# Combining Radar Attenuation and Partial Beam Blockage Corrections for Improved Quantitative Application

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ABSTRACT: Partial beam blockage (PBB) correction is an indispensable step in weather radar data quality control and subsequent quantitative applications, such as precipitation estimation, especially in urban and/or complex terrain environments. This paper developed a novel PBB correction procedure based on the improved ZPHI method for attenuation correction and regional specific differential propagation phase  $(K_{\rm DP})$ -reflectivity  $(Z_H)$  relationship derived from in situ raindrop size distribution (DSD) measurements. The practical performance of this PBB correction technique was evaluated through comparing the spatial continuity of reflectivity measurements, the consistency between radar-measured and DSD-derived  $K_{\rm DP}$  and  $Z_H$  relationships, as well as rainfall estimates based on  $R(Z_H)$  and  $R(K_{\rm DP})$ . The results showed that through incorporating attenuation and PBB corrections (i) the spatial continuity of  $Z_H$  measurements can effectively be enhanced; (ii) the distribution of radar-measured  $K_{\rm DP}$  versus  $Z_H$  is more consistent with the DSD-derived  $K_{\rm DP}$  versus  $Z_H$ ; (iii) the measured  $Z_H$  from a C-band radar in the PBB-affected area becomes more consistent with collocated S-band measurements, particularly in the rainstorm center area where  $Z_H$  is larger than 30 dBZ; and (iv) rainfall estimates based on  $R(Z_H)$  in the PBB-affected area are incrementally improved with better spatial continuity and the performance tends to be more comparable with  $R(K_{\rm DP})$ .

KEYWORDS: Precipitation; Rainfall; Algorithms; Radars/Radar observations; Remote sensing

## 1. Introduction

Radar quantitative precipitation estimation (QPE) is critical for extreme rainfall monitoring, forecast, and decision-making during contingent flash floods, mudslides, and debris flows. However, weather radars often suffer from complete or partial beam blockage (PBB) induced by surrounding terrains (Giangrande and Ryzhkov 2005; Zhang et al. 2013; Chen et al. 2020). The PBB effect is more evident in mountainous areas and/or complex urban environments because of the blockages from mountains and buildings. As a result, the measurements of radar reflectivity  $Z_H$  behind the blocking terrain are often biased (lower than they should be), and PBB correction is necessary to fully resolve the precipitation patterns.

PBB correction methodologies based on polarimetric radar measurements have become increasingly popular in recent years (e.g., Carey et al. 2000; Giangrande and Ryzhkov, 2005; Lang et al. 2009; Zhang et al. 2013). The basis of these PBB correction schemes can be attributed to the relatively insensitive characteristics of the differential propagation phase  $\Phi_{\rm DP}$  or the specific differential propagation phase  $K_{\rm DP}$  to PBB. In particular, the method of Carey et al. (2000) corrected the  $Z_H$  bias caused by PBB through analyzing the empirical relationship between  $Z_H$  and  $K_{\rm DP}$  in a specific  $K_{\rm DP}$  range, i.e.,  $K_{\rm DP} \geq 1^{\circ}\,{\rm km}^{-1}$  and  $K_{\rm DP} \leq 2^{\circ}\,{\rm km}^{-1}$  for S-band radars. However, this method is not flexible for practical applications and cannot be applied for high-frequency radars, which suffer more from

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attenuation, wet radome, and miscalibration effects than S-band radars. Giangrande and Ryzhkov (2005) utilized the linear self-consistency equation between  $Z_H$ , differential reflectivity  $Z_{DR}$ , and  $K_{DP}$  in their PBB correction procedure. The linear relationship was obtained using the statistics of large samples of raindrop size distribution (DSD) measurements. The  $Z_H$  bias was derived through minimizing the area-time integrals of the radar-measured  $K_{\rm DP}$  and the  $K_{\rm DP}$  estimated from  $Z_H$  and  $Z_{DR}$ . However, this method requires high-quality  $Z_{\rm DR}$  and the linear equation was only valid in pure rain situations (Giangrande and Ryzhkov 2005). The hydrometeor identification scheme, which can be used to ensure the appropriate hydrometeors are considered in the PBB correction procedure (Lang et al. 2009), also requires unbiased  $Z_H$  and  $Z_{\rm DR}$  measurements. Zhang et al. (2013) took into account the total span of the differential phase  $\Phi_{DP}$  along the radar beams in unblocked regions to dynamically estimate the  $Z_H$  bias within the blocked sectors. This method is essentially based on the nonlinear self-consistency between  $K_{\mathrm{DP}}$ ,  $Z_{H}$ , and  $Z_{\mathrm{DR}}$ , which requires that  $Z_H$  and  $Z_{DR}$  are well calibrated and not affected by attenuation. This method also assumes that the precipitation characteristics in the blocked sector are similar to those in the unblocked sectors. In practical applications, the requirement of high-quality  $Z_H$  and  $Z_{DR}$  is hard to achieve, especially at higher frequencies such as C and X bands, since the attenuations caused by propagation in rain cannot be neglected. Even at S band, the attenuation can be serious during heavy rainfall events. In fact, the specific attenuation  $A_H$  is often used to quantify rainfall intensity for S-band radars (e.g., Ryzhkov et al. 2014). As such, it is challenging to extend previous PBB correction techniques designed for S-band radars to

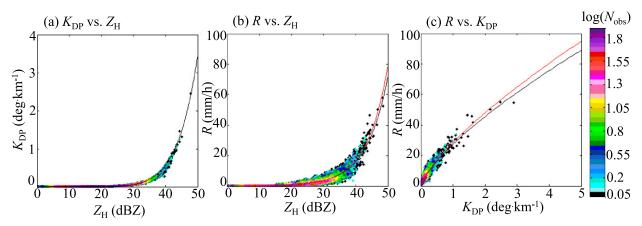


Fig. 1. Scattergrams between variables simulated from the DSD measurements between 0000 UTC 25 May 2019 and 2359 UTC 22 Jun 2019: (a)  $K_{\rm DP}$  vs  $Z_H$ , (b) R vs  $Z_H$ , (c) R vs  $K_{\rm DP}$ . The black curve in (a) refers to Eq. (2a); the black and red curves in (b) refer to Eqs. (5a) and (5c), respectively; and the black and red curves in (c) refer to Eqs. (5b) and (5d) in the main text, respectively.

generic applications. Although Diederich et al. (2015) utilized the  $Z_H$ - $A_H$  relationship to estimate the  $Z_H$  bias for X-band radars, this approach is sensitive to the DSD variability and temperature, which may change dramatically along the ascending altitudes of radar beams.

In this paper, a new PBB correction procedure was developed through incorporating attenuation correction. In addition, a nonlinear  $K_{\mathrm{DP}}-Z_H$  relationship fitted based on the local DSD measurements was incorporated into the PBB correction scheme in order to dynamically estimate the  $Z_H$  bias caused by PBB. The practical performance of this PBB correction approach was investigated using measurements from a C-band polarimetric (CPOL) radar in Hangzhou, China, during two severe rainfall events. The remainder of this paper is organized as follows: section 2 details the attenuation and PBB correction techniques; section 3 presents the demonstration study domain and dataset; section 4 addresses the practical performance of the proposed PBB correction procedure; the main findings are summarized in section 5.

