Optimum lionfish yield: A non-traditional management concept for invasive lionfish (*Pterois* spp.) fisheries

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38 Abstract: This paper describes a non-traditional fisheries management concept and an indicator-39 based framework to encourage and guide management of invasive lionfish (Pterois spp.) 40 fisheries in the temperate and tropical western Atlantic. We introduce the concept of optimum 41 lionfish yield (OLY) – an extension of the concept of ecologically sustainable yield – which 42 considers local ecological health in the establishment of fishery management targets. In contrast 43 to traditional fishery targets, OLY is a target exceeding maximum sustainable yield (MSY) that 44 still provides relatively high sustainable yield, but further contributes to population suppression beyond what is achievable through targets at or below MSY. Thus, OLY seeks to balance 45 46 management trade-offs from both natural resource and invasive species management 47 perspectives. In this study, we developed an age-structured population model and applied the 48 concept of OLY to quantify targets to initiate management of a nationally-managed lionfish 49 fishery in Belize. Socioeconomic and ecological data were used as indicators to formulate OLY values. The model indicates that lionfish in Belize are biologically robust to fishing pressure, 50 51 which corroborates previous findings. Fishing lionfish at rates above MSY levels is expected to 52 substantially reduce population abundance, much more so than fishing at rates below MSY 53 levels, while having relatively minimal impacts on yield. Population suppression can be further 54 enhanced by reducing size at selection, but this is expected to be done at a significant cost to 55 landings. Together, these data support continued establishment of (managed) commercial 56 lionfish fisheries throughout the invaded range to (1) provide an alternative sustainable fishery resource and (2) serve as a means of national- and international-level control. While the concept 57 and framework described here is introduced for management of invasive lionfish, it could be 58 59 applied to management of other invasive species, both aquatic and terrestrial.

61 **1. Introduction**

Numerous studies indicate invasive lionfish (Pterois spp.) negatively affect reef 62 63 communities in the temperate and tropical western Atlantic through predation on, and 64 competition with, native species (Albins and Hixon 2008, Green et al. 2012, Albins 2015, 65 Ballew et al. 2016, Chagaris et al. 2017). To regulate population densities and mitigate 66 ecological impacts, researchers and coastal managers have established lionfish control and 67 management programs that focus on direct removals (e.g., Johnston et al. 2015). These 68 programs, as well as community-based efforts such as recreational fishing tournaments, have 69 been successful at reducing lionfish densities and minimizing impacts on local reefs (Frazer et al. 70 2012, Dahl et al. 2016, Green et al. 2017). Lionfish are, however, established in most marine 71 habitats from North Carolina, USA to Brazil, and densities can exceed 300 fish/hectare (Côté et 72 al. 2013). Consequently, wide-scale eradication no longer seems plausible without major 73 technological advances for capture and a significant increase in the scale and magnitude of 74 removal efforts.

75 To increase the scale and magnitude of removal efforts, researchers and managers have 76 been promoting commercialization of lionfish over the last decade, particularly as seafood. Not 77 only are lionfish plentiful, they are safe to consume and a nutritious source of protein (Tremain 78 and O'Donnell 2014, Hardison et al. 2018Morris et al. 2011a). Lionfish are now being harvested 79 recreationally and commercially throughout much of the invaded region, but are not being 80 managed as a fishery resource. Similar to other natural resource markets, as demand increases so 81 too does the number of people who exploit the resource and, therefore, the number of individuals 82 who may become (more) reliant on the resource. For this reason, lionfish fisheries would benefit 83 from science-based management (Merrick 2018). Through proper management, invasive lionfish

could serve as an alternative fishery resource, which could help create more diversified markets
and potentially reduce fishing pressure on traditional native fishery species. Lionfish fisheries
could also indirectly improve stocks of fishery species impacted by lionfish.

87 The objective of traditional fisheries management is to maintain high sustainable yield 88 without causing overfishing. This is often accomplished by setting management targets at or 89 below a population's maximum sustainable yield (MSY) (Larkin 1977, Mace 2001) (Figure 1). 90 Maximum sustainable yield is defined as the maximum yield (or, harvest) that a population can 91 sustain without having adverse effects on its ability to replenish itself. In United States fisheries 92 management, for example, MSY and its associated fishing rate F_{MSY}, are typically treated as 93 upper limits with target levels set somewhat lower (Prager and Shertzer 2010). There exists, 94 however, a paradox with the management of invasive lionfish fisheries. From a natural resource 95 management perspective, lionfish fisheries should be managed to maintain high sustainable yield at levels that meet socioeconomic demand; however, from an invasive species management 96 perspective, the fishery should also be managed to suppress populations to levels that mitigate 97 98 ecological impacts. In the context of traditional fisheries management, these two objectives are 99 not sought in tandem.

