

# Comparative Analysis of Online Static GNSS Post-Processing Services

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**Abstract:** Several precise point positioning or relative positioning services are available online for post-processing static global navigation satellite system (GNSS) data collected on a single mark. The accuracy of five services (*OPUS-S*, *AUSPOS*, *CSRS-PPP*, *GAPS*, *TrimbleRTX*) were compared by processing the same 490 static GNSS files of varying session duration (from 2 to 10 hours) on six passive marks in minimal or moderate multipathing environments. First, only Global Positioning System observables at a 30-second logging rate were tested using each service. Then, the effects of including observables from Russia's GNSS (i.e., GLONASS) were investigated using *TrimbleRTX* and *CSRS-PPP*, and the accuracy of processing data at faster logging rates were evaluated using *TrimbleRTX*. The results from each service were differenced with coordinates derived from a high-accuracy campaign-style static GNSS survey. Increasing the logging rate from 30 seconds to 10 seconds did not significantly reduce the root-mean-square error (RMS) of the differences. However, adding GLONASS observables significantly reduced the horizontal RMS by an average of 17.1% and 36.7% at sites in minimal and moderate multipathing environments, respectively.

**Author Keywords:** GNSS, GPS, Precise point positioning, PPP, OPUS

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22        **Introduction**

23        A number of free, easy to use, online services have been developed for post-processing a  
24        single, static GNSS observational session on a mark. These services include but are not  
25        limited to *OPUS-S* (Online Positioning User Service - Static) developed by the United  
26        States' National Geodetic Survey (NGS) of the National Oceanic and Atmospheric  
27        Administration (NOAA); *AUSPOS* developed by Geoscience Australia; *CSRS-PPP*  
28        (Canadian Spatial Reference System - Precise Point Positioning) developed by Natural  
29        Resources Canada; *GAPS* (GNSS Analysis and Positioning Software) developed by the  
30        University of New Brunswick (Canada); and *TrimbleRTX* (Trimble Real Time eXtended)  
31        developed by Trimble, Inc.

32  
33        Most well known in the United States is *OPUS-S*, a service that has become very popular  
34        amongst surveyors, engineers, and scientists for deriving geodetic coordinates referenced  
35        to the National Spatial Reference System (Soler et al. 2011). Although *OPUS-S* is widely  
36        used, it has some limitations worth investigating. Currently, *OPUS-S* only uses static  
37        GPS, ignores observables from other GNSS (e.g., GLONASS, Galileo, BeiDou), and  
38        automatically decimates the data files to a maximum data logging rate of 30 seconds.  
39        Thus, *OPUS-S* is ignoring data that could be used in the derivation of geodetic  
40        coordinates for an observed mark.

41  
42        Some online services other than *OPUS-S* have the capability of post-processing multiple  
43        GNSS observables and/or at faster logging rates. Post-processing more observables,  
44        achieved by collecting at faster logging rates and from more satellites on differing orbital  
45        planes, could improve the redundancy in the observation and, ultimately, the accuracy of

46 the derived coordinates. Today, it is common practice to use GNSS receivers which are  
47 capable of collecting data from multiple GNSS signals. In addition, due to the rapid  
48 development of data storage devices, GNSS observables are often collected and stored at  
49 logging rates as fast as every 1 to 10 seconds, rather than every 30 seconds.

50

51 Accordingly, this study has two primary objectives. The first objective is to compare the  
52 accuracy of the aforementioned five online services by submitting and post-processing  
53 identical static data files in each and comparing the results. This comparison will provide  
54 information on the availability, accuracy, and utility of other services. The second  
55 objective is to investigate if additional capabilities that are not currently available in  
56 *OPUS-S*, but are available in other services, including the ability to post-process data  
57 collected at faster logging rates or the addition of GLONASS observables, in fact  
58 improve the accuracy of the resulting coordinates.

59

60 To accomplish these objectives, observational data files were collected on six passive  
61 marks in varying multipathing environments. First, the data files were prepared with  
62 GPS-only observables of durations ranging from 2 to 10 hours with a 30-second logging  
63 rate. These files were submitted to the aforementioned five services for post-processing,  
64 enabling a direct comparison of the services with identical inputs. The original data files  
65 were then prepared with GPS-only and GPS+GLONASS observables at logging rates of  
66 30, 15, and 10 seconds. All of these prepared files were then submitted to *TrimbleRTX*  
67 and the resulting coordinates were evaluated and compared. Lastly, the GPS+GLONASS  
68 data files at a data logging rate of 30 seconds were also post-processed in *CSRS-PPP*.

69           **Background on Online Post-Processing Services**

70   Table 1 provides a summary of the five post-processing services tested in this study. It is  
71   worth noting that all evaluated services can be used globally, thus all of these services  
72   can be used for international applications.

73

74   The five services can be divided into two categories based on processing technique:  
75   relative positioning and precise point positioning (PPP). *OPUS-S* and *AUSPOS* use  
76   relative positioning techniques, whereas *CSRS-PPP*, *GAPS*, and *TrimbleRTX* use PPP  
77   techniques.

78

79   Relative positioning is a more-traditional method for high-accuracy GNSS data  
80   processing. The method relies on a minimum of two GNSS receivers that simultaneously  
81   observe common satellites. Resulting carrier phase-angle observables collected by the  
82   receivers are differenced in order to fix integer ambiguities and reduce common GNSS  
83   errors, such as those due to satellite orbit bias, atmospheric refraction, clock bias, and  
84   cycle slips. The differencing results in a baseline observation or vector between the  
85   receivers (Figure 1). By establishing at least one receiver over a reference station with  
86   “known” coordinates, it is then possible to use the vector(s) referenced from these  
87   coordinates in order to compute the coordinates of the “unknown” mark. Thus, any error  
88   in the coordinates of the reference station is propagated to the coordinates derived for the  
89   unknown mark.

90

91   PPP is a relatively new category and quite different from relative positioning as it only

92 requires the use of a single dual-frequency GNSS receiver. PPP is based on the concept  
93 of absolute point positioning (APP) techniques because it only processes the satellite  
94 observations from the single receiver, as opposed to requiring at least two receivers.  
95 However, PPP is much more accurate than conventional APP techniques because it also  
96 employs corrections to reduce satellite orbit and clocks errors. Additionally, PPP requires  
97 dual-frequency GNSS equipment to decrease error from ionospheric delay and reduce  
98 ambiguities. Since only a single receiver is required, a baseline or vector is not generated  
99 (Figure 1). Thus, the coordinates at the observed mark are derived relative to the satellites  
100 and not relative to a reference station.

101

102 Relative positioning is commonly believed to produce more accurate results than PPP  
103 (especially for very short-duration GNSS observations); however, the development of  
104 PPP has grown significantly in recent years and, as will be later shown in this paper, the  
105 accuracy of services for post-processing GNSS sessions of at least 2 hours in duration  
106 using PPP algorithms rival the services that use relative positioning.

107

### 108 ***Relative Positioning Online Services***

#### 109 *OPUS-S*

110 *OPUS-S* is a GPS-only data processing service provided by NOAA NGS. A session of  
111 static, dual-frequency GPS data collected on a single mark can be submitted to *OPUS-S*  
112 for processing using its online portal. *OPUS-S* uses the NGS Continuously Operating  
113 Reference Stations (CORS) network or stations in the International GNSS Service (IGS)  
114 as reference stations to process data files from 2 to 48 hours in duration. NGS also  
115 provides a service for post-processing data files from 15 minutes to 2 hours in duration,

116 known as *OPUS Rapid-Static*; however, note that this service was not assessed in this  
117 study.

118

119 When a data file is submitted, *OPUS-S* computes single, independent baseline solutions  
120 from up to five of the closest and available CORS or IGS stations to the observed mark  
121 using an NGS baseline processor named *PAGES* (Program for the Adjustment of GPS  
122 EphemerideS). *PAGES* employs a number of corrections for reducing distance-dependent  
123 errors in the baseline solutions, including corrections from a tropospheric delay error  
124 model, iono-free combinations from the dual-frequency data for reducing ionospheric  
125 delay, and precise ephemerides from the IGS for decreasing orbit errors. It then finds the  
126 average coordinates at the observed mark from the three most-precise single baseline  
127 solutions. In the conterminous United States (CONUS), over 1,600 active CORS and IGS  
128 stations are available for use as reference stations at a spacing of roughly 70 to 150 km;  
129 outside of CONUS, *OPUS-S* must use a more sparse number of CORS and IGS stations.

130

131 In each solution, *OPUS-S* provides “peak-to-peak” errors for each coordinate component  
132 that show the discrepancy between the three selected baseline solutions in terms of  
133 northing, easting, and up. Solution accuracy is stated to be within a few centimeters  
134 (National Geodetic Survey 2014). Soler et al. (2006) provide empirical equations for  
135 estimating the horizontal and vertical RMS of *OPUS-S* as a function of the duration of  
136 the observation and showed that *OPUS-S* can process baselines up to several hundred km  
137 in length to an accuracy of a few centimeters.

