking          | dt_max        | Ranking | dt_max |
|            |         |                            |                      | Empirical         |                  |               |         |        |
| 2_IRI      | 1       | 0.10                       | 1                    | 0.21              | 1                | 12.3          | 1       | 10.6   |
| 1_IRI      | 2       | 0.08                       | 2                    | 0.08              | 2                | 15.7          | 2       | 13.2   |
|            |         |                            | Physics-b            | ased ionosphere   | model            |               |         |        |
| 1_SAMI3    | 1       | 0.55                       |                      |                   | 2                | 20.8          |         |        |
| 1_USU-IFM  | 2       | 0.34                       |                      | 0.45              | 1                | 13.3          |         | 11.7   |
|            |         | F                          | Physics-based couple | ed ionosphere-the | ermosphere model |               |         |        |
| 4_GITM     | 1       | 1.05                       | 2                    | 0.99              | 6                | 11.6          | 7       | 12.8   |
| 1_TIE-GCM  | 2       | 0.82                       | 1                    | 1.05              | 3                | 9.7           | 1       | 9.2    |
| 3_TIE-GCM  | 3       | 0.78                       | 3                    | 0.83              | 4                | 10.2          | 4       | 10.3   |
| 2_TIE-GCM  | 4       | 0.75                       | 4                    | 0.83              | 5                | 11.0          | 5       | 10.8   |
| 1_UAM      | 5       | 0.73                       | 6                    | 0.70              | 1                | 9.1           | 3       | 9.8    |
| 4_TIE-GCM  | 6       | 0.71                       | 5                    | 0.81              | 2                | 9.1           | 2       | 9.6    |
| 2_UAM      | 7       | 0.70                       | 8                    | 0.60              | 7                | 13.6          | 6       | 12.7   |
| 2_CTIPE    | 8       | 0.64                       | 7                    | 0.67              | 9                | 15.5          | 9       | 14.0   |
| 3_UAM      | 9       | 0.60                       | 9                    | 0.54              | 8                | 15.2          | 8       | 13.6   |
| 1_CTIPE    | 10      | 0.45                       | 10                   | 0.43              | 10               | 17.7          | 10      | 18.4   |
|            |         |                            | Physics-base         | ed data assimilat | ion model        |               |         |        |
| 1_USU-GAIM |         | 0.78                       |                      | 0.73              | 3                | 3.1           | 5       | 4.8    |



**Figure 8.** Same as Figure 6 but for model ranking based on Yield (ratio of the maximum modeled TEC to that of the observed TEC) and time difference, which is average of time delay (dt\_max >0) and |time advance| (dt\_max <0), of dTEC\_m (left) and dTEC\_q (right) from top to bottom.

The four TIE-GCM runs show similar performance especially in low and middle latitudes, and among them, 2–4\_TIE-GCM driven by Weimer2005 show similar performance for most cases at high latitudes. 1\_TIE-GCM driven by Heelis appears to overestimate Yield of dTEC\_q in both southern and northern high latitudes, whereas the other three TIE-GCMs tend to slightly underestimate Yield in southern high latitudes and produce almost perfect Yield in northern high latitudes. Compared to other physics-based coupled model simulations, 2–4\_TIE-GCM capture better the peak time of dTECs in northern middle (about 1 h for dTEC\_m and 3 h for dTEC\_q).

The three UAMs and two CTIPEs rank lower than others for most cases; however, 2\_CTIPE and 1\_UAM (driven by FAC) rank higher for dt\_max of dTEC\_m and dTEC\_q, respectively. 2\_CTIPE produces better ratios and time differences for all cases than 1\_CTIPe. 1\_UAM, which performs better than 2–3\_UAM for most cases, hardly shows differences in dt\_max between dTECs, while 2–3\_UAM produce noticeable differences in dt\_max between dTECs in most latitude regions.

The data assimilation model, I\_USU-GAIM, produces Yield of dTECs comparable to those of the highest-ranked physics-based coupled model simulations and predicts best the time at which the maximum dTECs occur in low and middle latitudes (about  $0.4 \sim 3-4$  h for dTEC\_m and 1-6 h for dTEC\_q).

