

38 model, it is implied that a water column velocity model must be created that accounts for any
39 variations in the raypaths within the water column which obscure the variations of interest in our
40 target (i.e., Wood et al., 2008; Benfield et al., 2017). As the requirements of spatial or temporal
41 resolution increase, processing is forced to increase the resolution and complexity of water
42 column models to more accurately represent their heterogeneity.

43 In the field known as seismic oceanography, the goal of the imaging exercise is to apply the
44 techniques of reflection seismology to the water column itself. Scientists attempt to spatially and
45 temporally map the changes in the water column impedance, which represents variations in
46 salinity, temperature, pressure and density, to gain insight into the ocean processes which drive
47 the stratification and variability of the water column. Holbrook et al. (2003) first showed that 2D
48 seismic reflection sections, if appropriately processed, provide high resolution images of the
49 ocean structures. Successively, Nandi et al. (2004) demonstrated that reflections within the water
50 column are well-correlated with temperature contrasts and that water velocity is mainly
51 influenced by temperature variations, and to a lesser extent, by salinity and density. These initial
52 studies prompted physical oceanographers and geophysicists to investigate ocean water column
53 physics using seismic data and, since then, seismic imaging and inversion have been proven to
54 be useful tools in investigating oceanographic processes such as internal waves (Dickinson et al.,
55 2017); thermohaline structures (Ruddick et al., 2009; Papenberg et al., 2010); and fronts, eddies
56 and boundaries between different water masses (Mirshak et al., 2010; Pinheiro et al., 2010).
57 However, to date, the preponderance of seismic oceanography studies have used 2D seismic
58 data, while 3D seismic data has been only minimally exploited by processing individual 2D
59 swath subsets of 3D data (Blacic and Holbrook, 2010). In seismic oceanography applications, the
60 water column acoustic impedance changes are on the order of 100 to 1000 times weaker than
61 those occurring in the solid earth; in terms of dynamic range, this requires processing to achieve
62 20-30 dB of gain when using conventional seismic data acquisition technologies. Reflections in
63 the water column are readily masked by both coherent noise (e.g., direct wave, swell noise,
64 subsurface reflections, strum noise) and non-coherent noise mechanisms (Holbrook et al., 2003;
65 Piete et al., 2013). The operational limits of acquisition are a very confining factor in data
66 processing since the acquisition is designed for subsurface imaging. Information theory assumes
67 that with enough data and the correct processing model, these signals could be recovered from
68 noise with sufficient processing gain. However, this may be beyond the limits of practicality in
69 all cases for a given data set.

70 In this work, we present enhanced 3D seismic images of the water column obtained by
71 implementing a processing workflow based on the common-reflection-surface (CRS) technique.
72 We evaluate the performance of the 3D CRS method on the water portion of a 3D multichannel
73 seismic data set collected in the deep water of the Gulf of Mexico for oil and gas exploration.
74 The results of the 3D CRS are compared with results of the standard 3D CMP to highlight the
75 improvements.

76 The CRS imaging is a data-driven and robust tool in seismic data processing that is particularly
77 suitable for imaging of weak reflections (Müller, 1999; Jäger et al., 2001; Mann, 2002). We

78 implement the CRS-based workflows in prestack and poststack domains to improve the quality
 79 and continuity of the reflections within the water column. The prestack data enhancement is
 80 handled by the partial CRS method (Baykulov and Gajewski, 2009) which is a robust method for
 81 data preconditioning and interpolation.

82 The standard CMP stack is based on the estimation of the root-mean-square (RMS) velocities
 83 that are usually obtained by manual picking of semblance panels, and as such is highly user-
 84 dependent. In turn, the CRS stack requires less user input, as the main user-selected parameter is
 85 the choice of the aperture size for data stacking in different domains. The semblance bandwidth
 86 and a rough estimate of the near-surface velocity must be defined by the user as well. In the CRS
 87 technique no prior information about the media interior is required for processing. Therefore, we
 88 believe this method is well-suited for modeling the variations in oceanic water velocity, which
 89 are small in absolute magnitude but widely varying in space.