This paper describes a non-traditional fisheries management concept and an indicatorbased framework to encourage and guide management of invasive lionfish fisheries throughout the western Atlantic. We propose the concept of optimum lionfish yield (OLY), which seeks to balance the competing objectives of high sustainable yield and population suppression, and describe one potential approach for formulating OLY values using the lionfish fishery in Belize as a case study. In contrast to traditional fisheries management targets, OLY is a target exceeding MSY that still provides relatively high sustainable yield, but further contributes to population

107 suppression beyond what is achievable through targets at or below MSY (Figure 1). Thus, OLY 108 balances management trade-offs from both natural resource and invasive species management 109 perspectives. Optimum lionfish yield is an extension of the concept of ecologically sustainable 110 yield (ESY) – a target yield that a community or ecosystem can sustain without shifting to an 111 undesirable ecological state (Zabel et al. 2003). While OLY targets lie above MSY and ESY 112 targets lie below MSY, both concepts suggest that traditional fishery management practices that 113 set single-species targets based solely on MSY can be insufficient. OLY and ESY suggest that 114 managers establish fishery targets that also consider overall ecological health. 115 Since 2011, the Belize Fisheries Department and its partners have worked to establish a 116 nationally managed lionfish fishery as a means of national-level control and to diversify local 117 markets (Chapman et al. 2019, Searle et al. 2012). Commercial lionfish markets have been 118 developed (e.g., as seafood and for jewelry) and the number of fishers targeting lionfish has 119 grown, but management of the fishery has not yet begun (Chapman et al. 2019). One of the 120 essential steps in establishing a well-managed fishery is understanding the population's response 121 to fishing pressure, which is typically achieved through application of population and stock 122 assessment models. Thus, we developed an age-structured population model and applied the 123 concept of OLY to quantify benchmark targets to initiate management of the lionfish fishery in 124 Belize. Available socioeconomic and ecological data for lionfish in Belize were used as indictors 125 to quantify and then validate that the proposed values of OLY satisfied the two general 126 objectives of lionfish fishery management – high sustainable yield that meets socioeconomic 127 demand and population suppression that mitigates ecological impacts. Data from the fishery are 128 not currently available to model temporal dynamics of the population, but do exist to examine 129 equilibrium behavior in response to fishing pressure and size at selection – two variables that

fishery managers can regulate. Although no real population is ever in true equilibrium, reference points derived under this assumption are useful as long-term targets even if met with nonequilibrium dynamics in practice (Goodyear 1993, Mace 2001). Model results are discussed within the context of tradeoffs between sustainable yield and population suppression.

134 **2. Methods**

135 2.1 General overview of approach

136 An age-structured population model was developed to quantify benchmark management targets, including values of OLY and its associated fishing rate FoLY, to initiate management of a 137 138 nationally-managed lionfish fishery in Belize. The model was used to evaluate trade-offs between equilibrium landings and abundance of lionfish in response to fishing pressure and size 139 at selection. Available socioeconomic and ecological data for lionfish in Belize were used as 140 141 indictors to quantify and then validate that the proposed values of OLY satisfied the two general 142 objectives of lionfish fishery management. Functional forms and parameter values used in the 143 population model were derived from Belize survey data when possible, but also drew on 144 published data from nearby Little Cayman Island (Edwards et al. 2014, Gardner et al. 2015). 145 Like Belize, lionfish were first observed at Little Cayman Island in 2008, and were considered 146 established in 2009 (Schofield 2010). Data used for parameter values in this study were obtained 147 through various surveys conducted in both locations in the period between 2011 and 2015. Age-148 specific parameter values are summarized in Table 1. The overall approach described here serves 149 as a model framework for formulating lionfish fishery management targets throughout the 150 western Atlantic.

151 2.2 Model description

152 Lionfish abundance at age (N_a) was computed as

$$N_a = N_{a-1} e^{-Z_{a-1}} \tag{1}$$

where Z_a is total instantaneous mortality at age *a*. The model included ages 1–7 years, with the oldest age treated as an accumulator class. The ages modeled were chosen based on the time since introduction to Belize and the initiation of this study (2008 – 2015). A plus group (7+) was used to account for older fish that may exist in the population, since we assume maximum age is 20 years (see below). The abundance of recruits (N_I , age-1 fish) was computed using the steepness formulation of the Beverton-Holt spawner-recruit function (Beverton and Holt 1957) $N_1 = \frac{(0.8R_0hS)}{[0.2R_0\Phi_0(1-h)+S(h-0.2)]}$ (2)

where R_0 is the asymptotic recruitment of age-1 fish, *h* defines the steepness of the curve, *S* is population fecundity (total egg production), and Φ_0 is the number of spawners (eggs) per recruit in an unfished population. Population fecundity (*S*) was computed as