138

139 *AUSPOS*

140 *AUSPOS* is a GPS-only data processing service provided by Geoscience Australia. Static  
141 dual-frequency GPS data can be submitted and processed. When a data file is submitted,  
142 simultaneous session baseline processing is completed between the observed mark and  
143 the 15 nearest IGS and APREF (Asia-Pacific Reference Frame) reference stations using  
144 the *Bernese Software System*. The published coordinates of the reference stations are  
145 constrained to 1 mm horizontally and 2 mm vertically (assumed 68% confidence level).  
146 *AUSPOS* solutions provide positional uncertainties at the 95% confidence level for  
147 reference stations and the observed mark. Uncertainties are scaled using an empirical  
148 model based on data duration, quality, and geographic location (Geoscience Australia  
149 2012).

150

### 151 ***Precise-Point Positioning Online Services***

152 *CSRS-PPP*

153 *CSRS-PPP* is a GNSS post-processing software provided by Natural Resources Canada  
154 (NRCan). It is capable of processing both GPS and GLONASS observables as well as  
155 static and kinematic observations. It is also possible to process individual data files with  
156 logging rates as short as 1 second. *CSRS-PPP* states that horizontal and vertical  
157 accuracies of 1 cm and 2 cm (assumed 68% confidence level), respectively, can be  
158 achieved using dual-frequency static data (Natural Resources Canada 2014).

159

160 *CSRS-PPP* is the only service tested in this paper with the capability of batch processing  
161 multiple data files with variable GNSS antenna types and heights on more than one mark

162 in a zipped archive. Additionally, users have an option to input custom ocean tidal  
163 loading files (Natural Resources Canada 2017).

164

#### 165 *GAPS*

166 *GAPS* (GNSS Analysis and Positioning Software) is developed and maintained by the  
167 Department of Geodesy and Geomatics Engineering at the University of New Brunswick.

168 *GAPS* uses PPP techniques for static and kinematic GNSS post-processing. Available  
169 GNSS constellations for *GAPS* processing include GPS, Galileo, and BeiDou.

170

171 While the other services tested in this study provide little functionality beyond post-  
172 processing, *GAPS* offers additional functions and processing options under an advanced  
173 submission portal. The user can estimate ionospheric and neutral atmospheric delays,  
174 receiver clock and inter-system biases, and code multipath. The user can select GNSS  
175 constellations to use in processing, set a-priori coordinates, window the observation,  
176 specify elevation cutoff angles, specify dilution of precision cutoff ranges, and more.

177 *GAPS* is an ongoing project; the development team is working to improve error modeling  
178 and provide real-time PPP (University of New Brunswick 2016).

179

#### 180 *TrimbleRTX*

181 *Trimble RTX* (Real Time eXtended) is a proprietary, dual-frequency static GNSS  
182 correction technology developed by Trimble, Inc. This technology is applied in several

183 Trimble services. One of these services is known as *Trimble CenterPoint RTX Post-*

184 *Processing*, a web-based GNSS post-processing service, which will be simply referred to



185 in this paper as “*TrimbleRTX*.” *TrimbleRTX* is capable of processing observables from  
186 GPS, GLONASS, QZSS, and BeiDou. It uses data from a global network of Trimble  
187 reference stations to compute satellite orbit, satellite clock, and other system corrections.  
188 These corrections can be transmitted to a receiver in real time via satellite or internet  
189 protocol. Post-processing can occur via webform or a client interface.

190

191 The minimum data logging rate is 60 seconds, but Trimble recommends using its highest  
192 processing rate of 10 seconds (Trimble 2017). *TrimbleRTX* states 2 cm or better  
193 horizontal and 6 cm or better vertical accuracy (assumed 68% confidence level) can be  
194 achieved for a 1-hour minimum observation. As the session duration approaches 24  
195 hours, the accuracy (assumed 68% confidence level) approaches 1 cm horizontal and 3  
196 cm vertical (Trimble 2014).

197

### 198 ***Previous Efforts Comparing Online Positioning Services***

199 Some studies have been completed on comparing online positioning services and  
200 positioning techniques. The following section provides a brief summary on papers  
201 involving evaluations and comparisons of more than one to two online services.

202

203 Ghoddousi-Fard and Dare (2005) assessed accuracy versus observation duration at eight  
204 active stations around the globe. GPS-only data files at a 30-second logging rate with  
205 session durations from 1 to 24 hours were submitted to *OPUS-S*, *AUSPOS*, *CSRS-PPP*,  
206 *SCOUT*, and *Auto-GIPSY* (now *JPL-APPS*), using default settings. Additional  
207 submissions were made to *OPUS-S* and *SCOUT* using the advanced option wherein the

208 user can specify which active stations to use as reference stations in the relative  
209 processing. For durations less than 6 hours, there were a few centimeters of disagreement  
210 with the published coordinates at the active stations. The accuracy of the coordinates  
211 hardly improved after session durations reach approximately 10 hours.

212

213 Ocalan et al. (2013) submitted 24-hour static, GPS-only data collected at eight active  
214 stations in Istanbul, Turkey, to *OPUS-S*, *AUSPOS*, *CSRS-PPP*, *SCOUT*, *GAPS*, *APPS*,  
215 and *magicGNSS*. They found all relative positioning solutions to be within 1 cm and PPP  
216 solutions to be within 2 cm when compared to a network solution computed in *Bernese*  
217 *Software*.

218

219 Tsakiri (2008) submitted multiple 24-hour static GPS-only data files from eight IGS  
220 stations on seven continents to *Auto-GIPSY* (now *JPL-APPS*), *SCOUT*, *AUSPOS*, and  
221 *CSRS-PPP*. The precision of the solutions for the multiple data files at each mark from  
222 each individual service was within 1-2 cm. The solutions generally had standard  
223 deviations in northing, easting, and up of 3 cm, 3 cm, and 5 cm, respectively.

224 Additionally, they found that solution quality degrades for shorter duration observations  
225 (e.g., 6 hours or 1 hour).

226

227 Dawidowicz and Krzan (2014) used *CSRS-PPP* and *ASG-EUPOS*, a relative-positioning  
228 GNSS service, to process static GNSS measurements from 0.5 to 6 hours in duration at  
229 three sites in Poland with varying satellite visibility. The study showed that dual-  
230 frequency data is more accurate than single-frequency data, the addition of GLONASS

231 improved results at sites with limited satellite visibility, and the two services yielded  
232 coordinates with similar accuracies, especially for files longer than 2 hours in duration.

233

234 There are other studies and articles that compared fewer services or data from fewer sites,  
235 such as El-Mowafy (2011), Martin et al (2011), and Silver (2013).

236

237 In addition to the aforementioned papers on comparisons of online services, other studies  
238 have been completed on how the inclusion of GLONASS with GPS affects the accuracy  
239 of the survey. Mohammed et al. (2016), Anquela et al. (2013), and Yigit et al. (2013)  
240 compared the accuracy of observations using GPS-only, GLONASS-only, and  
241 GPS+GLONASS. They generally concluded that GPS+GLONASS-derived coordinates  
242 were more accurate than GPS-only-derived coordinates, and both were more accurate  
243 than GLONASS-only for both static and kinematic observations using PPP techniques.  
244 Nevertheless, Yigit et al. (2013) found insignificant differences in the three constellation  
245 solutions at observation durations longer than 8 hours. Weaver et al. (2018) and Allahyari  
246 et al. (2018) showed that real-time observations using GPS+GLONASS allowed  
247 collection of fixed solutions at longer baseline lengths than can be obtained using GPS-  
248 only, and they showed that the inclusion of GLONASS with GPS improved accuracy,  
249 especially at sites with poorer satellite visibility. Bakula (2013) developed a method to  
250 obtain cm-level accuracies using GPS+GLONASS and multiple antennas on a special  
251 base at sites with some obstructed conditions.

252

253 The aforementioned studies provide a starting point for this project. However, due to the

254 rapid development of GNSS and regular updates to the online services, some of the  
255 results are somewhat dated. In addition, many of these studies primarily used GNSS data  
256 from active stations, which are typically constructed at sites with ideal overhead  
257 conditions, rather than using data collected from a field survey campaign.

258

259 Differing from these previous works, this paper will evaluate several services using  
260 GNSS data collected from a field survey campaign, where some of the sites have less  
261 than ideal conditions that are commonly encountered in practice. It will evaluate the  
262 combined effects of observation duration, multipathing environment, data logging rates,  
263 and the inclusion of GLONASS observables.