90

91 **2 Theory background**

92

93 *2.1 The Common-Reflection-Surface Stack*

94 The CRS stack operator is based on wavefront curvature attributes (Hubral, 1983; Schleicher et
 95 al., 1993) and has many applications in seismic data processing including multiple suppression
 96 (Dümmong and Gajewski, 2008), velocity model building (Duvencek, 2004; Bakhtiari Rad et al.,
 97 2015; Bauer et al., 2016), diffraction separation (Dell and Gajewski, 2011; Bakhtiari Rad et al.,
 98 2018; Bakhtiari Rad et al., 2018; Schwarz, 2019), seismology in crystalline environment (Ahmed
 99 et al., 2015), near-surface processing (Bakhtiari Rad and Hickey, 2019), data interpolation
 100 (Baykulov and Gajewski, 2009) to name a few. The common-reflection-surface (CRS) method is
 101 a multi-parameter stacking technique that, in contrast to the CMP stack (Mayne, 1962), includes
 102 many neighboring CMPs. The hyperbolic 2D zero-offset CRS stack operator is parameterized in
 103 terms of the CRS parameters from Hubral (1983) in equation form by Schleicher et al. (1993)
 104 and Jäger et al. (2001) as:

105

$$t_{\text{CRS}}^2(\Delta x_m, h) = \left(t_0 + \frac{2 \sin \alpha}{v_0} \Delta x_m \right)^2 + \frac{2t_0 \cos^2 \alpha}{v_0} \left(\frac{\Delta x_m^2}{R_N} + \frac{h^2}{R_{\text{NIP}}} \right) . \quad (1)$$

106

107 Equation 1 describes the stacking travelttime t_{CRS} in the vicinity of the CMP location x_0 in the
 108 midpoint $\Delta x_m = x_m - x_0$ and half-offset (h) coordinates, given the zero-offset travelttime t_0 and
 109 near-surface velocity v_0 . The three surface-related CRS parameters are the incidence/emergence
 110 angle at the coinciding central source and receiver locations (α), the radius of wavefront
 111 curvature due to a fictitious point source at the normal-incidence point (NIP) on the reflector
 112 (R_{NIP}), and the radius of the wavefront curvature from a notional exploding reflector element
 113 surrounding the NIP on the common-reflection-surface R_N as shown in Figure 1. As such, t_{CRS}
 114 may be used to coherently stack data on the reflection surface.

115

116 *2.2 Partial Common-Reflection-Surface Stack*

117 The CRS method may be implemented as a partial prestack operation (Baykulov and Gajewski,
 118 2009) for prestack data enhancement, data interpolation and offset regularization. Figure 2
 119 illustrates the CRS and partial CRS surfaces. The partial CRS makes use of the same zero-offset
 120 CRS parameters to calculate the local stacking surface. To implement the partial CRS, the zero-
 121 offset time t_0 of every finite-offset sample is estimated as:

$$t_0 = -\frac{h^2 \cos^2 \alpha}{v_0 R_{NIP}} + \sqrt{\left(\frac{h^2 \cos^2 \alpha}{v_0 R_{NIP}}\right)^2 + t^2(\Delta x_m, h)} \quad (2)$$

122

123 with the finite-offset travelttime of the arbitrary sample as $t(\Delta x_m, h)$. The other parameters in the
 124 above equation are the same parameters as in the Equation 1. The estimated t_0 can be found in a
 125 minimization procedure detailed in Baykulov and Gajewski (2009). Depending on the aperture
 126 size of the partial CRS, the number of traces used during the partial stacking may vary.
 127 Therefore, the constructive summation of coherent events leads to prestack data enhancement.
 128 Partial CRS stack has found interesting applications in seismic data interpolation and
 129 regularization (e.g., Baykulov and Gajewski, 2009; Bakhtiari Rad, 2016).

130

131 *2.3 3D Common-Reflection-Surface Extension*

132 As with the 2D zero-offset CRS stacking operator, the 3D version can be derived from paraxial
 133 ray theory assuming a mild lateral variation in the overburden. 3D CRS travelttime is expressed
 134 in terms of the zero-offset wavefront attributes and it is given (e.g., Bergler, 2004) by:

$$t_{CRS}^2(\Delta \mathbf{x}_m, \mathbf{h}) = (t_0 + 2\mathbf{p}\Delta \mathbf{x}_m)^2 + 2t_0 (\Delta \mathbf{x}_m^T \mathbf{M}_N \Delta \mathbf{x}_m + \mathbf{h}^T \mathbf{M}_{NIP} \mathbf{h}) \quad , \quad (3)$$

135

136 where \mathbf{M}_{NIP} and \mathbf{M}_N are symmetric 2×2 matrices that describe the wavefront curvatures of the
 137 normal and NIP waves, respectively, \mathbf{p} is the slowness vector in terms of incident angle α
 138 and azimuth β , the half-distance vector between shot and receiver coordinates is \mathbf{h} , and $\Delta \mathbf{x}_m$ is the
 139 midpoint displacement vector with respect to the central ray coordinate. Accordingly, there are
 140 eight parameters for a 3D CRS stack operator: three R_{NIP} components, three R_N components and
 141 two angles α , and β . More details on the 3D extension of the CRS method are found in Bergler
 142 (2004); Bakhtiari Rad et al. (2015) and Xie and Gajewski (2016).