164 $S = \sum_{a} 0.5 N_a m_a f_a \tag{3}$

165 where 0.5 is the proportion of females in the population, m_a is maturity at age a, and f_a is

- 166 fecundity at age *a*. Given a fishing mortality rate (*F*), total landings by number at age *a* (λ_a) was 167 derived using the Baranov catch equation (Baranov 1918)
- 168 $\lambda_a = \frac{F_a}{Z_a} N_a (1 e^{-Z_a}) \tag{4}$

169 where F_a is the fishing mortality rate at age *a*, computed as the product of *F* and selectivity at age 170 *a* (*s_a*). Total landings in weight (Y_F), as a function of *F*, was then computed as

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 $Y_F = \sum_a \lambda_a W_a \tag{5}$

172 where W_a is weight in kilograms at age *a*.

173 Length at age (*L_a*, total length in mm) was modeled using the von Bertalanffy growth
174 equation (von Bertalanffy 1957)

175 $L_a = L_{\infty}(1 - e^{-K(a - a_0)})$ (6)

where L_{∞} is asymptotic total length, *K* is the growth coefficient, and a_0 is the theoretical age at which length is zero. The growth parameters provided by Edwards *et al.* (2014) for both sexes combined were used: $L_{\infty} = 349$, K = 0.42, and $a_0 = -1.01$. The relationship between total length (mm) and weight (*W*, in g) was described by fitting a power function to data from Belize (n=352, sexes combined),

 $W = \alpha L^{\beta}$

(7)

182 The resulting parameter estimates were $\hat{\alpha} = 0.000007$ and $\hat{\beta} = 3.11$ (Figure 2).

183 Maturity at age (m_a) followed the logistic function from Gardner *et al.* (2015)

184

$$m_a = \frac{1}{1 + e^{-(L_a - L_{50})/\sigma}}$$
(8)

185 where L_a is total length at age, $L_{50} = 190$ mm is length at 50% maturity, and $\sigma = 13.1$ is the 186 parameter characterizing the slope of the fitted curve. Sex ratio was determined from 375 187 lionfish captured throughout Belize from 2011–2015. Forty-nine percent (n=184) were females 188 and 51% (n=191) were males. This proportion of females was not distinguishable from 0.5 (exact 189 binomial test; p=0.76) and thus the sex ratio in the model was assumed to be 50:50. A 50:50 sex 190 ratio is consistent with lionfish population sex structure reported elsewhere (e.g., Edwards et al. 191 2014, Morris 2009). Annual fecundity at age (f_a) was computed using the batch fecundity model 192 from Gardner et al. (2015)

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$$f_a = B(b_1 L_a - b_2) \tag{9}$$

where B = 152 is the mean number of batches per female per year and parameters $b_1 = 308.67$ and $b_2 = 58,265$ define the number of eggs per batch as a function of fish total length. The range of values used in this study are consistent with estimates of lionfish fecundity from other locations (*e.g.*, Morris 2009, Fogg *et al.* 2017).

198	Age-independent natural mortality (M) was computed using the mortality estimator
199	recommended by the meta-analysis in Then et al. (2015)

 $M = 4.889 * t_{max}^{-0.916} \tag{10}$

201 where t_{max} is maximum age. Maximum age of lionfish in the wild is unknown. The longest 202 observed lifespan of lionfish in captivity is 30 years (Potts et al. 2010). The oldest recorded 203 lionfish in the western Atlantic was 8 years and was captured off of North Carolina (Potts et al. 204 2010). Given the lack of studies on maximum age of lionfish in the wild, their maximum 205 observed age in captivity, and the presence of predation defense mechanisms, we assumed $t_{max} =$ 20 yrs and, therefore, M = 0.3. The M value used here is typical of a moderately short-lived reef 206 fish and is consistent with the natural mortality values used in other lionfish population modeling 207 studies (e.g., Barbour et al. 2011, Edwards et al. 2014, Johnston and Purkis 2015, Morris et al. 208 209 2011b).

210 Selectivity at age (s_a) was computed based on a normal distribution of sizes around the 211 mean length at age, computed from equation 6 (SD = 28.2; Johnson and Swenarton 2016), with 212 parameter $L_{vuln} = 250$ mm defining a threshold of vulnerability to harvest. That is, for each age, 213 s_a is the probability that length exceeds the vulnerability threshold, computed from the normal 214 cumulative distribution function with mean L_a and SD = 28.2 mm. The value of L_{vuln} = 250 mm 215 was derived from catch and fishing data obtained through semi-structured fisher and 216 restauranteur interviews conducted throughout Belize in 2015 and 2016 (Chapman et al. 2019). 217 Without data to estimate steepness (h), we assumed a value of 0.75. This value is consistent with 218 that of other reef fish populations that have similar life histories as lionfish, including rockfish 219 and scorpionfish (Scorpaenidae) (Forrest et al. 2010, Shertzer and Conn 2012, Thorson 2020).

