DOI: 10.1111/2041-210X.13619

RESEARCH ARTICLE

Worth the effort? A practical examination of random effects in hidden Markov models for animal telemetry data

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Handling Editor: Robert B. O'Hara

Abstract

- 1. Hidden Markov models (HMMs) that include individual-level random effects have recently been promoted for inferring animal movement behaviour from biotelemetry data. These 'mixed HMMs' come at significant cost in terms of implementation and computation, and discrete random effects have been advocated as a practical alternative to more computationally intensive continuous random effects. However, the performance of mixed HMMs has not yet been sufficiently explored to justify their widespread adoption, and there is currently little guidance for practitioners weighing the costs and benefits of mixed HMMs for a particular research objective.
- I performed an extensive simulation study comparing the performance of a suite of fixed and random effect models for individual heterogeneity in the hidden state process of a two-state HMM. I focused on sampling scenarios more typical of telemetry studies, which often consist of relatively long time series (30–250 observations per animal) for relatively few individuals (5–100 animals).
- 3. I generally found mixed HMMs did not improve state assignment relative to standard HMMs. Reliable estimation of random effects required larger sample sizes than are often feasible in telemetry studies. Continuous random effect models performed reasonably well with data generated under discrete random effects, but not vice versa. Random effects accounting for unexplained individual variation can improve estimation of state transition probabilities and measurable covariate effects, but discrete random effects can be a relatively poor (and potentially misleading) approximation for continuous variation.
- 4. When weighing the costs and benefits of mixed HMMs, three important considerations are study objectives, sample size and model complexity. HMM applications often focus on state assignment with little emphasis on heterogeneity in state transition probabilities, in which case random effects in the hidden state process simply may not be worth the additional effort. However, if explaining variation in state transition probabilities is a primary objective and sufficient explanatory covariates are not available, then random effects are worth pursuing as a more parsimonious alternative to individual fixed effects.

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 To help put my findings in context and illustrate some potential challenges that practitioners may encounter when applying mixed HMMs, I revisit a previous analysis of long-finned pilot whale biotelemetry data.

KEYWORDS

animal biotelemetry, biologging, dependent mixture model, latent Markov model, momentuHMM, state-space model, state-switching, TMB

1 | INTRODUCTION

Hidden Markov models (HMMs) are used extensively in ecology for inferences about unobservable state processes from sequential (e.g. time series) data (McClintock et al., 2020; Zucchini et al., 2016). Some of the most widely used HMMs in population ecology include capture-recapture (e.g. Pradel, 2005), species occurrence (e.g. Gimenez et al., 2014) and animal movement (e.g. Franke et al., 2004) models. As recent advances in animal-borne biologging technology have permitted the collection of detailed location and biotelemetry data (e.g. Cooke et al., 2004), HMMs for inferring animal movement behaviour have become particularly popular (e.g. Jonsen et al., 2005; Langrock et al., 2012; McClintock et al., 2012; Morales et al., 2004; Patterson et al., 2009). This has been bolstered by user-friendly software specifically tailored to HMMs for these data (McClintock & Michelot, 2018; Michelot et al., 2016).

While animal movement HMMs were originally formulated as relatively simple two-state (e.g. 'foraging' and 'transit') models describing steps and turns between successive locations (e.g. Franke et al., 2004; Morales et al., 2004), they have since become much more complicated by incorporating location measurement error (e.g. Jonsen et al., 2005), >2 movement behaviour states (e.g. Michelot et al., 2017; Pirotta et al., 2018), additional biotelemetry data streams (e.g. DeRuiter et al., 2017; Isojunno et al., 2017) and 'mixed HMMs' including individual-level random effects (e.g. Langrock et al., 2012; McClintock et al., 2013; McKellar et al., 2015; Schliehe-Diecks et al., 2012). While all of these advances bring the potential for new and exciting inferences about animal movement behaviour, they also pose various challenges (e.g. Patterson et al., 2017; Pohle et al., 2017). The inferential benefits of accounting for measurement error or including additional data streams to characterize >2 behavioural states can justify this added complexity (e.g. Bradshaw et al., 2007; McClintock, 2017), yet the general benefits of mixed HMMs that include individual random effects are less well understood.

There is evidence for the benefits of individual random effects on the (conditional) observation process of HMMs in other contexts (e.g. Altman, 2007; Rueda et al., 2013), but there is surprisingly little evidence for benefits on the hidden state process. In a simulation study, Altman (2007) concluded for their case that there was 'far more information about the parameters associated with the conditional model than those associated with the hidden model' and that mixed HMMs allowing for individual differences in the hidden state

process 'may explain very little additional variation in the observed data and, hence, may not be worthwhile from a statistical standpoint'. Yet, understanding individual heterogeneity in behaviour or life-history strategies is a fundamental component of ecology and evolution (e.g. Cam et al., 2002; Gimenez et al., 2018; Johnson et al., 1986; Réale et al., 2007; Revilla & Wiegand, 2008), and accounting for individual variation in the hidden state process is clearly worthwhile for this purpose. Most animal movement mixed HMM applications have employed random effects on the hidden state process more as a statistical tool to 'mop up' unexplained variation and improve goodness-of-fit, with little attempt to interpret the mechanisms or implications of this variation (e.g. DeRuiter et al., 2017; McKellar et al., 2015; Towner et al., 2016). Part of the reason for this may be that, unlike effect sizes for explanatory covariates (e.g. age, sex, weight), generic random effects are difficult to interpret (e.g. Altman, 2007; Gimenez et al., 2018), particularly in biological terms across free-ranging telemetered individuals, each typically with different deployment lengths and being observed in different environmental and behavioural contexts (e.g. DeRuiter et al., 2017; Towner et al., 2016). Nevertheless, failing to properly account for individual variation could be detrimental to the estimation of effect sizes for any explanatory covariates on the hidden state process (e.g. DeRuiter et al., 2017).

In their discussion of the benefits of individual random effects on the hidden state process, DeRuiter et al (2017) claim 'it is easy to argue that random effects to account for individual variation are a key component of animal behaviour models'. I certainly do not disagree with this, but the empirical performance of these complex models has not yet been sufficiently explored to justify their widespread adoption (sensu Hodges, 2019), and there is currently little guidance for practitioners to determine when and how they should pursue random effects. This would all be relatively moot if mixed HMMs were easy for practitioners to implement, but they typically are not. Mixed HMMs have historically required custom-coded model fitting algorithms at significant computational cost (e.g. Altman, 2007; Langrock et al., 2012; Maruotti & Rydén, 2009; McKellar et al., 2015; Schliehe-Diecks et al., 2012; Towner et al., 2016) and can be very challenging to reliably fit to time series of animal biotelemetry data (e.g. DeRuiter et al., 2017; Isojunno et al., 2017). Furthermore, unlike other ecological applications of mixed HMMs that typically include relatively many individuals (e.g. capture-recapture; Burnham & White, 2002; Gimenez & Choquet, 2010) or sites (e.g. occupancy; Gimenez et al., 2014) and relatively short time series, animal-borne

biotelemetry studies typically include relatively few individuals (e.g. due to financial and logistical constraints) and relatively long time series of unequal length for each individual (e.g. due to variable battery life, tag loss and mortality). Little is currently known about how well mixed HMMs perform under these sampling conditions.

These challenges and uncertainties prompted me to investigate the benefits of accounting for individual variation in the hidden state process of HMMs that are frequently used for inferring animal movement behaviour from biotelemetry data. Using extensive simulation and a case study, my goal is to provide some guidance to aid practitioners in weighing the costs and benefits of mixed HMMs for a particular research objective. I first describe several of the most common HMM formulations and inferential procedures that account for individual variation. I then present a large-scale simulation study evaluating the performance of these various approaches in terms of hidden state estimation, parameter estimation and detection of individual variation by standard information-theoretic model selection criteria. To help put my findings in context and illustrate some potential challenges that practitioners may encounter when applying mixed HMMs, I then revisit an analysis of long-finned pilot whale biotelemetry data originally performed by Isojunno et al. (2017). Finally, I discuss the implications of my findings in establishing some considerations for practitioners contemplating the inclusion of individual random effects in their own analyses.

2 | INDIVIDUAL-LEVEL EFFECTS IN HMMs

2.1 | Model formulations

Under 'complete pooling', standard HMMs for *M* individual time series of length T_m (m = 1, ..., M) assume no individual effects on parameters (i.e. a common set of parameters is shared among the *M* individuals). Assuming independence between individuals, the likelihood function for this 'null' model with *N* hidden states can be succinctly expressed using the forward algorithm:

$$\mathscr{L}_{\text{null}} = \prod_{m=1}^{M} \delta \Gamma \mathbf{P} \left(\mathbf{y}_{m,1} \right) \Gamma \mathbf{P} \left(\mathbf{y}_{m,2} \right) \cdots \Gamma \mathbf{P} \left(\mathbf{y}_{m,T_{m}-1} \right) \Gamma \mathbf{P} \left(\mathbf{y}_{m,T_{m}} \right) \mathbf{1}, \quad (1)$$

where $\delta = (\delta_1, ..., \delta_N)$ is a row vector of initial state probabilities $\left(\sum_{j=1}^{N} \delta_j = 1\right)$, $\Gamma = (\gamma_{i,j})$ is a $N \times N$ state transition probability matrix with entries $\gamma_{i,j}$ corresponding to the probability of switching from state *i* at time t - 1 to state *j* at time $t\left(\sum_{j=1}^{N} \gamma_{i,j} = 1\right)$, $\mathbf{P}(\mathbf{y}_{m,t}) = \text{diag}\left(f(\mathbf{y}_{m,t}|\mathbf{S}_{m,t} = 1), ..., f(\mathbf{y}_{m,t}|\mathbf{S}_{m,t} = N)\right)$ is a $N \times N$ diagonal matrix with entries $f(\mathbf{y}_{m,t}|\mathbf{S}_{m,t} = s)$ corresponding to the conditional probability density of observation $\mathbf{y}_{m,t}$ given the state $S_{m,t} \in \{1, ..., N\}$ at time *t*, and 1 is a column vector of *N* ones (e.g. Zucchini et al., 2016). Here I assume all individuals share common state-dependent distribution parameters, a case where pooling collective movements across *M* individuals using a joint likelihood has been demonstrated to improve behavioural state assignment in animal movement HMMs (Jonsen, 2016). When explanatory individual covariates (e.g. age, sex, weight)

are available, the likelihood can be extended to accommodate individual variation attributable to these factors through link functions for the model parameters (e.g. McClintock & Michelot, 2018).

Generic individual heterogeneity in HMMs is typically handled using individual-level fixed effects (termed 'no pooling'; e.g. Patterson et al., 2009), discrete-valued random effects based on finite mixtures (e.g. DeRuiter et al., 2017; Maruotti & Rydén, 2009; McKellar et al., 2015; Towner et al., 2016) or continuousvalued random effects (e.g. Altman, 2007; Schliehe-Diecks et al., 2012). For individual fixed effects in the hidden state process, we have:

$$\mathscr{L}_{fix} = \prod_{m=1}^{M} \delta_{m} \Gamma_{m} \mathbf{P} \left(\mathbf{y}_{m,1} \right) \Gamma_{m} \mathbf{P} \left(\mathbf{y}_{m,2} \right) \cdots \Gamma_{m} \mathbf{P} \left(\mathbf{y}_{m,T_{m}-1} \right) \Gamma_{m} \mathbf{P} \left(\mathbf{y}_{m,T_{m}} \right) \mathbf{1},$$
(2)

where $\delta_m = (\delta_{m,1}, ..., \delta_{m,N})$ and $\Gamma_m = (\gamma_{m,ij})$ is a $N \times N$ state transition probability matrix with entries $\gamma_{m,ij}$ corresponding to the probability of individual *m* switching from state *i* at time t - 1 to state *j* at time *t*. This model is highly parameterized with MN^2 state transition probabilities, but it avoids any distributional assumptions about the individual effects.