143 The estimation of the 3D CRS parameters is a typical problem of global optimization (e.g.,
 144 Bonomi et al., 2009). In general, for each sample in the zero-offset volume, the eight parameters
 145 of the 3D CRS must be estimated such that they provide the highest coherence for the data that is
 146 summed up along the stacking surface. However, since a global eight-parameter estimation is

147 computationally too expensive, a pragmatic and less-expensive approach that splits the eight-
148 parameter estimation into three independent searches in the sub-volumes of the data was
149 suggested by Müller (2003) and Bergler (2004). The pragmatic approach (PA) is composed of an
150 initial search and a local optimization scheme. After initial search is carried out, an initial CRS
151 stack volume is obtained. For further improvement of the stack, the initial stacking parameters
152 can be refined using an optimization technique, e.g., simulated annealing (SA) as proposed by
153 Müller (2003). The pragmatic approach is fast and reliable in mild areas with no sharp change in
154 velocity. However, in geologically complex areas, the attribute-search algorithm might fail when
155 many local extrema are present. In recent years, some global optimization algorithms have been
156 tested to estimate the 3D CRS parameters simultaneously (e.g., Xie and Gajewski, 2016;
157 Garabito, 2018). Despite promising results, they are still expensive and hard to implement. In the
158 framework of this project, we used the classical pragmatic approach followed by a local
159 optimization suggested by Müller (2003) and improved by Xie and Gajewski (2018) to partially
160 account for conflicting dips.

161

162 **3 Data and method**

163 *3.1 Data*

164 The seismic data used in this study are a portion of a larger multient 3D seismic survey MC
165 14-Q carried out by Schlumberger-Western Geco in the Northern Gulf of Mexico between 2002
166 and 2003. Seismic lines were acquired using a 5085 in³ dual source air gun with a source
167 separation of 50 m and shot spacing of 37.5 m for both sources acquired in a flip-flop shooting
168 pattern. The receivers were in eight streamers of eight km length towed at a 100 m spacing. The
169 number of receivers was 640 per streamer with the group interval of 12.5 m. The total number of
170 receivers per shot is 5120. The sample rate was 2 milliseconds with the Nyquist frequency of 250
171 Hz. The record length is 12 seconds and the nominal fold was 64. According to the acquisition
172 reports the sea surface conditions were calm throughout data acquisition. The survey vessel
173 maintained a velocity near 5 knots (2.5 m/s) running NW-SE survey lines (i.e., inline azimuth of
174 330°) over a gentle seafloor slope ranging from 800 to 1300 m water depth. For this study we
175 received 50 swaths covering an area of approximately 15 km × 15 km, including Mississippi
176 Canyon lease blocks 73, 74, 75, 117, 118, 119, 161, 162, and 163 (Figure 3). We received only
177 the water column portion of the seismic traces, which were muted out below the mud line.

178

179 *3.1 Data selection and preprocessing*

180 Data preprocessing was carried out before applying both the standard CMP and CRS imaging
181 workflows. After initial data analysis, trace editing and amplitude balancing were performed.
182 Data showed a dominant frequency of 65 Hz. Because long offsets are not useful for imaging
183 within the water column, traces with offsets greater than 4500 m were excluded from
184 preprocessing. The data were muted at the seafloor reflection to achieve a relative balance of
185 average amplitude levels of the remaining data containing the water column reflections of
186 interest. The data preprocessing used here employed standard techniques for subsurface seismic
187 imaging adapted to work with the water-column specific issues. In the data of interest (the data
188 above the first arrival from the seafloor), many of the noise sources are related to the acquisition
189 itself, such as air gun bubbles, direct arrivals from the source, ships engines, and reflection

190 energy returns from previous shots. Other sources of noise in the environment include wind,
191 shipping activity, and inherent ocean noise. A low-cut band pass filter with frequency of 5 Hz
192 attenuated most of low frequency noise. Given the various noise mechanisms, we needed to
193 carefully design a filtering strategy specifically tailored to remove or minimize as much noise as
194 possible while preserving the weak signals. For example, removing the direct source-to-receiver
195 wave was one of the most difficult noise sources to address in this process. The direct waves
196 directly overlap the subtle internal reflections of the water column and complicate the imaging.
197 The frequency-wavenumber (FK) filters were applied in different data domains (e.g., common
198 shot gather, common offset gather) to attenuate the direct waves. Furthermore, we employed
199 Radon-domain filtering followed by adaptive subtraction. A band pass filter of 5 to 150 Hz was
200 repeatedly applied after each processing step to attenuate high frequency noise and spikes. The
201 final step in preprocessing was a gain correction for spherical divergence. The preprocessed data
202 were then prepared for velocity analysis and stacking.