# 5. Summary and Conclusion

We quantitatively assessed the performances of ionospheric models in predicting geomagnetic storm impact on TEC in the selected eight longitude sectors during 2006 December storm event (DOY 347–350). For this study, the modeled values obtained from 15 simulations using eight ionospheric models were compared with the observed ground-based GPS TEC values. We considered TEC\* (dTEC\_m) during the storm, TEC changes (dTEC\_q) due to the storm, and maximum values of the dTECs.

The performance of the models was quantified using skill scores such as RMS error (RMSE), Normalized RMS error (NRMSE), the ratio of maximum value of the models to the observation (Yield), and the differences

(dt\_max) in peak time (dt\_max = t\_max\_model — t\_max\_obs) between the simulations and the observations. Using Yield, we evaluated the capability of the models to produce peak values of TEC increase during the storm. The skill scores were calculated for five latitude regions to investigate the latitudinal dependence of the performance of the models. The simulations were grouped based on the type of model and ranked first based on the average values of the skill scores over all eight longitude and three latitude sectors (low and middle latitudes). This was done because (1) 1\_SAMI3\_HWM93 data at high latitudes were excluded due to lack of reliability and (2) the relatively low data coverage of GPS TEC in high latitudes may have an effect on the overall scores. Therefore, we also ranked the simulations according to average skill scores over all longitude and latitude regions, and global RMSE and NRMSE for the error values over (1) only low and middle latitudes and (2) all latitudes. Ranking of the models in terms of RMSE and NRMSE appears not to depend heavily on the selection of any particular skill score among the four values. With respect to Yield and dt\_max, the global ranking of the simulations also does not seem to be strongly affected by including high latitudes in most cases, although there are noticeable ranking changes for dt\_max of dTEC\_m among four TIE-GCMs with better scores, and 2\_UAM and 1\_CTIPE with worse scores in high latitudes.

In agreement with our previous study (Shim et al., 2012, 2014), we found that model performance depends on the type of metrics and latitude as well. For instance, although our results based on the average skill scores show that the performance of the data assimilation model, 1\_USU-GAIM, is superior to the other models' performance in most cases, especially in low- and middle-latitude TEC predictions, other physics-based model simulations (e.g., TIE-GCMs) are better than or comparable to 1\_USU-GAIM in southern high-latitude dTECs prediction with respect to RMSE and NRMSE. In in northern high latitudes, TIEGCMs, except for 1\_TIE-GCM, show slightly better Yield than 1\_USU-GAIM due to the fact that 1\_USU-GAIM used for the study only assimilates GPS observations within ±60° geographic latitudes. For low-latitude TEC simulations, 4\_GITM and 1\_USU\_GAIM produce the best Yield and peak time differences (dt\_max), respectively.

In terms of RMS and NRMS errors, the empirical model simulations, 1\_IRI and 2\_IRI, show comparable performance to the physics-based models, which are ranked higher in their group. However, the two IRI simulations are inferior to other physics-based model simulations based on Yield and peak time differences since they represent the average ionospheric conditions rather than storm time perturbations.

Overall, for TEC\* (dTEC\_m) and TEC disturbance (dTEC\_q) prediction, the simulations have similar RMSE, which is larger than GPS TEC error for all cases (the average error over all bins of the eight longitude sectors is about 2 TECU). However, model performance also depends on the considered quantities. NRMSE and the difference in peak time are smaller for dTEC\_m than for dTEC\_q prediction for most model simulations, while the opposite holds true for Yield.

Our results for the comparisons among the same types of models suggest that two physics-based ionospheric models, 1\_ SAMI3\_HWM93 and 1\_USU-IFM show similar performance in general as shown in our previous validation studies (Shim et al., 2011, 2012, 2014). These two simulations were driven by the same empirical models for thermospheric inputs and low-latitude electric fields, but for 1\_SAMI3\_HWM93, an updated version of the models for neutral composition and winds was used. 1\_SAMI3\_HWM93 has better Yield and worse dt\_max of dTEC\_q than 1\_USU-IFM, and major differences occur in the low-latitude regions.