For mixed HMMs with discrete-valued random effects, we have:

$$\mathscr{D}_{mix} = \prod_{m=1}^{M} \sum_{k=1}^{K} \delta^{(k)} \Gamma^{(k)} \mathbf{P} \left(\mathbf{y}_{m,1} \right) \Gamma^{(k)} \mathbf{P} \left(\mathbf{y}_{m,2} \right) \cdots \Gamma^{(k)} \mathbf{P} \left(\mathbf{y}_{m,T_{m}-1} \right) \Gamma^{(k)} \mathbf{P} \left(\mathbf{y}_{m,T_{m}} \right) \mathbf{1} \pi^{(k)}, \tag{3}$$

where $K \in \{1, ..., M - 1\}$ is the number of mixtures (typically chosen a priori or based on model selection criteria; e.g. DeRuiter et al., 2017), $\delta^{(k)} = \left(\delta_1^{(k)}, ..., \delta_N^{(k)}\right)$ and $\Gamma^{(k)} = \left(\gamma_{ij}^{(k)}\right)$ have entries $\gamma_{ij}^{(k)}$ corresponding to the probability that an individual belonging to mixture *k* switches from state *i* at time t - 1 to state *j* at time *t*, and $\pi = (\pi^{(1)}, ..., \pi^{(K)})$ are the mixture probabilities $\left(\sum_{k=1}^{K} \pi^{(k)} = 1\right)$. One would expect finite mixtures to be most appropriate for explaining individual variation attributable to unmeasured categorical covariates, but many such factors (e.g. age class, sex) can be measured in biotelemetry studies where individuals must be captured for tag deployment. It is less clear how appropriate finite mixtures are for 'mopping up' unexplained continuous-valued variation, but they have recently been promoted for this purpose in animal movement HMMs (e.g. McKellar et al., 2015; Towner et al., 2016).

For mixed HMMs with continuous random effects, the simplest models typically assume independent and identically distributed Gaussian random effects $z_{m,ij} \stackrel{\text{id}}{\sim} \mathcal{N}\left(\mu_{ij}, \sigma_{ij}^2\right)$ for $i \neq j$, $z_{m,ij} = 0$ for i = j and $\gamma_{m,ij} = \frac{\exp(z_{m,ij})}{\sum_{i=1}^{N} \exp(z_{m,ij})}$ such that:

$$\mathscr{L}_{\text{cont}} = \prod_{m=1}^{M} \int_{\mathscr{X}} \delta_{m} \Gamma_{m} \mathbf{P}\left(\mathbf{y}_{m,1}\right) \Gamma_{m} \mathbf{P}\left(\mathbf{y}_{m,2}\right) \cdots \Gamma_{m} \mathbf{P}\left(\mathbf{y}_{m,T_{m}-1}\right) \Gamma_{m} \mathbf{P}\left(\mathbf{y}_{m,T_{m}}\right) \, \mathbf{1} f\left(\mathbf{z}_{m} | \boldsymbol{\mu}, \boldsymbol{\sigma}\right) \, \mathrm{d} \mathbf{z}_{m},$$
(4)

where $f(\mathbf{z}_m|\boldsymbol{\mu}, \boldsymbol{\sigma}) = \prod_{i=1}^{N} \prod_{j \neq i} f(\mathbf{z}_{m,ij}|\boldsymbol{\mu}_{ij}, \boldsymbol{\sigma}_{ij})$ is the joint density of $\mathbf{z}_m = (z_{m,ij})_{i \neq j}$ and $\mathcal{Z} \in \mathbb{R}^{N(N-1)}$ its support. One would expect continuous random effects to be more parsimonious than fixed effects (Equation 2), but this comes at the cost of additional distributional assumptions and computational complexity.

2.2 | Maximum likelihood inference

I focus on maximum likelihood (ML) inference because HMMs can be fitted relatively quickly using ML methods, thereby facilitating large-scale simulation experiments. Standard ML inference by direct numerical maximization of the likelihood is straightforward in principle for the null (Equation 1), fixed (Equation 2) and finite mixture (Equation 3) models (McKellar et al., 2015; Patterson et al., 2009; Zucchini et al., 2016), and there are R (R Core Team, 2020) packages specifically designed for fitting these HMMs (e.g. McClintock & Michelot, 2018; Visser & Speekenbrink, 2010).

The integral in the continuous random effects model (Equation 4) poses additional challenges that have historically made fitting by ML largely intractable (e.g. Altman, 2007; DeRuiter et al., 2017; Schliehe-Diecks et al., 2012). The dimension of the integral is N(N - 1), which for N > 2 is generally not feasible for direct maximization of the likelihood using standard numerical integration techniques such as Gaussian quadrature (e.g. Abramowitz & Stegun, 1964). This largely explains why custom Monte Carlo expectation-maximization (e.g. Altman, 2007) and Bayesian Markov chain Monte Carlo (e.g. McClintock et al., 2013) algorithms have often been employed for fitting HMMs with continuous random effects.

Framed as a compromise between null and fixed effect models, Burnham and White (2002) proposed an approximate but computationally simple method for continuous random effect estimation based solely on maximum likelihood estimates from fixed effect models. Little used outside of capture-recapture applications, their approach was originally developed for temporal random effects in the Cormack-Jolly-Seber model of survival and, to my knowledge, has not been applied or investigated in contexts other than capturerecapture. However, standard open population capture-recapture models are simply special cases of HMMs (e.g. McClintock et al., 2020; Pradel, 2005). Full technical details can be found in Burnham and White (2002), but I describe their approach in the context of individual random effects for the state transition probabilities (Equation 4) in Section S1 of the Supporting Information. Burnham and White (2002) demonstrated that their approximate random effects estimator worked well for the Cormack-Jolly-Seber model with a single temporal random effect on survival probability, but, as an approximate method, it is not immediately clear whether or not its simple extension to N(N - 1) individual random effects for the state transition probabilities in a N-state HMM would also perform well. One known issue with this approach is that it becomes unreliable when any $\gamma_{m,i,i}$ for the fixed effects model (Equation 2) is estimated near 0 or 1, and one could suspect that such boundary issues will become more likely as M increases, T_m decreases and N increases. Bayesian analogues to the two-stage approach of Burnham and White (2002) could be less susceptible to these boundary issues (Hooten et al., 2016, 2019).

More recently, the R package Template Model Builder (TMB; Kristensen et al., 2016), which relies on reverse-mode automatic differentiation and the Laplace approximation for high-dimension integrals, has made ML inference for continuous random effects much more tractable. TMB is less 'plug-and-play' than the approach of Burnham and White (2002) because it currently requires advanced programming skills to custom code the HMM likelihood (Equation 4) based on a C++ template. In addition, little is currently known about how well the Laplace approximation performs for mixed HMMs or for sample sizes typical of animal telemetry studies (see Albertsen et al., 2015; Auger-Méthé et al., 2017; Benhaiem et al., 2018; Whoriskey et al., 2017 for relevant applications). Nevertheless, continuous random effect HMMs implemented using TMB can be fitted exceptionally fast, are amenable to more complex correlation structures and likely do not suffer from the same boundary issues as the approximate approach of Burnham and White (2002). These promising capabilities of TMB facilitate large-scale simulation experiments for comparing the performance of these different approaches for modelling individual variation in the hidden state process.

3 | SIMULATION STUDY

3.1 | Simulation methods

Based on two-state HMMs commonly used in analyses of telemetry data (e.g. Franke et al., 2004; Morales et al., 2004), I performed a simulation experiment to evaluate the performance of models that include no effects, fixed effects, discrete random effects and continuous random effects to account for individual heterogeneity in state transition probabilities. Two sets of simulations were performed (see Table 1). In the first (hereafter 'without covariates'), the simulated data included no measurable individual-level covariates and the fitted models included no explanatory covariate terms for the state transition probabilities. In the second (hereafter 'with covariates'), the simulated data included a measurable individual-level covariate and the models were fitted both with and without terms for the covariate effect on the state transition probabilities. R (R Core Team, 2020) code for simulating data and fitting all models can be found in McClintock (2021).

3.1.1 | Without covariates

Data were simulated under five levels of individual heterogeneity: (a) no individual heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0$); (b) continuous random effects with 'moderate' heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0.202$); (c) continuous random effects with 'high' heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0.416$); (d) K = 2 discrete random effects with $\pi^{(1)} = 0.6$, $\gamma_{1,2}^{(1)} = 0.25$, $\gamma_{1,2}^{(2)} = 0.25$ and $\gamma_{2,1}^{(2)} = 0.5$ (hereafter 'mixA'); and (e) K = 2 discrete random effects with $\pi^{(1)} = 0.6$, $\gamma_{1,2}^{(1)} = 0.75$, $\gamma_{2,1}^{(1)} = 0.75$, $\gamma_{1,2}^{(2)} = 0.25$ and $\gamma_{2,1}^{(2)} = 0.25$ (hereafter 'mixB'). For the $z_{m,ij} \sim \mathcal{N}\left(\mu_{ij}, \sigma_{ij}^{2}\right)$ continuous random effect scenarios with $\sigma_{1,2} = \sigma_{2,1} \in \{0, 0.202, 0.416\}$, I included two levels for state persistence: (a) $\log t^{-1}(\mu_{1,2}) = \log t^{-1}(\mu_{2,1}) = 0.5$ (hereafter 'lower' state persistence), corresponding to $\gamma_{m,1,1} = \gamma_{m,2,2} = 0.5$ when $\sigma_{1,2} = \sigma_{2,1} = 0$; and (b) $\log t^{-1}(\mu_{1,2}) = \log t^{-1}(\mu_{2,1}) = 0.25$ (hereafter ter 'higher' state persistence), corresponding to $\gamma_{m,1,1} = \gamma_{m,2,2} = 0.75$ **TABLE 1** Design points for simulation scenarios with and without measurable covariate effects based on the degree of overlap in the state-dependent distributions, the support of the random effects (continuous or discrete), the number of individuals and the length of the individual time series. Scenarios without covariates and continuous random effects included logit⁻¹($\mu_{1,2}$) = logit⁻¹($\mu_{2,1}$) \in {0.5, 0.25} ('lower' and 'higher' state persistence, respectively). Scenarios with covariates and continuous random effects included logit⁻¹($\mu_{0,1,2}$) = logit⁻¹($\mu_{0,2,1}$) \in {0.5, 0.25} and ($\mu_{1,1,2}$, $\mu_{1,2,1}$) \in {0,0, (0.5, -0.5)}. There were therefore $3 \times (2 \times 3 + 2) \times 5 \times 3 = 360$ scenarios without covariates and $3 \times (2 \times 2 \times 3) \times 5 \times 3 = 540$ scenarios with covariates