203

204 *3.3 CMP stack and CRS stack*

205 The CMP stack was obtained after velocity analysis using semblance panels within a dense grid
206 of 250 m spacing in the inline and 100 m in the crossline line direction. In general, the stacking
207 velocities varied from 1410 to 1590 m/s. The normal-moveout (NMO) correction (Yilmaz, 2001)
208 and stacking were carried out assuming the native survey bin size of 6.25 m crossline and 25 m
209 inline with no traces interpolation. The semblance panels were picked manually since the
210 velocity variations within the water column were small and prone failure by automatic picking.
211 One of the complications of stack reflections within the water column is the time scale over
212 which thermohaline variations can occur, which may be shorter than that of the data acquisition
213 window. Klaeschen et al. (2009) demonstrated that when considering survey vessels with
214 standard acquisition speeds of about 2 m/s, the very narrow range of sound velocity variability in
215 the water and the very small reflections dips, water column reflectors do not move during the
216 shot and the recording of the reflected signal and 2D seismic lines are a correct snapshot
217 representation of water conditions. Blacic and Holbrook (2010) demonstrated that a single
218 seismic swath in a large 3D oilfield survey is not affected by water column reflectors movement
219 and that CMP stacking can be applied to the seismic data. Alternatively, water conditions can
220 vary from swath to swath altering
221 continuity of reflections and in which case the time effect must be considered when stacking the
222 entire volume.

223 Unlike with a standard subsurface imaging exercise, when we created our 3D CRS supergathers,
224 we had to consider both the spatial distribution of the traces as well as the time of acquisition.
225 Recalling that the survey spanned more than six months and considering the temporal variability
226 of the imaging targets as detailed above, we needed to add both time and spatial selection criteria
227 for the gather design. As such, we created supergathers spanning 1000 m in the inline direction,
228 100 m in the crossline direction, and removed traces that were not judged to fall within a time
229 window that we could reasonably assert represented a single snapshot of the environment.

230

231 **4 Imaging Results**

232 In order to test the capability of CRS workflow in enhancing seismic images of the water
233 column, CRS results are compared with the standard CMP method at different steps in the data
234 processing, namely CMP and CRS stack gathers, Velocity semblance panels and inlines,
235 crosslines and time slice sections. Results are displayed synoptically in the following sections.

236

237 *4.1 CMP vs CRS gathers*

238 An example of a CMP gather used as input for the stacking is shown in Figure 4(a). The CMP
239 gather exhibits lower fold and offset gaps due to operational problems during acquisition. The
240 corresponding CRS supergather is shown in Figure 4(b). We used partial CRS to improve the
241 quality of prestack data. The aperture size for partial stacking was determined after some trial
242 and error and was chosen as 300 m along the offset direction and 50 m along the midpoint. This
243 small size helps to improve the quality and infill missing offsets without stacking of traces
244 collected at different times. The CRS supergather shows an enhanced quality. Two large gaps
245 near the 1300 m and 2700 m offset ranges are infilled appropriately. Moreover, because of trace
246 interpolation via partial CRS, the number of traces (fold) in the CRS supergather is almost twice
247 the CMP gather.

248

249 *4.2 Velocity semblance panels*

250 Improving prestack data using partial CRS not only enhances the stacking, but also the velocity
251 model building. The associated velocity spectrum of CMP gather that is shown in Figure 4(a) is
252 displayed in Figure 5(a). It is observed that the semblance picks are mostly located in a narrow
253 band between 1400 to 1500 m/s. Despite noise and missing samples, the higher semblance values
254 are better focused from 0.3 to 0.8 s in two-way travel time (TWT). Figure 5(b) shows the
255 comparable semblances obtained from the corresponding CRS supergather (Figure 4(b)). This
256 velocity panel exhibits more focused picks with higher semblance values. In the CMP-derived
257 velocity panel, the pick trend is faint and hard to pick below 0.8 s TWT, while the CRS-derived
258 panel exhibits less noise and enhanced picks.

259

260 *4.3 Inline, crossline and time slice*

261 Figure 6(a) shows the CMP stack section of an arbitrary inline cutting through of the final
262 stacked 3D volume. The section starts at 0.2 s TWT because the top part of the record is missing
263 due to the lack of reflections in the near-offset records (the average minimum offset is 250 m).
264 This is because the acquisition geometry is optimized for deep oil exploration targets and not for
265 water column imaging. In addition to the low fold issue in the near offsets, this portion of the
266 record is the most affected by the signal distortion due to the direct wave suppression. The other
267 portion of the section between 0.4 to 1 s TWT shows clear horizontal reflections due to the ocean
268 temperature and density stratification. For the position below 1 s to the seafloor, it is observed
269 that the seismic data show less uniform layering of the reflections with more chaotic events
270 possibly due to water mixing processes. Figure 6(b) displays the CRS stack of the same inline.