220 Data from Belize on total lionfish abundance (N_{tot}) and total catch (C_{tot}) in numbers were 221 used to estimate R_0 and the current fishing mortality rate (F). Total initial abundance was 222 estimated using geospatial data on marine habitat sizes across Belize (provided by the Belize 223 Coastal Zone Management Authority and Institute) and habitat-specific lionfish density estimates 224 derived from Belize-wide surveys conducted in 2015 (Chapman et al. 2019). The habitat-specific 225 densities were scaled up to total habitat-specific abundances using the area of each habitat type. 226 Total area of the main barrier reef, back reef areas, and atolls was estimated to be 60,704 227 hectares, which scaled total abundance to $N_{\text{tot}} = 733,257$ lionfish. Based on information obtained through the semi-structured interviews mentioned above, total (or current) catch in 2015 was 228 estimated to be $C_{\text{tot}} = 89,902$ lionfish (Chapman *et al.* 2019). Given N_{tot} , natural mortality, 229 230 selectivity, and the relative abundance at age implied by Equation 1, we solved the Baranov catch equation in terms of numbers (*i.e.*, Equation 5 without the weight term) for the value of F 231 232 that provided $C_{\text{tot}} = 89,902$ lionfish. We refer to this value, F=0.32, as the current F. This 233 procedure was then used to back-calculate equilibrium recruitment (R_{eq})

$$N_{1} = R_{eq}$$

$$N_{2} = N_{1} e^{-Z_{1}}$$

$$N_{3} = N_{2} e^{-Z_{2}}$$

$$N_{4} = N_{3} e^{-Z_{3}}$$

$$N_{5} = N_{4} e^{-Z_{4}}$$

$$N_{6} = N_{5} e^{-Z_{5}}$$

$$N_{7+} = N_{6} e^{-Z_{6}} / (1 - e^{-Z_{7+}})$$

$$(11)$$

234

Given total mortality at age (*Z_a*) and $N_{tot} = \sum_a N_a = 733,257$, the recursive relationship of Equation 11 provides $\widehat{R_{eq}} = 266,000$. This value was then used to compute $\widehat{R_0} = 289,900$ as a function of equilibrium recruitment

238
$$R_0 = \frac{R_{eq}(h-0.2)\Phi_F}{0.8h\Phi_F - 0.2(1-h)\Phi_0}$$
(12)

where Φ_F is the number of spawners per recruit of a population fished at rate *F*. For any *F*, Φ_F is computed as

$$\Phi_F = \sum_a 0.5 \psi_a m_a f_a \tag{13}$$

where ψ_a is the number of fish per recruit at age *a* computed using Equation 11 with $N_I = 1$. The number of spawners per recruit of an unfished population (Φ_0) is computed similarly, but with *F* = 0.

245 2.3 Model application

246 The population model was developed and implemented using R Statistical Software (R 247 Core Team 2017) and applied to evaluate and identify initial lionfish fishery management targets for Belize, including values of OLY and F_{OLY}. More specifically, the model was used to quantify 248 249 equilibrium landings and abundance of lionfish across a range of fishing mortality rates from 250 $F_{LOW} = 0.0$ (no fishing effort) to $F_{HIGH} = 5.0$ (the maximum rate modeled). Fishing rates of 251 particular interest were F_{CURRENT} (the fishing rate in 2015), F_{MSY}, and F_{OLY}. The model was also 252 used to explore how lionfish size at selection (L_{vuln}) affects landings and abundance. For this 253 analysis, fishing mortality was fixed at $F = F_{OLY}$ and selectivity was adjusted as described above, 254 but with L_{vuln} set to different values across the range of 200 - 300 mm.

255 2.4 Formulation of OLY values

OLY and FOLY values will vary among management areas throughout the western Atlantic due to differences in local lionfish biology, socioeconomics, resources, data availability, and lionfish fishery management objectives (*i.e.*, desire for greater yield vs population suppression or vice versa). This paper describes one possible indicator-based approach for formulating OLY targets. Available socioeconomic and ecological data for lionfish in Belize were used as indicators to quantify and then cross-check or validate that the proposed values of OLY and *FoLY* would satisfy the two general objectives of lionfish fishery management – high
sustainable yield that meets socioeconomic demand and population suppression that mitigates
ecological impacts. More specifically, OLY values were quantified and validated based on the

estimated MSY, current yield levels (i.e., yield in 2015) (Chapman et al. 2019), fisher and

restauranteur satisfaction of current yield (Chapman et al. 2019), and Belize-specific lionfish

267 ecological threshold density estimates (Chapman et al. 2019).