# 2. Methodology

#### a. Attenuation and PBB corrections

In this study, an improved ZPHI method was adopted for attenuation correction before subsequent PBB correction. Compared to the conventional ZPHI method (Testud et al. 2000; Bringi et al. 2001), the improved attenuation correction scheme incorporates three additional constraints, including a nonnegative constraint on the  $A_H$  estimate, a constraint on the correlation coefficient  $\rho_{\rm HV}$  in the range gate partitioning, and a stricter convergence constraint in the computational process. The main processing chain for the attenuation correction of  $Z_H$  is given as follows [for details, the readers are referred to Gou et al. (2019)]:

$$A_{H}(r) = \frac{\left[Z_{H}^{M}\right]^{b} \left[10^{0.1b\alpha\Delta\Phi(r_{0},r_{m})} - 1\right]}{I(r_{0},r_{m}) + \left[10^{0.1b\alpha\Delta\Phi(r_{0},r_{m})} - 1\right]I(r,r_{m})}, \tag{1a}$$

$$\Delta\Phi_{\rm DP}(r_0,r_m) = \Phi_{\rm DP}^{\rm filtered}(r_m) - \Phi_{\rm DP}^{\rm filtered}(r_0), \tag{1b}$$

$$I(r_0, r_m) = 0.46b \int_{r_0}^{r_m} [Z_H^M(r)^b dr],$$
 (1c)

$$I(r, r_m) = 0.46b \int_{r_m}^{r_m} [Z_H^M(r)^b] dr,$$
 (1d)

$$\Phi_{\mathrm{DP}}^{\mathrm{rec}}(r_0, r_m) = \int_{r_m}^{r_m} \frac{A_H(s, \alpha)}{\alpha} ds, \tag{1e}$$

$$Z_{H}^{\text{AC}}(r) = Z_{H}^{M}(r) + \text{PIA}(0, r) = Z_{H}^{M}(r) + 2 \int_{0}^{r} A_{H}(s, \alpha_{\text{opt}}) ds,$$
(1f)

where  $Z_H^M$  stands for the measured reflectivity;  $Z_H^{AC}$  represents the  $Z_H$  measurements after attenuation correction; the coefficient b is set as a constant of 0.78 at C band; r refers to the range gate along a radial profile;  $r_0$  and  $r_m$  refer to the starting and ending gates of a range segmentation, respectively; PIA(0, r) is the path integrated attenuation (PIA);  $\Phi_{\rm DP}^{\rm filtered}$  represents the  $\Phi_{\rm DP}$  profile after filtering out the backscattering phase (i.e.,  $\delta$  bumps) from the measured total differential phase  $\Psi_{\rm DP}$ ;  $\Phi_{\rm DP}^{\rm rec}$  is the reconstructed  $\Phi_{\rm DP}$  profile in the processing chain. The optimal coefficient  $\alpha$  is searched from the predefined range [0.03, 0.18] with a step of 0.01 to minimize the difference between  $\Phi_{\rm DP}^{\rm filtered}$  and  $\Phi_{\rm DP}^{\rm rec}$ .

Considering the insensitivity of  $K_{\rm DP}$  to the PBB effect, the nonlinear self-consistency relationship between  $K_{\rm DP}$  and  $Z_H$  is utilized to estimate the optimal  $Z_H^B$  bias along each partially blocked beam through the following PBB processing chain:

$$\hat{K}_{\rm DP} = 0.1926 \times 10^{-14} Z_H^{8.3965},$$
 (2a)

$$\Delta K_{\rm DP} = \int_{r_b}^{r} [\hat{K}_{\rm DP} - K_{\rm DP}^{M}] dr,$$
 (2b)

$$Z_H^{ABC}(r) = Z_H^{AC}(r) + Z_H^B(r),$$
 (2c)

where the relationship between  $Z_H$  and  $K_{\rm DP}$  is derived from simulations based on local DSD measurements (see Fig. 1a);

 $r_{\rm b}$  stands for the first partially blocked range gate;  $Z_H^B$  stands for the  $Z_H$  bias caused by PBB, and it is assumed that the range gates with the same PBB ratio have the same  $Z_H^B$  bias;  $\hat{K}_{\rm DP}$  and  $K_{\rm DP}^M$  denote the  $K_{\rm DP}$  estimated by  $Z_H^{\rm ABC}$  through Eq. (2a) and the  $K_{\rm DP}$  directly estimated from  $\Phi_{\rm DP}^{\rm filtered}$ , respectively; and  $Z_H^{\rm ABC}$  stands for the reflectivity after attenuation and PBB correction. The estimation of  $K_{\rm DP}$  from  $\Phi_{\rm DP}^{\rm filtered}$  is further explained in section 2b.

Through adjusting  $Z_H^B$  and iteratively imposing  $Z_H^B$  on the partially blocked range gates based on Eq. (2c),  $\hat{K}_{\mathrm{DP}}$  in Eq. (2a) can be estimated and the optimal  $Z_H^B$  can be obtained by minimizing  $\Delta K_{\mathrm{DP}}$  in Eq. (2b). Note that in practical implementations, only the range gates with  $\rho_{\mathrm{HV}} \geq 0.98$  and  $\rho_{\mathrm{HV}} \leq 1$  are taken into account in minimizing  $\Delta K_{\mathrm{DP}}$ . In addition,  $Z_H^B$  starts from  $0\,\mathrm{dB}Z$  with an incremental step of  $0.1\,\mathrm{dB}Z$ .

Here, it should be noted that the PBB-affected regions need to be identified before correction. Assuming that the radar-transmitted power is concentrated in the main lobe of the radar antenna pattern, one can compute the height of the radar beam center at a distance r from the radar using a general geometric optics approach, as expressed in Eq. (3):

$$H(r) = \sqrt{r^2 + (k_e R)^2 + 2rk_e R \sin\theta} - k_e R + H_0,$$
 (3a)

$$k_e = \left[1 + R\left(\frac{dN}{dh}\right)\right]^{-1},\tag{3b}$$

where R is Earth's radius;  $k_e$  is the ratio between R and the equivalent Earth's radius; dN/dh is the refractive index gradient of the standard atmosphere;  $\theta$  is the antenna scan elevation angle; and  $H_0$  is the antenna height.

The interception function between the radar beam center and the terrain elevation can be rewritten as

PBB = 
$$(\pi a)^{-1} y \sqrt{a^2 - y^2} + a^2 \arcsin \frac{y}{a}$$
, (4)

where *a* represents the radius of the radar beam cross section and *y* is the difference between the radar beam center and the terrain elevation [for more details, see Bech et al. (2003)]. Accordingly, the PBB ratios at different range gates and azimuthal angles can be derived, and the PBB correction is executed upon the partially blocked range gates.

## b. Processing of $Z_H$ , $\Psi_{DP}$ , and $K_{DP}$

The terms  $Z_H$ ,  $\Phi_{\rm DP}$ , and  $K_{\rm DP}$  are three key radar variables utilized in the data processing described in section 2a. In this study, several quality control steps were implemented to ensure the creditability of these measurements. In particular, in order to eliminate ground clutter contaminations, the clutter mitigation decision (CMD) algorithm described in Hubbert et al. (2009) was adopted to identify and suppress ground clutter from the radar signals. The CMD algorithm incorporates clutter phase alignment from I (in phase) and Q (quadrature phase), the spatial texture and spin change of  $Z_H$ , the standard deviations of  $Z_{\rm DR}$  and  $\Psi_{\rm DP}$ , and a fuzzy logic scheme (see also Hubbert et al. 2009).

In  $\Psi_{DP}$  processing, a nine-gate smoothing is first utilized to suppress and remove spike signals with large fluctuations

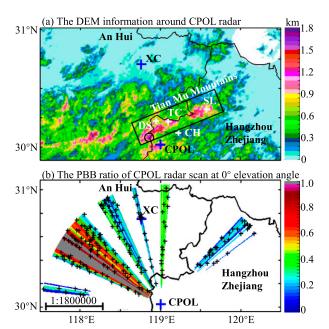


FIG. 2. (a) The digital elevation model (DEM) information around the CPOL radar; (b) the partial beam blockage (PBB) ratio of 0° elevation scan of the CPOL radar. The four white "+" in (a) indicate the locations of the four disdrometer units, the black "+" in (b) indicates the gauge network in the partially blocked areas, and the blue "+" indicates the location of the Xuan Cheng (XC) S-band and CPOL radars. The PBB ratio in (b) was derived using the refraction index under the standard atmospheric conditions.

within a short range along a radial profile. A  $\Psi_{DP}$  dealiasing procedure is then executed based on the standard deviation of  $\Psi_{DP}$  derived from the nine aligned range gates (Wang and Chandrasekar 2009). Then, the iterative filtering method (Hubbert and Bringi 1995) is applied to filter the potential backscatter differential phase along the  $\Psi_{DP}$  profile. Consequently, a high-quality  $\Phi_{DP}$  profile can be derived after subtracting the initial system phase of  $\Psi_{DP}$ .