		Random effect	s				
		Continuous			Discrete		
Simulation scenario	Overlap	State persistence	$(\mu_{1,1,2}, \mu_{1,2,1})$	σ		No. individuals (M)	Time-series length (T _m)
Without covariates	Little, some, much	Lower, higher		0, 0.202, 0.416	mixA, mixB	5, 15, 30, 50, 100	30-250, 110, 250
With covariates	Little, some, much	Lower, higher	(0, 0), (0.5, -0.5)	0, 0.202, 0.416		5, 15, 30, 50, 100	30-250, 110, 250

when $\sigma_{1,2} = \sigma_{2,1} = 0$. Scenarios with lower state persistence and $\sigma_{1,2} = \sigma_{2,1} = 0.202$ correspond to a mean of 0.5 and standard deviation of 0.05 on the state transition probability scale, whereas those with lower state persistence and $\sigma_{1,2} = \sigma_{2,1} = 0.416$ correspond to a mean of 0.5 and standard deviation of 0.10. Scenarios with lower persistence and no individual heterogeneity are equivalent to generating data from a (non-Markov) finite mixture model and could be viewed as a 'worst-case scenario' in terms of serial correlation in the hidden state process. For the discrete random effect scenarios, 'mixA' can be considered less heterogeneous than 'mixB' (because the 'mixA' mixtures are more similar). All parameter values were chosen to keep state transition probabilities roughly between 0.1 and 0.9 (see Figure S1), thereby helping to reduce potential parameter boundary issues during model fitting and prevent either state from being relatively rare (Beyer et al., 2013). For simplicity, data were generated with $\delta_m = (0.5, 0.5)$ for m = 1, ..., M in all scenarios.

I limited simulated observations to a single data stream generated from a (state-dependent) gamma distribution for 'step length', $y_{mt} | S_t = s \sim \Gamma(\mu_s^{\gamma}, \sigma_s^{\gamma})$ for $S_t \in \{1, 2\}$, with varying degrees of overlap between the states based on the mean (μ_s^{γ}) and standard deviation (σ_s^{γ}) . These correspond to 'little' overlap ($\mu_1^y = 1$, $\mu_2^y = 10$, $\sigma_1^y = 1$, $\sigma_2^y = 2$), 'some' overlap ($\mu_1^y = 5$, $\mu_2^y = 10$, $\sigma_1^y = 2$, $\sigma_2^y = 2$) and 'much' overlap ($\mu_1^y = 5$, $\mu_2^y = 10$, $\sigma_1^y = 2$, $\sigma_2^y = 6$; Figure 1). The Kolmogorov-Smirnov test statistics for these distributions are, respectively, 0.99, 0.80 and 0.49, where 0 indicates the distributions are identical and 1 indicates no overlap. Standard HMMs are known to perform poorly when the state-dependent distributions overlap (e.g. Beyer et al., 2013; Jonsen, 2016), but I included these scenarios to assess whether or not the inclusion of individual effects somehow alters this behaviour. While movement HMMs typically include two data streams (step length and turn angle), the number of data streams is arbitrary for my purposes. I therefore chose a single data stream to minimize the number of observations and parameters to be estimated, thereby reducing run times and facilitating interpretation across a large number of simulated scenarios.

Simulated sample sizes were chosen based on animal-borne telemetry studies that typically tend to include relatively few individuals, but relatively long time series for each individual (e.g. DeRuiter et al., 2017; Isojunno et al., 2017; Langrock et al., 2012; McClintock et al., 2013; Morales et al., 2004; Towner et al., 2016). I included five levels for the number of individuals $M \in \{5, 15, 30, 50, 100\}$ and three levels for the number of observations per individual (30–250, 110, 250). For scenarios with 30–250 observations per individual, individuals were assigned to one of $T_m \in \{30, 50, 70, 150, 250\}$ in equal proportions such that $\sum_{m=1}^{M} T_m$ is identical for scenarios with 30–250 or 110 observations per individual. I limited $T_m \leq 250$ both to reduce computation time and to reflect the lengths of time series in many prominent applications of animal movement HMMs (e.g. Jonsen et al., 2005; Morales et al., 2004) and mixed HMMs (e.g. DeRuiter et al., 2017; Isojunno et al., 2017; Towner et al., 2016).

For each of the 360 scenarios examined, up to nine models were fitted to 400 simulated datasets using maximum likelihood methods. These models included two-state HMMs with no individual effects ('null'; Equation 1), individual fixed effects ('fixed'; Equation 2), discrete random effects with $K \in \{2, 3, 4, 5, 6\}$ mixtures ('mix2', 'mix3', 'mix4', 'mix5' and 'mix6', respectively; Equation 3), approximate continuous random effects estimated from the 'fixed' model based on Burnham and White (2002; 'BW'), and continuous random effects using numerical integration ('TMB'; Equation 4) for the state transition probabilities. To reduce simulation run times, discrete random effect models with K = 5 or K = 6were only fitted if the K - 1 mixture model resulted in a lower bias-corrected Akaike's Information Criterion (AICc; Burnham & Anderson, 2002) value relative to the K - 2 mixture model. Models with K = 5 or K = 6 are therefore only included in model selection and multimodel inference results (see Section 3.1.4). Simulated data were generated using the simData function in R package momentuHMM (version 1.5.2; McClintock & Michelot, 2018). The R package TMB (Kristensen et al., 2016) was used for fitting model TMB, and the momentuHMM function fitHMM was used for fitting all other models. The momentuHMM function randomEffects was used for implementing the BW approach based on the maximum likelihood estimates of the fixed effects model returned by fitHMM.

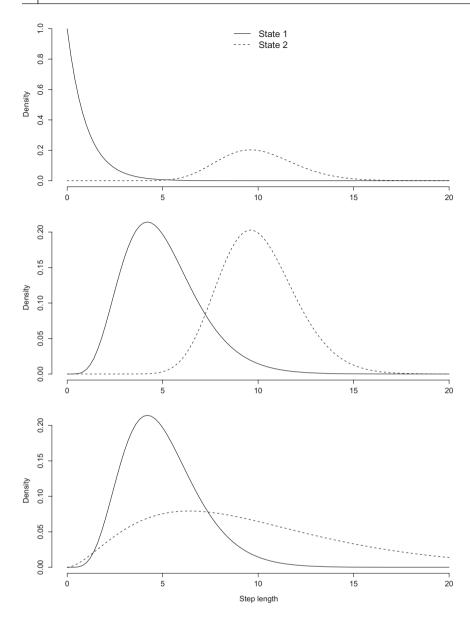


FIGURE 1 State-dependent observation distributions for 'step length' in simulated scenarios with 'little' (top panel), 'some' (middle) and 'much' (bottom) overlap

3.1.2 | With covariates

To investigate estimator performance in the presence of a (measurable) continuous-valued individual covariate, I performed an additional set of simulations with $\text{logit}^{-1}(\mu_{0,1,2}) = \text{logit}^{-1}(\mu_{0,2,1}) \in \{0.5, 0.25\},\$ $\sigma_{1,2} = \sigma_{2,1} \in \{0, 0.202, 0.416\}, M \in \{5, 15, 30, 50, 100\}, and the same$ three levels for the degree of overlap ('little', 'some', 'much') and the number of observations per individual (30-250, 110, 250). Two covariate scenarios were included: (a) $\mu_{1.1,2} = \mu_{1.2,1} = 0$ and (b) $\mu_{1.1,2} = 0.5$ and $\mu_{1,2,1} = -0.5$, where $z_{m,ij} \sim \mathcal{N} \left(\mu_{0,ij} + x_m \mu_{1,ij}, \sigma_{ij}^2 \right)$ and x_m is a measurable individual covariate drawn from a standard normal distribution. The covariate scenarios with $\mu_{1,1,2} = \mu_{1,2,1} = 0$ were included to investigate the potential for inferring spurious covariate effects from the different models, whereas the scenarios with $\mu_{1,1,2} = 0.5$ and $\mu_{1,2,1} = -0.5$ have $\gamma_{m,1,2}$ and $\gamma_{m,2,1}$ increasing and decreasing with x_m , respectively (Figure S2). For these 540 scenarios each consisting of 400 simulated datasets, I fitted the fixed effect model (with no covariate effects) and the null, finite mixture and continuous random effect models both with and without terms for the covariate effects (up to 17 models total). For the finite mixture models, each of the *K* mixtures included contextspecific $\mu_{0,ij}^{(k)}$ and $\mu_{1,ij}^{(k)}$ parameters (e.g. DeRuiter et al., 2017), from which population-level covariate effects were derived for comparisons with other models (see Section S2.1.3 in Supporting Information).

3.1.3 | Estimator performance

For both sets of simulations, estimator performance for $\sigma = (\sigma_{1,2}, \sigma_{2,1})$, $\Gamma_m = (\gamma_{m,i,j})$ for m = 1, ..., M, $\mu^{\gamma} = (\mu_1^{\gamma}, \mu_2^{\gamma})$ and $\sigma^{\gamma} = (\sigma_1^{\gamma}, \sigma_2^{\gamma})$ was evaluated based on mean bias, 95% confidence interval coverage and standard error (or confidence interval length). For the set of simulations with covariates, summaries of estimator bias and precision for $\mu_{1,1,2}$ and $\mu_{1,2,1}$ were based on medians because with smaller sample sizes the means for these (unconstrained) parameters could be heavily influenced by a small number of outliers when estimated state transition probabilities

fell on the boundary of the parameter space. I examined the performance of the Viterbi algorithm for global state decoding (e.g. Zucchini et al., 2016) while accounting for state classification agreement entirely due to chance using the Kappa statistic (Beyer et al., 2013; Congalton, 1991), which ranges from 0 (entirely chance agreement) to 1 (perfect agreement not attributable to chance). I also evaluated the proportion of estimated local state probabilities (based on the forward-backward algorithm; e.g. Zucchini et al., 2016) with at least 0.50 and 0.20 probability assigned to the true state: $\sum_{m=1}^{M} \sum_{t=1}^{T_m} I(p_{m,t,s_{m,t}} \ge q) / \sum_{m=1}^{M} T_m$ where I() is the indicator function, $p_{m,tj}$ is the estimated probability of state j for individual m at time t, s_{mt} is the true state for individual *m* at time *t*, and $q \in \{0.50, 0.20\}$. To facilitate comparisons across models, individual-level estimates for state transition probabilities were derived from the maximum likelihood estimates for the finite mixture models. For global state decoding and local state probabilities, I used modified Viterbi and forward-backward algorithms accommodating finite mixtures (see Sections S2.1.3-S2.1.5 in Supporting Information). For the continuous random effect models, the standard Viterbi and forward-backward algorithms were used based on the shrinkage estimates for each individual $(\hat{\gamma}_{mii})$.