268 2.5 Sensitivity analysis

Sensitivity (*Z_i*) of model results to parameter values were computed using local
perturbation analysis (Ellner and Guckenheimer 2006)

271
$$Z_i = \frac{Y(1.05p_i) - Y(0.95p_i)}{0.1Y(p_i)}$$
(14)

where *Y* is the model output of interest and $Y(p_i)$ is the value of *Y* as a function of the *i*th parameter p_i . A positive value of Z_i shows that an increase in parameter p_i leads to an increase in *Y*, while a negative value shows the opposite effect. A value of $|Z_i| \ge 1.0$ indicates that a 10% change in parameter p_i results in a >10% change in output *Y*. The larger the $|Z_i|$, the greater the sensitivity. We examined sensitivity of MSY, F_{MSY} , and N_{MSY} , the expected total abundance when fishing at F_{MSY} . Model results were considered sensitive to perimeter values when $|Z_i| \ge 1.0$. Sensitivities were also used to identify lionfish fishery research needs in Belize.

279 3. Results and Discussion

Overall, the model indicates that harvest of lionfish effectively reduces population abundance (Figure 3). Equilibrium abundance at $F_{LOW} = 0$ was estimated at 1.5 million lionfish, while abundance at $F_{HIGH} = 5.0$ was 220,000 lionfish. The model suggests that the current fishing effort in Belize has already reduced lionfish abundance by 34%, but increasing effort to $F_{MSY} =$ 0.67 could reduce abundance by an additional 21% (Figure 3). The model also suggests that the 285 population in Belize can withstand high rates of fishing without collapse, as indicated by the 286 relatively high abundance of lionfish predicated at F_{HIGH} – an improbable fishing mortality rate 287 (Figure 3). Other lionfish population modeling studies have reported similar findings. Morris et 288 al. (2011b) predicted monthly exploitation of 27% of the adult population in the temperate and 289 tropical western Atlantic would result in zero net growth; Barbour et al. (2011) predicted annual 290 exploitation rates between 35 and 65% of the total population in North Carolina would be 291 required to cause recruitment overfishing; Edwards et al. (2014) predicted annual exploitation 292 rates between 15 and 35% of the total population at Little Cayman Island would be required to 293 cause recruitment overfishing; and Chagaris et al. (2017) predicted fishing mortality rates greater than F = 1.0 are required to cause population declines on the West Florida Shelf. The results 294 295 from these studies, which vary in terms of model design, data inputs, and geographic and spatial scales, all indicate a key population characteristic – invasive lionfish are biologically robust to 296 297 fishing pressure. This population characteristic is likely due to lionfish biology and ecology 298 (Côté et al. 2013) and is an important finding in terms of both lionfish control and establishing 299 managed lionfish fisheries. This finding highlights the (1) biological sustainability of lionfish as 300 a fishery resource and (2) indicates that the level of fishing effort required to overfish lionfish is 301 substantial and unlikely to be achieved, especially without commercial-scale fishing practices. 302 These data support continued establishment of (managed) commercial lionfish fisheries 303 throughout the invaded range to provide an alternative sustainable fishery resource and serve as a 304 means of national- and international-level control.

305 The model indicates that fishing lionfish at rates above F_{MSY} is expected to contribute 306 substantially to population suppression, much more so than fishing at rates below F_{MSY} , while 307 having relatively minimal impacts on yield (Figure 3). Fishing at F_{HIGH} is predicted to further 308 reduce lionfish abundance by an additional 63%, while only reducing landings by 42% relative 309 to fishing at F_{MSY} (Figure 3). While any harvest of lionfish beyond MSY can be considered 310 beneficial for local reef ecology, the model indicates that trade-offs exist where increased 311 population suppression is done at a cost to landings (Figure 3). OLY seeks to balance these 312 trade-offs to meet socioeconomic demand, while suppressing populations to levels that mitigate 313 ecological impacts. OLY values in this study were formulated using available socioeconomic 314 and ecological data for lionfish in Belize. These data were used as indicators to quantify and then 315 validate that the proposed values of OLY and Foly would satisfy the two general objectives of 316 lionfish fishery management. While distribution challenges exists in Belize, Chapman et al. 317 (2019) reported that Belizean fishers and restaurateurs were, in general, satisfied with catch 318 levels in 2015 due to relatively sufficient supply to meet demand and the fact that lionfish are 319 predominately caught and sold opportunistically. For these reasons, and because the current 320 catch level was only 10% below the estimated MSY, yield in 2015 was used as a benchmark for 321 quantifying OLY and F_{OLY} . OLY, and subsequently F_{OLY} , was quantified as the yield above MSY 322 that produced equivalent yield as the current catch level. The proposed value of $F_{OLY} = 1.51$ for 323 lionfish in Belize is predicted to provide the same yield as the current fishing levels, thus 324 generally satisfying current socioeconomic demand in Belize, while reducing abundance by an 325 additional 42% relative to current levels (Figure 3).