264

## 265 **Methodology**

266 During a 2014 static survey campaign, GNSS observations were collected on 18 existing  
267 bench marks set in road corridors in western Oregon. During each of the 15 total  
268 sessions, five or six Leica GS14 integrated antenna/receivers were set up on 2-m fixed-  
269 height tripods on five or six marks. Then, for 10 hours per session, raw GPS+GLONASS  
270 observables were collected simultaneously at a 1-second logging rate and a 10 degree  
271 elevation mask (Gillins and Eddy 2015, 2016). Each of the 18 marks were observed for  
272 three to ten 10-hour sessions.

273

274 Gillins and Eddy (2016) described the procedure for post-processing all of the  
275 aforementioned data to generate most-probable geodetic coordinates for each of the 18  
276 passive marks. In summary, each session was first post-processed in *OPUS-Projects*

277 following recommendations in Armstrong et al. (2015). Note that *OPUS-Projects* only  
278 processes the GPS observables and decimates the data files to a logging rate of 30  
279 seconds. Afterwards, the session solutions were uploaded to *ADJUST*, where a  
280 constrained least squares adjustment of the campaign-style survey network was  
281 performed by constraining the coordinates of seven CORS and setting weights on the  
282 constraints equal to the inverse of the published standard deviations of the coordinates of  
283 the CORS. The coordinates were then stored in the ITRF2008 reference system at the  
284 mean epoch of the observation.

285

286 By formal error propagation, the estimated horizontal uncertainties on the resulting  
287 coordinates for each mark ranged from 0.4 to 0.5 cm at 95% confidence, and the  
288 estimated vertical uncertainties (in terms of ellipsoid height) ranged from 1.1 to 1.3 cm at  
289 95% confidence. Although the final coordinates have these estimated errors, they were  
290 held as “truth” or as a basis for evaluating the accuracy of the coordinates produced by  
291 the five online positioning services.

292

293 The GNSS data collected on six of the 18 marks in varying multipathing environments  
294 were compiled for future submission to the online positioning services. To provide some  
295 context of the type of environment at each of the six marks, Figure 2 shows terrestrial  
296 photographs of each mark used in this study.

297

298 Figure 3 presents overhead visibility plots of each of these six marks. These visibility  
299 diagrams were produced using *Skyplotter*, a custom Java application. To use this  
300 application, a camera equipped with a circular fisheye lens was mounted on top of the

301 fixed-height tripod set up on each mark and a zenith photograph was taken. Then, each  
302 photo was uploaded in the application. *Skyplotter* maps the distorted circular image on an  
303 orthographic grid, draws vertical angle circles in increments of 15 degrees (from 0  
304 degrees to 90 degrees), and depicts the azimuth lines in 30 degree increments.

305

306 Three of the marks (i.e., B726, GLAS, and LBCC), depicted along the top row of Figures  
307 2 and 3, are in “moderate” multipathing environments, and three of the marks (i.e., BICK,  
308 Y683, U727), depicted along the bottom row of the figures, are in “minimal”  
309 multipathing environments.

310

311 The “moderate” multipathing environments include power lines, metallic street signs, and  
312 a wooden lamp pole in close proximity to the observed mark. At B726, power lines are  
313 overhead and a wooden lamp pole is within just one meter. At GLAS, a large metallic  
314 road sign is located within one meter and obstructed some view up to 45 degrees. At  
315 LBCC, a small metallic sign is within two meters. Although these items were close to the  
316 mark and pose multipathing potential, each of these six sites were still considered  
317 reasonably favorable for making GNSS observations. Mark U727 has worse satellite  
318 visibility than the other marks, but the tree tops shown in its visibility plot are over 20  
319 meters from the mark and pose minimal likelihood for causing multipathing.

320

321 As per Table 2, a total of 35 10-h GNSS data files, in Receiver Independent Exchange  
322 Format (RINEX) version 2.11, were gathered from the 2014 survey. The RINEX files  
323 were then prepared and edited using the *TEQC* command line program developed by

324 UNAVCO. First, the data files were edited to only include GPS observables and  
325 decimated to a 30 second logging rate. This ensured the submission of identical data to  
326 each of the five services for direct comparison purposes since *OPUS-S* and *AUSPOS* are  
327 currently only capable of processing GPS observables at a 30-second logging rate. Each  
328 of the 10-h RINEX files were next windowed or divided to shorter durations of 2, 3, 4, 5,  
329 and 7 hours. This resulted in a total of 490 RINEX files, as listed in Table 2.

330

331 Each of the 490 data files were submitted to the five online services, with version  
332 numbers listed in Table 3. All five of the online services solved for geodetic coordinates  
333 for the observed mark in the ITRF2008 reference system at the mean epoch of the  
334 observation. These coordinates were differenced with the aforementioned “true”  
335 coordinates from the static survey campaign for each of the associated six marks, and the  
336 resulting differences in terms of northing ( $\Delta n$ ), easting ( $\Delta e$ ), and up ( $\Delta u$ ) within a local  
337 geodetic horizon frame at each mark were computed and stored for later evaluation.

338

339 The next step was to investigate the effects of processing data collected at faster logging  
340 rates and/or with GLONASS observables. Of the five services tested, only *TrimbleRTX*  
341 and *CSRS-PPP* are capable of processing GPS+GLONASS observables. In addition,  
342 these are the only two services that are capable of processing data at faster logging rates.  
343 Trimble recommends processing data at its fastest data logging processing rate of 10 s  
344 when using *TrimbleRTX*. Therefore, we decided to process data files at 30, 15, and 10-  
345 second logging rates in *TrimbleRTX* in order to evaluate if, and by how much, processing  
346 data at faster logging rates improves its accuracy.

347

348 Thus, the original RINEX data files were prepared using *TEQC* such that they included  
349 either GPS-only or GPS+GLONASS observables at logging rates of 30, 15, and 10  
350 seconds. Then, these data files were again windowed to the same shorter observation  
351 durations of 2, 3, 4, 5, and 7 hours, producing 490 RINEX data files for each of the six  
352 different permutations. All six permutations of the RINEX data files were submitted to  
353 *TrimbleRTX*, and the two permutations with GPS-only and GPS+GLONASS data files at  
354 a 30-second logging rate were submitted to *CSRS-PPP*. The resulting coordinates from  
355 all submissions were differenced with the “true” coordinates to find  $\Delta n$ ,  $\Delta e$ , and  $\Delta u$ .

356

## 357 **Results and Discussion**

358 The differences in coordinates were calculated in terms of horizontal RMS (HRMS) and  
359 vertical RMS (VRMS) per Equations 1 and 2, where  $n$  is the total number of solutions  
360 from a service for each mark and for each session duration. These statistics were  
361 primarily used for evaluating each of the online services.

362

$$363 \quad HRMS = \sqrt{\frac{\Sigma(\Delta n^2 + \Delta e^2)}{n}} \quad (1)$$

$$364 \quad VRMS = \sqrt{\frac{\Sigma(\Delta u^2)}{n}} \quad (2)$$

365

366 In addition to calculating HRMS and VRMS, the RMS in northing (NRMS) and easting  
367 (ERMS) were computed. Furthermore, the range, mean, and standard deviations of  $\Delta n$ ,  
368  $\Delta e$ , and  $\Delta u$  were found for each service at each mark (see supplemental data).



369

### 370 *Comparison of Online Services*

371 Figures 4 and 5 show HRMS and VRMS versus observation duration, respectively, for  
372 each mark. Note that the six subplots in each of these figures are ordered in the same  
373 manner as in Figures 2 and 3, where the top row is for the marks in moderate  
374 multipathing environments and the bottom row is for marks in minimal multipathing  
375 environments.

376

377 For an unknown reason, *AUSPOS* produced wildly incorrect geodetic coordinates for two  
378 of the 10-hour data files, once for mark B726 and once for LBCC, both marks in  
379 moderate multipathing environments. The  $\Delta n$ ,  $\Delta e$ , and  $\Delta u$  of these two solutions were in  
380 error as much as 75 m. Both of these data files were re-submitted to *AUSPOS*, but  
381 *AUSPOS* produced the same incorrect coordinates. The solution files from *AUSPOS* gave  
382 an indication that the coordinates were in error, because the files estimated unusually  
383 large standard deviations for the coordinates ranging from 15 to 18 m. These two  
384 solutions were removed as outliers prior to producing any of the statistics and figures  
385 showing the results. Oddly, *AUSPOS* appeared to successfully process these same data  
386 files when they were windowed to the shorter durations of 2, 3, 4, 5, and 7 hours.