3.1.4 | Model selection and multi-model inference

Standard model selection criteria are often used to choose among competing HMMs (e.g. DeRuiter et al., 2017; Isojunno et al., 2017; Pohle et al., 2017). For both sets of simulations, I evaluated the performance of AIC, in selecting among competing models for individual heterogeneity in state transition probabilities by calculating the standard AIC, for the null, fixed and finite mixture models, the conditional AIC_c for the BW random effects model (Burnham & White, 2002), and the marginal AIC_c for the TMB random effects model using $n = \sum_{m=1}^{M} T_m$ as the sample size. While the BW conditional AIC_c is comparable with the AIC_c for the null, fixed and finite mixture models, it is unclear how well the marginal AIC. for TMB will perform for selecting among fixed and random effect models (e.g. Bolker et al., 2009; Gimenez & Choquet, 2010). I therefore also performed a likelihood ratio test (LRT) comparing the null and TMB models as suggested by Gimenez and Choquet (2010). To my knowledge, there is currently no straightforward way to calculate a conditional AIC even for simpler (non-Markov) random effect models fitted in TMB; for example, the TMB-based generalized linear mixed modelling R package glmmTMB (Brooks et al., 2017) only provides marginal AIC. Multi-model inference can be used to account for model selection uncertainty, and I calculated model-averaged estimates, standard errors and 95% confidence intervals for Γ_m , μ^{γ} and σ^{γ} based on AIC, weights (Burnham & Anderson, 2002) for four sets of candidate models: (a) null and finite mixture models (hereafter 'modMix'); (b) null, fixed and finite mixture models ('modFix'); (c) null, fixed, finite mixture and BW models ('modBW') and (d) null, finite mixture and TMB models ('modTMB'). For simulations with covariates, model-averaged estimates for $\mu_{1,ij}$ were calculated from AIC_c weights for the models that included the covariate effect.

3.1.5 | Nested loop plots

Simulation scenario results are presented using the nested loop plot of Rücker and Schwarzer (2014). Similar to a time-series plot, nested loop plots serve to present a large number of simulation results by putting all scenarios into a lexicographical order and arranging them consecutively along the horizontal axis. The quantity of interest (e.g. bias, coverage) is then plotted on the vertical axis. The decision on how to nest the results is subjective, with the top level of nesting receiving the most emphasis. For BW and modBW, results are only reported for those scenarios where at least 50 of the simulated datasets yielded admissible Γ_m estimates from the fixed effects model, where I considered any $\hat{\gamma}_{m,i,i} < 0.01$ or $\hat{\gamma}_{m,i,i} > 0.99$ as inadmissible.

3.2 | Simulation results

3.2.1 | Summary

Given the large amount of information afforded by so many simulation scenarios, I first provide a brief summary of the main findings before delving into more detail on the simulation results without (Section 3.2.2) and with (Section 3.2.3) covariates. As expected, across all simulated scenarios, the data-generating model tended to perform better in terms of state assignment and parameter estimation as sample sizes (M and T_m) increased, the degree of overlap in state-dependent distributions decreased, and state persistence increased. There was generally little difference in state assignment among the null, fixed and random effect models, indicating mixed HMMs did not improve classification of the hidden state process. Owing to negative bias and poor precision, the continuous random effect variance parameters (σ) generally proved difficult to reliably estimate except with larger sample sizes (e.g. M > 50). While little difference was found between the various models in terms of state-dependent distribution parameter ($\mu^{\gamma}, \sigma^{\gamma}$) estimation, discrete random effect models exhibited poor coverage of state transition probabilities ($\gamma_{m,i,j}$) under continuous variation, and continuous random effect models exhibited inflated standard errors for $\gamma_{m,ij}$ under discrete variation. Model selection and model averaging based on AIC_c generally worked well when the datagenerating model was included in the candidate model set, but it did little to mitigate model misspecification in the 'modMix' and 'modFix' model sets for the continuous variation scenarios. Finally, in the 'with covariates' scenarios, discrete random effect models again proved to be a poor (and potentially misleading) approximation for continuous variation, often resulting in a substantial reduction in confidence interval coverage for the covariate effects $(\mu_{1,ij})$ and, in some cases, less accurate state assignment relative to the other models.

3.2.2 | Without covariates

State assignment

The degree of overlap between the (state-dependent) observation distributions was by far the most important factor for state estimation. The performance of each model declined as overlap increased, but, within each level of overlap ('little', 'some', 'much'), there was little difference among the null, fixed and random effect models (Figure 2; Table S1). When there was 'some' or 'much' overlap, performance tended to slightly improve as state persistence increased (Figure S3) and as individual heterogeneity, the number of individuals and the lengths of the time series increased. After accounting for chance agreement, the Viterbi algorithm for global state decoding produced an average correct state assignment of 99% (range: 99%-99%) for 'little' overlap, 82% (range: 76%-84%) for 'some' overlap and 51% (range: 40%-57%) for 'much' overlap across all scenarios and models. The proportion of correct state assignments using the Viterbi algorithm therefore closely corresponded to the degree of overlap in the state-dependent distributions as calculated by the Kolmogorov-Smirnov test statistic (respectively 0.99, 0.80 and 0.49). Estimated state probabilities tended to assign at least 0.5 probability to the true state >75% of the time (and at least 0.20 probability to the true state >90% of the time) across all scenarios and models, indicating local state probabilities are better able to account for uncertainty in state assignment that is attributable to overlap in state-dependent observation distributions. While the discrete random effect models tended to assign less probability to the true state with 'some' or 'much' overlap, the inclusion of individual fixed, discrete random or continuous random effects generally made little difference in local state probabilities relative to the null model.

Random effect variance

Models that included continuous random effects (BW and TMB) generally performed best in terms of bias, coverage and confidence interval length with 'little' overlap, 'higher' state persistence $(logit^{-1}(\mu_{1,2}) = logit^{-1}(\mu_{2,1}) = 0.25)$, 'high' heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0.416$) and larger sample sizes (Table 2; Figure 3). With percent confidence interval lengths (calculated as $100(\hat{\sigma}_{upper} - \hat{\sigma}_{lower})/\sigma$ for $\sigma > 0$) for individual scenarios ranging from 81% (M = 100, $T_m = 250$ and 'little' overlap) to 5,139% $(M = 5, T_m = 30-250 \text{ and 'much' overlap})$, both estimators tended to produce very wide confidence intervals for σ as the number of individuals decreased, the length of the time series decreased and the degree of overlap increased. With 'little' overlap and few individuals, BW tended to perform better than TMB, and, because its point estimates and confidence intervals can include zero, BW also tended to perform better than TMB for scenarios with no heterogeneity (i.e. $\sigma_{1,2} = \sigma_{2,1} = 0$; Figure 3). However, with individual heterogeneity and 'some' or 'much' overlap, BW tended to underperform relative to TMB as the number of individuals increased and the length of the time series decreased, particularly when there was 'lower' state persistence. Under these conditions,

the fixed model increasingly tended to estimate at least one state transition probability near a boundary, thereby making it unsuitable for the BW approach. This likely explains the increased negative bias for BW with 'some' and 'much' overlap, as the subset of simulated datasets that produced admissible Γ_m estimates from the fixed model will exhibit truncated tails for the random effect distributions (and hence smaller σ). However, the fact that the bias tended to be greater for $\sigma_{2,1}$ than for $\sigma_{1,2}$ also suggests that the sampling variance-covariance matrix approximation of Burnham and White (2002) might be inadequate in accounting for the additional state uncertainty under scenarios with non-negligible overlap. TMB therefore appears to be more robust to overlap in state-dependent observation distributions and shorter time series with 'moderate' to 'high' heterogeneity, but, owing to negative bias and poor precision, neither TMB nor BW performed particularly well except in scenarios with 'little' overlap, 'high' heterogeneity and at least M = 50 individuals.

State transition probabilities

All models generally exhibited little bias in state transition probabilities with 'little' or 'some' overlap, but performance was more variable in terms of confidence interval coverage and precision (Table 3; Figure 4). Although the overall mean bias across all Γ_m was close to zero with 'much' overlap (Table 3), this is somewhat misleading because the overlap tended to induce increasing negative bias for $\gamma_{m,1,2}$ and positive bias for $\gamma_{m,2,1}$ as the number of individuals decreased, particularly for the finite mixture scenarios ('mixA' and 'mixB') and the continuous random effect scenarios with lower state persistence (Figure S4; Tables S2-S3). Despite the null and finite mixture models generally exhibiting little bias under continuous variation, it is worth noting that by construction these models are not able to correctly capture the individual-level state transition probabilities (as indicated by poor coverage and underestimation of uncertainty), and other measures of estimator performance (such as absolute bias or mean squared error) would perhaps better reflect this. With 'little' overlap, the null model tended to perform best with no heterogeneity and BW tended to perform best with 'moderate' to 'high' heterogeneity because TMB tended to underestimate uncertainty (except when M = 100). Consistent with its performance for σ estimation, BW did not perform as well as TMB under 'some' or 'much' overlap, often exhibiting larger variances and asymmetric biases for $\gamma_{m,1,2}$ and γ_{m21} (albeit with somewhat better coverage).

As expected, the mix2 model generally performed best in the 'mixA' and 'mixB' finite mixture scenarios, but coverage was increasingly below the nominal 95% as the number of individuals increased, the length of time series decreased and the degree of overlap increased. Underestimation of uncertainty by the mix2 model was unexpected under these scenarios, but the finite mixture models did not appear to always be able to adequately distinguish individuallevel variability from sampling variability when estimating mixture probabilities for individuals with shorter time series. However, the mix2 model was less prone to reduced coverage for shorter time

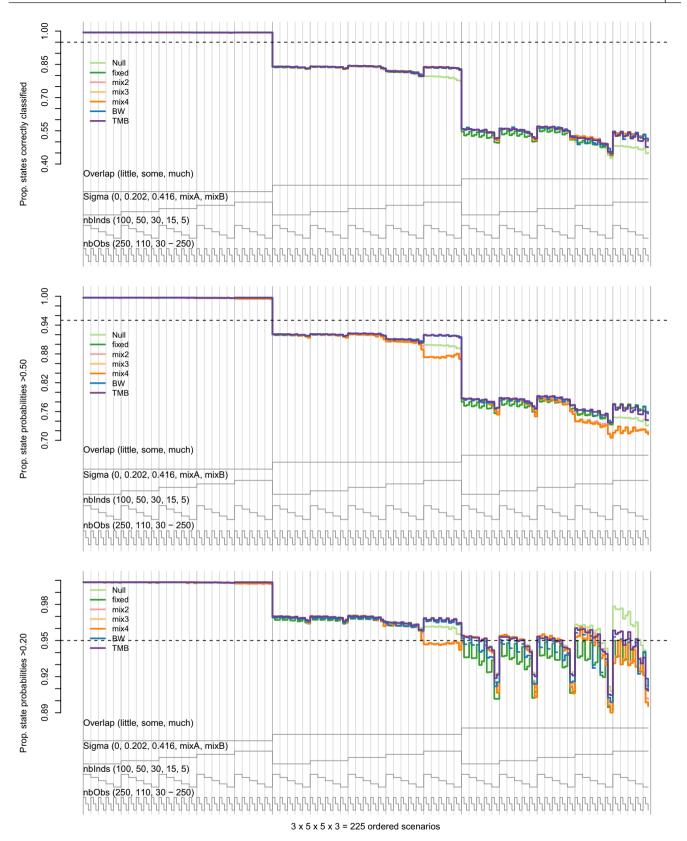


FIGURE 2 Nested loop plots for the proportion of Viterbi-decoded states that were correctly classified after accounting for chance agreement (top) and the proportion of estimated state probabilities in which the true state received at least 0.50 (middle) or 0.20 (bottom) probability from 225 simulated scenarios without covariate effects. Scenarios are ordered from outer to inner loops by the degree of state-dependent distribution overlap ('Overlap'), individual heterogeneity ('Sigma'), number of individuals ('nblnds') and length of time series ('nbObs'). Comparisons are for the null (light green), fixed (dark green), mix2 (pink), mix3 (light orange), mix4 (dark orange), BW (blue) and TMB (purple) models. Continuous random effect scenarios are limited to those with 'higher' state persistence