Belize-specific lionfish ecological threshold densities reported in Chapman *et al.* (2019) were then used to cross-check that the proposed OLY targets would sufficiently reduce lionfish populations to a level that is expected to mitigate their ecological impacts. Threshold densities were estimated for the five major Belizean marine protected areas (MPAs) in 2015 following the approach in Green *et al.* (2014). The approach in Green *et al.* (2012) estimates location-specific 331 lionfish densities at which their ecological impacts are predicted to be mitigated. Threshold 332 densities are quantified based on local sea surface temperature, reef fish densities, lionfish prey 333 consumption rates, and lionfish prev production rates. Estimated threshold density across the 334 Belizean MPAs ranged from 10 to 40 fish/hectare (Chapman et al. 2019). The predicated 335 abundance of lionfish at FoLy, converted to density, is 7 fish/hectare. Thus, the proposed OLY is 336 expected to substantially reduce the ecological impacts of lionfish in Belize. OLY in this study 337 was quantified and validated based on available ecological and socioeconomic indicators. When 338 ecological and socioeconomic data are not available to formulate OLY targets, setting OLY 339 targets based on a percent yield below MSY is a good initial approach. Based on the trade-offs 340 identified in this study (Figure 3), OLY targets based on percent yields closer to MSY are 341 expected to favor higher yields while percent yields further from MSY are expected to favor 342 population suppression.

343 Encouraging and/or achieving fishing effort beyond MSY levels will likely be a 344 challenge for lionfish fishery managers. From the perspective of single-species fisheries 345 management, fishing at rates beyond F_{MSY} is economically counterproductive because more 346 fishing effort is needed to obtain the same yield. However, from a broader management 347 perspective, fishers, managers, researchers, and the public can view the effort beyond F_{MSY} as 348 effort devoted to marine conservation and control of an invasive species. This additional effort 349 can be viewed and marketed as an investment in native species that are negatively affected by 350 lionfish and/or are overfished. One approach to achieve target FoLy values is to set the target 351 commercial $F = F_{MSY}$, then make up the additional effort needed through recreational fishing. 352 Regularly scheduled and well-advertised recreational lionfish derbies and tournaments, which 353 almost always incorporate some form of marine conservation messaging, have been highly

successful at reducing lionfish densities and impacts on local reefs throughout the invaded range (e.g., Green *et al.* 2017). Making up this effort deficit through recreational fishing is much more likely than through commercial fishing, given that recreational fishing priorities are based more on angler satisfaction than on economic efficiency. Monitoring fishing effort and determining fishing mortality rates from these events would not be difficult; not only would these efforts aid in achieving increased fishing mortality, they can also enhance awareness and education of marine conservation issues.

In addition to fishing mortality and landings, size at selection is a variable that fishery 361 managers often regulate. Typically, the objective is to allow juveniles to reach maturity and 362 spawn before becoming susceptible to the fishery. Like fishing mortality (Figure 3), the model 363 indicates that a trade-off exists in which increased harvest of smaller lionfish can significantly 364 365 reduce abundance, and theoretically reduce the potential for ecological impact, but comes with a significant cost to landings (Figure 4). Equilibrium landings and abundance at the current size 366 367 selection threshold of 250 mm were estimated at 28.3 t (1000 kg) and 422,000 lionfish (Figure 368 4). A shift in size selection to smaller lionfish (*i.e.*, 200 mm fish) indicated a 68% reduction in 369 landings as well as a 72% reduction in abundance, whereas an increase in size selection to larger 370 lionfish (*i.e.*, 300 mm fish) indicated a 20% increase in landings and a 56% increase in 371 abundance (Figure 4). This result is consistent with model predictions in Barbour et al. (2011), 372 Morris et al. (2011b), and Edwards et al. (2014), all of which indicated that the removal of 373 smaller (juvenile) lionfish may have the strongest effect on population abundance. As with other 374 fish species, this characteristic is attributed to lionfish reproductive biology, particularly their age 375 and size at maturity and their fecundity at age and size. Lionfish become mature at age 1 or ~ 100 376 mm (Edwards et al. 2014), and annual egg production per female generally increases with size

and age (Morris 2009). As such, increased harvest of smaller lionfish reduces total annual egg
production. While this population characteristic is common among fishery species, it is an
important characteristic for both lionfish control and lionfish fishery management. For general
lionfish control, it supports the need to target smaller lionfish to enhance population suppression.
For lionfish fishery management, it indicates that size selection thresholds could help managers
balance the trade-offs between sustainable yield and population suppression.