387

388 Other challenges were discovered when processing the data using *GAPS*. Unfortunately,  
389 *GAPS* truncates all submitted data files to midnight in GPS Time. All of the 10-hour data  
390 files for the marks concluded 1 to 3 hours after GPS midnight because the local time in  
391 Oregon is approximately 7 or 8 hours behind GPS time. Thus, the plots in Figures 4 and 5  
392 do not show any HRMS or VRMS values for *GAPS* for the 10-hour sessions. Compared

393 to the other services, *GAPS* also produced solutions with significantly higher HRMS and  
394 VRMS values at mark B726 when the sessions were less than 5 hours in duration. For the  
395 2-hour sessions on B726, *GAPS* produced an HRMS and VRMS values equal to 8.6 and  
396 12.4 cm, respectively; for the 3-hour sessions on B726, the HRMS and RMS values equal  
397 7.1 and 7.7 cm, respectively. Because of these challenges, solutions from *GAPS* were  
398 removed from further evaluation in this paper.

399

400 Aside from the poor HRMS and VRMS values for *GAPS* on mark B726, it is apparent  
401 that the HRMS and VRMS curves are similar for the marks in moderate or the minimal  
402 multipathing environments, except for an occasional spike which may be explained by  
403 the somewhat small sample sizes. Thus, residual differences of  $\Delta n$ ,  $\Delta e$ , and  $\Delta u$  were  
404 pooled together according to either of the two multipathing environment categories, and  
405 new HRMS and VRMS values were computed for each service, except *GAPS*. The  
406 standard deviations for the residual differences, NRMS, ERMS, and other statistics for  
407 the pooled data were also calculated and listed in the supplemental data. Figure 6 shows  
408 HRMS and VRMS versus observation duration, where the curves on the left two subplots  
409 are for the pooled data from the three marks in minimal multipathing environments, and  
410 the curves on the right two subplots are for the three marks in moderate multipathing  
411 environments.

412

413 In general, the HRMS and VRMS values in Figure 6 appear similar for each of the four  
414 services. HRMS and VRMS for the sites in minimal multipathing environments rarely  
415 vary by more than 1 cm when comparing services. For the most part, the HRMS and

416 VRMS curves for *AUSPOS* are slightly lower or roughly equal to the other services,  
417 except for sessions less than or equal to 3 hours. For the sites in moderate multipathing  
418 environments, the HRMS and VRMS curves for *TrimbleRTX* tend to be slightly higher  
419 than the other curves.

420

421 One consistent pattern in Figure 6 is that the HRMS and VRMS values for sessions  
422 shorter than 5 hours are much higher for the sites in moderate multipathing environments  
423 than for the sites in minimal multipathing environments. However, when collecting more  
424 than 5 hours of data, the HRMS and VRMS values for both environment categories  
425 appear similar and the services vary by less than 1 cm. After 5 hours, there is limited  
426 improvement in the HRMS and VRMS values. Thus, a conservative recommendation is  
427 to collect 5 hours of data regardless of the two multipathing environment categories; a  
428 minimum of 5 hours of data is clearly beneficial for sites in a moderate multipathing  
429 environment. However, for sites in a minimal multipathing environment, the HRMS and  
430 VRMS hardly improve, especially after sessions as short as 3 hours.

431

432 Equations 1 and 2 showed how RMS can be computed as a function of the residual  
433 differences between the coordinates of a sample of data and the “true” coordinates of the  
434 spatial data. RMS is a popular statistic for evaluating spatial data because it is a function  
435 of both: (1) the bias or systematic error between the coordinates of the sample and the  
436 “true” coordinates, and (2) the precision of the coordinates in the sample. In other words,  
437 RMS can also be written in more general terms as:

438 
$$RMS = \sqrt{\mu^2 + \sigma^2} \quad (3)$$

439 where  $\mu$  is the aforementioned bias and  $\sigma$  is the standard deviation of the coordinates of  
440 the sample.

441

442 Of course, it is desirable for each service to produce solutions with unbiased coordinates.

443 If  $\mu = 0$  in Equation 3, then RMS will be equal to  $\sigma$ . If bias can be detected, either the  
444 service should be further scrutinized or the “truth” coordinates may be incorrect.

445

446 To assess the presence of bias in the solutions,  $\mu$  was computed per Equations 4a – 4c  
447 using the samples of pooled residual differences organized by online service source,  
448 multipathing environment category, and session duration (see supplemental data).

$$449 \quad \mu_n = \sqrt{|NRMS^2 - \sigma_n^2|} \quad (4a)$$

$$450 \quad \mu_e = \sqrt{|ERMS^2 - \sigma_e^2|} \quad (4b)$$

$$451 \quad \mu_u = \sqrt{|VRMS^2 - \sigma_u^2|} \quad (4c)$$

452 where  $\mu_n$ ,  $\mu_e$ ,  $\mu_u$  are the bias in northing, easting, and up, respectively;  $\sigma_n$ ,  $\sigma_e$ , and  $\sigma_u$  are  
453 the standard deviation in northing, easting, and up, respectively.

454

455 Values of  $\mu_n$ ,  $\mu_e$ , and  $\mu_u$  were found to be roughly constant at all observation durations for  
456 a given sample of data organized by service source and multipathing environment. Thus,  
457 the mean value of  $\mu$  for all observation durations was computed according to service and  
458 multipathing environment, as illustrated in Figure 7. As shown, the values are typically  
459 sub-centimeter and approaching the estimated uncertainty of the “truth” coordinates.

460 Values of  $\mu_u$  for the solutions from *OPUS-S* are higher than the other services, and values

461 of  $\mu_n$ ,  $\mu_e$ , and  $\mu_u$  are generally lower for the solutions from *AUSPOS*. Values of  $\mu_n$ ,  $\mu_e$ ,

462 and  $\mu_u$  are generally similar, but in some cases slightly lower, for moderate multipathing  
463 environments as compared to minimal multipathing environments. This may be due to a  
464 larger spread in the solutions from moderate multipathing environments, which seems to  
465 make it more difficult to detect a consistent offset from the truth coordinates.

466

467 For further investigation, statistical F-tests were performed, testing the null hypothesis  
468 that the difference in the square of RMS and the variance (square of the standard  
469 deviation) equals zero at 95% confidence. These tests were performed for three directions  
470 (i.e., northing, easting, and up) for each of the four services, at each of the six observation  
471 durations, and for the two multipathing environment categories, resulting in a total of 144  
472 tests (see supplemental data). Table 4 summarizes the number of tests that passed and  
473 failed the F-test. When the null hypothesis cannot be rejected, it indicates that the square  
474 of the RMS and variance for a sample of data cannot be proven to be statistically  
475 different and implies that there is a lack of statistical evidence that a bias is present in the  
476 sample.

477

478 Approximately 74% of these tests did not reject the null hypothesis and therefore  
479 conclude that there is no evidence that the square of the RMS and variance values are  
480 statistically different (i.e., no statistical evidence of a bias). Of the 26% of tests that did  
481 reject the null hypothesis, 63% of rejections occurred in the northing direction. Of the 36  
482 tests performed using *OPUS-S* data, 14 rejected the null hypothesis (39%). Eight of these  
483 *OPUS-S* rejections (57%) occurred in the northing direction. *CSRS-PPP* rejections  
484 predominantly occurred in the northing direction (8 of 16) and vertical direction (6 of

485 16). *TrimbleRTX* produced 6 rejections, all in the northing direction. Interestingly,  
486 *AUSPOS* produced the least number of rejections. It may be because *AUSPOS* processes  
487 data against 15 base stations, while *OPUS-S* starts with only five base stations and  
488 ultimately only uses three base stations as control. Use of such a small number of base  
489 stations as constraints appears to allow more bias in the coordinates of the control to shift  
490 or bias the solution at the observed mark.

491

492 ***Effects of Logging Rates using TrimbleRTX and Addition of GLONASS Observables***  
493 ***using TrimbleRTX and CSRS-PPP***

494 As mentioned previously, the effects of including GLONASS could only be tested in  
495 *TrimbleRTX* and *CSRS-PPP* because these are the only two services that are currently  
496 capable of processing GPS+GLONASS observables. For this paper, processing data at  
497 faster logging rates were only evaluated in *TrimbleRTX*, and future work could involve  
498 testing the effects of data logging rates in *CSRS-PPP*.

499

500 Figures 8 and 9 show HRMS and VRMS values, respectively, from *TrimbleRTX* versus  
501 observation duration for each of the six marks.

502

503 Similar to the previous section, the HRMS and VRMS curves are generally similar for  
504 the marks in moderate or the minimal multipathing environments. Thus, values of  $\Delta n$ ,  $\Delta e$ ,  
505 and  $\Delta u$  were pooled together according to either of the two multipathing environment  
506 categories, and new HRMS and VRMS values were computed. Figure 10 shows HRMS  
507 and VRMS versus observation duration for the pooled data.

