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3 **Large-Scale Environmental Controls on the Seasonal Statistics of Rapidly Intensifying North**
4 **Atlantic Tropical Cyclones**
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Abstract

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This study is concerned with the connections between the large-scale environment and the seasonal occurrence of rapid intensification (RI) of North Atlantic tropical cyclones. Physically-motivated statistical analysis using observations and reanalysis products suggests that for tropical cyclones over the open tropical North Atlantic, the interannual variability of the probability of storms undergoing RI is influenced by seasonal large-scale atmospheric and oceanic variables, but not so for storms over the Gulf of Mexico and western Caribbean Sea. We suggest that this differentiated response is due to the former region exhibiting a strong negative correlation between the seasonal anomalies of vertical wind shear and potential intensity. Differences in the mean climatology and subseasonal variations of the large-scale environment in these regions appear to play an insignificant role in the distinctive seasonal environmental controls on RI. We suggest that the interannual correlation of vertical wind shear and potential intensity is an indicator of seasonal predictability of tropical cyclone activity (including RI) across the tropics.

49 **1. Introduction**

50

51 Despite recent improvement in forecasting tropical cyclone (TC) genesis and tracks, prediction of their
52 changes in intensity even on timescales of days has remained challenging (e.g. Elsberry et al. 2007,
53 Rappaport et al. 2009, Elsberry 2014). Of particular scientific interest are those TCs that undergo rapid
54 intensification (RI), owing to their widespread impacts on society and the relatively little lead time for
55 preparation they may provide. Following existing literature (e.g. Kaplan and DeMaria 2003, Kaplan et
56 al. 2010), an RI event is defined as a TC intensification of at least 30 knots (15.4 m/s) in 24 hours,
57 separated by more than 24 hours from each other. Recently, Lee et al. (2016) suggested that the vast
58 majority of global major storms rapidly intensified at least once during their lifetime, and highlighted
59 their important role in the climatology of TCs. Moreover, the frequency of storms that intensify rapidly
60 is projected to increase substantially in future climate (Emanuel 2017, Bhatia et al. 2018), and may
61 have already increased in the North Atlantic (Bhatia et al. 2019), emphasizing the importance of
62 improved predictions of rapidly intensifying TCs.

63

64 There has been continuing research on rapidly intensifying TCs at the storm scale and at weather
65 forecast timescales (e.g. Bosart et al. 2000, Kaplan and DeMaria 2003, Lin et al. 2009, Kaplan et al.
66 2010, Shieh et al. 2013, Zhuge et al. 2015, Chen et al. 2017), while a few studies have attempted to
67 study their predictability on seasonal timescales (e.g. Wang and Zhou 2008, Wang et al. 2017). Before
68 the hurricane season starts, can the large-scale environment for the upcoming season be used to say
69 something about the RI activity of TCs? The provision of seasonal predictions for RI events would
70 serve to improve societal preparedness for rapidly intensifying tropical cyclones, complementing
71 existing seasonal forecasts for TC frequency. Such examples include forecasts issued by the United
72 States Climate Prediction Center (CPC), Geophysical Fluid Dynamics Laboratory (GFDL), Colorado
73 State University (CSU), and the European Centre for Medium-Range Weather Forecasts (ECMWF),
74 among others. To advance this goal, our approach here is to examine the relationship between seasonal

75 statistics of the occurrence of RI in the North Atlantic and the large-scale environment on seasonal
 76 timescales. Predictions of the seasonal environment from numerical models could then be used for
 77 predictions of RI activity. Besides, knowledge about seasonal environmental controls on RI can
 78 connect with those about the environmental footprints of different modes of climate variability, such as
 79 the El Niño-Southern Oscillation (e.g. Gray 1984, Shapiro 1987), the Atlantic Meridional Mode
 80 (Chiang and Vimont 2004) and the North Atlantic Oscillation (Hurrell et al. 2003), which have been
 81 shown to exhibit seasonal predictability (Barnston et al. 2012, Vimont 2012).

82

83 A conceptual model for the large-scale environmental controls on intensity change of TCs, including
 84 RI, can be developed with the equation

$$85 \quad dI(t)/dt = \tau^{-1}(I^* - I(t)) = f(\tau(t), I^*(t)) \quad - (1)$$

86 (Lloyd et al. 2011), which considers how the time rate of change of TC intensity (dI/dt) is affected by
 87 the environmental potential intensity (I^*) and other environmental parameters known to influence TC
 88 intensity, such as vertical wind shear and tropospheric humidity, through the relaxation timescale τ . In
 89 this study, instead of considering the environment at each time instant t following the TC, the function
 90 f is now a function of the seasonal-mean large-scale environment, so that we consider the effects of
 91 the seasonal environment on the time tendency of intensity:

$$92 \quad dI(t)/dt = \tilde{f}(\text{seasonal environment}) + \epsilon(t) \quad - (2)$$

93 where $\epsilon(t)$ concerns with subseasonal fluctuations such as intraseasonal oscillations and weather-scale
 94 variations. For all the TCs in each season with its corresponding seasonal-mean environment, a
 95 distribution of dI/dt results from $\epsilon(t)$ at each time instant t following the TCs. Then, the equivalent
 96 question is whether the seasonal environment can change the statistics of the dI/dt distribution, in
 97 particular the proportion of the distribution that exceeds the threshold for RI.

98

99 To study the variability of the annual counts of RI instances (which we denote by $n(RI)$), we first note
100 that part of its variance comes from the variance of the number of tropical cyclones (which we denote
101 by N). Absent other information, one would expect more RI to occur simply when there are more
102 tropical cyclones in a given year, all other aspects being equal. As is shown below, the variance of N
103 only explains part of the variance of $n(RI)$, so that it is as important to understand the climate controls
104 on the probability of each TC experiencing RI, *i.e.*, $p(RI) = n(RI)/N$. In other words, $n(RI)$ is
105 dependent on the total number of storms, which may in turn be determined by factors outside of those
106 influencing TC intensification, and $p(RI)$ can be considered as a ‘normalized’ measure of RI activity.
107 For this reason, statistical relationships developed directly using the $n(RI)$ metric may not genuinely
108 reflect large-scale environmental controls on RI. For example, in Wang et al. (2017) the seasonal large-
109 scale atmospheric and oceanic conditions are linearly regressed to the RI number. A similar metric to
110 $p(RI)$, the ‘RI ratio’, defined by the number of 24-hour intensity changes above 30 knots divided by
111 total 24-hour intensity changes, was used in Bhatia et al. (2018) and Bhatia et al. (2019) for studying
112 the response of RI to climate change and anthropogenic forcing. The month-to-month variations of RI
113 ratio in the Northwest Pacific were also considered in Wang and Zhou (2008) and Ge et al. (2018),
114 while Shu et al. (2012) described the variations of RI ratio with TC category in the Northwest Pacific.
115 Since the statistical modeling for the number of tropical cyclones (N) over the North Atlantic has been
116 performed in previous studies (Villarini et al. 2010, Vecchi et al. 2011, Murakami et al. 2016b), our
117 approach in this study is to examine climate variability of $n(RI)$ through modeling the probability that
118 a TC will experience RI. Any potential for prediction skill in RI probability can combine with existing
119 seasonal outlooks of tropical cyclone frequency to provide additional information with regard to RI.
120
121 In this study, we will also investigate how RI activity varies within the North Atlantic basin. Previous
122 studies on RI have focused on statistics for the entire basin or the Main Development Region (MDR).

123 For instance, linear regressions in Wang et al. (2017) were performed between the seasonal large-scale
124 environment and RI number in the entire North Atlantic basin, and they suggested that certain
125 variables in certain regions could be used to predict basinwide RI frequency. On the other hand,
126 Klotzbach (2012) suggested that the number of RI occurrences is significantly higher during the La
127 Niña phase and certain phases of the Madden-Julian Oscillation, for both the North Atlantic and MDR.
128 However, few studies have considered sub-basin variability of RI activity, including those outside of
129 the MDR. As the skill of seasonal TC forecasts has been shown to vary within the North Atlantic basin
130 (Vecchi et al. 2014, Murakami et al. 2016a, Liu et al. 2018) and across the tropics (DeMaria et al.
131 2007, Vecchi et al. 2014, Zhang et al. 2016b), we will examine how the statistics of sub-basin RI
132 probability and its variability are related to regional large-scale atmospheric and oceanic conditions on
133 seasonal timescales.

134

135 This paper is structured as follows. Section 2 describes the data and methods employed in this study,
136 while Section 3 analyzes the statistics of RI and its relationship with large-scale atmospheric and
137 oceanic conditions. Sections 4 and 5 discuss sub-basin differences in this relationship, followed by
138 some concluding remarks in Section 6.

139

140 **2. Data & Methods**

141

142 Sub-basin classification of RI activity in the North Atlantic is determined by a cluster analysis of
143 tropical cyclone tracks, while the large-scale environmental controls on RI in each cluster are
144 examined by statistical regression of large-scale climate variables on RI statistics. This section
145 describes the datasets and climate reanalysis products studied, the cluster analysis and regression
146 methods employed, and the methods to analyze subseasonal variations of certain variables.

147

148 **2a. Tropical Cyclones and Large-Scale Variables**

149

150 North Atlantic tropical cyclone data is obtained from the Atlantic Hurricane Database (HURDAT2,
151 Landsea and Franklin 2013, version updated on April 11, 2017). HURDAT2 provides best-track
152 positions, maximum sustained surface wind speed, minimum central pressure and wind radii of North
153 Atlantic tropical cyclones at 6-hourly time intervals. Extratropical cyclones, tropical depressions and
154 disturbances are removed prior to analysis. HURDAT2 data between 1979-2015 is studied (the satellite
155 era, e.g. Rienecker et al. 2011, Truchelut et al. 2013).