ModelParm.Percent relative biasBW $\sigma_{1,2}$ BW $\sigma_{2,1}$ TMB $\sigma_{2,1}$ TMB $\sigma_{2,1}$ BWBW	Little	Overlap		State persistence	sistence	a		No. indiv	No. individuals (M)				Time-ser	Time-series length (T_m)	T_m)	
Percent relative bias BW $\sigma_{1,2}$ BW $\sigma_{2,1}$ TMB $\sigma_{1,2}$ TMB $\sigma_{2,1}$ Coverage		Some	Much	Higher	Lower	0.202	0.416	100	50	30	15	5	250	110	30-250	Overall
	-6.6	-13.4	-46.3	-16.8	-22.9	-21.9	-17.6	-16.4	-18.9	-21.1	-22.4	-19.6	-15.9	-23.7	-19.9	-19.8
	-6.6	-20.4	-22.6	-11.6	-20.5	-17.1	-14.8	-13.4	-15.0	-16.3	-18.5	-16.1	-9.8	-18.0	-21.3	-15.9
	-12.4	-14.6	-22.8	-16.9	-16.3	-19.6	-13.6	-6.7	-9.6	-12.8	-18.5	-35.4	-12.8	-17.7	-19.3	-16.6
	-12.1	-15.3	-21.5	-16.8	-15.8	-19.5	-13.2	-6.1	-8.9	-12.3	-18.6	-35.7	-12.9	-17.1	-19.0	-16.3
	0.96	0.96	0.89	0.95	0.93	0.94	0.94	0.91	0.93	0.94	0.95	0.97	0.93	0.94	0.96	0.94
BW $\sigma_{2,1}$	0.96	0.94	0.96	0.95	0.95	0.95	0.95	0.93	0.95	0.95	0.96	0.96	0.95	0.95	0.95	0.95
TMB $\sigma_{1,2}$	0.96	0.95	0.95	0.97	0.94	0.94	0.96	0.96	0.96	0.96	0.95	0.92	0.97	0.94	0.95	0.95
TMB σ _{2,1}	0.96	0.95	0.94	0.97	0.94	0.94	0.96	0.96	0.96	0.96	0.95	0.92	0.97	0.94	0.95	0.95
Percent confidence interval length	terval lengt	ų														
BW $\sigma_{1,2}$	408	495	710	545	495	1, 349	386	203	276	347	507	1,164	409	544	635	521
BW $\sigma_{2,1}$	408	477	815	564	519	1,409	400	213	294	368	530	1,197	428	584	638	542
TMB $\sigma_{1,2}$	400	534	897	646	574	1,740	376	277	417	526	733	1,098	447	710	673	610
TMB $\sigma_{2,1}$	402	523	983	679	592	1799	398	289	438	542	761	1,149	470	730	707	636

TABLE 2 BW and TMB overall mean percent relative bias, 95% confidence interval coverage and percent confidence interval length for $\sigma_{1,2}$ and $\sigma_{2,1}$ by design points for state-dependent distribution overlap, state persistence, individual heterogeneity (σ), number of individuals and time-series length in simulations without covariates

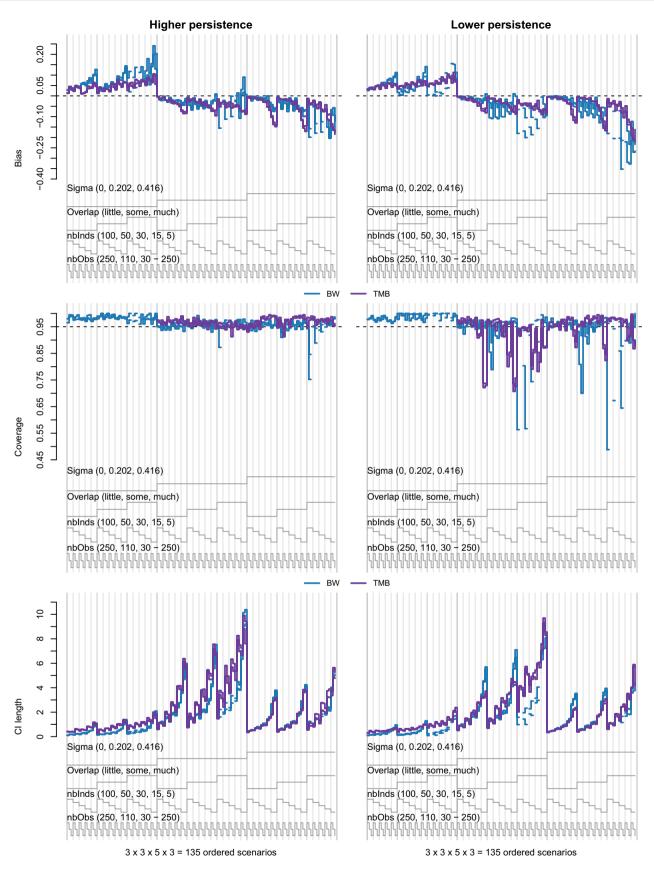


FIGURE 3 Nested loop plots for BW (blue) and TMB (purple) mean bias (top), 95% confidence interval coverage (middle) and confidence interval length (bottom) for $\sigma_{1,2}$ and $\sigma_{2,1}$ from 135 simulated scenarios without covariates that included 'higher' (left column) or 'lower' (right column) state persistence. Missing values for BW indicate scenarios with <50 datasets producing admissible estimates for the state transition probabilities from the fixed effects model. Coverage for TMB was 0% for all scenarios with $\sigma_{1,2} = \sigma_{2,1} = 0$

						,													
				Random effects	effects														
				Continuous	sno				Discrete										
	Overlap			State pe	State persistence	ø					No. indiv.	No. individuals (M)				Time-series length (T_m)	es length	(T_m)	
Model	Little	Some	Much	Higher	Lower	0	0.202	0.416	mixA	mixB	100	50	30	15	5	250	110	30- 250	Overall
Bias																			
null	-0.01	-0.01	-0.01	-0.01	0.00	00.0	0.00	-0.01	-0.05	0.01	-0.01	-0.01	-0.01	-0.01	-0.01	-0.01	-0.01	-0.01	-0.01
fixed	0.01	0.01	0.03	0.02	0.01	0.02	0.02	0.02	0.02	0.01	0.01	0.01	0.01	0.02	0.01	0.01	0.01	0.02	0.01
mix2	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
modMix	0.00	0.00	0.00	0.00	0.00	00.0	0.00	0.00	0.00	0.00	00.0	0.00	00.00	0.00	0.00	0.00	0.00	0.00	0.00
modFix	0.00	0.00	0.00	0.00	0.00	00.0	0.00	0.00	0.00	0.00	0.00	0.00	00.00	0.00	0.01	0.00	0.00	0.00	0.00
BW	0.00	0.00	-0.02	0.01	-0.02	00.0	0.00	0.00	0.00	-0.01	00.0	0.00	00.00	-0.01	0.00	0.00	-0.01	0.00	0.00
modBW	0.00	0.00	0.00	0.01	-0.01	00.0	0.00	0.00	0.00	0.00	00.0	0.00	00.00	0.00	0.00	0.00	0.00	0.00	0.00
TMB	0.00	0.00	0.00	0.00	0.00	00.0	0.00	0.00	-0.01	0.01	00.0	0.00	00.00	0.00	0.00	0.00	0.00	0.00	0.00
modTMB	0.00	0.00	0.00	0.00	0.00	00.0	0.00	0.00	0.00	0.00	00.0	0.00	00.0	0.00	0.00	0.00	0.00	0.00	0.00
Coverage																			
null	0.40	0.50	0.62	0.61	0.64	0.94	0.57	0.37	0.19	0.11	0.38	0.43	0.48	0.55	0.69	0.46	0.53	0.53	0.51
fixed	0.95	0.95	0.92	0.95	0.94	0.94	0.94	0.94	0.94	0.94	0.95	0.95	0.95	0.94	0.93	0.95	0.94	0.94	0.94
mix2	0.70	0.76	0.80	0.69	0.72	0.93	0.66	0.52	0.91	0.91	0.67	0.72	0.75	0.79	0.84	0.73	0.78	0.76	0.75
modMix	0.76	0.80	0.82	0.74	0.77	0.95	0.68	0.63	0.92	0.91	0.73	0.77	0.79	0.82	0.86	0.79	0.81	0.79	0.79
modFix	0.86	0.85	0.84	0.81	0.84	0.95	0.72	0.81	0.93	0.93	0.78	0.82	0.85	0.88	0.92	0.88	0.85	0.83	0.85
BW	0.96	0.95	0.93	0.96	0.94	0.98	0.94	0.94	0.94	0.94	0.96	0.96	0.95	0.95	0.94	0.95	0.95	0.95	0.95
modBW	0.96	0.95	0.92	0.95	0.94	0.98	0.91	0.93	0.95	0.95	0.93	0.95	0.95	0.95	0.94	0.95	0.94	0.95	0.94
TMB	0.93	0.93	0.90	0.92	0.92	0.96	0.89	0.91	0.92	0.90	0.93	0.93	0.92	0.91	0.89	0.93	0.91	0.91	0.92
modTMB	0.90	0.90	0.87	0.88	0.89	0.95	0.83	0.87	0.92	0.92	0.90	0.90	0.89	0.89	0.89	0.91	0.89	0.87	0.89
SE																			
null	0.01	0.03	0.05	0.02	0.03	0.03	0.03	0.03	0.03	0.04	0.01	0.02	0.02	0.03	0.06	0.02	0.03	0.03	0.03
fixed	0.06	0.08	0.13	0.08	0.10	0.09	0.09	0.09	0.10	0.09	0.09	0.09	0.09	0.09	0.09	0.07	0.10	0.11	0.09
mix2	0.02	0.03	0.05	0.03	0.04	0.03	0.03	0.04	0.03	0.03	0.02	0.02	0.03	0.04	0.06	0.03	0.04	0.04	0.03
modMix	0.02	0.03	0.05	0.03	0.04	0.03	0.03	0.04	0.04	0.04	0.02	0.02	0.03	0.04	0.06	0.03	0.04	0.04	0.03
modFix	0.03	0.04	0.06	0.03	0.05	0.03	0.04	0.06	0.05	0.04	0.02	0.03	0.04	0.05	0.08	0.04	0.05	0.05	0.04
BW	0.05	0.07	0.12	0.07	0.09	0.07	0.07	0.08	0.08	0.08	0.07	0.07	0.07	0.08	0.09	0.06	0.08	0.09	0.08
																		Q	(Continues)

Overall 0.06 0.06 0.04 0.06 0.07 0.05 30-250 Time-series length (T_m) 0.06 0.06 0.05 110 0.04 0.04 0.03 250 0.08 0.07 0.06 S 0.06 0.06 0.05 15 0.05 0.05 0.04 8 No. individuals (M) 0.04 0.05 0.03 20 0.04 0.05 0.03 100 mixB 0.05 0.08 0.04 Discrete mixA 0.06 0.08 0.04 0.416 0.06 0.06 0.07 0.202 0.06 0.05 0.04 0.05 0.03 0.03 0 ь Lower State persistence 0.07 0.06 0.05 Random effects Continuous Higher 0.05 0.04 0.03 Much 0.08 0.08 0.06 Some 0.05 0.06 0.04 Overlap Little 0.04 0.04 0.03 modTMB modBW TMB Model

series under the more distinct 'mixB' scenario with 'little' or 'some' overlap, so this behaviour also appears to depend on the specific characteristics of the mixture distributions. All models except the null generally performed well with data generated under K = 2 finite mixtures (albeit with mean standard errors 3.2, 3.5 and 3.7 times larger than mix2 for the TMB, BW and fixed models, respectively), but the finite mixture models did not generally perform well with data generated under continuous random effects. Under these scenarios, the discrete random effect models tended to perform slightly better in terms of coverage as the number of mixtures increased, but coverage was still well below nominal (as low as 32% with K = 4) and tended to decrease as sample sizes *increased* (Table 3; Figure 4).