271 This section exhibits more reflections, especially in the middle parts. The white arrows in Figure
272 6(b) show some strong reflections that are better imaged using the CRS versus the CMP result in
273 Figure 6(a). The reflected
274 events also have more lateral continuity. This is more evident in the zoomed area in the white
275 box. The deeper portion of the water column is the most enhanced by the CRS workflow, with
276 many new reflectors imaged, short horizons with increased continuity and less random noise
277 overall in the seismic image. Moreover, while with the CMP stack method the shallow signals
278 are muted due to stretch NMO effect (Yilmaz, 2001), the CRS parameters are estimated
279 independently and hence the NMO- stretch effect is less pronounced (note the very shallow area
280 in both sections). The CRS stack performance is poor at the edges of the section. This is because
281 boundary effects deteriorate the CRS parameters determination (Bakhtiari Rad et al., 2015).
282 A 3D Kirchoff time migration with the RMS velocities estimated from user-picking of the
283 semblances was applied. Afterwards, the data were converted to depth using the same velocities.
284 A short migration aperture in crossline direction was considered to avoid summing up
285 inconsistent traces from two swaths. Poststack filtering was performed to attenuate migration
286 artifacts. A CMP-based crossline is shown in Figure 7(a) while Figure 7(b) shows the CRS
287 results of the same crossline. Overall, water column crosslines show lower quality, acquisition
288 footprint and swath effect produce a noise with vertical pattern and the time effect segments a
289 large part of the reflections. However, by comparing the two results, in particular within the
290 portion of the lines belonging to the same swath or consecutive swaths, it is possible to observe
291 that the CRS processing improves the data and reduces the footprint gaps (note the black
292 arrows). The temporal variability of the ocean is more significant in the shallow portion (from
293 200 to 400 m) where water is more subject to ocean mixing and seasonal effects than the deep
294 ocean where water masses are more stable over time. Seismic depth slices reflect this process.
295 Figure 8(a) and Figure 8(b) show the 350 m depth slice obtained using the CMP and CRS
296 processing, respectively. Overall, the footprint affects both images, but edges of the footprint
297 stripes are more smoothed using the CRS-based processing (see the red arrows for comparison).
298 Figure 8(c) and Figure 8(d) show the 650 m depth slice obtained using the CMP and CRS
299 processing, respectively. The signal amplitude's reduce with depth confirms a decreasing
300 temperature gradient. Figure 8(e) and Figure 8(f) show the 850 m depth slice obtained using the
301 CMP and CRS processing, respectively. The area in solid grey is the seafloor. In such deeper
302 parts where water conditions are more stable, the CRS workflow delivers better results especially
303 in terms of reflections consistency and continuity (red arrows). This is further evidenced in
304 Figure 9(a) and Figure 9(b) where a $7.5 \times 6.25 \times 0.4$ km³ sub-volume display the CMP and CRS
305 results, respectively, both in inline and crossline direction. The CRS sub-volume shows higher
306 continuity of the reflections in the water column, in particular for the events close to the seafloor
307 (red arrows).

308

309 **5 Discussion**

310 We have tried to enhance water column images of 3D seismic data acquired for deeper targets.

311 Water column imaging needs specific processing, in particular to remove the noise affecting the

312 signal. For 3D data collected for oil exploration purposes, orientation and timing of the survey is
313 essentially random with respect to oceanographic processes. Because a 3D seismic data set may
314 be acquired over several months, thermohaline interfaces can move during data collection. Our
315 results show that, even for very large surveys, water conditions in this region of the Gulf of
316 Mexico appear to be stable during the recording of a single seismic swath. CRS supergathers
317 designed preferentially along the inline directions produce better inlines sections than the
318 equivalent CMP gathers. Crosslines and horizontal slices do not show the same promising
319 results. To address this issue, we suggest that a detailed analysis of time variability should be
320 carried out for the entire volume. For example, the analysis of the correlation among inlines
321 would indicate the portion of the seismic volume with similar water conditions. Using this
322 portion, then the processing workflow could be run on appropriately segmented subsets of data.
323 Additionally, including independent oceanographic measurements in seismic processing may
324 improve the final image. For example, the stacking velocities can be improved using the
325 information obtained from the Expendable Bathythermograph (XBT) or Conductivity,
326 Temperature Depth (CTD) casts. Those casts are in-situ measurements that contain information
327 about water temperature and salinity that can be inverted to sound speed (Nandi et al., 2004;
328 Ruddick et al., 2009). Moreover, Fortin and Holbrook (2009) showed that including XBT casts
329 in the velocity semblance panel could improve picking and enhance the velocity model building.
330 In addition to inverting oceanographic casts, a velocity model can also be modeled using the
331 wavefront tomography technique introduced by Duveneck (2004), which is an inversion scheme
332 based on the CRS parameters. In this approach, the NIP-wave is iteratively inverted to produce a
333 consistent velocity model. During the inversion process, a velocity model is found that
334 minimizes the misfits between the modeled and estimated (observed) radius of curvature of NIP
335 wavefront. Higher resolution velocity model building methods, e.g., full waveform inversion
336 (e.g., Pratt, 1999) can also be implemented.