Overall, the model results were relatively sensitive to the growth and fecundity 383 384 parameters (Table 2), which is consistent with other lionfish population modeling studies (e.g., 385 Barbour et al. 2012, Edwards et al. 2014). While growth and fecundity estimates for lionfish from nearby Little Cayman Island were used in this study, robust age, growth, and fecundity data 386 387 for lionfish in Belize could improve model predictions and overall management of the fishery, 388 particularly estimates of F_{MSY}. The largest sensitivity described the response of MSY to changes in the length-weight parameter β ($|Z_i| = 19.9$, Table 2), indicating the importance of precise β 389 390 estimates. This level of sensitivity is due to the exponential relationship between length and 391 weight and, therefore, the potential for β to strongly influence estimates of yield in weight. 392 However, given the well-defined relationship between length and weight described in this study 393 (Figure 2), we do not view this as a critical research need in Belize. In general, model results were not sensitive to natural mortality, suggesting the model provided by Then et al. (2015) is 394 395 adequate for describing natural mortality of lionfish, at least until lionfish-specific estimates 396 become available. Data derived from several surveys conducted to develop Belize's National 397 Lionfish Management Strategy (Chapman et al. 2019) were used in this study. These included 398 data on current landings, total lionfish abundance, fisher and restauranteur satisfaction of current 399 landings, and lionfish ecological threshold densities. While these data are informative and

satisfactory for model development and initiation of management, establishment of systematic
and regular fishery-dependent and fishery-independent monitoring is imperative for successful
long-term lionfish fishery management in Belize and elsewhere.

403 **4. Conclusions**

404 This paper describes the application and extension of fishery management concepts to the 405 management of an invasive species. This paper introduces the concept of optimum lionfish yield, 406 which seeks the balance management trade-offs from both the natural resource and invasive 407 species management perspectives. We applied this concept to quantify initial lionfish fishery 408 management targets in Belize. This case study highlights an alternative approach to invasive 409 species management and is an illustrative example of a sentiment summarized by Oficialdegui et 410 al. (2020): "Legal instruments regulating the commercial use of non-native invasive species need 411 to overcome simplistic approaches (full exploitation or complete ban) and involve more flexible 412 and adaptive strategies because there is no one-size-fits-all solution." Through proper 413 management, invasive lionfish can serve as a biologically robust alternative fishery resource, 414 which could help create more diversified markets and potentially reduce stress on traditional 415 native fishery species. While the concept and framework described here is introduced for 416 management of invasive lionfish, it could be applied to management of other invasive species, 417 both aquatic and terrestrial.

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428	and opinions expressed herein, are those of the authors and do not necessarily reflect those of						
429	any government agency.						
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Tables and Figures 568

	Parameter	1	2	3	4	5	6	7+	
	Maturity	0.665	0.990	0.999	0.999	0.999	0.999	0.999	
	(<i>m</i>) Fecundity (f eggs)	478,705	2,892,869	4,479,088	5,521,309	6,206,096	6,656,034	6,951,664	4
	Natural mortality (M)	0.30	0.30	0.30	0.30	0.30	0.30	0.30	
	Mean Length (L, mm)	198.97	250.42	284.23	306.44	321.04	330.63	336.93	
	Mean Weight (W, g)	98.69	201.82	299.23	378.13	437.00	478.90	507.85	7
570	Selectivity (S)	0.035	0.507	0.889	0.978	0.995	0.999	1	
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Table 1: Age-specific parameter values used in the population model 569

583 Table 2: Sensitivity of model results to parameter values. Values > 1.0 or < -1.0 indicate that a

584 10% change in the parameter results in a >10% change in the model output, which were

585 considered significant in this study (*). The larger the absolute value, the greater the sensitivity.

Parameter	Description	F_{MSY}	MSY	N _{MSY}
Ro	Asymptotic recruitment level	0.00	1.02*	1.00*
h	Steepness of recruitment	2.24*	0.80	0.03
M	Natural mortality	1.49*	-0.58	-0.62
L_{∞}	Mean asymptotic length	-2.39*	2.97*	-0.41
K	Growth coefficient	0.00	1.18*	-0.48
a_0	Theoretical age of length 0	0.15	0.32	-0.20
α	Length-weight coefficient	0.00	1.02*	0.00
β	Length-weight exponent	-0.60	19.90*	0.21
В	Batches spawned per year	0.00	0.00	0.00
b_1	Batch fecundity coefficient	1.34*	0.32	-0.14
b_2	Batch fecundity intercept	-1.19*	-0.32	0.12
L_{50}	Length at 50% maturity	-0.30	-0.06	0.02
σ	Slope of maturity curve	0.00	0.00	0.00
Lvuln	Length of vulnerability to harvest	4.03*	0.58	0.26









Figure 3: Equilibrium landings (top) and abundance (bottom) of lionfish in Belize across a range of fishing mortality rates: $F_{LOW} = 0$ (\blacksquare), $F_{CURRENT} = 0.32$ (\blacklozenge), $F_{MSY} = 0.67$ (\blacktriangle), $F_{OLY} = 1.51$ (\blacklozenge), and $F_{HIGH} = 5.0$