State-dependent distributions

There was not much variability in the performance of the models when estimating state-dependent probability distribution parameters $(\mu_1^{y}, \mu_2^{y}, \sigma_1^{y}, \sigma_2^{y})$. With 'little' overlap, all models performed well (see Figures S7-S12; Tables S4-S7). With smaller sample sizes under 'some' or 'much' overlap, bias tended to increase and coverage tended to decrease. Under these scenarios, increasing overlap generally resulted in positive bias for μ_1^{γ} , large positive bias for μ_2^{γ} , positive bias for σ_1^{γ} and negative bias for σ_2^{γ} , particularly for the continuous random effect scenarios with lower state persistence (Figures S8, S9, S11 and S12). Although coverage remained near nominal under these scenarios, none of the models were able to recover unbiased point estimates for all of the state-dependent distribution parameters. Thus, model performance was primarily driven by the degree of overlap, and the inclusion of individual fixed, discrete random or continuous random effects generally made little difference in statedependent distribution parameter estimation.

Model selection and multi-model inference

When the candidate model set was limited to null and finite mixture models ('modMix'), AIC, model selection performed well for data generated under no heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0$) and the finite mixture scenarios, with the generating model (null and mix2, respectively) generally receiving the most AIC, support (Figures S13-S14) and the modMix model-averaged parameter estimates performing well (Figures S5-S10; Table 3; Tables S2-S7). However, with moderate to high individual heterogeneity ($\sigma_{1,2} = \sigma_{2,1} > 0$), AIC_c tended to favour models with increasingly more finite mixtures as individual heterogeneity and sample sizes increased, with poor coverage of model-averaged Γ_m estimates. When the candidate set of models was expanded to include the fixed model ('modFix'), performance was similar for the no heterogeneity and finite mixture scenarios, but the fixed model tended to receive greater support as individual heterogeneity increased, sample sizes increased and the degree of overlap decreased (Figures S13 and S14), resulting in improved (but still less than nominal) performance of the modFix model-averaged Γ_m estimates (Figures S5 and S6; Table 3; Tables S2 and S3).

For the full candidate model set including the null, fixed, finite mixture and BW models ('modBW'), AIC_c model selection generally performed well across most simulation scenarios, but support for

TABLE 3 (Continued)

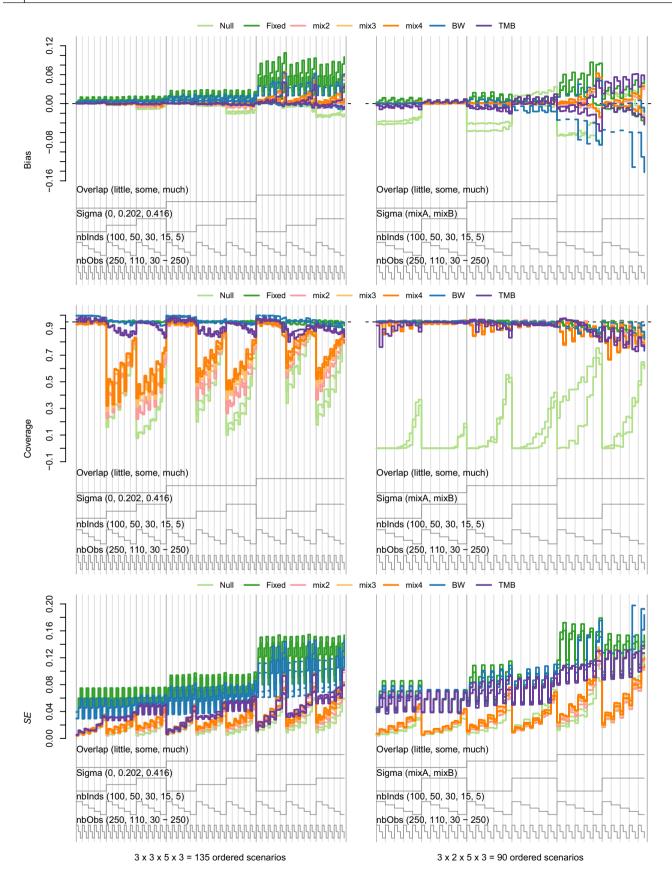


FIGURE 4 Nested loop plots for mean bias (top row), 95% confidence interval coverage (middle row) and standard error (*SE*; bottom row) for $\gamma_{m,2,2}$ and $\gamma_{m,2,1}$ from simulated scenarios without covariates, including 135 scenarios with 'higher' state persistence (left column) and 90 scenarios with 'mixA' or 'mixB' finite mixtures (right column). Missing values for BW indicate scenarios with <50 datasets producing admissible estimates

the generating model tended to decline with smaller sample sizes and higher degrees of overlap (Figures S13 and S14). In terms of Γ_m estimation, modBW generally exhibited less bias and greater precision than BW, but performance relative to TMB declined with moderate or high heterogeneity as sample sizes increased, the degree of overlap increased and state persistence decreased (Figure 4; Figures S5 and S6; Table 3; Tables S2 and S3). However, under these scenarios, modBW tended to perform better than BW, indicating that AIC_c model averaging can help mitigate poorer performance of BW in scenarios with 'some' or 'much' overlap that tend to produce inadmissible Γ_m estimates from the fixed model.

For the 'modTMB' candidate set, the marginal AIC_c performed better than I expected, but proved to be conservative when selecting among fixed and random effect models for scenarios with moderate or high individual heterogeneity (Figures S15 and S16). Under these scenarios, AIC_c tended to favor the null model as individual heterogeneity decreased, the degree of overlap increased and sample sizes decreased. Unlike modBW, modTMB generally reduced coverage of Γ_m estimates relative to TMB (Figure 4; Figures S5 and S6; Table 3; Tables S2 and S3). Likelihood ratio tests between the null and TMB models were less conservative and not as sensitive to the degree of overlap and sample sizes under these scenarios (Figures S15 and S16). However, LRTs do not provide a means for selecting between discrete and continuous random effect models, and LRTs tended to strongly favour TMB over the null model when data were generated from finite mixtures (scenarios 'mixA' and 'mixB').

3.2.3 | With covariates

For the set of simulations examining measurable individual covariate effects, performance patterns were similar to the set of simulations without covariate effects (see Section 3.2.2) for the null, fixed, finite mixture and continuous random effect models in terms of state assignment, parameter estimation and AIC_c model selection (see Table S8; Figures S17–S25). Both BW and TMB performed well in estimating the covariate effects (Figure 5), although for ($\mu_{1,1,2}, \mu_{1,2,1}$) = (0.5, -0.5) with smaller sample sizes and moderate to high heterogeneity, BW exhibited a small negative bias for $\mu_{1,1,2}$ and a small positive for $\mu_{1,2,1}$ that was mitigated by AIC_c model averaging, but became worse as state-dependent distribution overlap increased (Figures S26 and S27; Tables S9 and S10).

While the finite mixture models performed better than the null model in terms of coverage of $\mu_{1,i,j}$, they generally exhibited greater bias and performance became increasingly poor as individual heterogeneity increased. Coverage of $\mu_{1,i,j}$ for the discrete random effect models increased with the number of mixtures, but it was still well below nominal with K = 4 mixtures under higher levels of heterogeneity and 'little' overlap (Figure 5). Coverage for the discrete random effect models actually tended to become worse as sample sizes *increased* and overlap *decreased* (Figure S26; Tables S9 and S10). Under the 'best' data-generating scenarios with 'little' overlap, M = 100, $T_m = 250$, finite mixture models in some cases reduced coverage of

 $\mu_{1,ij}$ by >37% relative to the TMB model. In a handful of small sample scenarios with σ_{ij} > 0 where finite mixture models had near-nominal coverage, this was attributable to large standard errors (up to 101% larger than the TMB model). Because coverage of the finite mixture models was often poor when $\mu_{1,ij} = 0$, there was clearly a greater risk of Type I error (i.e. inferring a covariate effect when there is none) when discrete random effects were used to account for continuous individual variation. With AIC_c for the modMix candidate set tending to support models with both covariate effects and a large number of mixtures (Figure S25), model averaging did little to mitigate this risk under these scenarios (Figure S27; Tables S9 and S10).

4 | EXAMPLE: LONG-FINNED PILOT WHALES

To help put my findings in context and illustrate some potential challenges that practitioners may encounter when applying mixed HMMs to animal telemetry data, I revisit a N = 4 state multivariate mixed HMM analysis of long-finned pilot whale biotelemetry data originally performed by Isojunno et al. (2017). Full details can be found therein, but the data consist of 11 data streams believed to characterize 'exploratory' (state 1), 'foraging' (state 2), 'crowded' (state 3) and 'directed' (state 4) diving behaviours for M = 15 individuals, with T_m ranging from 50–254 (median = 148). To limit the number of models in the candidate set, Isojunno et al. (2017) first used model selection criteria to determine N = 4 was the optimal number of states under the null (K = 1) model, then used model selection criteria to choose among finite mixture random effect models (up to K = 3) and finally used this model to investigate individual and timedependent explanatory covariates (e.g. size class, sonar exposure) for the state transition probabilities.

I focus on the second stage of this analysis, where they used AIC and the Bayesian Information Criterion (BIC; e.g. Burnham & Anderson, 2002) to select the best-supported random effect model for subsequent covariate modelling and model selection. They found conflicting results based on AIC and BIC, with AIC favouring K = 3 mixtures (5.2 unit decrease in AIC relative to the null model) and BIC strongly favouring the null model with K = 1. Faced with this apparent conundrum, Isojunno et al. (2017) sided with BIC to 'avoid selection of overly complex models' given the relatively 'weak support for any random effects' afforded by AIC, and proceeded with covariate model fitting and selection under the null model (K = 1) with no individual random effects on state transition probabilities.