337

338 **6 Conclusions**

339 We have presented the results of improving water column seismic imaging using 3D
340 multichannel

341 seismic data collected in the deep-water Gulf of Mexico for oil and gas prospecting. We
342 improved the imaging by applying the common-reflection-surface (CRS) stack technique which
343 had not been previously used for water column imaging. We applied the CRS method in both
344 zero-offset and finite-offset domains to enhance data quality and extract more accurate velocities
345 from weak reflections. Particular care was taken to design appropriate CRS supergathers
346 considering the time varying nature of water reflections. Accordingly, CRS stack parameters
347 have been selected using both temporal and spatial constraints privileging the inline direction. In
348 comparison to CMP stack sections, we observe the CRS technique offers improvements in both
349 pre- and poststack domains. The CRS-processed data have improved acquisition footprint
350 attenuation, increased reflection event continuity, and can image events previously absent in the
351 deeper part of the seismic record. At the moment, our method offers good results for inline

352 sections, but fails to enhance crosslines and horizontal slices which are more sensitive to both the
353 acquisition geometry and temporal variability of ocean water masses.

354

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Figure Captions

Figure 1: The 2D CRS parameters: the incidence angle is denoted by α ; R_{NIP} is the radius of curvature of a wavefront emitted by a fictitious point source at the normal incidence point (NIP); R_N is the radius of wavefront curvature of the fictitious so-called normal wave that would be generated normally to the reflector from a region surrounding the normal incidence point. This region represents the common-reflection-surface.

Figure 2: The black curves indicate the prestack traveltimes. The 2D CRS stacking surface is indicated by red. The blue surface indicates the partial 2D CRS stack surface. While the result of CRS stacking is assigned to a zero-offset sample, e.g., the red point (x_0, t_0) , the result of partial CRS can be assigned to any offset sample, e.g., the blue point.

Figure 3: Location of the study area in the northern Gulf of Mexico continental shelf. The zoom-in insertion highlights the 3D seismic survey carried out by Wesrne-Geco for oil and gas exploration. The seafloor bathymetry (curtesy from <https://www.boem.gov/oil-gas-energy/mapping-and-data/map-gallery/boem-northern-gulf-mexico-deepwater-bathymetry-grid-3d>) shows water depth and complex Gulf of Mexico seafloor topography.

Figure 4: Example of an arbitrary CMP gather (a) and the enhanced CRS supergather (b) from the same location.

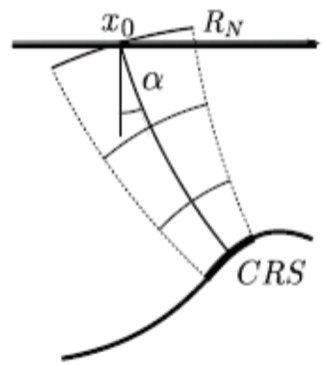
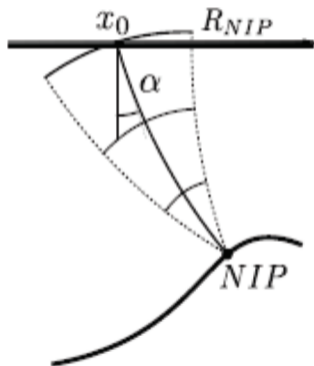
Figure 5: (a) Original and (b) partial CRS enhanced velocity spectrum of the same CMP gather in the Figure 4(a). The semblance is increased and allows for more reliable picking.

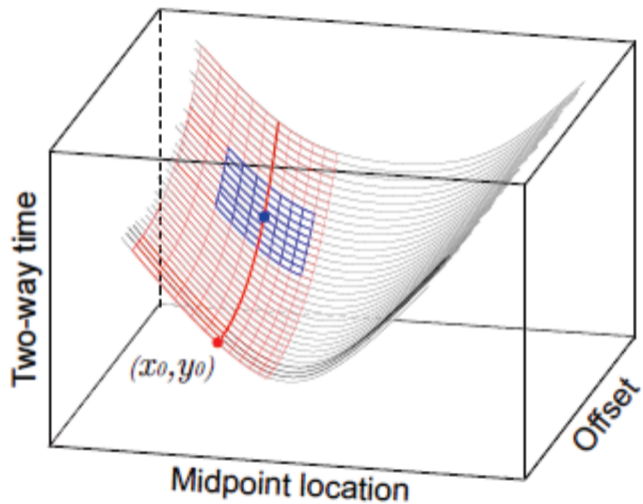
Figure 6: The CMP stack section of an inline extracted in the middle from the stacked volume of (a) and the CRS stack section of the same inline (b). Please note the same gain in both images. Boxes and arrows highlight areas where reflections between (a) and (b) are improved.