156

157 Large-scale atmospheric and oceanic variables are obtained from various climate reanalysis products
158 and observational datasets. Monthly-mean values of atmospheric variables including relative humidity,
159 temperature and winds at various tropospheric levels are taken from MERRA (Rienecker et al. 2011)
160 and the Japanese 55-year Reanalysis (JRA-55, Kobayashi et al. 2015), following, for example, Vimont
161 and Kossin (2007), Hendricks et al. (2010), Vecchi et al. (2013), Wing et al. (2015), Zhang et al.
162 (2016a), and Wang et al. (2017). Sea-surface temperature (SST) is taken from HadISST (Rayner et al.
163 2003) and the NOAA OISST Version 2 High Resolution Dataset (Reynolds et al. 2007), from which
164 we calculate the relative sea-surface temperature (RELSST) defined as the difference between local
165 SST and the tropical-mean SST (Vecchi and Soden, 2007). From MERRA and JRA-55, the vertical

166 wind shear (VWS) is calculated as the magnitude of the vector difference between 200hPa and 850hPa
167 winds. Potential intensity (PI) is calculated from the atmospheric profile in MERRA and JRA-55
168 following Bister and Emanuel (1998, 2002). PI is defined as $PI^2 = C_K/C_D T_S/T_0 (CAPE^* -$
169 $CAPE)|_m$, where C_K is the exchange coefficient for enthalpy, C_D is the drag coefficient, T_S is the sea
170 surface temperature, T_0 is the mean outflow temperature, $CAPE^*$ is the convective available potential
171 energy of air lifted from saturation at sea level in reference to the environmental sounding, and $CAPE$
172 is that of boundary layer air. Both $CAPE$ terms are evaluated near the radius of maximum winds of the
173 TC. Saturation deficit (SDEF), which provides a measure of the moist entropy deficit of the middle
174 troposphere, is calculated as $SDEF = (s_b - s_m)/(s_0^* - s_b)$, where s_m, s_b, s_0^* are respectively the moist
175 entropies of the middle troposphere, boundary layer (taken as 750hPa and 900hPa respectively,
176 determined by a separate analysis of the tropical moist entropy profile), and the saturation moist
177 entropy of the sea surface (Emanuel 2010). Tropical cyclone heat potential (TCHP) is calculated from
178 the NCEP Global Ocean Data Assimilation System reanalysis (GODAS, Behringer et al. 1998), as the
179 vertical integral of temperature from the sea surface to the depth of the 26°C isotherm. We considered
180 these variables as candidates for large-scale environmental controls on RI, since they have been
181 suggested to influence TC activity and development in a number of studies, e.g. Ryan et al. (1992),
182 Watterson et al. (1995), Bister and Emanuel (1998), Bister and Emanuel (2002), Wong and Chan
183 (2004), Camargo et al. (2007), Vecchi and Soden (2007), and Tang and Emanuel (2012). Data for
184 VWS, PI, SDEF, RELSST and TCHP in the period of 1980-2015 are studied.

185

186 **2b. Cluster Analysis**

187

188 To consider sub-basin variability of RI statistics within the North Atlantic, we performed a K-means
189 cluster analysis on the HURDAT2 data, based on the location of genesis, lysis and maximum intensity

190 of each TC, with the number of clusters (K) to be determined. A similar K-means clustering approach
191 was used in Elsner (2003), Elsner and Liu (2003) and Ramsay et al. (2012), for TCs in the North
192 Atlantic, Northwest Pacific and Southern Hemisphere basins respectively. In these studies, various TC
193 statistics for each cluster were calculated, but not specifically related to RI events. TC genesis (lysis) is
194 defined as the first (last) 6-hourly position with sustained wind speed above 34 knots (i.e. above
195 tropical storm intensity), following, for example, Murakami et al. (2015) and Murakami et al. (2016b).

196

197 Based on the within-cluster spread (inertia) for each choice of K (not shown), we subjectively decided
198 to choose $K \geq 4$, since the $K = 2, 3$ cases provide high marginal improvement in cluster spread.
199 Meanwhile, there is an inherent upper bound to K since the number of data in each cluster decreases
200 with K , which in turn increases noise when considering interannual variability and seasonal
201 environmental controls on RI in the later sections. Thus, a value of K between 4 and 5 seems to be
202 desirable. In deciding between these values, a cluster analysis is performed for both values, with the
203 latter case further separating the cluster in the subtropics (not shown). Considering the relatively small
204 number of RI instances in the subtropics, we decided to treat this as one cluster, hence performing the
205 K-means cluster analysis with four clusters. The results of this cluster analysis are shown in Section 3a.

206

207 **2c. Statistical Regressions**

208

209 To explore statistical connections between the seasonal large-scale variables and regional RI
210 probability for each TC cluster, we performed linear least-squares regressions between RI activity in
211 each JJASON season between 1980-2015, and the 36-year time series of JJASON-mean atmospheric
212 and oceanic variables, and calculated Spearman's correlation coefficients. In addition, to test the
213 robustness of the linear least-squares regression, a linear median of pairwise slopes fit (Lanzante 1996)
214 was also performed between the RI statistics and large-scale variables. The choice of the JJASON

215 season follows from our analysis of HURDAT2 data that in the North Atlantic, all RI events in the
216 period of 1980-2015 occurred between the months of June and November. This regression
217 methodology is similar to that in Wang et al. (2017), in which they explored the relationship between
218 the large-scale environment and RI number in the entire North Atlantic basin; here the correlations are
219 also calculated for the $p(RI)$ metric and for the individual clusters. The significance of the Spearman
220 correlations is determined by a bootstrap test with 1000 samples, using a two-sided 90% or 95%
221 significance level.

222

223 Limitations are inherent in the assumptions underlying the above linear least-squares regression, which
224 encourages the application of other generalized linear models in studying RI occurrence. In particular,
225 the predicted value of $p(RI)$ from explanatory variables should inherently take values between 0 and 1.
226 As this is not guaranteed by the linear regression model, and since RI is by its nature a binary process,
227 we adopt the binary logistic regression, which assumes that $n(RI)$ follows a binomial distribution
228 $B(N, p(RI))$. The logistic regression uses the large-scale environmental variables as exogenous
229 regressors (explanatory variables), with the endogenous (response) variable being n^* (number of
230 successes) and $N - n^*$ (number of failures) for each year, where $n^*(RI)$ represents the number of RI
231 instances which considers multiple RI instances of the same tropical cyclone as one. The metric $n^*(RI)$
232 is introduced because by virtue of the definition of RI, a TC can experience more than one RI instance
233 if the RI occurrences are separated by more than 24 hours, so that $p(RI)$ can exceed unity (but rarely
234 do so). The statistical package ‘statsmodels’ (Skipper and Perktold, 2010), with the binomial model
235 family and the logit link function, performs the logistic regression using the iteratively reweighted
236 least-squares (IRLS) method. The logit link function takes the form

$$237 \quad \text{logit}(p) = \ln\left(\frac{p}{1-p}\right) = \beta_0 + \beta_i x_i \quad - (3)$$

238 so that

239
$$p = \frac{1}{1 + \exp(-\beta_0 - \beta_i x_i)} \in [0, 1] \quad - (4)$$

240 where positive values of β_i represent $p(RI)$ increases with the exogenous regressor x_i .

241

242 In the statistical modeling of $n(RI)$, given the nature of the data (counts), a Poisson regression model
 243 is adopted (Villarini et al. 2010), so that the expected value of $n(RI)$ is given by $\exp(\beta_0 + \beta_i x_i) \in$
 244 $[0, \infty)$. Similar to above, the statistical significance of the Spearman correlations between observed and
 245 predicted values is determined by a bootstrap test, while the skill of the regression models relative to
 246 climatology is calculated as

247
$$Skill = \left(1 - \frac{MSE_{prediction}}{MSE_{climatology}} \right) \times 100\% = \left(1 - \frac{\sum_{i=1980}^{2015} (n_{i,pred} - n_{i,obs})^2}{\sum_{i=1980}^{2015} (\bar{n}_{i,obs} - n_{i,obs})^2} \right) \times 100\% \quad - (5)$$

248 where $\bar{n}_{i,obs} = \frac{1}{36} \sum_{i=1980}^{2015} n_{i,obs}$. Positive (negative) values represent predictions with skill above
 249 (below) climatology.

250

251 **2d. Decomposition of Daily Variations**

252

253 Daily data is used to examine the control of the seasonal environment on RI (Section 5). In particular,
 254 daily tropospheric profiles are obtained from MERRA reanalysis, for the period 1980-2015, from
 255 which VWS and PI (shown in Section 3b to significantly influence RI) are calculated. We decompose
 256 the daily values of VWS and PI as follows:

257
$$X(day) = \bar{X} + \langle X \rangle + X' = \bar{\bar{X}} + X_{SC} + \langle X \rangle + X', \quad X = VWS, PI \quad - (6)$$

258 where $\bar{X} = \bar{X}(month)$ represents the 1980-2015 JJASON climatological seasonal cycle, and can be
 259 further separated into a scalar climatological mean ($\bar{\bar{X}}$) and average seasonal cycle anomalies given by

260 $X_{SC} = X_{SC}(month)$. The interannual variability of the large-scale environment $\langle X \rangle = \langle X \rangle(year)$ is
 261 given by

$$262 \quad \langle X \rangle(t_i) = \left(\frac{1}{N_{day}} \sum_{June\ 1, Year\ i}^{Nov\ 30, Year\ i} X \right) - \bar{X} \quad \forall i \in [1980, 2015] \quad - (7)$$

263 with $N_{day} = 183$ (number of days in each season), representing the JJASON-mean departure from
 264 climatology in each season. $X' = X'(day)$ represents subseasonal variations of the large-scale
 265 environment.