The  $K_{\mathrm{DP}}$  is estimated along the  $\Phi_{\mathrm{DP}}$  range profile using the linear fitting approach detailed by Wang and Chandrasekar (2009), with an additional nonnegative constraint on the  $K_{\mathrm{DP}}$  estimates, as well as a monotonic increasing constraint on the reconstructed  $\Phi_{\mathrm{DP}}$  in the fitting process. In addition, if there is no range gate featuring  $\rho_{\mathrm{HV}} > 0.85$  in the nine consecutive gates, these gates are removed to avoid possible contamination from nonuniform beam filling (NUBF). The additional constraints on the  $K_{\mathrm{DP}}$  estimation aim to ensure the high quality of  $K_{\mathrm{DP}}$  for PBB correction and  $K_{\mathrm{DP}}$ -based radar rainfall retrievals.

### c. Radar QPE estimators and evaluation metrics

Utilizing four Parsivel (particle size and velocity) disdrometer units deployed in the northwest of Hangzhou (see Fig. 2a), we collected a large amount of in situ DSD data under the radar coverage domain (detailed in section 3). However, instead of deriving "fixed" climate radar rainfall estimation algorithms for local applications using the DSD data collected during a large number of precipitation events, this study used

the 6371 DSD samples collected from 25 to 27 May 2019 and 15 017 DSD samples collected from 17 to 20 June 2019 to derive the radar rainfall relationships particularly suitable for these two precipitation events. The main goal was to quantify the impact of PBB correction on the radar QPE performance during these two selected events: event 1 (25–27 May 2019) was dominated by large-scale moderate rain, whereas event 2 (17–20 June 2019) was dominated by torrential heavy rain. A more detailed description of these two precipitation events is provided in section 3b.

The radar rainfall relationships for these two events are established as

$$R(Z_H) = \begin{cases} 0.0529 \times Z_H^{0.6196}, & Z_H < 40 \,\mathrm{dBZ} \\ 0.0968 \times Z_H^{0.5764}, & Z_H \ge 40 \,\mathrm{dBZ} \end{cases} \tag{5a}$$

$$R(K_{\rm DP}) = 23.3894 \times K_{\rm DP}^{0.7491},$$
 (5b)

$$R(Z_H) = \begin{cases} 0.0689 \times Z_H^{0.6197}, & Z_H < 40 \,\mathrm{dB}Z \\ 0.1054 \times Z_H^{0.5859}, & Z_H \ge 40 \,\mathrm{dB}Z \end{cases} \tag{5c}$$

$$R(K_{\rm DP}) = 28.5717 \times K_{\rm DP}^{0.7472},$$
 (5d)

where Eqs. (5a) and (5b) are for event 1 and Eqs. (5c) and (5d) are for event 2. Equations (5a)-(5d) were fitted using the standard weighted least squares method based on the simulated  $Z_H$  and  $K_{DP}$  and the rain rates R computed directly from the DSD data (see Figs. 1b,c). The polarimetric radar observables were simulated at C-band frequency using the T-matrix method (Waterman 1965). Therein, the raindrop aspect ratio of Brandes et al. (2002) was adopted, and the temperature was obtained from a local sounding station. In Eqs. (5a) and (5c), two Z-R relationships were utilized to discriminate light-moderate rain ( $Z_H < 40 \,\mathrm{dB}Z$ ) from moderate-heavy rain ( $Z_H \ge 40 \,\mathrm{dB}Z$ ). The differences between Eqs. (5a) and (5b) and Eqs. (5c) and (5d) also reflect that different precipitation microphysical characteristics were observed in the two events. With such eventbased rainfall algorithms, the uncertainties inherent in radar rainfall relationships can be reduced so as to further highlight the impact of attenuation and PBB corrections.

Radar hourly rainfall accumulations based on  $R(Z_H)$  and  $R(K_{\mathrm{DP}})$  were then derived using the pixel-to-pixel linear average accumulation scheme as follows:

$$R_{\text{hour}} = \frac{(t_1 - t_{\text{st}})}{t_{\text{total}}} \times \frac{(R_0 + R_1)}{2} + \sum_{i=1}^{n-2} \frac{(t_{i+1} - t_i)}{t_{\text{total}}} \times \frac{(R_i + R_{i+1})}{2}$$

$$+\frac{(t_{\rm ed} - t_{n-1})}{t_{\rm total}} \times \frac{(R_{n-1} + R_n)}{2},$$
 (6)

where  $R_{\rm hour}$  refers to the hourly rainfall estimates accumulated through the time series of  $R_i$  obtained in different time frames; the average of  $R_i$  and  $R_{i+1}$  is used to represent the rainfall intensity during the time window from  $t_i$  and  $t_{i+1}$ ;  $t_{\rm st}$  and  $t_{\rm ed}$  refer to the starting and ending time of the time series;  $t_{\rm total}$  is the difference between  $t_{\rm ed}$  and  $t_{\rm st}$  (i.e., 1 h in this study);  $t_i$  and  $t_{i+1}$  refer to the starting or ending time of  $R_i$  and  $R_{i+1}$ , and their difference ranges from 170 to 230 s for the CPOL radar.

The 3-h rainfall estimates were then derived by aggregating the hourly rainfall estimates  $R_{\rm hour}$ , which were then used in the verification analysis mainly because the longer-term temporal averaging could further reduce the random errors involved in the radar measurements. The radar QPE performance was quantitatively evaluated through comparison with corresponding gauge rainfall measurements. In particular, the performance of different radar rainfall estimators within the PBB area was investigated. Four evaluation scores, including the mean bias  $E_{\rm BIAS}$ , the normalized mean absolute error  $E_{\rm NM}$ , the root-mean-square error  $E_{\rm RMS}$ , and the correlation coefficient  $E_{\rm CC}$ , were used to quantify the impact of PBB correction on the rainfall estimation:

$$E_{\text{BIAS}} = \frac{\sum_{i=1}^{n} r_i}{\sum_{i=1}^{n} g_i},$$
 (7a)

$$E_{\text{NM}} = \frac{\sum_{i=1}^{n} |r_i - g_i|}{\sum_{i=1}^{n} g_i} \times 100\%,$$
 (7b)

$$E_{\text{RMS}} = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (r_i - g_i)^2},$$
 (7c)

$$E_{\text{CC}} = \frac{\sum_{i=1}^{n} (r_i - \overline{r})(g_i - \overline{g})}{\sqrt{\sum_{i=1}^{n} (r_i - \overline{r})^2} \sqrt{\sum_{i=1}^{n} (g_i - \overline{g})^2}},$$
 (7d)

where n is the sample number;  $r_i$  and  $g_i$  stand for the radarestimated and the gauge-observed 3-h rainfall accumulations, respectively;  $\overline{r}$  and  $\overline{g}$  stand for their average values, respectively.

## 3. Demonstration study domain and dataset

As shown in Fig. 2a, the study domain is mainly located to the north and northwest of the CPOL radar deployed in the south Tian Mu Mountains (TMM) over eastern China. The coverage of the CPOL radar shown in Fig. 2b is 150 km. Most of this area (the rectangular region in Fig. 2a) is located between the provinces of Anhui and Zhejiang. Qing Liang Peak (QLP) is the highest peak (1787.4 m above mean sea level, the circle in Fig. 2a) to the west of Zhejiang Province. Due to the complex mountainous terrain and the orographic enhancement of precipitation, this domain often suffers from severe rainfall that causes catastrophic flooding. Strong precipitation systems are frequently triggered when the western air flows with abundant moisture pass through this area during the summer monsoon seasons.

# a. Radar and surface observations

Considering the high altitude of the CPOL radar (1512 m above mean sea level), we reconfigured its volume coverage pattern (VCP) mode from March 2018 to enhance its capability to monitor rapidly developing severe rainstorms. The current

VCP scan mode includes 11 elevation angles:  $0^\circ$ ,  $0.5^\circ$ ,  $1.5^\circ$ ,  $0^\circ$ ,  $2.5^\circ$ ,  $3.5^\circ$ ,  $4.5^\circ$ ,  $6.0^\circ$ ,  $7.5^\circ$ ,  $9.0^\circ$ , and  $12^\circ$ . The azimuthal resolution was set as  $0.5^\circ$  at the lowest five elevation angles and  $0.98^\circ$  at the other six elevations. The scan strategy was rigorously implemented to complete one VCP scan in 6 min. Note that the lowest elevation angle (i.e.,  $0^\circ$ ) was repeated twice within a VCP scan cycle in order to improve the temporal resolution so as to capture more low-level details of fast-evolving rainstorms. We also want to note that the CPOL radar is the first and only radar site that adopts such flexible VCP in China, which is groundbreaking from an operational perspective.