To explore this further, I re-analysed the pilot whale data by fitting the null, fixed, finite mixture (up to K = 4), and TMB models using the same methods described in Section 3, but with δ_m assumed to be the stationary distribution (as in Isojunno et al., 2017) instead of freely estimated (for data and R code, see McClintock, 2021). In addition to AIC_c, I calculated standard BIC for the null, fixed and finite mixture models, as well as the marginal BIC for TMB, using $n = \sum_{m=1}^{M} T_m = 2,314$ for the sample size (as in Isojunno et al., 2017). Unfortunately, the fixed model yielded Γ_m estimates on

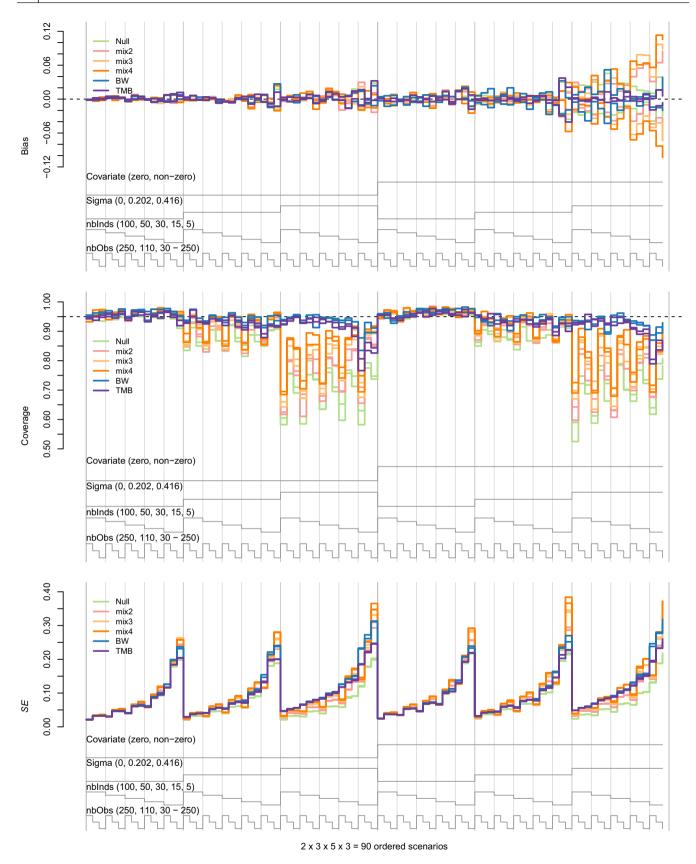


FIGURE 5 Nested loop plots for median bias (top row), mean 95% confidence interval coverage (middle row) and median standard error (SE; bottom row) for covariate effects $\mu_{1,1,2}$ and $\mu_{1,2,1}$ from 90 simulated scenarios with 'little' overlap, 'higher' state persistence, and $(\mu_{1,1,2}, \mu_{1,2,1}) \in \{(0, 0), (0.5, -0.5)\}$. Scenarios are ordered from outer to inner loops by the data-generating values for the covariate effect ('Covariate', where 'zero' = (0, 0), 'non-zero' = (0.5, -0.5)), individual heterogeneity ('Sigma'), number of individuals ('nblnds') and length of time series ('nbObs')

the boundary, thereby making this dataset inadmissible for the BW model. With boundary issues becoming more likely as the number of individuals increases, the lengths of time series decrease and the number of states increases, this highlights a key limitation of the BW approach in practice.

Despite due diligence by Isojunno et al. (2017) in exploring the likelihood surface using 50 sets of randomly drawn starting values for optimization, I found that their finite mixture models failed to converge to global maxima. Relative to those reported by Isojunno et al. (2017), my fits increased the log likelihood for the mix2 and mix3 models by 14.6 and 36.7 units, respectively (Table 4). This high-lights a common pitfall when attempting to fit complex mixed HMMs to relatively small datasets, where flat likelihood surfaces, local minima and numerical instability can become increasingly problematic as the number of states and/or parameters increase. Indeed, it is certainly possible that my fits also failed to converge to the global maxima, although I was unable to improve them any further using hundreds of random normal perturbations of the maximum likelihood estimates as starting values for the optimization.

Both AIC_c and BIC now favor TMB (Table 4), and the LRT between the null and TMB model with N(N - 1) = 12 random effects

also favors TMB
$$(\sum_{r=0}^{12} 2^{-12} {12 \choose r} \chi_r^2 = 101.4, p < 0.001)$$
. Thus,

whether one prefers AIC_c , BIC or LRT, there is clearly evidence of individual variation in the state transition probabilities that is not well explained by null or finite mixture models. As could be expected for relatively short time series with N = 4 states, some of the random effect variance estimates were imprecise (Table 5), particularly for state transitions that were relatively rare (Figure 6). Evidence of individual variation was greatest for transitions from the 'exploratory' and 'directed' states, and, based on the results of Isojunno et al. (2017), this variation was not well explained by any of the individual covariates included in their analysis. However, it is possible that these explanatory covariates could now better account for any additional variation that is not already well explained by the individual random effects.

Although I have found new evidence of individual variation in the state transition probabilities, accounting for this heterogeneity made little impact on state assignment and estimated activity budgets. Consistent with my simulation results (see Figure 2), Viterbidecoded states for the null and TMB models were in agreement 94% of the time. However, while 'foraging' and 'crowded' state assignments were largely unchanged, estimated overall activity budgets changed slightly for the 'exploratory' state (36% for null, 33% for TMB) and the 'directed' state (36% for null, 40% for TMB).

I do not intend to be critical of Isojunno et al. (2017) for limiting their candidate model set to finite mixtures or failing to achieve convergence for these complex models. They focused on discrete random effect models presumably because maximum likelihood inference for HMMs with continuous random effects has historically been very difficult (e.g. Altman, 2007; Langrock et al., 2012; Schliehe-Diecks et al., 2012). Discrete random effects have been promoted as a practical alternative for movement HMMs (e.g. DeRuiter et al., 2017; McKellar et al., 2015; Towner et al., 2016), and the potential for TMB (Kristensen et al., 2016) as a tool to overcome such problems has only recently begun to be recognized by movement ecologists (e.g. Auger-Méthé et al., 2017). False convergence to a local maximum is notoriously difficult to assess, and it was entirely due to luck that my random draws of starting values for the finite mixture models happened to converge to parameter estimates with higher likelihood. Finally, as state assignment and calculating activity budgets were the primary purposes of the mixed HMM analysis performed by Isojunno et al. (2017), their main results and conclusions would likely be largely unaltered if they were instead based on a model that accounted for this individual variation. However, this would not be the case had their primary objective been to quantify individual heterogeneity in state transition probabilities.

If the primary objective of this analysis had been to gain an understanding of heterogeneity in individual movement behaviour, it is not clear how one would proceed with such a complex random effects model. Interpreting generic individual variation is already difficult in simpler finite mixture models (e.g. DeRuiter et al., 2017; Towner et al., 2016), and it would be challenging to concoct a biological story explaining these various pieces of evidence for individual heterogeneity across N(N - 1) = 12 continuous random effects (Table 5) and $MN^2 = 240$ state transition probabilities (Figure 6). The random effects could reflect unexplained population-level behavioural heterogeneity attributable to different animal personalities (e.g. Hertel et al., 2020; Réale et al., 2007), but they could also simply be an artefact of deployments of differing lengths being observed in different environmental and behavioural contexts (e.g. DeRuiter et al., 2017;

TABLE 4 Model selection results for the long-finned pilot whale example. Results include AIC_c weights, ΔAIC_c , BIC weights, ΔBIC , negative log-likelihood value (NLL) and number of parameters (nPar)

Model	AIC _c weight	∆AIC _c	BIC weight	ΔΒΙϹ	NLL	nPar
ТМВ	0.65	0.00	0.99	0.00	18,459.69	84
mix3	0.35	1.27	0.00	79.37	18,445.14	98
mix4	0.00	15.75	0.00	166.03	18,438.12	111
mix2	0.00	45.37	0.00	50.96	18,481.29	85
null	0.00	75.71	0.01	8.47	18,510.40	72
fixed	0.00	86.78	0.00	933.87	18,322.38	240

Parameter	Estimate	SE	Lower	Upper	%CV	%CIL
$\sigma_{1,2}$	0.47	0.27	0.17	1.35	58	251
$\sigma_{1,3}$	1.17	0.69	0.40	3.39	59	256
$\sigma_{1,4}$	1.16	0.30	0.71	1.92	26	104
$\sigma_{2,1}$	0.56	0.41	0.15	2.03	74	336
$\sigma_{2,3}$	0.25	2.96	0.00	19.63	1,173	7,766
σ _{2,4}	0.03	0.34	0.00	2.26	1,195	7,895
$\sigma_{3,1}$	0.02	0.38	0.00	2.35	1926	11,773
$\sigma_{3,2}$	0.22	7.62	0.00	40.52	3,498	18,611
$\sigma_{3,4}$	0.91	0.39	0.41	2.04	43	179
$\sigma_{4,1}$	0.55	0.18	0.29	1.04	34	138
$\sigma_{4,2}$	1.14	0.40	0.58	2.24	36	146
$\sigma_{4,3}$	0.79	0.32	0.37	1.68	40	166

TABLE 5 Estimates, standard errors (*SE*), 95% confidence intervals (lower, upper), percent coefficient of variation (%CV) and percent confidence interval length (%CIL) for individual random effect variance parameters (*σ*) from the TMB model fitted to the long-finned pilot whale data

Towner et al., 2016). This is very difficult to determine, and I will not attempt to do so here. However, this highlights the challenge of interpreting random effects in biological terms.

5 | DISCUSSION

I have investigated the benefits of accounting for individual variation in the hidden state process of HMMs from a practical perspective, with emphasis on datasets common to animal movement behaviour biotelemetry studies. While my simulations covered a wide range of scenarios, they were by no means exhaustive. For example, I did not investigate pathological or degenerate cases with 'bathtub-shaped' distributions for the state transition probabilities and instead focused on less extreme forms of individual heterogeneity. While limiting $T_m \leq 250$ proved sufficient for demonstrating general patterns in model performance as a function of time series lengths, telemetry devices can of course produce much longer time series. For much larger datasets (e.g. $M \gg 100$ and $T_m \gg 250$), parameter estimates from the data-generating model can be expected to exhibit reduced bias and increased precision relative to the scenarios examined here. I did not examine sampling scenarios more typical of capture-recapture (Pradel, 2005) or species occurrence (Gimenez et al., 2014) HMMs, which often involve a larger number of individuals and shorter time series than the scenarios examined here. I also limited my study to maximum likelihood inference via direct numerical maximization of the likelihood, although I believe similar patterns would emerge using expectation-maximization (e.g. Altman, 2007) or Bayesian analysis methods (e.g. Turek et al., 2016).

I focused on individual-level random effects in the hidden state process because these have received the most attention in the movement modelling literature so far (e.g. DeRuiter et al., 2017; Isojunno et al., 2017; McKellar et al., 2015; Towner et al., 2016). Importantly, I have not examined individual effects on the statedependent observation distribution parameters and would not necessarily expect the same patterns to emerge from a similar investigation of individual variation in the observation process. While this also warrants further investigation, there is already some evidence for the importance of accounting for individual variation in the state-dependent distributions (e.g. Altman, 2007; Carter et al., 2020; Langrock et al., 2012; McClintock et al., 2013; Rueda et al., 2013; Schliehe-Diecks et al., 2012). In particular, I would expect unexplained individual variation in the observation process to be more consequential for state assignment.