266
 267 This decomposition enables us to distinguish between the large-scale environmental variations on
 268 seasonal and subseasonal (including weather) timescales. The difference between $X_{sub} = \bar{X} + X'$ and
 269 $X_{tot} = X_{sub} + \langle X \rangle = \bar{X} + \langle X \rangle + X'$ indicates the role of interannual variability $\langle X \rangle$. By construction,
 270 X_{sub} has the same JJASON seasonal-mean for each year, and has the same climatological mean as
 271 X_{tot} .

272
 273 We then consider the VWS-PI phase space and compute the two-dimensional probability density
 274 function (PDF) of subseasonal (X_{sub}) and total (X_{tot}) VWS and PI values, denoted by PDF_{sub} and
 275 PDF_{tot} respectively. PDF_{sub} and PDF_{tot} are calculated using X_{sub} and X_{tot} values respectively, for
 276 each season and as area-averages for each TC cluster. These calculations involve Gaussian kernel
 277 density estimation, which is provided by the `gaussian_kde` function of the SciPy Python-based package
 278 (Jones et al. 2001), with the estimator bandwidth determined using Scott's Rule. In other words, we
 279 calculate

$$280 \quad PDF_{sub} = PDF_{sub}(year) = p(VWS_{sub}, PI_{sub} | JJASON) \quad - (8a)$$

$$281 \quad PDF_{tot} = PDF_{tot}(year) = p(VWS_{tot}, PI_{tot} | JJASON) \quad - (8b)$$

282 which represent the average large-scale environment in each cluster, for each season.

283

284 As will be discussed in Section 5, we consider the typical environment in which an RI event occurs.
285 We calculate the PDF of VWS and PI values averaged over a $10^\circ \times 10^\circ$ box, centered at the storm on the
286 day an RI event occurs, for all RI occurrences in the period 1980-2015. The PDF is denoted as PDF_{RI} .
287 When defining the day at which an RI event occurs, we consider the 6-hourly time evolution of TC
288 intensity from HURDAT2, and compute the average date (\bar{d} , YY-MM-DD, where $\bar{\cdot}$ represents average
289 over the variable \cdot), time (\bar{t} , UTC) and location ($\overline{lat}, \overline{lon}$) of all 6-hourly positions at which TC
290 intensity increases by over 30 knots in its subsequent 24-hour period. Since the environmental
291 parameters are obtained from daily-resolution MERRA time series, VWS and PI values at date \bar{d} ,
292 averaged over a $10^\circ \times 10^\circ$ box centered at ($\overline{lat}, \overline{lon}$), is considered as a representation of the typical RI
293 environment. The distribution of all such representations is used to construct PDF_{RI} .

294

295 Similarly, the typical environment in which a TC occurs (PDF_{TC}) is computed using VWS and PI
296 values averaged over a $10^\circ \times 10^\circ$ box, centered at every 6-hourly TC position, for all TC occurrences in
297 the period 1980-2015. Since TC positions are obtained 6-hourly from HURDAT2, but VWS and PI
298 values are at daily resolution, up to four TC positions may correspond to the same set of daily VWS
299 and PI values from MERRA. In this case, however, this set of VWS and PI values is averaged over
300 different $10^\circ \times 10^\circ$ boxes following the 6-hourly TC best track, and will therefore still lead to different
301 environments used to compute PDF_{TC} . In notation form, PDF_{RI} and PDF_{TC} could be written as:

$$302 \quad PDF_{RI} = p(VWS, PI | 10^\circ \times 10^\circ \text{ centered at RI, } 1980 - 2015) \quad - (9a)$$

$$303 \quad PDF_{TC} = p(VWS, PI | 10^\circ \times 10^\circ \text{ centered at TC, } 1980 - 2015) \quad - (9b)$$

304 Then, we calculate the convolution of PDF_{sub} and PDF_{tot} with PDF_{RI} , as a measure of how conducive
305 the large-scale environment is to RI (how close the environment is to one in which RI occurs) in each
306 season, i.e. we consider

307 $C_{sub}(year) \equiv convolution(PDF_{sub}(year), PDF_{RI}) \quad - (10a)$

308 $C_{tot}(year) \equiv convolution(PDF_{tot}(year), PDF_{RI}) \quad - (10b)$

309 The convolution framework is then extended from the North Atlantic to the Northeast Pacific and
 310 Northwest Pacific basins, to test the robustness of the statistical results. TC data for the Northeast
 311 Pacific, again for the period of 1980-2015, is obtained from the HURDAT2 dataset (Landsea and
 312 Franklin 2013), while that for the Northwest Pacific is obtained from best-track data compiled by the
 313 Joint Typhoon Warning Center, as part of the International Best Track Archive for Climate
 314 Stewardship dataset (IBTrACS, Knapp et al. 2010).

315

316 To further study the statistical sensitivity of rapid intensification to VWS and PI, PDF_{RI} is fitted to a
 317 two-dimensional hyperbolic tangent function of the form

318 $PDF_{RI} = c_1 \cdot \tanh(c_2VWS + c_3PI + c_4VWS \cdot PI + c_5) + c_6 \quad - (11)$

319 The motivations, assumptions and implications of this curve fitting are discussed in Section 5. The
 320 fitting is performed with the `curve_fit` function of SciPy, which adopts the Levenberg-Marquardt
 321 Algorithm for nonlinear least-squares curve fitting, optimizing the parameter values of the fitted
 322 function to minimize the sum of squared residuals between the fitted and actual data.

323

324 **3. Seasonal Environmental Controls on RI**

325

326 This section presents the statistical analysis of the seasonal large-scale environmental controls on RI
327 for each North Atlantic TC cluster.

328

329 **3a. Location and Statistics of Clusters**

330

331 A K-means cluster analysis is first performed on HURDAT2 with four clusters, as described in Section
332 2b. These four clusters are plotted in Figure 1, indicating their regional distinction and hence potential
333 insufficiency to categorize North Atlantic RI by entire-basin statistics. Cluster 0 is centered at the
334 subtropics, while cluster 1 is centered at the Gulf of Mexico and western Caribbean Sea. Both clusters
335 2 and 3 contain tropical cyclones that form in the open tropical Atlantic; the former cluster tends to
336 move along the subtropical ridge and dissipate (or undergo extratropical transition) at higher latitudes,
337 while the latter tends to dissipate within the tropics. While these two clusters are centered in the open
338 North Atlantic, a significant portion of these TCs that experience RI do make landfall along the East
339 Coast of the United States (Figure 2). Table 1 displays the basic statistics for each TC cluster,
340 including the number of TCs, the number of TCs that experience RI, and the percentage of TCs that
341 experience RI. Although Kossin et al. (2010) used a different clustering method which involved a
342 mixture of quadratic regression models, and performed their computation with TC data from different
343 time periods, their four clusters also include a subtropical cluster, and tropical storms that are zonally
344 separated into a subset of Gulf of Mexico storms and those that span the MDR, as is the case here.

345

346 **3b. Sub-basin Environmental Controls**

347

348 **(i) Linear Regression**

349

350 As mentioned in the introduction, the variance of $n(RI)$ is not entirely explained by that of N , so the
351 potential predictability of $p(RI)$ is fundamental to the predictability of annual RI counts. Indeed,
352 analysis of the basinwide annual RI counts gives a variance of 3.68, out of which 30% is from the
353 variance of N , *i.e.*, $var(N(t) \cdot \bar{p}) = 1.11$, where \bar{p} represents the time-average over the annual counts.
354 On the other hand, over 58% of the variance is associated with the probability of RI, *i.e.*, $var(p(t) \cdot$
355 $\bar{N}) = 2.15$. Thus, we linearly regress the interannual variability of $n(RI)$ and $p(RI)$ in each cluster on
356 the seasonal-mean large-scale atmospheric and oceanic variables, to study whether seasonal
357 environmental anomalies have a significant role in controlling the statistics of seasonal RI occurrence.
358
359 The annual $n(RI)$ and $p(RI)$ in clusters 0 and 3 is frequently zero, giving a weak signal and large
360 noise, and both the least-squares and median of pairwise slopes regressions give a constant response of
361 $p(RI)$ to the variables (*i.e.* the regression line has zero slope, not shown). For these two clusters, it
362 appears that there are too few RI occurrences to perform statistically sound analysis. A longer record
363 with reliable RI data could help mitigate this issue. In addition, the behavior of subtropical TC rapid
364 intensifications (in cluster 0, hereafter C0) may be influenced by tropical-extratropical interactions and
365 transient baroclinicity; Murakami et al. (2016a) obtained a lower level of seasonal predictability for
366 subtropical TCs than tropical ones in the North Atlantic for the GFDL CM2.5-FLOR model. On the
367 other hand, since both clusters 2 and 3 tropical cyclones form in the open tropical North Atlantic,
368 distinguishing between these TC clusters near their time of genesis might be difficult from a practical
369 viewpoint, hence it might be worthwhile to combine the statistics for these two clusters (and this gives
370 more robust statistical results). Hence, for the remainder of this study we will focus on the RI
371 properties of cluster 1 (hereafter C1) and clusters 2 and 3 combined (hereafter C23).