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⁶²³ Figure 4: Equilibrium landings (top) and abundance (bottom) of lionfish in Belize across a range

⁶²⁴ of sizes at selection with $F = F_{OLY} = 1.51$. The point on the graph indicates current size at 625 selection = 250 mm

630 Appendix 1: Additional Analyses

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632 Part 1: Exploring Uncertainty in Landings and Abundance

As described in the main text, the 2015 field estimates of abundance and landings were
733,257 lionfish and 89,902 lionfish. Abundance and landings directly affect estimates of the
current fishing mortality rate (current F) and the asymptotic recruitment of age-1 fish (R0) and,
therefore, model output (see Section 2.2 in the main text). Here, we explore uncertainty in our
point estimates of abundance and landings on current F, R0, and model output.

638 To do this, we conducted Monte Carlo simulations (N=2000 iterations in each analysis) 639 in which each iteration repeated our analysis but with different values of (1) abundance and landings and then (2) current F and R0. First, we drew a new value of abundance and a new 640 641 value of landings each from a normal distribution with mean equal to the 2015 field estimates 642 and an assumed coefficient of variation (CV) of CV=0.1 (Appendix Figure 1A,B). Using these 643 values, we computed distributions of current F (Appendix Figure 1C) and of R0 (Appendix 644 Figure 1D). We then propagated uncertainty in current F and R0 into the estimated management 645 quantities. Similar to above, we conducted Monte Carlo simulations (N=2000 iterations) in 646 which each iteration repeated our analysis but with different values of current F and R0 drawn 647 from their distributions produced above (i.e., Appendix Figure 1C,D). This produced distributions of current landings (Lcurrent), MSY, and OLY (Appendix Figure 2A), as well as in 648 649 the levels of abundance associated with those values (Appendix Figure 2B). The general 650 conclusion presented in the main text remains the same as that inferred from the corresponding 651 point estimates - fishing at OLY provides current levels of landings (by design) while 652 suppressing the abundance to substantially lower levels than current.

We additionally propagated uncertainty in current F and R0 into estimates of equilibrium landings and abundance as a function of fishing rate (Appendix Figure 3). We caution that this analysis does not produce true confidence bands as it is predicated on our assumed value of CV=0.1. It does, however, indicate the conditional degree of uncertainty in results stemming from the field estimates of abundance and landings.

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659 Part 2: Exploring Uncertainty in the standard deviation of size-at-age

As part of our analyses in the main text, we examined effects of the size-at-selection on equilibrium abundance and landings (Figure 4). The size-at-selection, along with growth characteristics including the standard deviation of size-at-age, determined the pattern of selectivity as the proportion of fish-at-age that were vulnerable to fishing. In Appendix Figure 4, we show how size-at-selection and standard deviation of size-at-age affect the resulting selectivity curves. In general, the curves are far more sensitive to the size-at-selection (our pivot) than to the standard deviation.

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675 676 Appendix Figure 1. Assumed distributions of initial lionfish abundance (A) and landings (B) 677 used to compute the current fishing rate (current F) (C) and the asymptotic recruitment of age-1 678 fish (R0) (D). Vertical lines indicate the 2015 field estimates of abundance and landings (A,B) and the point estimates of current F and R0 derived from those field estimates (C,D). 679



681 682 Appendix Figure 2. Distributions of results derived from assumed distributions of field estimates 683 of abundance and landings. Panel A shows distributions of landings corresponding to Lcurrent 684 (blue), OLY (purple), and MSY (green). Note that Lcurrent is not apparent because it overlaps 685 entirely with OLY (by design). Panel B shows the levels of abundance that correspond to the 686 landings in Panel A.



Appendix Figure 3. Equilibrium landings (A) and abundance (B) of lionfish in Belize across a

- 690 range of fishing mortality rates: $F_{MIN} = 0$ (**■**), $F_{CURRENT} = 0.32$ (**●**), $F_{MSY} = 0.67$ (**▲**), $F_{OLY} = 1.51$
- 691 (\blacklozenge), and $F_{HIGH} = 5.0$. Intervals shown represent the 2.5th and 97.5th percentiles from N=2000
- 692 Monte Carlo simulations with variability in the 2015 field estimates of lionfish abundance and
- 693 landings.
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- 695 696 Appendix Figure 4. Selectivity as a function of the size-at-selection (Lvuln) and the standard
- 697 deviation (SD) of size-at-age. Our base values were $L_{vuln} = 250$ mm and SD = 28.2, and values
- used to create Figure 4 (main text) varied Lvuln over the range 200mm to 300mm, with SD = 698
- 699 28.2 in all cases. For this figure, we additionally varied SD±25% of the base value.