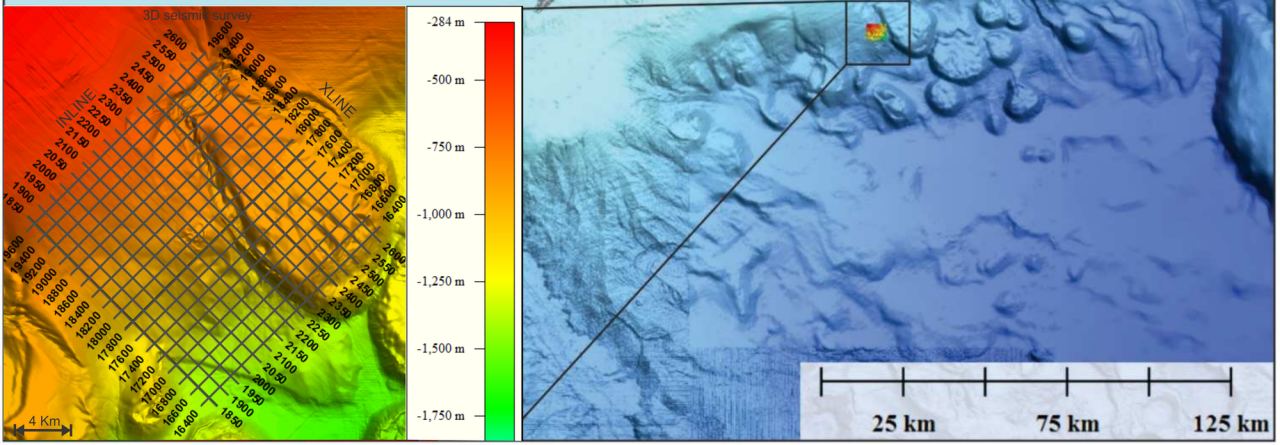
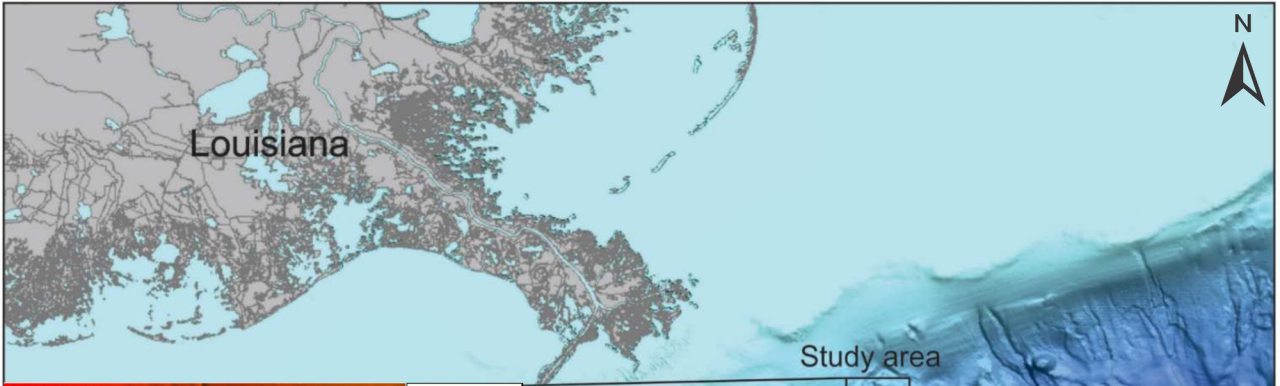
Figure 7: Depth converted crossline obtained from CMP (a) and the CRS (b) processing. Please note the same gain in both images. CRS reduce the vertical noise pattern due to acquisition footprint effect.

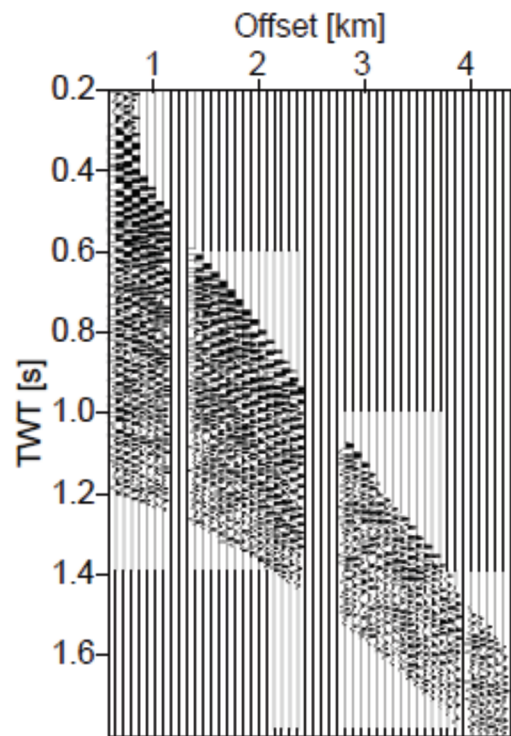
Figure 8: Three depth slices 350 m (a and b), 650 m (c and d) and 850 m (e and f) are presented to highlight CRS results (b, d and f) versus CMP (a, c, e). The same gain is used in all the images, the red arrows highlight the most significant differences.