However, the 0° elevation angle of the CPOL radar is completely blocked in the azimuth directions of [298.5°, 308°] (see Fig. 2b) due to the QLP, which is located only 17 km from the CPOL radar. In addition, some azimuths in the north and northwest directions of the CPOL radar are partially blocked, as indicated in Fig. 2b.

The gauge network within the PBB-affected area of the CPOL radar includes 219 tipping-bucket gauge stations, and their sampling resolution is 1 min. All of the gauges are well maintained by the local meteorological bureaus, and they are considered one of the most important data sources for severe rainfall monitoring and warnings. The gauge measurements were aggregated and only rainfall time series without any transmission interruptions were used in this study.

In addition, four Parsivel disdrometer units were deployed in the north mountainous areas of Hangzhou (see white "+" in Fig. 2a), including the Dao Shi (DS), Tian Chi (TC), Changhua (CH), and Shi Ling (SL) stations. The disdrometers were used to collect in situ DSD data in the study domain, and the temporal resolution of these disdrometers was configured as 1 min. All of these disdrometer stations are equipped with municipal electricity and an optical fiber, and they are well maintained to ensure the quality of the measured DSD. As mentioned in section 2c, 21 388 one-minute DSD samples were used to derive the appropriate  $K_{\rm DP}\!-\!Z_H$  relationship and the radar rainfall estimators.

# b. Brief overview of the selected precipitation events

As mentioned, two convective rainstorm events during the monsoon season in 2019 were investigated in this paper. The rainfall during the first event (25 May 2019) was characterized by continuous rainfall over 12 h, with some hourly accumulations exceeding 20 mm. The widespread rainstorms slowly passed over the target domain from the southwest to the northeast between 0600 and 2000 UTC 25 May 2019. During this event, the maximum 12-h rainfall accumulation recorded by gauges reached 187.3 mm in Shuang County of Xuan Cheng (XC) city at 2200 UTC 25 May 2019, and the rainfall measurements at more than 10 gauge stations in Huangshan city exceeded 100 mm during this 12-h period. The other event was a severe convective rainfall event that occurred on 20 June 2019. Large amounts of rainfall were recorded in most areas of XC city between 1800 and 2100 UTC 20 June 2019. The 3-h rainfall accumulation at the Seven Tower station reached 105.2 mm, and many villages suffered serious flooding and waterlogging.

The  $Z_H$  measurements from the  $0^{\circ}$  elevation scans were seriously degraded. As indicated by the plan position indicator

(PPI) plots in Figs. 3a and 3b, the  $Z_H$  patterns exhibit obvious discontinuity along the west and north azimuthal directions of the CPOL radar. This discontinuity corresponds to the radar beams that suffer from PBB due to the TMM. In addition, the maximum  $\Phi_{\rm DP}$  values in the azimuthal directions pointing to XC city were increased over  $100^\circ$  (see Figs. 3c,d), which implies that significant attenuation might be involved in the CPOL radar measurements in both the PBB and non-PBB areas. In contrast to the  $Z_H$  measurements in Figs. 3a and 3b, the  $K_{\rm DP}$  in Figs. 3e and 3f present good continuity without being affected by attenuation or PBB. Again, in this case, it is difficult to use conventional approaches to simultaneously correct the  $Z_H$  biases caused by attenuation and PBB.

#### 4. Results and discussion

The practical performance of the designed PBB correction scheme was verified through comparing the CPOL radar reflectivity with the collocated S-band reflectivity measurements from the XC radar and the reflectivity simulated from the DSD data. The impact of PBB correction on radar QPE was thoroughly investigated by comparing the continuity of the radar rainfall field derived from uncorrected and corrected  $Z_H$ . Cross comparisons with gauge rainfall measurements and the rainfall estimates derived from  $R(K_{\rm DP})$  were also performed.

### a. Comparison with the DSD-based simulations

Ideally, the scattergram of radar-measured  $K_{\rm DP}$  versus  $Z_H$  should roughly follow the black curves (regression curves from the DSD data) in Figs. 4a and 4b (for the PBB-affected areas). However, a large number of scatter points deviate from the simulated curves. Most of these outliers correspond to small  $Z_H^M$  ( $Z_H < 40~{\rm dB}Z$ ) and high  $K_{\rm DP}$  ( $K_{\rm DP} > 1^\circ {\rm km}^{-1}$ ), as indicated by the ellipses. High liquid water content was anticipated for these large  $K_{\rm DP}$  measurements, which should be characterized by higher  $Z_H$ ; however, high  $Z_H^M$  was not observed because of the attenuation and PBB effects.

After attenuation correction, the scattergrams of  $K_{\rm DP}$  versus  $Z_H^{\rm AC}$  in Figs. 4c and 4d are more consistent with the theoretical curves compared to Figs. 4a and 4b, especially when  $Z_H^{\rm AC}$  is larger than 40 dBZ. In addition, the spatial continuity of  $Z_H^{\rm AC}$  in Figs. 5c and 5d is more reasonable than that in Figs. 5a and 5b. Such enhancement can be attributed to the attenuation correction on  $Z_H$ . Nevertheless, there are still many scatter points with  $Z_H < 40\,{\rm dB}Z$  and  $K_{\rm DP} > 1^{\circ}\,{\rm km}^{-1}$  (see ellipses in Figs. 4c,d), which correspond to the radial gaps in the PBB areas indicated in Figs. 5a and 5b.

After correcting the PBB, the scattergrams of  $K_{\mathrm{DP}}$  versus  $Z_{H}^{\mathrm{AC}}$  in Figs. 4e and 4f present a coherent distribution and they follow the theoretical  $K_{\mathrm{DP}}$ – $Z_{H}$  curves fairly well. At the same time,  $Z_{H}^{\mathrm{ABC}}$  in Figs. 5e and 5f exhibits better spatial continuity than that in Figs. 5c and 5d, and the radial gaps have been completely eliminated. It can be concluded that the residual bias of  $Z_{H}^{\mathrm{AC}}$  caused by PBB (i.e., data in the ellipses in Figs. 4c,d) were effectively corrected after the PBB correction. The overall scattergram of the radar-measured  $K_{\mathrm{DP}}$  versus  $Z_{H}$  is more consistent with that simulated from DSD, demonstrating the effectiveness of the PBB correction procedure.

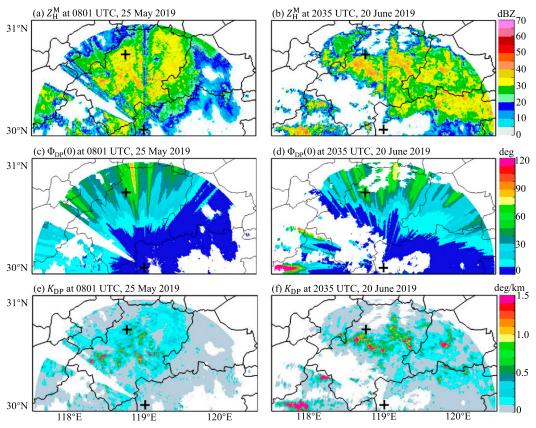


FIG. 3. Plan position indicator (PPI) observations of the CPOL radar at the  $0^{\circ}$  elevation angle: (a),(c),(e)  $Z_H^M$ ,  $\Phi_{\rm DP}$  (0), and  $K_{\rm DP}$  collected at 0801 UTC 25 May 2019; (b),(d),(f) As in (a),(c),(e), but collected at 2035 UTC 20 Jun 2019. The black "+" indicates the locations of the XC and CPOL radars.

# b. Comparison with the S-band XC radar measurements

To further verify the attenuation and PBB correction performance,  $Z_H$  measurements from the CPOL radar were compared with the  $Z_H$  measurements from a nearby S-band radar, which is a well-calibrated single-polarization system. The comparison was performed in the common sampling volumes (overlapped range gates) that were not affected by PBB for both the CPOL and XC radars. To this aim, the matched  $Z_H$  measurements from the CPOL and XC radars were selected. In particular, if the altitude differences between the two radar beams in their overlapped area were less than 0.01 km, the common sampling volumes were considered available and the corresponding data pairs were selected for comparison. In total, 62 598 data pairs were selected between 0700 and 0900 UTC 25 May 2019 for event 1, and 40 138 data pairs were selected between 1930 and 2130 UTC 20 June 2019 for event 2.