HMMs tend to perform better as serial dependence in the data increases, particularly when state-dependent observation distributions overlap. Thus, there may be specific conditions (e.g. 'much' overlap with much stronger serial dependence) where discrete random effects may perform better as an approximation for continuous variation. However, the consequences of this model misspecification will be dependent on the form of heterogeneity, the degree of overlap, the amount of serial dependence and other qualities of the data. I showed that this approximation is not generally robust, and, in practice, it may be very difficult to determine whether it is reliable when truth is unknown.

The simulations and case study have highlighted some important considerations for practitioners contemplating the inclusion of individual random effects in their own analyses. As the results have provided much to digest, I break down these considerations under the following themes: (a) When to account for individual variation?; (b) How to account for individual variation?; (c) Is there evidence of individual variation? and (d) How to interpret individual variation?

5.1 | When to account for individual variation?

Accounting for generic individual variation comes at significant cost in terms of implementation and computation, particularly for random effects. When weighing the costs and benefits of random effects, three primary considerations are the study objectives, sample size and model complexity. If the objective is strictly state assignment, then the inclusion of individual effects on the hidden state process makes little difference in terms of inference. Many movement HMM

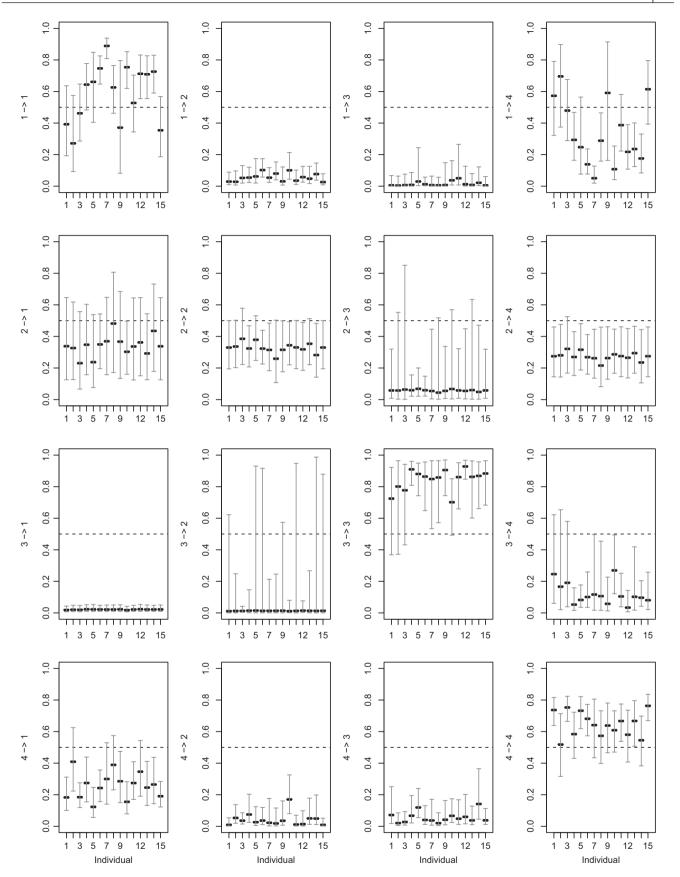


FIGURE 6 Estimated state transition probabilities (and 95% confidence intervals) among N = 4 states (1 = 'exploratory', 2 = 'foraging', 3 = 'crowded', 4 = 'directed') for M = 15 long-finned pilot whales from the TMB model including continuous individaul-level random effects. Each of the $4 \times 4 = 16$ state transition probabilities is labelled on the y-axis as ' $i \rightarrow j$ ', indicating the probability of switching from state *i* to state *j*

applications primarily focus on state assignment for inferences about behaviour, activity budgets and/or resource selection (e.g. Beyer et al., 2013; Pirotta et al., 2018; Roever et al., 2014), with little emphasis on quantifying or understanding heterogeneity in state transition probabilities. Under these circumstances, random effects in the hidden state process simply may not be worth the additional effort.

If inference about individual variation in state transition probabilities is a primary objective, then random effect models should certainly be explored. When properly specified and fitted, individual random effects never hurt and tend to decrease bias and increase coverage (relative to the null model) and increase precision (relative to the fixed effects model). Using random effects to account for unexplained individual variation can also improve our ability to reliably estimate the effects of measurable covariates on the hidden state process. However, it is important to consider that the feasibility and performance of a given mixed HMM will depend on model complexity and the amount of information contained in the data, as well as other factors that are typically out of the control of researchers, such as the degree of state-dependent distribution overlap (where less is generally better) and state persistence (where more is generally better). My results suggest that mixed HMMs generally do not perform that well (and can be challenging to fit) with relatively few individuals and short time series, and these issues will only be exacerbated when N > 2. As N increases, the likelihood of observing all state transitions for individuals with very short time series decreases, thereby potentially making the estimation less reliable. With smaller sample sizes typical of animal biotelemetry studies (e.g. M < 50 and $T_m < 250$), inferences about individual heterogeneity based on continuous random effects will tend to be weak. This is due to poor precision for the random effects variance parameters, which also tend to be underestimated with smaller sample sizes. When designing studies, researchers interested in applying continuous random effect models should consider allocating additional resources to maximize M (and, to a lesser degree, T_m).

5.2 | How to account for individual variation?

Continuous random effect models (BW and TMB) proved more robust to the underlying form of individual heterogeneity than null or discrete random effect models. The approximate approach of BW generally performed as well as (or better than) TMB when there was little overlap in the observation distributions, but the TMB model proved more robust to higher degrees of overlap. Thus, if custom coding a continuous random effects model using TMB is beyond the skill set of a practitioner, the BW approach can be a reliable alternative in limited cases with very distinct observation distributions. This often applies to animal movement HMMs describing very different modes of movement (e.g. 'foraging' and 'transit'), but the degree of overlap should be investigated (e.g. Beyer et al., 2013) before proceeding with the BW approach. As demonstrated in the long-finned pilot whale example, BW is also of limited utility due to boundary issues that are more likely to occur as the number of states increases, the number of individuals increases, the lengths of time series decrease and the degree of overlap increases. The TMB model does not suffer from these limitations, and I generally found the Laplace approximation as implemented in TMB to perform reasonably well across all HMM scenarios examined.

Discrete random effects are generally the best option only when individual heterogeneity is attributable to unmeasured categorical factors. While many categorical factors (e.g. sex, age class) can often be measured when deploying telemetry tags, others such as disease or breeding status often cannot. I do not advise using discrete random effects to account for continuous individual variation as this can underestimate uncertainty in state transition probabilities and lead to spurious inferences about covariate effects. If inference about individual variation in state transition probabilities is the primary objective, then investigating both discrete and continuous random effect models appears to be worth the effort for potential gains in terms of parameter estimation and state assignment. Yet, care must be taken when fitting these complicated models. As illustrated by the long-finned pilot whale example, false convergence of random effect models can be particularly problematic as the number of states increases and sample sizes decrease.

Individual covariates are arguably the best way to account for (and learn about) potential factors driving individual heterogeneity in the hidden state process. Relative to random effect models, covariate models are also much easier to implement using existing software (Table 6). When designing telemetry studies, careful thought should be put towards identifying and collecting any measurable individual covariates that may be informative. When available covariates do not sufficiently explain individual heterogeneity, then random effects are certainly worth pursuing as a more parsimonious alternative to individual fixed effects. Discrete random effects and the approximate continuous random effect approach of Burnham and White (2002) can be implemented using the R package momentuHMM (McClintock & Michelot, 2018). If the user is familiar enough with the C++ template to custom code HMMs from scratch, then TMB (Kristensen et al., 2016) can be used to implement any of the models. TMB will also often be faster than optimization routines that rely on numerical differentiation.

5.3 | Is there evidence of individual variation?

There are several ways to evaluate the strength of evidence for individual variation. These can include null hypothesis tests for the estimated coefficients of individual effects (for covariate, fixed or discrete random effect models) or random effect variance estimates (for continuous random effect models). Estimated coefficients or random effect variances that are significantly different from zero typically indicate evidence of individual variation. Model selection criteria such as AIC or BIC can also be used for selecting or averaging models from a candidate set. I found the conditional AIC to work well for selecting among null, fixed, finite mixture and BW models TABLE 6R packages for fitting HMMswith individual variation in the hiddenstate process using maximum likelihoodmethods

	Individual	Random effec	ts	
Package	covariates	Discrete	Continuous	Reference
moveHMM	1			Michelot et al. (2016)
msm	1			Jackson (2011)
depmixS4	1			Visser and Speekenbrink (2010)
momentuHMM	1	✓	\checkmark^{\dagger}	McClintock and Michelot (2018)
ТМВ	\checkmark	✓	1	Kristensen et al. (2016)

[†]Continuous random effects are limited to the approximate approach of Burnham and White (2002).

when sample sizes were larger and the observation distributions more distinct. The marginal AIC also worked reasonably well for selecting among the null, finite mixture and TMB models under these scenarios, but it was conservative relative to the null likelihood ratio test. If inference about individual variation in the hidden state process is the primary objective and the exact form of any unexplained heterogeneity is unknown, my results suggest that candidate model sets should include models with both discrete and continuous random effects. This was evident in the long-finned pilot whale example, where I found stronger evidence for continuous random effects than for finite mixture models.

5.4 | How to interpret individual variation?

Interpretation of measured individual covariate effects is straightforward, but it can be difficult to interpret generic individual-level effects. Discrete random effect models are sensitive to small sample sizes and can tend to identify spurious 'behavioural contexts' that are an artefact of shorter time series (e.g. DeRuiter et al., 2017; Towner et al., 2016). In my simulation study, I also found individual fixed effect models to be susceptible to these small sample issues. Care should therefore be taken to avoid overinterpretation of individual fixed effects or finite mixture distributions. Continuous random effect models will tend to be less susceptible to small sample issues because they will shrink effect sizes for individuals with shorter time series towards the population mean. However, as demonstrated in the long-finned pilot whale example, this makes continuous random effects no less difficult to interpret in biological terms. Generic individual random effects only indicate evidence of individual variation in the hidden state process, but from evolutionary theory we already understand that biological parameters must in reality vary across individuals. Perhaps the most useful inference from evidence of generic individual heterogeneity is that there remains a need to identify and collect more informative covariates that can help explain the drivers of the underlying variation in the hidden state process.

ACKNOWLEDGEMENTS

P. Conn, S. DeRuiter, S. Isojunno, D. Johnson, R. Langrock and T. Michelot for helpful discussions. The findings and conclusions in the manuscript are those of the author(s) and do not necessarily represent the views of the National Marine Fisheries Service, NOAA. Any use of trade, product or firm names does not imply an endorsement by the US Government.

PEER REVIEW

The peer review history for this article is available at https://publons. com/publon/10.1111/2041-210X.13619.

DATA AVAILABILITY STATEMENT

Supporting data and code for simulation and the pilot whale example are available on GitHub, versioned and archived on Zenodo https://doi.org/10.5281/zenodo.4606789 (McClintock, 2021).

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SUPPORTING INFORMATION

Additional supporting information may be found online in the Supporting Information section.

How to cite this article: McClintock BT. Worth the effort? A practical examination of random effects in hidden Markov models for animal telemetry data. *Methods Ecol Evol.* 2021;00:1–23. https://doi.org/10.1111/2041-210X.13619