Figure 9: Sub portion of the 3D depth volume both for CMP (a) and CRS (b) processing. The size of sub volume is $7.5 \times 6.25 \times 0.4 \text{ km}^3$ with the depth (vertical axis) starting at 600m. The red arrows highlight the differences.

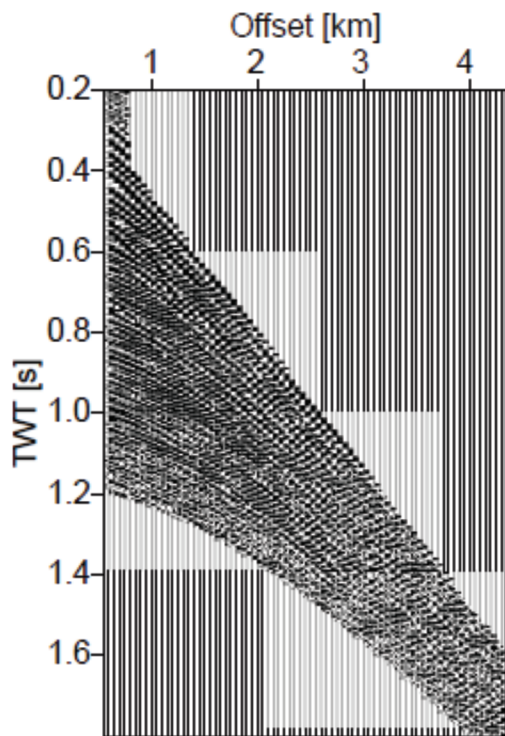




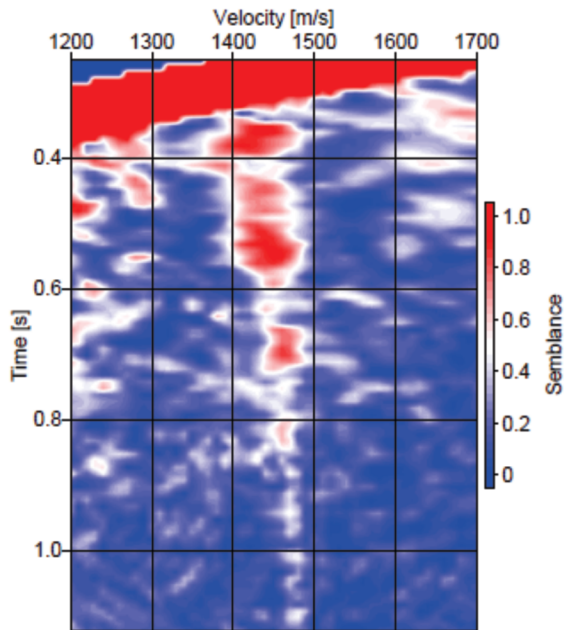




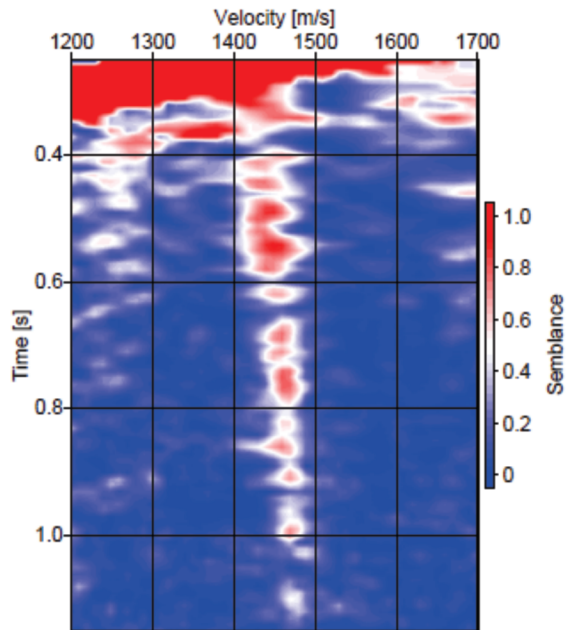
(a)



(b)



(a)



(b)