The scattergrams of  $K_{\mathrm{DP}}$  versus  $Z_{H}^{\mathrm{AC}}$  and  $K_{\mathrm{DP}}$  versus  $Z_{H}^{\mathrm{AC}}$  of the CPOL radar in the selected common sampling volumes are shown in Figs. 6a–d. As indicated in Figs. 6a and 6b, some  $Z_{H}^{\mathrm{M}}$  measurements suffered from serious attenuation in the areas not affected by PBB and the scatter density distributions deviate far from the theoretical curves derived from the DSD data. After attenuation correction,  $Z_{H}^{\mathrm{AC}}$  in the non-PBB areas were effectively enhanced, and the scattergrams of  $K_{\mathrm{DP}}$  versus

 $Z_H^{\rm AC}$  are more coherent with the theoretical curves (see Figs. 6c,d). In addition,  $Z_H^{\rm AC}$  in the non-PBB-affected areas can be used to cross check the quality of the  $Z_H$  measurements from the S-band XC radar. Figures 6e and 6f show the scattergram of  $Z_H^{\rm AC}$  from the CPOL radar versus the  $Z_H$  measurements from the XC radar in the common sampling volumes. Note that an additional constraint of  $K_{\rm DP} > 0.1^{\circ}\,{\rm km}^{-1}$  was imposed in this comparison in order to alleviate the impact of weaker echoes. As a result, 28 210 and 12 576 sample pairs were included in Figs. 6e and 6f, respectively. As expected, Figs. 6e and 6f show obvious consistency between the two radar systems. Compared to the  $Z_H^M$  measurements in Figs. 5a and 5b,  $Z_H^{\rm AC}$  in Figs. 5c and 5d in the non-PBB-affected areas presents a more consistent spatial pattern with the S-band  $Z_H$  measurements illustrated in Figs. 5g and 5h.

The arithmetic bias between the reflectivity measurements from these two radars was also computed as follows:

$$\Delta Z_{H}(Z_{T}) = \frac{1}{n} \sum [Z_{H}^{C}(Z_{T}) - Z_{H}^{S}(Z_{T})], \tag{8}$$

where n is the total number of common sampling resolution volumes between the XC and CPOL radars;  $Z_H^c$  stands for the C-band reflectivity (i.e.,  $Z_H^M, Z_H^{AC}$ , or  $Z_H^{ABC}$ ); and  $Z_T$  is a reflectivity threshold used to take into account the beam-filling

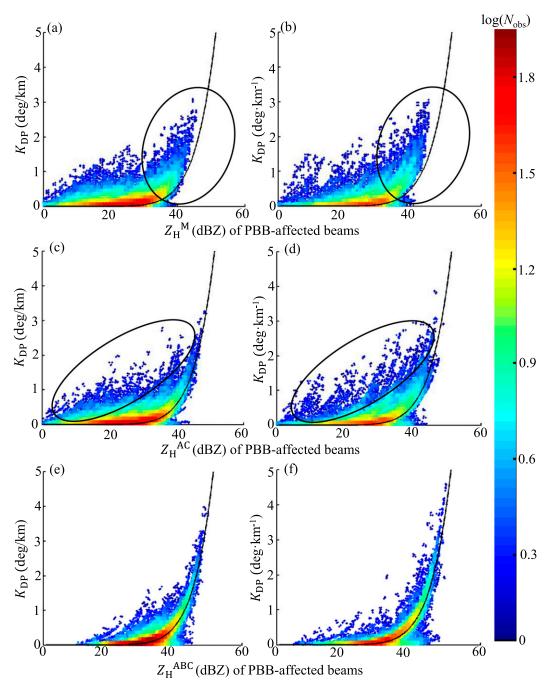


FIG. 4. The scattergram of  $K_{\rm DP}$  vs  $Z_H$  within the PBB-affected area of the CPOL radar: (a),(b)  $K_{\rm DP}$  vs  $Z_H^M$  shown in Figs. 3a and 3b; (c),(d)  $K_{\rm DP}$  vs  $Z_H^{\rm AC}$  shown in Figs. 5c and 5d; (e),(f)  $K_{\rm DP}$  vs  $Z_H^{\rm ABC}$  shown in Figs. 5e and 5f. The black curve in exponential form corresponds to Eq. (2a) in the main text.

issue of the XC radar, since the range and azimuthal resolutions of the XC radar (1000 m) are coarser than that of the CPOL radar (125 m). The threshold  $Z_T$  is particularly important near the edge of a rainstorm, where the precipitation echoes may completely fill the CPOL radar range volumes, but only partially fill the XC radar range volumes. Accordingly, when  $Z_T > 20 \, \mathrm{dB} Z$ ,  $\Delta Z$  is 1.31 and 3.11 dBZ in Figs. 6e and 6f,

respectively; when  $Z_T > 30\,\mathrm{dB}Z$ ,  $\Delta Z$  is -0.49 and  $0.88\,\mathrm{dB}Z$ , respectively. This indicates excellent agreement between the  $Z_H$  measurements from the S-band XC radar and the CPOL radar, especially in heavy rainfall regions.

In the PBB-affected areas, the  $Z_H^M$  measurements from the CPOL radar (see Figs. 5a,b) are much lower than those from the XC radar (see Figs. 5g,h). As shown by the scattergram in

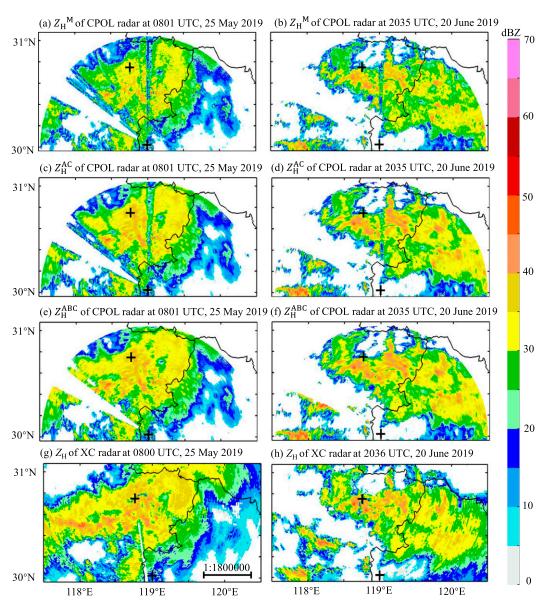


FIG. 5. PPI observations of the CPOL and S-band XC radars: (a),(b)  $Z_H^M$  measurements at the 0° elevation angle at 0801 UTC 25 May 2019 and 2035 UTC 20 Jun 2019, respectively; (c),(d)  $Z_H^{\rm AC}$  measurements corresponding to (a) and (b); (e),(f)  $Z_H^{\rm ABC}$  measurements corresponding to (a) and (b); (g),(h)  $Z_H$  measurements from the S-band XC radar at the 1.5° elevation angle. The black "+" marks indicate the locations of the CPOL and XC radars.

Figs. 7a and 7d, many sample pairs are distributed below the diagonal line, and  $\Delta Z$  is -4.12 and  $-3.63\,\mathrm{dB}Z$ , respectively, when  $Z_T > 20\,\mathrm{dB}Z$ . After attenuation correction, the  $Z_H^{\mathrm{AC}}$  measurements in the PBB-affected area were slightly enhanced, as illustrated in Figs. 5c and 5d. Nevertheless, Figs. 7b and 7e show that there are still many sample pairs that are distributed below the diagonal line, and  $\Delta Z$  is -3.85 and  $-2.30\,\mathrm{dB}Z$ , respectively, when  $Z_T > 20\,\mathrm{dB}Z$ . This, again, indicates that the PBB effect cannot be resolved only with attenuation correction.

In contrast,  $Z_H^{ABC}$  in Figs. 5e and 5f shows more continuous reflectivity patterns with less PBB contamination. The reflectivity

patterns also agree well with the XC S-band measurements in Figs. 5g and 5h. As shown in Figs. 7c and 7f, most of the data pairs are distributed along the diagonal line, similar to the measurements in the regions not affected by PBB (see Figs. 6e,f). The  $\Delta Z$  in Figs. 7c and 7f is 0.64 and 2.74 dBZ, respectively, when using a threshold of  $Z_T > 20$  dBZ. The larger  $\Delta Z$  in event 2 is likely due to the beam-filling issues, and it can be reduced to 0.16 dBZ when using a threshold of  $Z_T > 30$  dBZ.