508

509 It is clear that increasing the logging rate only marginally improved the HRMS and  
510 VRMS values at both the sites in moderate and minimal multipathing environments and  
511 for all session durations. Increasing the data logging rate from 30 seconds to 10 seconds  
512 only improved the RMS of the solution by an average of 5% vertically and 2%  
513 horizontally. Only one data point (Figure 8) for mark LBCC at a duration of 2 hours  
514 showed improvement in RMS more than 10% by increasing the data logging rate.

515

516 Although increasing the data logging rate showed little improvement, the addition of  
517 GLONASS observables reduced the HRMS and VRMS as much as 60% at some of the  
518 marks. The greatest benefit of adding GLONASS was for the marks in moderate  
519 multipathing environments. For the marks in minimal multipathing environments, lower  
520 HRMS and VRMS values are also noticeable for GPS+GLONASS sessions less than 5  
521 hours in duration; after 5 or more hours, the GPS-only and GPS+GLONASS HRMS and  
522 VRMS curves are similar at these sites.

523

524 Figures 11 and 12 show HRMS and VRMS values, respectively, from *CSRS-PPP* versus  
525 observation duration for each of the six marks. Similar to the previous sections, the  
526 HRMS and VRMS curves are generally similar for the marks in moderate or minimal  
527 multipathing environments. Similar to the results for *TrimbleRTX*, the HRMS values  
528 from GPS+GLONASS were consistently smaller or negligibly different than HRMS  
529 values using GPS-only. However, surprisingly, VRMS values at B726 behave  
530 unexpectedly; except at  $T = 2$  h, the GPS-only solutions are an average of 50% smaller  
531 than the GPS+GLONASS solutions. *CSRS-PPP* shows less improvement and less

532 consistency in VRMS versus HRMS when comparing GPS-only versus  
533 GPS+GLONASS. VRMS for GPS+GLONASS are generally smaller than GPS-only at  
534 stations GLAS and BICK, negligibly different at Y683, and generally larger at B726,  
535 LBCC, and U727.

536

537 Again, values of  $\Delta n$ ,  $\Delta e$ , and  $\Delta u$  were pooled together according to either of the two  
538 multipathing environment categories, and new HRMS and VRMS values were computed.  
539 Figure 13 shows HRMS and VRMS versus observation duration for the pooled data.  
540 HRMS is consistently improved by including GLONASS observables. When pooled, the  
541 curves for VRMS and HRMS look similar for *TrimbleRTX* and *CSRS-PPP*, where RMS  
542 values hardly improve after  $T = 5$  h for sites in either multipathing category. But, for the  
543 GPS+GLONASS solutions, the VRMS values from *TrimbleRTX* are 10-20% smaller than  
544 from *CSRS-PPP*. Based on this finding, it seems that *TrimbleRTX* is combining  
545 GLONASS with GPS more effectively than *CSRS-PPP*.

546

547 Table 5 summarizes the percent reduction in HRMS and VRMS values when using  
548 GPS+GLONASS versus GPS-only for a data logging rate of 30 seconds using either  
549 service. The table presents the reductions for the marks in minimal and moderate  
550 multipathing environments and for each of the tested session durations.

551

## 552 **Conclusions**

553 The objectives of this paper were to compare the accuracy of five online services, namely  
554 *OPUS-S*, *AUSPOS*, *CSRS-PPP*, *GAPS*, and *TrimbleRTX*, by submitting identical GPS-



555 only sessions of varying durations from 2 to 10 hours on six marks. Additionally, this  
556 paper investigated if processing data at faster logging rates using *TrimbleRTX* and/or  
557 including observables from GLONASS using *TrimbleRTX* and *CSRS-PPP* improved the  
558 accuracy of the results.

559

560 All five services generally produced similar results when processing identical GPS-only  
561 files at a 30-second logging rate. It was found that for session durations of 5 hours or  
562 greater, the HRMS and VRMS values between services vary by less than 1 cm. In  
563 addition, the HRMS and VRMS values are similar when comparing sites in moderate and  
564 minimal multipathing environments, and there is limited improvement in HRMS and  
565 VRMS values for longer durations. For sites in minimal and moderate multipathing  
566 environments, HRMS and VRMS values hardly improved beyond approximately 2 cm  
567 after 3 and 5 hours, respectively.

568

569 For the most part, the coordinates from each service's set of solutions were centered  
570 about the "truth" coordinates at a given mark that were derived from a static survey  
571 campaign. Note the coordinates held as truth have estimated horizontal uncertainties from  
572 0.4 to 0.5 cm and vertical uncertainties from 1.1 to 1.3 cm, both at 95% confidence. If a  
573 set of solutions does not center about the truth coordinates, it indicates that there is a  
574 systematic error or bias present in the service or in the truth coordinates and this bias  
575 would have increased the RMS of the set of solutions. The majority of the statistical F-  
576 tests (i.e., 74%) could not reject the null hypothesis that the square of the RMS for a  
577 given sample of solutions from a service, organized by multipathing environment and

578 observation duration, was equal to the variance of the sample. Thus, the majority of the  
579 statistical testing could not detect a bias between the solutions from each online service  
580 and the truth coordinates.

581

582 In addition to the comparison of the accuracy of each service, it is worthwhile to note that  
583 all of the evaluated services are easy to use and return similar solutions within an hour or  
584 two of submission. The services vary most in submission method and solution format.  
585 The authors preferred *CSRS-PPP* for ease of batch processing and the included solution  
586 information and figures. Each *CSRS-PPP* solution includes data file details, a 95% error  
587 ellipse, satellite tracks with residuals, and more. For high-accuracy work, surveyors  
588 should consider submitting data to multiple services, since they are easy to use. In any  
589 case, the user should review the information returned with the solution and check the  
590 quality of the statistics provided by the service. For example, *AUSPOS* estimated  
591 unusually large standard deviations (i.e.,  $> 1$  m) for the coordinates of the poor solutions  
592 for two of the 10-h data files; users should beware of solutions from any service which  
593 report large error estimates.

594

595 Using *TrimbleRTX*, it was also found that increasing the logging rate hardly reduced the  
596 HRMS and VRMS values for all session durations, at sites in both minimal and moderate  
597 multipathing environments. However, the addition of GLONASS observables  
598 substantially improved results using *TrimbleRTX*, especially at observation durations less  
599 than 5 hours and at sites in moderate multipathing environments. For sites in minimal  
600 multipathing environments, the average reduction using *TrimbleRTX* in HRMS and

601 VRMS is 18.1% and 9.2%, respectively. For sites in moderate multipathing  
602 environments, the average reduction in HRMS and VRMS is 39.6% and 19.0%,  
603 respectively.  
604  
605 *CSRS-PPP* GPS+GLONASS results also improved at observation durations less than 5  
606 hours; VRMS and HRMS improved at sites in minimal multipathing environments and  
607 HRMS improved at sites in moderate multipathing environments. For the  
608 GPS+GLONASS solutions, the VRMS values from *TrimbleRTX* are 10-20% smaller than  
609 from *CSRS-PPP*. Based on this finding, it seems that *TrimbleRTX* is combining  
610 GLONASS with GPS more effectively than *CSRS-PPP*.

611  
612 This study was limited to an evaluation of four to ten 10-h sessions of data collected on  
613 six bench marks in western Oregon. It is recommended that future research involves an  
614 evaluation of a much larger sample of data collected over multiple seasons and across a  
615 wider geographic area in order to reach deeper conclusions on the accuracy of the five  
616 services. Additionally, this study could be expanded to assess other available services  
617 (e.g. *SCOUT* and *JPL-APPS*), make use of other viable GNSS constellations (e.g.,  
618 Galileo, BeiDou), and/or test the accuracy when using IGS rapid ephemerides versus  
619 final ephemerides.

620

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631

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714

715

716 **Tables**

717 **Table 1.** Summary of online services for post-processing static GNSS data

Service Name	Positioning Technique	Satellites	Minimum Duration (Recommended)	Fastest Logging Rate	Orbit Source	Batch Processing
<b>OPUS-S</b>	Relative	GPS only	2 hours (4 hours)	30 sec	IGS	Yes
<b>AUSPOS</b>	Relative	GPS only	1 hour (6 hours)	30 sec	IGS	No
<b>CSRS-PPP</b>	PPP	GPS, GLONASS	None ( >2 hours)	1 sec*	IGS and NRCan	Yes
<b>GAPS</b>	PPP	GPS, Galileo, BeiDou	None (2 to 3 hours)	30 sec	IGS and NRCan	No
<b>TrimbleRTX</b>	PPP	GPS, GLONASS, QZSS, BeiDou	10 min ( >1 hour)	10 sec	Trimble	No

\*During batch processing, *CSRS-PPP* decimated our data files that were more than 4 hours in duration to a logging rate of 30 seconds. However, we found that *CSRS-PPP* processed our data files at a 1-second logging rate if they were uploaded individually to the service.