372

373 Seasonal RI statistics of the open-ocean cluster (C23) are potentially predictable from some large-scale
374 atmospheric and oceanic conditions. The median of pairwise slopes regression response of $p(RI)$ to
375 the large-scale environmental variables for the entire North Atlantic (all clusters combined) is shown in
376 Figure 3, while that for C23 is shown in Figure 4. Similar results hold for least-squares regressions (not
377 shown). Figure 3 can be compared to Figure 9 of Wang et al. (2017), which show statistical regressions
378 of annual RI number, for data between 1950-2014; Figure 4 suggests that high $p(RI)$ of C23 across
379 seasons is associated with high seasonal PI, high RELSST and low VWS in the deep tropics,
380 particularly below 20°N. These correlations are significant at the 95% level in certain regions, for
381 MERRA, JRA-55, HadISST and NOAA OISST. Similar results hold for linear regressions with the
382 $n(RI)$ metric and with ASO-mean composites (not shown). MERRA SDEF, 850hPa relative humidity
383 and TCHP do not show statistically significant correlations to RI probability for C23. On the other
384 hand, the Gulf of Mexico cluster (C1) does not exhibit a statistically significant response to the
385 regional environmental anomalies. Some correlation exists at regions away from the typical TC
386 locations in C1 (Figure 1), and we interpret this as a coincidental correlation between variables as
387 opposed to any physical reasons connecting the non-local environment to RI in this cluster. From a
388 large-scale perspective, regional atmospheric and oceanic conditions less significantly impact RI for
389 C1 than C23; RI statistics in C23 vary interannually via the influence of regional sea-surface
390 temperature, potential intensity and vertical wind shear, and less so from atmospheric humidity.

391

392 **(ii) Logistic Regression**

393

394 Logistic regressions on the large-scale variables for C23 are shown in Figure 5: RELSST, VWS and PI
395 are significantly correlated with RI successes/failures in some portions of the deep tropical Atlantic,
396 though less ubiquitous than in the linear regression (particularly for VWS).

397

398 The interannual variability of RI counts and probability is modeled using Poisson regression and
399 binary logistic regression, respectively, with PI and VWS as exogenous co-regressors, using the
400 methodology outlined in Section 2c. The exogenous variables are averaged over 10°N-30°N, 100°W-
401 80°W for C1 (see magenta box in Figure 4a), and over 10°N-20°N, 80°W-20°W for C23 (considering
402 that this is the region which exhibits high $p(RI)$ correlation, see magenta box in Figure 4d). The results
403 of the statistical modeling for C1 and C23 are shown in Figure 6. Logistic regression is unskillful
404 relative to climatology in modeling RI probability of C1, while there is slight skill (14%) for C23.
405 Poisson regression is able to provide some skill for annual RI counts in both clusters, with higher skill
406 (27%) in C23. In addition, prediction of $n^*(RI)$ through separate predictions of N and $p(RI)$ shows
407 promise in both C1 and C23, since prediction for RI counts calculated as the product of predicted RI
408 probability and predicted TC counts shows comparable skill to the direct Poisson regression (Figure
409 6g-h).

410

411 In summary, statistical regressions suggest that for the tropical open-ocean cluster (C23), the
412 probability of storms experiencing RI in each season is correlated with seasonal regional
413 environmental anomalies, in particular those of vertical wind shear (VWS), relative sea-surface
414 temperature (RELSST) and potential intensity (PI). Thus, this cluster exhibits potential for RI seasonal
415 predictability through the seasonal large-scale environment. On the other hand, for the cluster of
416 tropical cyclones in the Gulf of Mexico and western Caribbean Sea (C1), the seasonal large-scale
417 environment does not exert significant controls on RI. Yet, on the seasonal timescale, why do these
418 TCs at similar latitudes of the North Atlantic exhibit such distinctive relationships to the large-scale
419 environmental anomalies? What is so ‘special’ about the Gulf of Mexico region that leads to the

420 observed differences in RI environmental controls? We will explore into this question in the next
421 section.

422

423 4. Hypotheses for Sub-basin Difference

424

425 In Section 3, we showed that on seasonal timescales, the statistics of RI activity in terms of probability
426 and annual counts are significantly influenced by seasonal VWS, PI and RELSST, for the TC cluster in
427 the Central/Eastern tropical North Atlantic (C23), but not for the Gulf of Mexico/Western Caribbean
428 cluster (C1). Such a difference is also depicted in Figure 9c of Wang et al. (2017); the physical reasons
429 for which, however, was not explored in their study. Why does there exist a difference in the seasonal
430 large-scale environmental controls on RI between these TC clusters? Given the result of the statistical
431 regressions above, and following some existing literature as discussed in Section 2a, we will focus on
432 two environmental parameters shown to influence RI activity, namely VWS and PI, so that the
433 physical model (Section 1) simplifies to the form $dI/dt = \tau^{-1}(PI - I)$, where $\tau = \tau(VWS)$.

434

435 We make the following hypotheses to explain the distinctive seasonal environmental controls on RI
436 between C1 and C23:

- 437 1. The weaker seasonal environmental control on RI in C1 than C23 results from the seasonal
438 anomalies of VWS and PI being less ‘cooperative’ (less negatively correlated) in C1 than C23.
- 439 2. We also hypothesize that there is a contribution from the climatology in C1 being overall more
440 conducive to RI than C23, so that a larger magnitude of environmental changes is needed to
441 influence seasonal variations of RI activity in C1. In other words, the seasonal RI statistics is less
442 sensitive to seasonal environmental changes in C1 than C23, giving a weaker ‘signal’. In C23, the
443 more cooperative nature of the seasonal anomalies of VWS and PI, superimposed on its less RI-
444 conducive climatology, is significant to influence RI activity on interannual timescales.
- 445 3. Our final hypothesis is that the reduced seasonal reproducibility of RI activity in C1 is driven by
446 larger subseasonal (weather and intraseasonal timescale) fluctuations (‘noise’), contributing to its
447 weaker seasonal ‘signal’. Subseasonal variations are smaller in C23, so that its seasonal large-scale
448 environment can significantly impact seasonal RI statistics.

449

450 In Section 5, we will discuss the framework to examine these hypotheses, and establish the validity of

451 some of these hypotheses in each subsection.

452

453 **5. Discussion of Sub-basin Difference**

454

455 This section examines each of the hypotheses presented in Section 4 by exploring the connections
456 between the typical RI environment and variations of the large-scale environment in C1 and C23.

457

458 **5a. Framework for Exploring Variations of VWS and PI**

459 To examine the relationship between the seasonal large-scale environment and RI statistics, we study
460 the variations of the large-scale environment in each cluster, again taking the average of 10°N-30°N,
461 100°W-80°W for C1, and that of 10°N-20°N, 80°W-20°W for C23. In particular, as described in
462 Section 2d, we study the daily VWS and PI variations (denoted by X , where $X = VWS, PI$)
463 decomposed into a climatology \bar{X} , an interannual variability $\langle X \rangle$, and a subseasonal X' component, for
464 C1 (hereafter denoted by the subscript W for C1 in Western North Atlantic) and C23 (subscript E for
465 C23 in Central/Eastern North Atlantic), from which the subseasonal (X_{sub}) and total (X_{tot}) variations
466 are calculated. We build a framework to consider the VWS-PI phase space, and compute the
467 subseasonal (PDF_{sub}) and total (PDF_{tot}) cluster-average VWS and PI values (the *average cluster*
468 *environment* in each season), and the distribution of VWS and PI during RI events (PDF_{RI} , the *typical*
469 *RI environment*).

470

471 We then hypothesize that RI activity in each cluster is connected to how close the *average cluster*
472 *environment* is to the *typical RI environment*, and compute $C_{sub}(year)$ and $C_{tot}(year)$. As mentioned
473 in Section 2d, these convolutions quantify the conduciveness of the seasonal large-scale environment
474 in each cluster to RI. Indeed, comparing between PDF_{RI} and PDF_{TC} (Figure 7) suggests that during RI
475 events, VWS (PI) is generally lower (higher) than the average TC environment. In other words, most
476 RI occurs during the low-VWS and high-PI stages relative to the entire TC life cycle. Similar results

477 are obtained using PDF_{RI} and PDF_{TC} trained with RI and TC cases from the North Atlantic, Northeast
478 Pacific and Northwest Pacific combined.

479

480 **5b. Role of Interannual Variability $\langle X \rangle$**

481 We test our hypothesis by first comparing between the interannual variability terms $\langle X \rangle_W$ and $\langle X \rangle_E$. As
482 can be seen in Figure 8, the seasonal anomalies of VWS and PI are more negatively correlated in C23
483 (correlation = -0.7586) than C1 (correlation = -0.2260). That is, these two variables tend to reinforce
484 each other in C23, for example by becoming more RI-conducive by decreasing VWS and increasing
485 PI. This convergence can potentially bring the climate towards the typical RI environment (high PDF_{RI}
486 region, lower right in the VWS-PI phase space, see Figure 7c) in some years, and away from it in
487 others.