# c. Impact on the radar QPE

In this study, radar-derived rainfall accumulations were used as another way to demonstrate the practical performance of

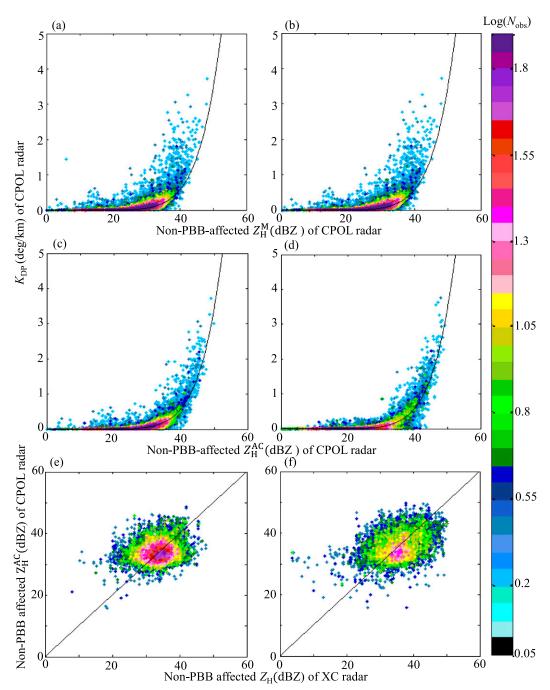


FIG. 6. Scatter density plots of (a),(b)  $K_{\rm DP}$  vs  $Z_H^M$  and (c),(d)  $K_{\rm DP}$  vs  $Z_H^{\rm AC}$  of the CPOL radar for the common (overlapped) range gates between the S-band XC radar and the CPOL radar without any PBB; (e),(f)  $Z_H^{\rm AC}$  of the CPOL radar vs  $Z_H$  of the XC radar for the common range gates. Shown are (left) event 1 and (right) event 2. The black curve in exponential form in (a)–(d) corresponds to Eq. (2a) in the main text.

the designed PBB correction procedure. Hereafter, the radar QPE estimators based on  $Z_H^M$ ,  $Z_H^{AC}$ , and  $Z_H^{ABC}$  are denoted by  $R(Z_H^M)$ ,  $R(Z_H^{AC})$ , and  $R(Z_H^{ABC})$ , respectively. The radar-derived 3-h rainfall fields were investigated, in particular, since the random errors could be eliminated through temporal averaging. The analysis was performed from the following aspects:

#### 1) SPATIAL CONTINUITY OF THE RAINFALL FIELD

As shown by the examples in Figs. 8a–d, although  $R(Z_H^{\rm AC})$  presents enhanced and higher rainfall estimates than  $R(Z_H^{\rm AC})$  in the non-PBB-affected areas due to attenuation correction, the rainfall fields derived from both  $R(Z_H^{\rm M})$  and  $R(Z_H^{\rm AC})$  present serious spatial discontinuity with large gaps along the PBB-affected

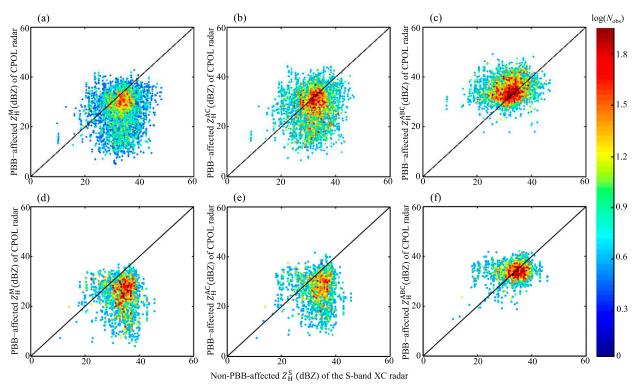


FIG. 7. Cross comparison of the measurements from the CPOL and XC radars for the common range gates: (a)–(c) PBB-affected  $Z_H^M$ ,  $Z_H^{AC}$ , and  $Z_H^{ABC}$ , respectively, of the CPOL radar vs the non-PBB-affected  $Z_H^S$  of the XC radar during event 1; (d)–(f) as in (a)–(c), but for event 2. The black line indicates the 1:1 line.

radial profiles, indicating obvious underestimation of  $R(Z_H^{AC})$  in this area. In contrast, the rainfall textures of  $R(Z_H^{ABC})$  in Figs. 8e and 8f show better spatial continuity than those of  $R(Z_H^{M})$  and  $R(Z_H^{AC})$ . In addition,  $R(Z_H^{ABC})$  is more consistent with  $R(K_{DP})$  in Figs. 8g and 8h. Such improvement demonstrates that the  $Z_H$  measurements at the  $0^\circ$  elevation angle in all time frames were corrected properly.

According to sections 2a and 2b, an improvement in continuity can be introduced by combining attenuation and PBB corrections. The contribution of attenuation correction, the first term in Eq. (2c), depends on the PIA(0,  $r_0$ ) along the radial profile. It is tightly related to  $A_H$ , which is derived using the dynamic  $\alpha_{\rm opt}$  coefficient. As depicted in Fig. 9a, the max PIA value at the last range gate along a radial profile (azimuthal angle of 0.25°) of the 0° elevation angle scan is 2.33 dB (difference between the red and green curves). Similarly, the max PIA value is 2.18 dB at the last range gate along the radial of azimuthal angle of 0.08° (see Fig. 9b).

The second term in Eq. (2c), i.e.,  $Z_H^B(r_b)$ , is tightly associated with the PBB ratios; it is also the main part of the proposed PBB correction procedure. However, the atmospheric states are always changing, indicating that PBB correction with fixed  $Z_H^B(r_b)$  based on the blockage ratios derived at standard atmospheric conditions may not be appropriate. In this paper,  $Z_H^B(r_b)$  was also dynamically determined based on the insensitivity of  $K_{\rm DP}$  to the PBB effect. In particular,  $Z_H^B(r_b)$  in Figs. 9a and 9b is 17.83 and 16.98 dBZ (i.e., difference between the blue and red curves), respectively, which are much larger

than the max PIA values along the same radial directions. That is to say, the PBB correction contributes more to the spatial continuity of the radar reflectivity measurements and rainfall estimates than the attenuation correction.

#### 2) COMPARISON WITH THE GAUGE MEASUREMENTS

For the sake of comparison, the radar rainfall estimates were deemed to agree well with the gauge rainfall measurements if  $|r_i - g_i| < 5$  mm. Note that both the radar and gauge rainfall measurements were of a 3-h scale. To see the clear trends of the rainfall scatters, three diagonal lines were included in the rainfall comparisons in Fig. 10, namely, the upper diagonal line (y = x + 5), the middle diagonal line (y = x), and the lower diagonal line (y = x - 5). According to the  $E_{BIAS}$  scores in Table 1,  $R(Z_H^{AC})$  slightly reduced the underestimation of  $R(Z_H^M)$  after attenuation correction. Consequently, the  $E_{\rm NM}$ ,  $E_{\rm RMS}$ , and  $E_{\rm CC}$  scores of  $R(Z_H^{\rm AC})$  improved by 7.7%, 17.6%, and 5.6%, respectively, for the estimates on 25 May 2019 and by 14%, 5.5%, and 7.6%, respectively, for the estimates on 20 June 2019. Nevertheless, there are no obvious differences between the scatter distributions in Figs. 10a and 10b, or Figs. 10e and 10f. More than 20% of the scatters are distributed below the lower diagonal line, which indicates that the underestimation of  $R(Z_H^M)$  can hardly be resolved with attenua-

In contrast, the  $E_{\rm BIAS}$  scores of  $R(Z_H^{\rm ABC})$  are close to 1. After applying  $R(Z_H^{\rm ABC})$ , nearly all of the scatters distributed below the lower diagonal line in Figs. 10b and 10f were enhanced,