718

719 **Table 2.** Number of windowed RINEX files on each mark, organized by observation duration

Mark Name	Duration of Observation						Total
	2h	3h	4h	5h	7h	10h	
B726	20	12	8	8	4	4	56
GLAS	20	12	8	8	4	4	56
LBCC	35	21	14	14	7	7	98
BICK	50	30	20	20	10	10	140
Y683	30	18	12	12	6	6	84
U727	20	12	8	8	4	4	56
<i>Total</i>	<i>175</i>	<i>105</i>	<i>70</i>	<i>70</i>	<i>35</i>	<i>35</i>	<i>490</i>

720

721 **Table 3.** Software details for the five services

Service Name	Service Version	Underlying Software	Software Version	Solution Format(s)
<b>OPUS-S</b>	-	PAGES	page5 1209.04	Email, XML
<b>AUSPOS</b>	2.2	Bernese	5.2	PDF, SINEX
<b>CSRS-PPP</b>	V1.05_11216	-	-	PDF, CSV, SUM, POS
<b>GAPS</b>	v5.9.1	-	-	HTML, JPG, KML, etc.
<b>TrimbleRTX</b>	-	Trimble CenterPoint RTX	5.0.0.15127	PDF, XML

722



723

724 **Table 4.** Summary of F-test results for pooled observations

Service	# rejects out of 12			Total
	North	East	Up	
OPUS-S	8	2	4	14 / 36
AUSPOS	2	0	0	2 / 36
CSRS-PPP	8	1	7	16 / 36
TrimbleRTX	6	0	0	6 / 36
<i>total</i>	<i>24 / 48</i>	<i>3 / 48</i>	<i>11 / 48</i>	<i>38 / 144</i>

725

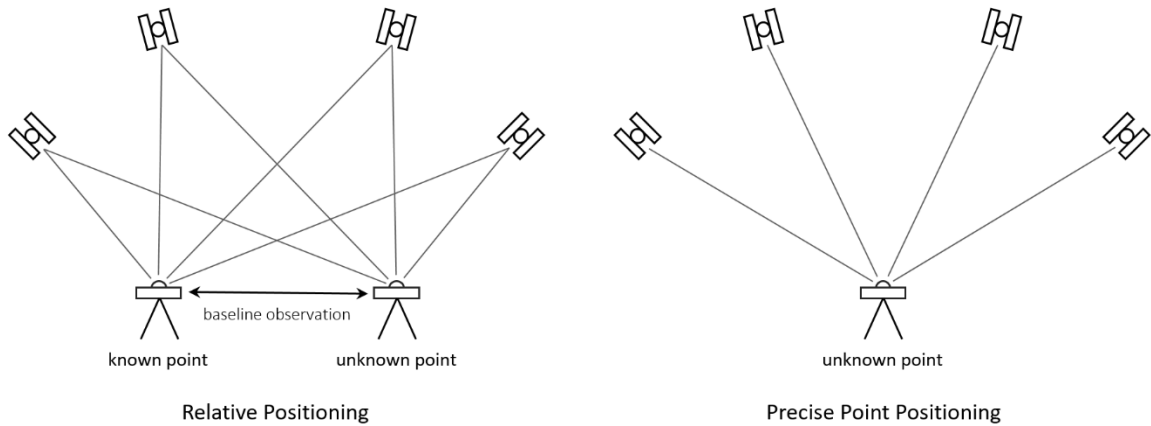
726 **Table 5.** Percent reduction in HRMS and VRMS from *TrimbleRTX* when using GPS+GLONASS  
727 observables instead of only GPS-observables at a 30-second data logging rate

Hours	<i>TrimbleRTX</i>				<i>CSRS-PPP</i>			
	% Reduct. HRMS		% Reduct. VRMS		% Reduct. HRMS		% Reduct. VRMS	
	Min	Mod	Min	Mod	Min	Mod	Min	Mod
2	19.2	22.8	23.1	27.4	24.2	41.1	14.0	29.7
3	19.6	27.8	15.6	21.3	20.3	32.7	14.3	-5.5
4	26.0	57.4	12.1	23.5	18.7	36.5	5.7	-1.6
5	19.5	44.6	0.2	14.8	23.2	43.6	18.7	-6.9
7	12.2	47.7	11.9	23.5	4.9	29.0	-9.9	-12.3
10	11.9	37.5	-7.3	3.3	5.0	19.1	-6.3	-16.7
<i>mean</i>	<i>18.1</i>	<i>39.6</i>	<i>9.2</i>	<i>19.0</i>	<i>16.0</i>	<i>33.7</i>	<i>6.1</i>	<i>-2.2</i>

Note: negative values indicate an increase in RMS rather than a reduction

728

729



730

731 **Figure 1.** Schematic depicting (a) relative positioning vs (b) absolute point positioning