488

489 Next, we test whether $\langle X \rangle$ plays a significant role in affecting the interannual variability of RI statistics.
490 As illustrated in Section 2d, the difference between $C_{tot}(year)$ and $C_{sub}(year)$ indicates the role of
491 $\langle X \rangle$. Figure 9 suggests that for C23, C_{tot} is significantly correlated with $n(RI)$ and $p(RI)$ over the
492 period of 1980-2015 (Spearman correlation = 0.60, 0.44 respectively). This supports our hypothesis
493 that the convolution, being a measure of how close the average cluster environment is to the typical RI
494 environment, could be used as a proxy for RI activity. However, when the interannual variability of the
495 environment is excluded, C_{sub} now has no significant relationship with both RI metrics, and RI
496 predictability is lost. Also, the variance of the convolution decreases by about 9.8 times, as opposed to
497 about 3.3 times for C1. The larger difference between C_{tot} and C_{sub} in C23 than C1 indicates a larger
498 role of the environmental interannual variability in shifting VWS and PI in and out of the region
499 favorable for RI (in the VWS-PI space). Therefore, in C23, seasonal timescale fluctuations of the
500 environment $\langle X \rangle$ can explain the interannual variability of RI statistics: When the interannual

501 variability of the environment pushes climate into (away from) RI-conducive region, leading to high
502 (low) convolution C_{tot} , RI probability is high (low). Such results do not hold for C1; the correlation to
503 RI metrics does not decrease from C_{tot} to C_{sub} .

504

505 PDF_{RI} is averaged over $10^\circ \times 10^\circ$ boxes (see Section 2d), so the above calculation is repeated with
506 PDF_{sub} and PDF_{tot} computed using values averaged at consecutive $10^\circ \times 10^\circ$ boxes in each cluster
507 (instead of averages over the entire cluster), to provide a more consistent comparison. In this case,
508 X_{sub} , X_{tot} and $\langle X \rangle$ for C23 consist of VWS and PI values over six east-west oriented boxes, while
509 those for C1 consist of four boxes. As in the previous calculation, VWS and PI are more negatively
510 correlated in C23 than C1, and C_{tot} is significantly correlated with both RI counts and RI probability in
511 C23 (not shown). In addition, similar results hold when PDF_{sub} and PDF_{tot} are calculated using VWS,
512 PI values weighted by RI density in each cluster (instead of using box averages, Figure 10), and also
513 hold for PDF_{RI} trained with RI from the North Atlantic, Northeast Pacific and Northwest Pacific
514 combined (yielding 768 cases in total, Figure 11).

515

516 **5c. Role of Mean Climatology \bar{X}**

517 We now test the hypothesis that different states of climatology between C1 and C23 may lead to
518 different responses of RI statistics to seasonal environmental changes. A cluster environment that is
519 very close to high PDF_{RI} values will require larger changes in the environment to significantly affect
520 the convolution, than one that lies away from the high PDF_{RI} values (e.g. lying at regimes where
521 PDF_{RI} has a large gradient in the VWS-PI phase space). Figure 12 compares between the average
522 cluster environments \bar{X}_W and \bar{X}_E , and suggests that: (1) \bar{X}_E has higher VWS and lower PI than \bar{X}_W ; (2)
523 \bar{X}_E has higher VWS and lower PI at a larger portion of the season than \bar{X}_W . Thus, the climatology is
524 indeed different between C1 and C23, with the latter being on average further away from RI-conducive

525 values in the VWS-PI phase space, so that RI activity can potentially have a larger response to changes
526 in the cluster environment. In other words, RI activity is potentially more sensitive to environmental
527 changes in C23.

528

529 However, is the larger sensitivity of RI activity to seasonal environmental changes in C23 significant
530 to provide environmental controls on RI seasonal statistics? If this were true, it would mean that if C23
531 had a lower sensitivity, just like in C1, then the interannual variability of RI statistics would be lost. In
532 other words, if C23 had the less sensitive climatology of C1, does this different sensitivity change the
533 significance of $\langle X \rangle$ in determining RI? For this purpose, we switch between the climatology of C1 and
534 C23, and compare between the convolutions calculated with the C23 environment $\bar{X}_E + \langle X \rangle_E + X'_E$ and
535 the hypothetical environment $\bar{X}_W + \langle X \rangle_E + X'_E$.

536

537 Calculations indicate that switching between C1 and C23 climatology leads to very different
538 convolutions (correlation = -0.36), and the hypothetical convolution has no correlation with $n(RI)$ and
539 $p(RI)$ (correlation = -0.15, -0.01 respectively). However, considering PDF_{RI} and PDF_{tot} in the VWS-
540 PI phase space suggests that in the hypothetical situation where C23 now has the C1 climatology, the
541 new PDF_{tot} now lies in the phase space where PDF_{RI} drops to zero at very high PI and low VWS
542 values. We interpret this as an artifact of the limited number of RI samples observed (134 samples in
543 the period of 1980-2015): Such RI has not been observed since it is rare for TCs to be existent when
544 the environment attains such extreme VWS and PI values. While an RI event at such extreme values
545 has not been observed, we posit that the decrease of PDF_{RI} at these values is unphysical; PDF_{RI} should
546 monotonically increase with PI and decrease with VWS. To correct this sampling issue, PDF_{RI} is fitted
547 to a two-dimensional hyperbolic tangent function of VWS and PI (Figure 13), using the methodology
548 described in Section 2d. The curve fitting as shown is performed using $VWS \in [0,40]$, $PI \in [30,81]$

549 as the support; these bounds are chosen to be close to the observed environmental VWS and PI limits,
550 and to minimize the variance of the parameter estimates. The choice of these bounds only affects the
551 curve fitting parameters but not the results of the convolutions presented above. Other bounds give a
552 similar shape to the fitted hyperbolic tangent curve as shown, though the values of the fitted PDF carry
553 no physical meaning since the choice of the bounds is artificial. This curve fitting to the hyperbolic
554 tangent function also assumes the following: (1) Favorability to RI monotonically increases with PI
555 and decreases with VWS, less so at extreme values than others and remains bounded; (2) The
556 simultaneous VWS decrease and PI increase is more conducive to RI than to changes in only one
557 variable; (3) The c_4 term is added to include any possible nonlinearities in the variation of RI statistics
558 with VWS and PI. The convolutions of the fitted PDF_{RI} with PDF_{sub} and PDF_{tot} behave similarly to
559 those shown in Figure 9 (not shown), and the standard deviation of the parameter estimates amounts to
560 0.8-4% of the parameter values.

561

562 Having attempted to correct the sampling issue, the hypothetical convolution (with East-West
563 climatology switched) now looks like the before-switch convolution (correlation = 0.95), and is
564 significantly correlated with $n(RI)$ and $p(RI)$ (correlation = 0.52, 0.40 respectively). This implies that
565 even with C1 climatology, the negatively correlated $\langle X \rangle_E$ can explain interannual variations in RI
566 statistics in C23, indicating the importance of the interannual variability of VWS and PI over the
567 climatology. On the other hand, while we previously showed that $\langle X \rangle_W$ is not significant to explain RI
568 interannual variability in C1, this also holds if C1 had a less conducive C23 climatology (comparing
569 between $\bar{X}_W + \langle X \rangle_W + X'_W$ and $\bar{X}_E + \langle X \rangle_W + X'_W$), again indicating that the state of climatology plays
570 a secondary role compared to the interannual variability of VWS and PI. The importance of $\langle X \rangle$ only
571 breaks down at very extreme climatological values, for example when \bar{PI}_E is increased by at least 30
572 m/s (not shown), which is much larger than the projected PI increase over the 21st century (e.g. Vecchi

573 and Soden 2007, Yu et al. 2010, Camargo 2013, Knutson et al. 2013, Sobel et al. 2016, Vecchi et al.
574 2019).

575

576 **5d. Role of Subseasonal Variations X'**

577 Lastly, we study the impact of subseasonal environmental variability on the interannual variability of
578 RI statistics, and test whether the significance of $\langle X \rangle_E$ depends on X'_E . For this purpose, we consider
579 the hypothetical situation in which C23 had the subseasonal variation of C1, and compare between the
580 convolutions calculated with $\bar{X}_E + \langle X \rangle_E + X'_E$ and $\bar{X}_E + \langle X \rangle_E + X'_W$ (i.e. switching between C1 and
581 C23 subseasonal variations). These convolutions are very similar to each other (correlation = 0.92,
582 Figure 14a), and the exclusion of $\langle X \rangle$ from $\bar{X} + X'$ decreases variance of the convolution by 10.48
583 times, similar to results shown previously. In addition, similar results hold when comparing the
584 original convolution with that calculated with $\bar{X}_E + \langle X \rangle_E + X'_{2010,E}$ (using subseasonal variations in
585 say year 2010 for all years, Figure 14b). This highlights the importance of the negatively correlated $\langle X \rangle$
586 in C23 over X' (and the interannual variability of X') in explaining interannual variations of RI
587 statistics.

588

589 In summary, the argument presented in this section suggests that the negatively correlated seasonal
590 anomalies of VWS and PI are significant controls of seasonal RI statistics in C23, while the mean
591 climatology and subseasonal variations of the large-scale environment are not important, at least for
592 ‘realistic’ magnitudes. Meanwhile, VWS and PI vary less consistently interannually in C1, so that
593 $\langle X \rangle_W$ is not a significant control on the interannual variability of seasonal RI statistics. This results in a
594 relatively larger importance of subseasonal variations of the environment or storm-scale dynamics in
595 controlling RI in C1 than C23 – and, accordingly, lower seasonal predictability. This finding is
596 consistent with that of Kossin et al. (2010), in which they suggested that TCs in the Gulf of Mexico are

597 strongly modulated by the Madden-Julian Oscillation, which is known to modulate TCs on subseasonal
598 timescales (e.g. Maloney and Hartmann 2000).