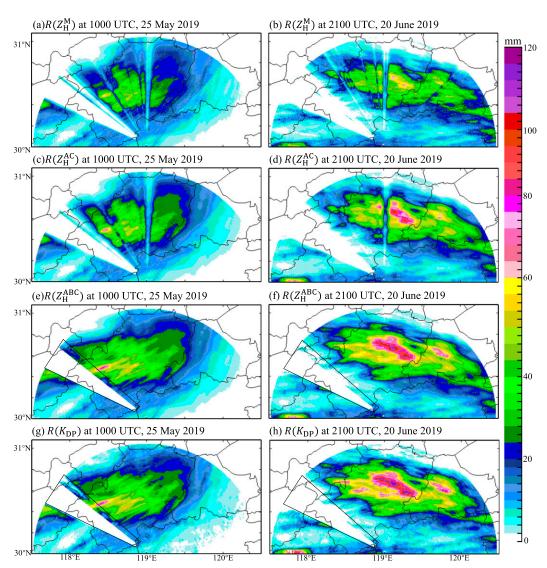


FIG. 8. Three-hour rainfall estimates based on the CPOL radar PPI observations at the  $0^{\circ}$  elevation angle: (a),(b) derived from  $R(Z_H^{M})$ ; (c),(d) derived from  $R(Z_H^{AC})$ ; (e),(f) derived from  $R(Z_H^{ABC})$ ; (g),(h) derived from  $R(K_{DP})$ . (left) Estimates at 1000 UTC 25 May 2019 and (right) estimates at 2100 UTC 20 Jun 2019.

as shown in Figs. 10c and 10g. Much fewer scatters can be found below the lower diagonal lines. We also noted that most of the underestimated values are located in the rectangles illustrated in Figs. 8e and 8f. Since radar beams are completely blocked when the PBB ratios are close to 1, the radar signals are extinct at farther range gates in this area. This is also why we still have some radial gaps in Figs. 8e and 8f in the completely blocked area. In addition, the radar estimates of  $R(Z_H^{\rm ABC})$  in Figs. 10c and 10g were overestimated at some points, conversely demonstrating the enhanced  $Z_H$  along these radials after PBB correction.

As the most important result,  $R(Z_H^{ABC})$  further reduced the underestimation involved in  $R(Z_H^{AC})$ . The  $E_{\rm NM}$  and  $E_{\rm RMS}$  scores of  $R(Z_H^{ABC})$  decreased by 72.7% and 67.8%, respectively, for the first event, and by 56.5% and 55.8%, respectively, for the second event. Meanwhile, the  $E_{\rm CC}$  scores increased by 59.6% and 12.9%, respectively, for the two

events. The relative improvements of  $R(Z_H^{\rm ABC})$  to  $R(Z_H^{\rm AC})$  quantitatively demonstrate the necessity and effectiveness of the PBB correction procedure.

## 3) Comparison with $R(K_{DP})$

The  $R(K_{\mathrm{DP}})$  can be used as another objective reference because of the insensitivity of  $K_{\mathrm{DP}}$  to attenuation and PBB. First, the  $E_{\mathrm{BIAS}}$  scores of  $R(K_{\mathrm{DP}})$  in Table 1 indicate that  $R(K_{\mathrm{DP}})$  slightly underestimated the rainfall. However, such underestimation mainly exists when the gauge rainfall measurements were less than 20 mm for the 25 May 2019 event, or less than 40 mm for the 20 June 2019 event (see Figs. 10d,h). Otherwise, an overestimation of  $R(K_{\mathrm{DP}})$  can be observed. As a result, nearly all of the scores of  $R(K_{\mathrm{DP}})$  listed in Table 1 are inferior to that of  $R(Z_H^{\mathrm{ABC}})$ . This also indicates that the combination of different rainfall relationships can more

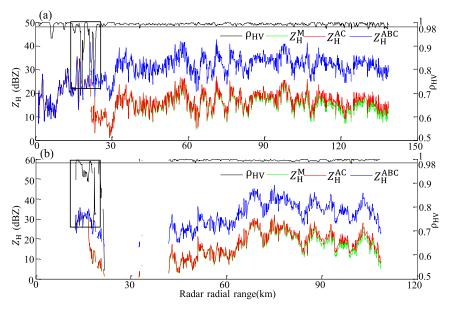


FIG. 9. Example radial range profiles of the CPOL radar at the  $0^{\circ}$  elevation angle: (a) Azimuthal angle is  $0.25^{\circ}$  at 0801 UTC 25 May 2019; (b) azimuthal angle is  $0.08^{\circ}$  at 2035 UTC 20 Jun 2019. The rectangles in (a) and (b) indicate the location of the terrain.

adequately represent the precipitation characteristics of the rainstorms.

Second, the rainfall textures of  $R(Z_H^{\rm AC})$  in Figs. 8a and 8b, and of  $R(Z_H^{\rm AC})$  in Figs. 8c and 8d in the PBB-affected area present many more discontinuities than that of  $R(K_{\rm DP})$  in Figs. 8g and 8h. In contrast, the rainfall textures of  $R(Z_H^{\rm ABC})$  in Figs. 8e and 8f are similar to those of  $R(K_{\rm DP})$ , especially in the rainfall center area. In addition, 99 328 and 99 826 point-wise samples  $[R(Z_H)$  versus  $R(K_{\rm DP})]$  within the PBB-affected area in Fig. 8 were selected and

used for detailed comparison for the first and second events, respectively. The scattergrams of the rainfall estimates for the selected samples during these two events are shown in Fig. 11. As shown in Fig. 11a, there are only 42 539 (42.8%) samples  $[R(Z_H^M)]$  versus  $R(K_{\rm DP})]$  between the upper and lower diagonal lines during event 1. Similarly, there are only 46 321 (46.4%) samples between the upper and lower diagonal lines during event 2 (see Fig. 11c). Most of these samples correspond to the light-rain regions (i.e., 3-h rainfall less than 20 mm). After attenuation

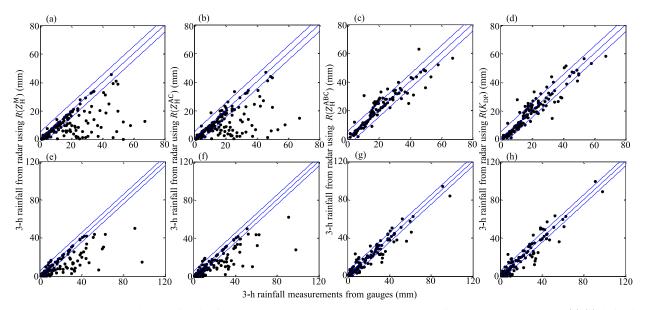


FIG. 10. Scattergrams of the 3-h rainfall estimates from the radar vs the gauge measurements in the PBB-affected areas: (a),(e) derived from  $R(Z_H^{AC})$ ; (b),(f) derived from  $R(Z_H^{AC})$ ; (c),(g) derived from  $Z_H^{ABC}$ ; (d),(h) derived from  $R(K_{DP})$ . (top) Estimates at 1000 UTC 25 May 2019 and (bottom) estimates at 2100 UTC 20 Jun 2019. The three blue lines indicate y = x and  $y = x \pm 5$ .

TABLE 1. Evaluation results of the 3-h rainfall estimates using different radar rainfall relationships.

Time frame	Radar QPE estimators	Statistical scores			
		$\overline{E_{ ext{BIAS}}}$	$E_{\mathrm{NM}}$	$E_{ m RMS}$	$E_{\rm CC}$
1000 UTC 25 May 2019	$R(Z_H^M)$	0.59	68.52	13.83	0.54
	$R(Z_H^{AC})$	0.63	63.22	13.05	0.57
	$R(Z_H^{ABC})$	1.05	17.27	5.67	0.91
	$R(K_{\mathrm{DP}})$	0.95	22.25	6.94	0.87
2100 UTC 20 Jun 2019	$R(Z_H^M)$	0.63	62.26	12.5	0.79
	$R(Z_H^{AC})$	0.68	51.29	10.75	0.85
	$R(Z_H^{ABC})$	0.98	16.54	4.75	0.96
	$R(K_{\mathrm{DP}})$	0.97	21.45	5.71	0.95

correction, the total number of samples lying between the upper and lower diagonal lines increased to 49 684 (50%) and 51 609 (51.7%), respectively, for the two events (see Figs. 11b,e).