732

B726 - North



GLAS - East



LBCC - East



BICK - North



Y683 - North



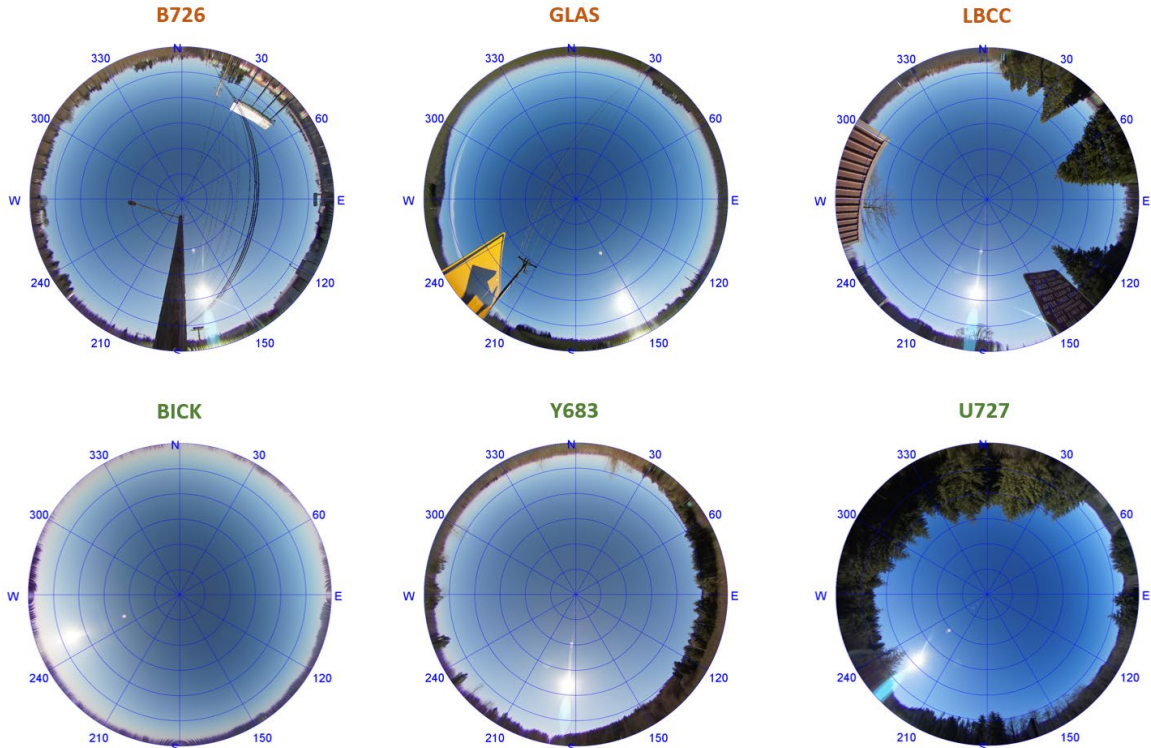
U727 - West



733

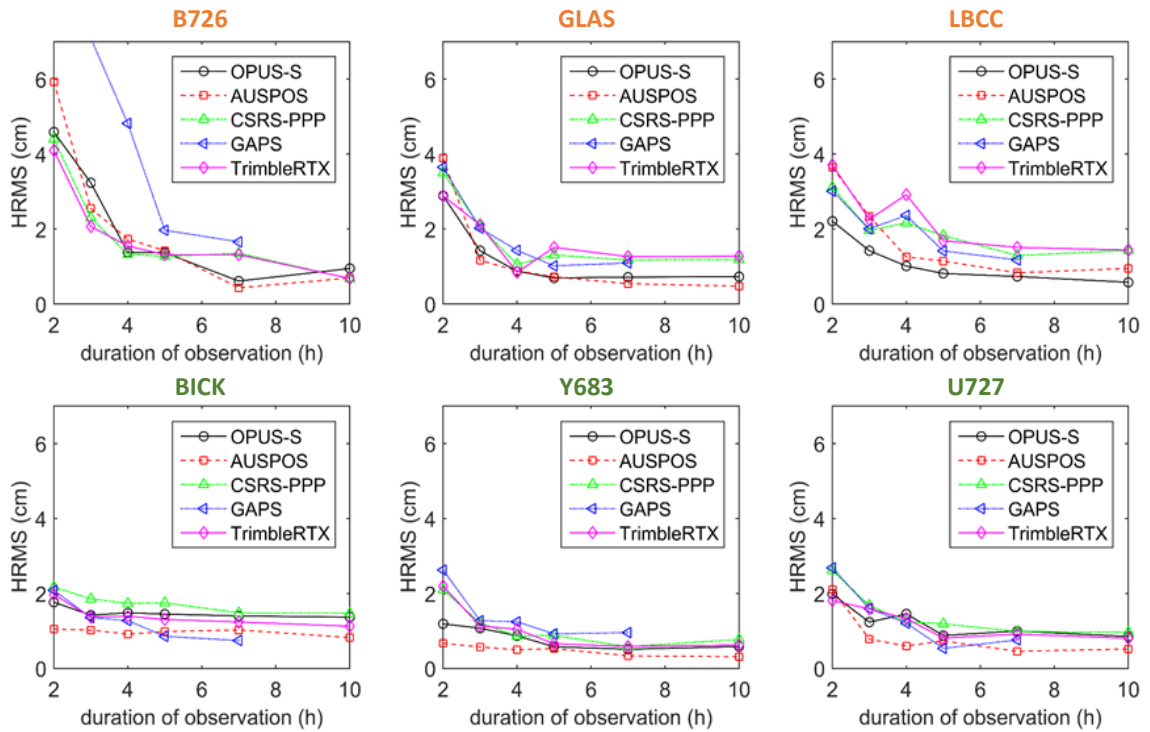
734 **Figure 2.** Terrestrial photos of the setup at each of the six test marks, with approximate direction  
735 of the camera noted

736



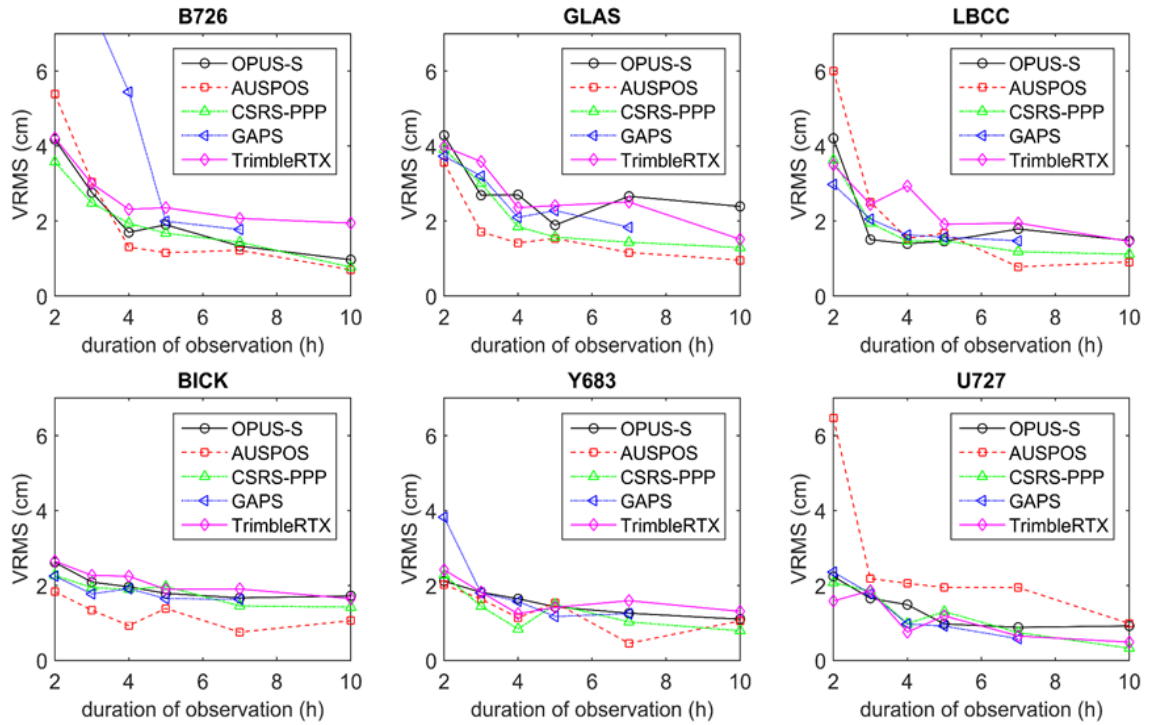
737

738 **Figure 3.** Visibility plots for the six test marks; the circles are shown in 15-degree vertical-angle  
 739 increments from the top of the fixed-height tripod above each mark.



740

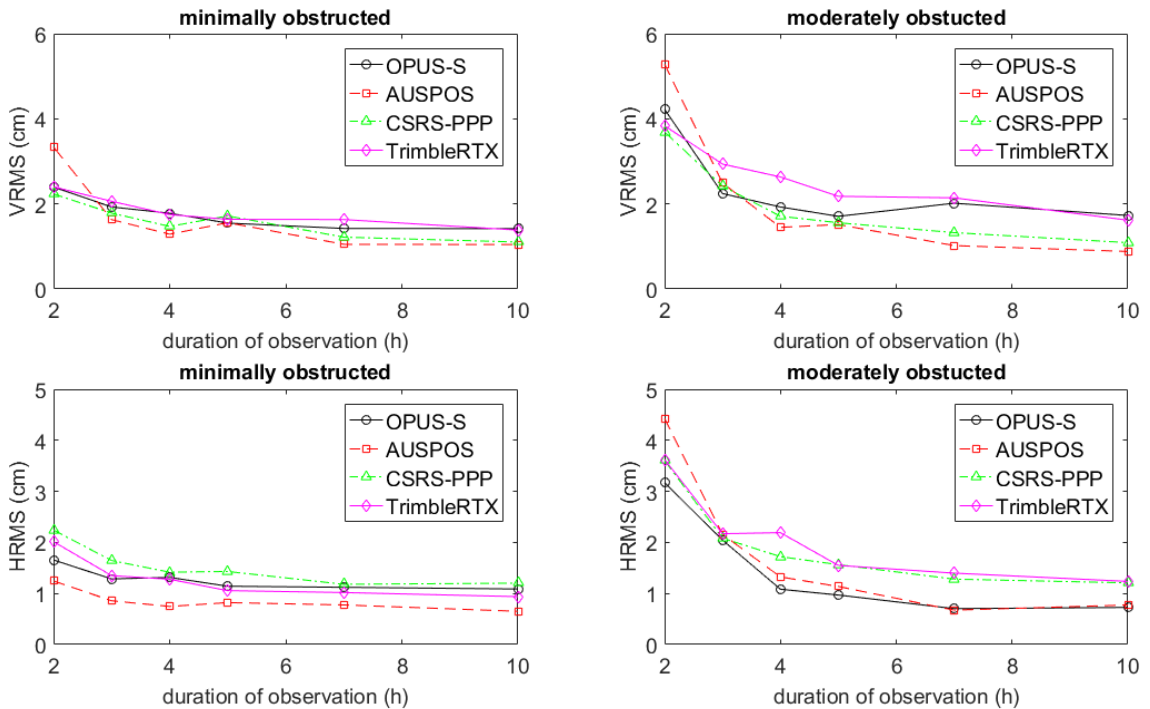
741 **Figure 4.** HRMS versus observation duration for each of the six test marks



742

743

**Figure 5.** VRMS versus observation duration for each of the six test marks

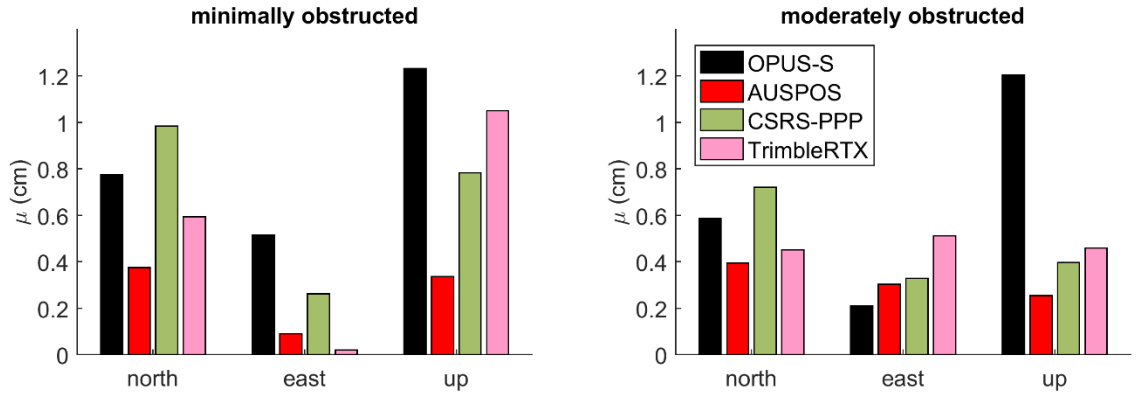


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**Figure 6.** HRMS and VRMS versus observation duration, grouped by multipathing environment category