599

600 **6. Concluding Remarks**

601

602 This study is concerned with the large-scale environmental controls on the seasonal statistics of RI of

603 North Atlantic TCs. Statistical analysis indicates that on interannual timescales, increased probability

604 of TCs undergoing RI in the open tropical North Atlantic (C23) is significantly related to increased

605 seasonal relative sea-surface temperature (RELSST), increased potential intensity (PI), and decreased

606 vertical wind shear (VWS). However, tropical cyclones in the Gulf of Mexico and western Caribbean

607 Sea (C1) and the Sargasso Sea (C0) do not exhibit such behavior.

608

609 We demonstrated that the interannual variability of RI statistics in C23 is significantly controlled by

610 the *negatively correlated* ('cooperative') interannual variability of VWS and PI, due to which seasonal

611 anomalies of VWS and PI act constructively to change the probability that the environment will move

612 in and out of the 'RI-favorable' space (region of high PDF_{RI} in the VWS-PI space). At least for

613 'realistic' magnitudes, changes in the mean climatology, which we hypothesized might have lead to

614 different sensitivities of RI activity to environmental changes, and changes in subseasonal variations of

615 the large-scale environment are not significant to alter the seasonal environmental controls on RI.

616 Making assumptions on the likelihood of RI at very extreme VWS and PI values beyond the currently

617 observed range, the importance of the interannual variability of VWS and PI breaks down at extreme

618 climatological values beyond future climate projections, which suggest that projected changes in

619 climate may not affect RI seasonal predictability assuming small changes in the interannual variability

620 of the large-scale environment.

621

622 On the other hand, for the Gulf of Mexico cluster (C1), the seasonal anomalies of VWS and PI are

623 weakly correlated and do not significantly control RI statistics on seasonal timescales, suggesting the

624 potential importance of subseasonal environmental variability and storm-scale dynamics in controlling

625 RI. In the former sense, RI occurrences over this region could be mostly considered as ‘weather-
626 related’ events.

627

628 This study provides a step towards RI seasonal predictability by exploring the statistical sensitivity of
629 RI to large-scale environmental anomalies. Our statistical framework is developed using two climate
630 predictors, while future study could include more RI predictors such as sea-surface height, high-
631 altitude divergence, and others used by Kaplan et al. (2010). In addition, the analysis presented in this
632 study could be repeated with inclusion of the most recent hurricane seasons, as new data becomes
633 available. The finding here that a significant seasonal environmental control on RI is determined by the
634 negative correlation of VWS and PI seasonal anomalies, invites applications to other basins in which
635 the distribution of RI activity could be compared to that of the correlation between seasonal VWS and
636 PI in these basins. In addition, VWS and PI are among the factors discussed in Camargo et al. (2007)
637 to influence genesis of tropical cyclones, while Tang and Emanuel (2012) modeled the probability of
638 TC genesis as a function of the ventilation index (which depends on VWS, PI and entropy deficit).
639 These suggest that the interannual correlation between VWS and PI may be extended to one involving
640 other environmental anomalies to understand the seasonal predictability of TC activity across the
641 tropics. Noting the significance of VWS and PI interannual variability in controlling RI in the
642 Central/Eastern tropical North Atlantic, another application is to investigate whether coupled climate
643 models could be used to predict VWS and PI seasonal anomalies in this region as a means of RI
644 seasonal predictability, in both present and future climates. In particular, our findings highlight the
645 importance of assessing future changes in the correlation between seasonal anomalies of VWS and PI,
646 as opposed to changes in their absolute values, in speculating the potential of future RI seasonal
647 predictability through climate change simulations. Lastly, work is underway to understand the physical
648 mechanisms behind the observed strong (weak) negative correlation between VWS and PI in C23

649 (C1), and more generally to understand physical controls of the spatial distribution of such a
650 correlation across global ocean basins.

651

652 In light of the societal impact of rapidly intensifying TCs, this research is aimed at improving our
653 understanding of their predictability on seasonal timescales through exploring their statistical
654 connections with large-scale atmospheric and oceanic conditions. It is apparent that improved forecasts
655 for the seasonal statistics of rapidly intensifying TCs that occur closer to land would be more beneficial
656 to society than those further away. The results from this study show that on seasonal timescales, RI
657 experienced by TCs furthest away from land (C23) are the most predictable, some of which indeed
658 making landfall on the eastern sector of the Caribbean and North American region (Figure 2). The
659 seasonal statistics of RI events that occur closer to the East Coast of the United States (C0), and those
660 that affect population in Central America, Mexico and southern United States (C1), seem to be less
661 predictable than their counterparts in the open tropical North Atlantic.

662

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664

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668

669 **References**

670

- 671 1. Barnston, A.G., Tippett, M.K., L'Heureux, M.L., Li, S. and DeWitt, D.G., 2012: Skill of real-time
672 seasonal ENSO model predictions during 2002-11: Is our capability increasing?. *Bulletin of the*
673 *American Meteorological Society*, 93, 631-651
- 674 2. Behringer, D.W., Ji, M. and Leetmaa, A., 1998: An improved coupled model for ENSO prediction
675 and implications for ocean initialization. Part I: The ocean data assimilation system. *Monthly*
676 *Weather Review*, 126, 1013-1021
- 677 3. Bhatia, K., Vecchi, G., Murakami, H., Underwood, S. and Kossin, J., 2018: Projected response of
678 tropical cyclone intensity and intensification in a global climate model. *Journal of Climate*, 31,
679 8281-8303
- 680 4. Bhatia, K.T., Vecchi, G.A., Knutson, T.R., Murakami, H., Kossin, J., Dixon, K.W. and Whitlock,
681 C.E., 2019: Recent increases in tropical cyclone intensification rates. *Nature communications*, 10,
682 635
- 683 5. Bister, M. and Emanuel, K.A., 1998: Dissipative heating and hurricane intensity. *Meteorology and*
684 *Atmospheric Physics*, 65, 233-240
- 685 6. Bister, M. and Emanuel, K.A., 2002: Low frequency variability of tropical cyclone potential
686 intensity 1. Interannual to interdecadal variability. *Journal of Geophysical Research: Atmospheres*,
687 107, ACL-26
- 688 7. Bosart, L.F., Bracken, W.E., Molinari, J., Velden, C.S. and Black, P.G., 2000: Environmental
689 influences on the rapid intensification of Hurricane Opal (1995) over the Gulf of Mexico. *Monthly*
690 *Weather Review*, 128, 322-352
- 691 8. Camargo, S.J., Emanuel, K.A. and Sobel, A.H., 2007: Use of a genesis potential index to diagnose
692 ENSO effects on tropical cyclone genesis. *Journal of Climate*, 20, 4819-4834
- 693 9. Camargo, S.J., 2013: Global and regional aspects of tropical cyclone activity in the CMIP5 models.
694 *Journal of Climate*, 26, 9880-9902

- 695 10. Chen, X., Wang, Y., Zhao, K. and Wu, D., 2017: A numerical study on rapid intensification of
696 Typhoon Vicente (2012) in the South China Sea. Part I: Verification of simulation, storm-scale
697 evolution, and environmental contribution. *Monthly Weather Review*, 145, 877-898
- 698 11. Chiang, J.C. and Vimont, D.J., 2004: Analogous Pacific and Atlantic meridional modes of tropical
699 atmosphere-ocean variability. *Journal of Climate*, 17, 4143-4158
- 700 12. DeMaria, M., Knaff, J.A. and Sampson, C., 2007: Evaluation of long-term trends in tropical
701 cyclone intensity forecasts. *Meteorology and Atmospheric Physics*, 97, 19-28
- 702 13. Elsberry, R.L., Lambert, T.D. and Boothe, M.A., 2007: Accuracy of Atlantic and eastern North
703 Pacific tropical cyclone intensity forecast guidance. *Weather and Forecasting*, 22, 747-762
- 704 14. Elsberry, R.L., 2014: Advances in research and forecasting of tropical cyclones from 1963-2013.
705 *Asia-Pacific Journal of Atmospheric Sciences*, 50, 3-16
- 706 15. Elsner, J.B., 2003: Tracking hurricanes. *Bulletin of the American Meteorological Society*, 84, 353-
707 356
- 708 16. Elsner, J.B. and Liu, K.B., 2003: Examining the ENSO-typhoon hypothesis. *Climate Research*, 25,
709 43-54
- 710 17. Emanuel, K., 2010: Tropical cyclone activity downscaled from NOAA-CIRES reanalysis, 1908-
711 1958. *Journal of Advances in Modeling Earth Systems*, 2
- 712 18. Emanuel, K., 2017: Will global warming make hurricane forecasting more difficult?. *Bulletin of*
713 *the American Meteorological Society*, 98, 495-501
- 714 19. Enfield, D.B. and Mayer, D.A., 1997: Tropical Atlantic sea surface temperature variability and its
715 relation to El Niño-Southern Oscillation. *Journal of Geophysical Research: Oceans*, 102, 929-945
- 716 20. Ge, X., Shi, D. and Guan, L., 2018: Monthly variations of tropical cyclone rapid intensification
717 ratio in the western North Pacific. *Atmospheric Science Letters*, 19, e814
- 718 21. Gray, W.M., 1984: Atlantic seasonal hurricane frequency. Part I: El Niño and 30mb quasi-biennial
719 oscillation influences. *Monthly Weather Review*, 112, 1649-1668