Among the 10 physics-based coupled ionosphere-thermosphere model simulations, in terms of RMSE and NRMSE, 2–4\_TIE-GCM and 2\_CTIPE appear to perform similar to each other and better than the other six simulations for most cases. However, 4\_GITM and 1\_TIE-GCM, which appear to overestimate dTECs in northern high latitudes, take the first and second places among the 10 simulations based on the average Yield over all five latitude regions. 1\_UAM driven by FAC, which is the only simulation that includes penetration electric fields physically, ranks higher for dt\_max of dTEC\_q.

It is worth pointing out the improvements of model performance caused by enhanced and/or more complex input drivers and/or more accurate input data. 1\_IRI (IRI-2007 with NeQuick model for topside Ne) and 2\_IRI (IRI-2012 with IRI-corr model for topside Ne) show similar performance, although 2\_IRI is slightly better than 1\_IRI for all cases except for low-latitude dTEC\_m.

From the comparison of 1\_CTIPE and 2\_CTIPE, it is found that 2\_CTIPE has better scores for most cases, but 1\_CTIPE is slightly better for low-latitude dTEC\_q predictions based on all four skill scores. In most cases 1\_CTIPE performs worse than 2\_CTIPE in northern middle and high latitudes. The better performance of

 $2\_$ CTIPE appears to be mainly caused by nontrimmed IMF data from the ACE satellite. The improved version of CTIPe used for  $2\_$ CTIPe simulation is more robust during geomagnetic storm conditions and has been further tuned to better reflect the energy input to the system. The ratio between the Joule Heating contribution of the main E field and its variability has been changed based on total mass density comparisons between CTIPe and CHAMP and GRACE measurements (Fedrizzi et al., 2012).

Only 1\_TIE-GCM, among four TIE-GCM simulations, was obtained from TIE-GCM1.93 driven by the Heelis high-latitude electric potential model, and the other three simulations, 2–4\_TIE-GCM, used TIE-GCM1.94 with Weimer-2005. Although the skill scores for the four TIE-GCM simulations are more or less similar for all cases, 2–4\_TIE-GCM (with Weimer-2005) performs better than 1\_TIE-GCM (with Heelis) especially in northern high latitudes. 4\_TIE-GCM (TIE-GCM1.94 with Weimer-2005 and SABER/TIDI lower boundary conditions in double resolution) and 1\_TIE-GCM (TIE-GCM1.93 driven by Heelis) performs the best and worst, respectively, in most cases. 2\_TIE-GCM (with default resolution) and 3\_TIE-GCM (with double resolution) display small differences in their performance. The improvement of 2\_TIE-GCM compared to 1\_TIE-GCM in predicting ionospheric parameters during the strong storm was also shown in Shim et al. (2011, 2012, 2014).

The three UAM simulations obtained from UAM with different high-latitude ionospheric drivers show no significant differences in their performance in predicting TEC during the storm in general. However, 1\_UAM driven by FAC (with double resolution in longitude) tends to perform somewhat better than the other two simulations in low-latitude TEC predictions for all cases except for the Yield of dTEC\_q for which 2\_UAM (with AMIE electric potentials) performs better. Also, 1\_UAM performs better in northern high latitudes all cases except for NRMSE of dTEC\_q for which 3\_UAM (with Weimer-2005) performs better.

Along with our earlier results (Shim et al., 2011, 2012, 2014), our findings of this systematic assessment of TEC change prediction of IT models during the geomagnetic storm provide a baseline for future validation studies using new models and improved models, although this study considered only the eight 5° wide longitude sectors and has the shortcomings described in section 1. In the near future, we will extend our study to overcome the shortcomings. For example, we will perform regional TEC validation (e.g., North American Sector and European sector) for more storm events with longer quiet time references (e.g., the median for the 30 days prior to storms and the average of the five quietest days within the 30 days). Furthermore, we will investigate the local time dependence of storm impacts on TEC and how well the local time dependence can be predicted by the ionosphere models. We will also study in more detail the effects of high-latitude drivers (e.g., electric potential and auroral particle precipitations) on TEC changes during geomagnetic storm events. For future studies, we will use additional TEC data sets (e.g., low Earth orbit satellite-based TEC) to overcome the limitation of data coverage of ground-based GPS TEC over high-latitude regions (>60°-70°) and over the oceans.

Model output and observational data used for the study will be permanently posted at the CCMC website (http://ccmc.gsfc.nasa.gov) and provided as a resource for the space science community to use in the future.

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