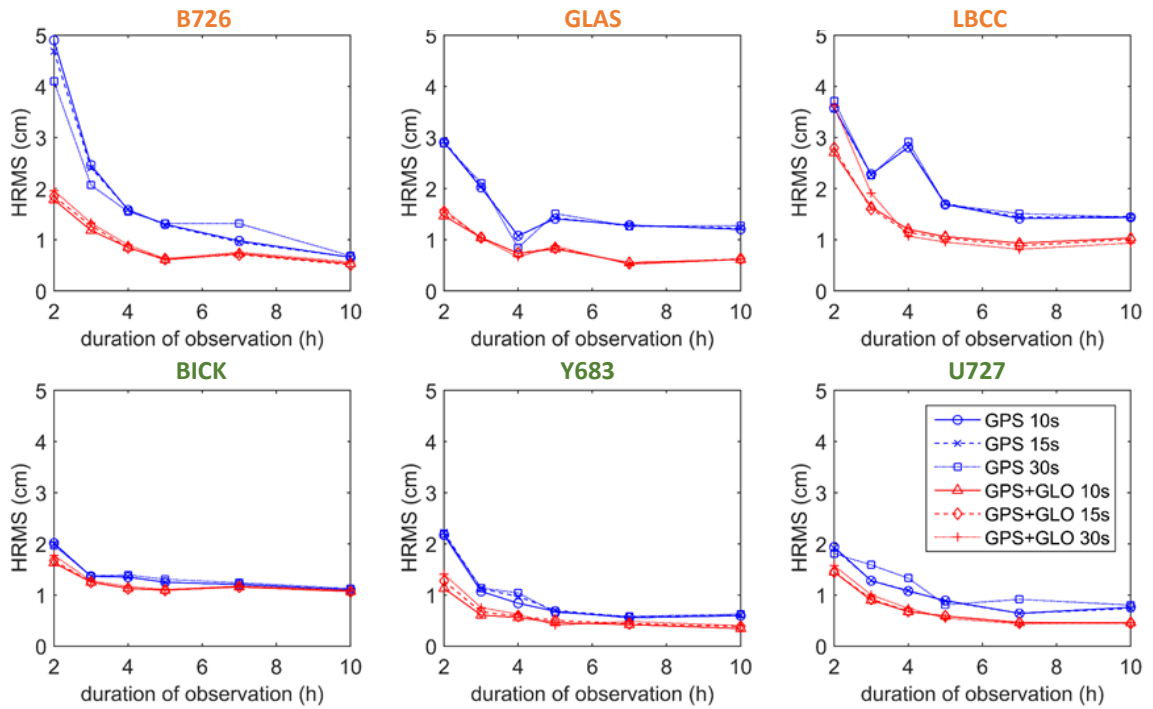
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**Figure 7.** Mean values of  $\mu$  for solutions from each service pooled by multipathing environment category

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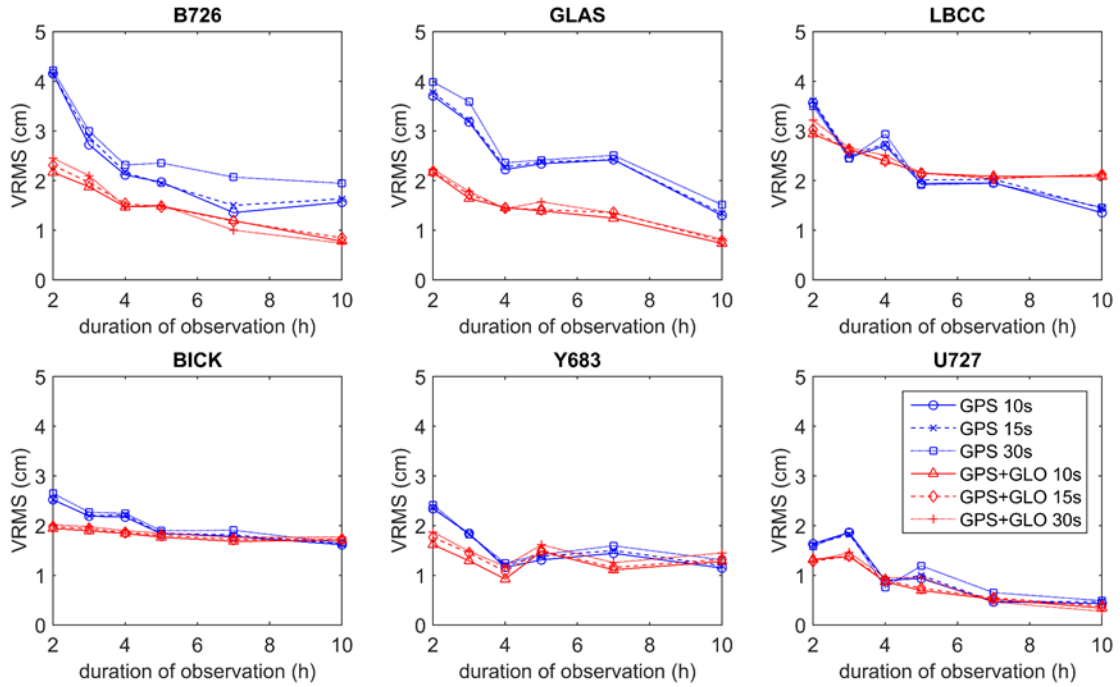


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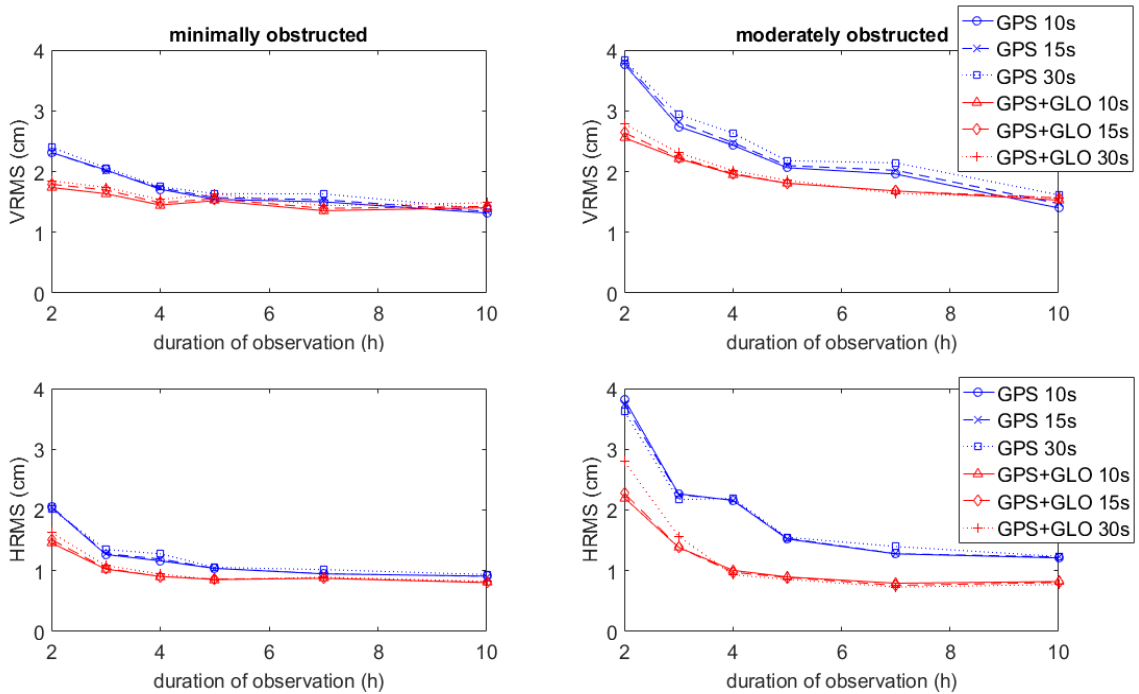
**Figure 8.** HRMS versus observation duration for each of the six test marks; all values are based on solutions from *TrimbleRTX*

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756 **Figure 9.** VRMS versus observation duration for each of the six test marks; all values are based  
 757 on solutions from *TrimbleRTX*



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759 **Figure 10.** HRMS and VRMS vs observation duration, grouped by station multipathing  
 760 environment; all values are based on solutions from *TrimbleRTX*