- 720 22. Hendricks, E.A., Peng, M.S., Fu, B. and Li, T., 2010: Quantifying environmental control on
721 tropical cyclone intensity change. *Monthly Weather Review*, 138, 3243-3271
- 722 23. Hurrell, J.W., Kushnir, Y., Ottersen, G. and Visbeck, M., 2003: An overview of the North Atlantic
723 Oscillation. *The North Atlantic Oscillation: Climatic significance and environmental impact*, 134,
724 1-35
- 725 24. Jones E, Oliphant E, Peterson P, et al. *SciPy: Open Source Scientific Tools for Python*, 2001
- 726 25. Kaplan, J. and DeMaria, M., 2003: Large-scale characteristics of rapidly intensifying tropical
727 cyclones in the North Atlantic basin. *Weather and Forecasting*, 18, 1093-1108
- 728 26. Kaplan, J., DeMaria, M. and Knaff, J.A., 2010: A revised tropical cyclone rapid intensification
729 index for the Atlantic and eastern North Pacific basins. *Weather and Forecasting*, 25, 220-241,
730 doi:10.1175/2009WAF2222280.1
- 731 27. Klotzbach, P.J., 2012: El Niño-Southern Oscillation, the Madden-Julian Oscillation and Atlantic
732 basin tropical cyclone rapid intensification. *Journal of Geophysical Research: Atmospheres*, 117
- 733 28. Knapp, K.R., Kruk, M.C., Levinson, D.H., Diamond, H.J. and Neumann, C.J., 2010: The
734 international best track archive for climate stewardship (IBTrACS) unifying tropical cyclone data.
735 *Bulletin of the American Meteorological Society*, 91, 363-376
- 736 29. Knutson, T.R., Sirutis, J.J., Vecchi, G.A., Garner, S., Zhao, M., Kim, H.S., Bender, M., Tuleya,
737 R.E., Held, I.M. and Villarini, G., 2013: Dynamical downscaling projections of twenty-first-
738 century Atlantic hurricane activity: CMIP3 and CMIP5 model-based scenarios. *Journal of Climate*,
739 26, 6591-6617
- 740 30. Kobayashi, S., Ota, Y., Harada, Y., Ebita, A., Moriya, M., Onoda, H., Onogi, K., Kamahori, H.,
741 Kobayashi, C., Endo, H. and Miyaoka, K., 2015: The JRA-55 reanalysis: General specifications
742 and basic characteristics. *Journal of the Meteorological Society of Japan. Ser. II*, 93, 5-48
- 743 31. Kossin, J.P., Camargo, S.J. and Sitkowski, M., 2010: Climate modulation of North Atlantic
744 hurricane tracks. *Journal of Climate*, 23, 3057-3076

- 745 32. Landsea, C.W. and Franklin, J.L., 2013: Atlantic hurricane database uncertainty and presentation
746 of a new database format. *Monthly Weather Review*, 141, 3576-3592
- 747 33. Lanzante, J.R., 1996: Resistant, robust and non-parametric techniques for the analysis of climate
748 data: Theory and examples, including applications to historical radiosonde station data.
749 *International Journal of Climatology: A Journal of the Royal Meteorological Society*, 16, 1197-
750 1226
- 751 34. Lee, C.Y., Tippett, M.K., Sobel, A.H. and Camargo, S.J., 2016: Rapid intensification and the
752 bimodal distribution of tropical cyclone intensity. *Nature communications*, 7, 10625
- 753 35. Lin, I.I., Chen, C.H., Pun, I.F., Liu, W.T. and Wu, C.C., 2009: Warm ocean anomaly, air sea
754 fluxes, and the rapid intensification of tropical cyclone Nargis (2008). *Geophysical Research*
755 *Letters*, 36
- 756 36. Liu, M., Vecchi, G.A., Smith, J.A., Murakami, H., Gudgel, R. and Yang, X., 2018: Towards
757 Dynamical Seasonal Forecast of Extratropical Transition in the North Atlantic. *Geophysical*
758 *Research Letters*, 45, 12-602
- 759 37. Lloyd, I.D., Marchok, T. and Vecchi, G.A., 2011: Diagnostics comparing sea surface temperature
760 feedbacks from operational hurricane forecasts to observations. *Journal of Advances in Modeling*
761 *Earth Systems*, 3
- 762 38. Maloney, E.D. and Hartmann, D.L., 2000: Modulation of hurricane activity in the Gulf of Mexico
763 by the Madden-Julian oscillation. *Science*, 287, 2002-2004
- 764 39. Murakami, H., Vecchi, G.A., Underwood, S., Delworth, T.L., Wittenberg, A.T., Anderson, W.G.,
765 Chen, J.H., Gudgel, R.G., Harris, L.M., Lin, S.J. and Zeng, F., 2015: Simulation and prediction of
766 category 4 and 5 hurricanes in the high-resolution GFDL HiFLOR coupled climate model. *Journal*
767 *of Climate*, 28, 9058-9079

- 768 40. Murakami, H., Vecchi, G.A., Villarini, G., Delworth, T.L., Gudgel, R., Underwood, S., Yang, X.,
769 Zhang, W. and Lin, S.J., 2016a: Seasonal forecasts of major hurricanes and landfalling tropical
770 cyclones using a high-resolution GFDL coupled climate model. *Journal of Climate*, 29, 7977-7989
- 771 41. Murakami, H., Villarini, G., Vecchi, G.A., Zhang, W. and Gudgel, R., 2016b: Statistical-dynamical
772 seasonal forecast of North Atlantic and US landfalling tropical cyclones using the high-resolution
773 GFDL FLOR coupled model. *Monthly Weather Review*, 144, 2101-2123
- 774 42. Rappaport, E.N., Franklin, J.L., Avila, L.A., Baig, S.R., Beven, J.L., Blake, E.S., Burr, C.A., Jiing,
775 J.G., Juckins, C.A., Knabb, R.D. and Landsea, C.W., 2009: Advances and challenges at the
776 National Hurricane Center. *Weather and Forecasting*, 24, 395-419
- 777 43. Ramsay, H.A., Camargo, S.J. and Kim, D., 2012: Cluster analysis of tropical cyclone tracks in the
778 Southern Hemisphere. *Climate Dynamics*, 39, 897-917
- 779 44. Rayner, N.A., Parker, D.E., Horton, E.B., Folland, C.K., Alexander, L.V., Rowell, D.P., Kent, E.C.
780 and Kaplan, A., 2003: Global analyses of sea surface temperature, sea ice, and night marine air
781 temperature since the late nineteenth century. *Journal of Geophysical Research: Atmospheres*, 108
- 782 45. Reynolds, R.W., Smith, T.M., Liu, C., Chelton, D.B., Casey, K.S. and Schlax, M.G., 2007: Daily
783 high-resolution-blended analyses for sea surface temperature. *Journal of Climate*, 20, 5473-5496
- 784 46. Rienecker, M.M., Suarez, M.J., Gelaro, R., Todling, R., Bacmeister, J., Liu, E., Bosilovich, M.G.,
785 Schubert, S.D., Takacs, L., Kim, G.K. and Bloom, S., 2011: MERRA: NASA's modern-era
786 retrospective analysis for research and applications. *Journal of climate*, 24, 3624-3648
- 787 47. Ryan, B.F., Watterson, I.G. and Evans, J.L., 1992: Tropical cyclone frequencies inferred from
788 Gray's yearly genesis parameter: Validation of GCM tropical climates. *Geophysical Research*
789 *Letters*, 19, 1831-1834
- 790 48. Seabold, S. and Perktold, J., 2010: Statsmodels: Econometric and statistical modeling with python.
791 In *Proceedings of the 9th Python in Science Conference*, 57, 61

- 792 49. Shapiro, L.J., 1987: Month-to-month variability of the Atlantic tropical circulation and its
793 relationship to tropical storm formation. *Monthly Weather Review*, 115, 2598-2614
- 794 50. Shieh, O.H., Fiorino, M., Kucas, M.E. and Wang, B., 2013: Extreme rapid intensification of
795 Typhoon Vicente (2012) in the South China Sea. *Weather and Forecasting*, 28, 1578-1587
- 796 51. Shu, S., Ming, J. and Chi, P., 2012: Large-scale characteristics and probability of rapidly
797 intensifying tropical cyclones in the western North Pacific basin. *Weather and Forecasting*, 27,
798 411-423
- 799 52. Smirnov, D. and Vimont, D.J., 2011: Variability of the Atlantic Meridional Mode during the
800 Atlantic hurricane season. *Journal of Climate*, 24, 1409-1424
- 801 53. Sobel, A.H., Camargo, S.J., Hall, T.M., Lee, C.Y., Tippett, M.K. and Wing, A.A., 2016: Human
802 influence on tropical cyclone intensity. *Science*, 353, 242-246
- 803 54. Tang, B. and Emanuel, K., 2012: A ventilation index for tropical cyclones. *Bulletin of the*
804 *American Meteorological Society*, 93, 1901-1912
- 805 55. Truchelut, R.E., Hart, R.E. and Luthman, B., 2013: Global identification of previously undetected
806 pre-satellite-era tropical cyclone candidates in NOAA/CIRES Twentieth-Century Reanalysis data.
807 *Journal of Applied Meteorology and Climatology*, 52, 2243-2259
- 808 56. Vecchi, G.A. and Soden, B.J., 2007: Effect of remote sea surface temperature change on tropical
809 cyclone potential intensity. *Nature*, 450, 1066
- 810 57. Vecchi, G.A., Zhao, M., Wang, H., Villarini, G., Rosati, A., Kumar, A., Held, I.M. and Gudgel, R.,
811 2011: Statistical-dynamical predictions of seasonal North Atlantic hurricane activity. *Monthly*
812 *Weather Review*, 139, 1070-1082
- 813 58. Vecchi, G.A., Fueglistaler, S., Held, I.M., Knutson, T.R. and Zhao, M., 2013: Impacts of
814 atmospheric temperature trends on tropical cyclone activity. *Journal of Climate*, 26, 3877-3891