Although some of the moderate rainfall estimates (i.e., higher than 20 mm) in the PBB-affected area were enhanced, the underestimation of  $R(Z_H^{\rm AC})$  remains a problem. In contrast, there are 89 615 (90.2%) and 79 413 (79.5%) samples between the upper and lower diagonal lines in Figs. 11c and 11f, respectively, which shows excellent agreement between  $R(Z_H^{\rm ABC})$  and  $R(K_{\rm DP})$ . The improvement brought by  $R(Z_H^{\rm ABC})$  compared to  $R(Z_H^{\rm M})$  or  $R(Z_H^{\rm AC})$  is dramatic, especially in the heavy-rain regions where the 3-h rainfall estimates are higher than 50 mm. Such dramatic improvement is mainly attributed to the implementation of the PBB correction.

In addition, extra attention was paid to the higher rainfall estimates of  $R(Z_H^{ABC})$  compared to  $R(K_{DP})$ . As shown in Fig. 11c

where the radar rainfall estimates are less than 20 mm, these samples are mainly from the range gates featuring  $\rho_{\rm HV} < 0.85$ ,  $Z_H > 20 \,\mathrm{dB}Z$ , but  $K_{\mathrm{DP}} > 1^{\circ} \,\mathrm{km}^{-1}$ . These range gates were suspected to be contaminated by the NUBF effect and many of them were eliminated during  $K_{\rm DP}$  estimation. However, the  $Z_H$  measurements seem to be less affected by the NUBF effect. The attenuation can be corrected with ever-increasing PIA values along the radial profile, and the PBB correction only requires that the corrected  $Z_H$  and  $K_{\mathrm{DP}}$  are consistent in the range gates with  $\rho_{\rm HV} \ge 0.98$  and  $\rho_{\rm HV} \le 1$ . As a result,  $R(Z_H^{\rm ABC})$  shows some higher rainfall accumulations in the polygonal area in Fig. 8e compared to  $R(K_{DP})$  in Fig. 8g. Moreover, the rainfall estimates derived from  $R(Z_H^{ABC})$  are weaker than those derived from  $R(K_{DP})$ , particularly when rainfall estimates are higher than 20 mm in Fig. 11f. Combining the scores of  $R(K_{DP})$  in Table 1,  $R(Z_H^{ABC})$ seems more reasonable than  $R(K_{DP})$  for rainfall estimation.

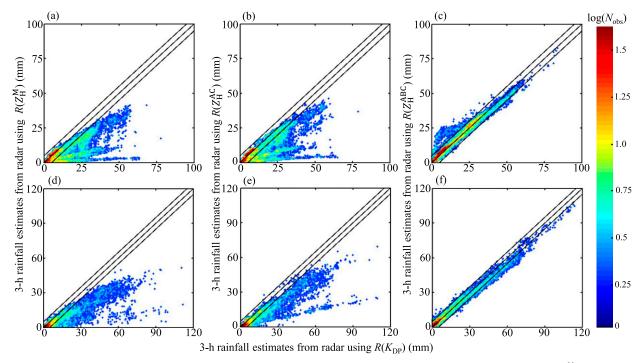


FIG. 11. Scattergrams of the 3-h rainfall estimates based on  $R(Z_H)$  vs  $R(K_{DP})$  in the PBB-affected areas: (a),(d)  $R(Z_H^M)$  vs  $R(K_{DP})$ ; (b),(e)  $R(Z_H^{AC})$  vs  $R(K_{DP})$ ; (c),(f)  $R(Z_H^{ABC})$  vs  $R(K_{DP})$ . (top) Estimates at 1000 UTC 25 May 2019 and (bottom) estimates at 2100 UTC 20 Jun 2019. The three black lines indicate y = x and  $y = x \pm 5$ .

At the very least, the combination of more  $K_{\rm DP}$ -R relationships may be necessary to enhance the performance of  $R(K_{\rm DP})$ .

#### d. Discussion

Although significant progress has been made in PBB correction, a number of relevant issues may need to be considered in practical implementations:

- (i) PBB is not the only quality control issue in polarimetric radar applications. The residual ground clutter contaminations on Z<sub>H</sub>, ρ<sub>HV</sub>, and Ψ<sub>DP</sub> measurements are not significant for the CPOL radar due to its high altitudes and the rigorous application of the CMD algorithm. However, clutter contaminations may still be a critical issue for many low-altitude S-band radars. More complex signal filtering and processing techniques may be therefore required, along with the PBB correction scheme.
- (ii) The 0° elevation angle radar data during warm season precipitation events were used in this paper, which could partially explain the high accuracy of the precipitation estimates relative to the gauge rainfall reports. However, the bright band effect may be a more serious issue during cooler seasons or shallow stratiform events. In such cases, multiradar observations, including vertical profiles of reflectivity, are necessary to fully resolve the precipitation structures and to provide reliable QPE.
- (iii) Although the radar measurements and QPE products were significantly improved after PBB correction, the correction scheme was established based on a fixed  $K_{\rm DP}$ – $Z_H$  relationship that may cause some uncertainties. On the one hand, the  $K_{\rm DP}$ – $Z_H$  relationship may be somewhat different in different precipitation events. Ideally, it should be adjusted according to different precipitation microphysics. On the other hand, the  $K_{\rm DP}$  at X band/S band are more/less sensitive to rain than that at C band. When extending this PBB correction method for S- and/or X-band applications, the  $K_{\rm DP}$ – $Z_H$  relationship should be reestablished. Fortunately, construction of local  $K_{\rm DP}$ – $Z_H$  relationships at different frequencies should not be difficult nowadays.
- (iv) The residual  $\delta$  and NUBF effects along the radial profiles of  $\Phi_{\rm DP}$  may contaminate the  $K_{\rm DP}$  estimation, which will result in the overestimation of  $Z_H^B(r_b)$  and, subsequently, degrade the PBB correction performance. This phenomenon is closely related to the mixed-phase hydrometeors or the edge area of rainstorms, which should be carefully treated during practical implementations.
- (v) This paper performed attenuation correction first and then PBB correction afterward. Although not presented, if PBB correction is conducted first and attenuation correction is incorporated afterward, similar results can be obtained. The key is that both A<sub>H</sub> and K<sub>DP</sub> are immune to attenuation and PBB effects.

#### 5. Summary

PBB correction is an important step in weather radar data quality control, and it is critical for rainfall estimation and subsequent flood warnings, especially in complex urban and mountain environments. This paper developed an improved PBB correction approach for polarimetric radar applications. The practical performance of this PBB correction technique was verified by comparing the spatial continuity of reflectivity, the consistency between radar-measured and DSD-derived  $K_{\rm DP}$  versus  $Z_H$ , as well as radar-derived QPE. The main findings are summarized as follows:

- (i) The spatial continuity of reflectivity can be effectively enhanced after attenuation and PBB corrections, and the reflectivity measurements of the CPOL radar in PBB-affected areas can become more consistent with the collocated S-band radar measurements. This is particularly evident in the rainstorm center area, where the Z<sub>H</sub> measurements are larger than 30 dBZ. The PBB correction contributes more to mitigating the Z<sub>H</sub> bias than the attenuation correction along the PBB-affected radial profiles.
- (ii) The consistency between radar-measured K<sub>DP</sub> and Z<sub>H</sub> can be incrementally enhanced after attenuation and PBB corrections. While attenuation correction can partly mitigate some biases in radar-measured K<sub>DP</sub> and Z<sub>H</sub>, PBB correction can further enhance the measurement quality. The radar-measured K<sub>DP</sub> and Z<sub>H</sub> are more consistent with DSD-derived K<sub>DP</sub>-Z<sub>H</sub> distributions after PBB correction.
- (iii) Rainfall estimates based on the  $Z_H$  measurements in PBB-affected areas can be significantly improved and the spatial continuity of the derived rainfall field is more realistic after PBB correction. The  $R(Z_H)$  tends to be more comparable with  $R(K_{DP})$  after attenuation and PBB corrections.

The PBB correction procedure developed in this paper is not limited to C-band applications. It is very flexible and can easily be extended to S- and/or X-band radar frequencies. With this improved PBB correction approach, it is also expected that multi-radar-based composite reflectivity will be more complete, especially at the lower atmospheric layers over complex terrain regions. The enhanced reflectivity is useful for many relevant applications such as QPE, hydrometeor identification, nowcast of severe rainfall and flood, and the development of data assimilation techniques to improve numerical weather prediction models.

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