- 815 59. Vecchi, G.A., Delworth, T., Gudgel, R., Kapnick, S., Rosati, A., Wittenberg, A.T., Zeng, F.,
816 Anderson, W., Balaji, V., Dixon, K. and Jia, L., 2014: On the seasonal forecasting of regional
817 tropical cyclone activity. *Journal of Climate*, 27, 7994-8016
- 818 60. Vecchi, G.A., Delworth, T.L., Murakami, H., Underwood, S.D., Wittenberg, A.T., Zeng, F.,
819 Zhang, W., Baldwin, J.W., Bhatia, K.T., Cooke, W. and He, J., 2019: Tropical cyclone sensitivities
820 to CO2 doubling: roles of atmospheric resolution, synoptic variability and background climate
821 changes. *Climate Dynamics*, 53, 5999-6033
- 822 61. Villarini, G., Vecchi, G.A. and Smith, J.A., 2010: Modeling the dependence of tropical storm
823 counts in the North Atlantic basin on climate indices. *Monthly Weather Review*, 138, 2681-2705
- 824 62. Vimont, D.J. and Kossin, J.P., 2007: The Atlantic Meridional Mode and hurricane activity.
825 *Geophysical Research Letters*, 34
- 826 63. Vimont, D.J., 2012: Analysis of the Atlantic Meridional Mode using linear inverse modeling:
827 Seasonality and regional influences. *Journal of Climate*, 25, 1194-1212
- 828 64. Wang, B. and Zhou, X., 2008: Climate variation and prediction of rapid intensification in tropical
829 cyclones in the western North Pacific. *Meteorology and Atmospheric Physics*, 99, 1-16
- 830 65. Wang, C., Wang, X., Weisberg, R.H. and Black, M.L., 2017: Variability of tropical cyclone rapid
831 intensification in the North Atlantic and its relationship with climate variations. *Climate Dynamics*,
832 49, 3627-3645
- 833 66. Watterson, I.G., Evans, J.L. and Ryan, B.F., 1995: Seasonal and interannual variability of tropical
834 cyclogenesis: Diagnostics from large-scale fields. *Journal of climate*, 8, 3052-3066
- 835 67. Wing, A.A., Emanuel, K. and Solomon, S., 2015: On the factors affecting trends and variability in
836 tropical cyclone potential intensity. *Geophysical Research Letters*, 42, 8669-8677
- 837 68. Wong, M.L. and Chan, J.C., 2004: Tropical cyclone intensity in vertical wind shear. *Journal of the*
838 *atmospheric sciences*, 61, 1859-1876

- 839 69. Yu, J., Wang, Y. and Hamilton, K., 2010: Response of tropical cyclone potential intensity to a
840 global warming scenario in the IPCC AR4 CGCMs. *Journal of Climate*, 23, 1354-1373
- 841 70. Zhang, W., Vecchi, G.A., Murakami, H., Villarini, G. and Jia, L., 2016a: The Pacific meridional
842 mode and the occurrence of tropical cyclones in the western North Pacific. *Journal of Climate*, 29,
843 381-398
- 844 71. Zhang, W., Vecchi, G.A., Murakami, H., Delworth, T., Wittenberg, A.T., Rosati, A., Underwood,
845 S., Anderson, W., Harris, L., Gudgel, R. and Lin, S.J., 2016b: Improved simulation of tropical
846 cyclone responses to ENSO in the western North Pacific in the high-resolution GFDL HiFLOR
847 coupled climate model. *Journal of Climate*, 29, 1391-1415
- 848 72. Zhuge, X.Y., Ming, J. and Wang, Y., 2015: Reassessing the use of inner-core hot towers to predict
849 tropical cyclone rapid intensification. *Weather and Forecasting*, 30, 1265-1279

850

851 **Tables**

852

853 Table 1: The number of TCs, the number of RI events, and the ratio between these two variables, in
854 each TC cluster. Cluster analysis is performed with the K-means method, for HURDAT2 data between
855 1979-2015

856

	Number of TCs, N	Number of RI events, $n(RI)$	$p(RI) = n(RI)/N$
Cluster 0	134	23	17%
Cluster 1	158	59	37%
Cluster 2	82	58	71%
Cluster 3	79	21	27%

857

858 **Figure Captions**

859

860 **Fig. 1** TC density for each cluster, defined by the number of TC 6-hourly positions per year over a
861 $10^\circ \times 10^\circ$ box centered at each location. Also shown are the average locations of genesis, maximum
862 intensity and lysis for each cluster

863

864 **Fig. 2** Tracks of TCs that experience RI, in each cluster in the North Atlantic. Crosses indicate landfall
865 positions of these TCs, as indicated in the HURDAT2 dataset. The title in each subplot indicates the
866 number of such landfalling RI TCs, and the percentage of landfall TCs that experience RI

867

868 **Fig. 3** Slope of the linear (median of pairwise slopes) regression of JJASON-mean MERRA PI,
869 HadISST RELSST and MERRA VWS with RI probability, for all TCs in the North Atlantic.
870 Regressions at 95% statistical significance are shaded in crosses, while those at 90% are shaded in dots

871

872 **Fig. 4** Slope of the linear (median of pairwise slopes) regression of JJASON-mean MERRA PI,
873 HadISST RELSST and MERRA VWS with RI probability, for (a-c) C1 and (d-f) C23. The magenta
874 boxes indicate areas over which averages for C1 and C23 are computed. (g-i) As in (d-f), but for PI,
875 RELSST and VWS from JRA-55 and NOAA OISST. Regressions at 95% statistical significance are
876 shaded in crosses, while those at 90% are shaded in dots

877

878 **Fig. 5** As in Figure 4d-f, but for logistic regression with the slope parameter β_1 plotted

879

880 **Fig. 6** Observed and predicted (a-b) RI probability ($p^*(RI)$, predicted with the binary logistic
881 regression), (c-d) RI counts ($n^*(RI)$, predicted with the Poisson regression) and (e-f) TC counts (N ,

882 predicted with the Poisson regression), for C1 and C23. (g-h) Prediction for RI counts in C1 and C23
883 calculated as the product of predicted RI probability and predicted TC counts

884

885 **Fig. 7** The typical large-scale environment in which RI and TCs exist. The green shading and contours
886 show the two-dimensional probability density function (a) PDF_{RI} , for all 134 RI occurrences in C1 and
887 C23 during the period of 1980-2015, and (b) PDF_{TC} , for all TCs in C1 and C23 during the same
888 period. (c) The difference between PDF_{RI} and PDF_{TC} . (d-f) As in (a-c), but for all 768 RI occurrences
889 and all TCs in the North Atlantic, Northeast Pacific and Northwest Pacific combined

890

891 **Fig. 8** Interannual variability $\langle X \rangle$ of VWS and PI values in C1 (left) and C23 (right), where each dot
892 represents one JJASON season. Seasonal anomalies of VWS and PI are more negatively correlated in
893 C23 than C1

894

895 **Fig. 9** Reconstruction of RI seasonal statistics without and with interannual variability of the large-
896 scale environment, as given by C_{sub} (blue) and C_{tot} (red) respectively, for C1 (left) and C23 (right),
897 over the 36-year period of 1980-2015. See text for a description of these convolutions. The tables
898 below show the lag-zero Spearman correlation of C_{sub} and C_{tot} with seasonal $p(RI)$ and $n(RI)$
899 statistics in each cluster. Statistical significance is computed with the Student's t-test using $36-2=34$
900 degrees of freedom, as provided by the SciPy statistical package

901

902 **Fig. 10** As in Figures 8 and 9, but with PDF_{sub} and PDF_{tot} calculated using VWS and PI values
903 weighted by RI density for each cluster, instead of box averages over the cluster region

904

905 **Fig. 11** As in Figure 9, but with PDF_{RI} calculated using all RI events in the North Atlantic, Northwest
906 Pacific and Northeast Pacific combined (shown in Figure 7d)

907

908 **Fig. 12** Two-dimensional probability density function PDF_{RI} (green contours, as in Figure 7a) in the
909 VWS-PI space, superimposed by that of the 1980-2015 MERRA climatological JJASON seasonal
910 cycle \bar{X} (blue) and scalar-mean JJASON climatology $\bar{\bar{X}}$ (red), where $X = VWS, PI$, averaged for C1
911 (left) and C23 (right)

912

913 **Fig. 13** Best fit of the North Atlantic PDF_{RI} (shown in Figure 7a) to the hyperbolic tangent function in
914 the VWS-PI space, as described in Section 2d

915

916 **Fig. 14** Impact of subseasonal environmental variability (X') on seasonal RI statistics in C23. (a)
917 Convolution between PDF_{RI} and the two-dimensional PDF computed from $\bar{X}_E + \langle X \rangle_E + X'_E$ (blue) or
918 $\bar{X}_E + \langle X \rangle_E + X'_W$ (red), where X'_E and X'_W represents subseasonal variations in C23 and C1
919 respectively. See text for a full explanation of these variables. (b) As in (a), but the red plot indicates
920 the convolution computed using subseasonal variations in C23 in 2010 for all years ($\bar{X}_E + \langle X \rangle_E +$
921 $X'_{2010,E}$)