

# Multi-species Stock Assessment for walleye pollock, Pacific cod, and arrowtooth flounder in the Eastern Bering Sea

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## Executive Summary

This is a three species stock assessment for walleye pollock (*Gadus chalcogrammus*), Pacific cod (*Gadus macrocephalus*) and arrowtooth flounder (*Atheresthes stomias*), from the Eastern Bering Sea (EBS), Alaska updated from Holsman et al. (in press). Results are presented from models estimated and projected without trophic interactions (single-species mode, SSM) and with trophic interactions (multi-species mode, MSM). The main features and settings for this multispecies model include:

- Predation natural mortality was specified to be age specific and annually varying (M2). Residual (non-predation) natural mortality (M1) was age specific but not-annually varying and differs slightly from current assessments for each species (see Table 3 below).
- Predator overlap index was set to 1 for all species (i.e., all prey are available to all predators).
- A Ricker stock recruitment curve is fit a sub-model within CEATTLE by providing point estimates of stock and recruits and estimating parameters for projection purposes. For this assessment, optional environmental covariates were omitted.
- Weights at age were estimated outside of the model using a temperature-dependent von Bertalanffy models using the original series and assume 2012 weight at ages for 2013-2016.
- The acoustic trawl survey selectivity estimates were specified to equal the SAFE report model estimates (earlier versions of the model omitted age composition information from this survey).
- Fisheries selectivity and survey selectivity were specified to be age specific but held constant over time.
- Predator-prey suitability was also age-specific and constant over time.
- Arrowtooth flounder stock was treated as sexes combined (weight at age was estimated separately for males and females and combined using a mortality-based mean).
- Maturity schedules were based on 2012 assessments and differ slightly from 2015 assessments.

Key updates from the original paper include:

- Pacific cod fishery composition data was based on lengths rather than model estimates of catch at age.
- Bottom temperature was based on average survey bottom temperatures (observed) for the Bering Sea and are updated through 2015.
- Projected bottom temperatures were held constant at mean historical values (constant) rather than using climate forecasts.

- Only two harvest control rules are presented here: (1) harvest rate that results in spawning biomass at 40% of unfished biomass (for all three species simultaneously) and (2) aggregate multi-species MSY.
- Bottom trawl survey data now includes 2012-2016 (Holsman et al. *in press* was only through 2011) and was updated for each species based on most recent assessment data.

Results from model runs show that pollock total and spawning biomass remains relatively high and similar to the past 3 years. Multispecies model predictions may indicate a slight decline in total and spawning biomass in 2016. Pacific cod total biomass remains relatively high, although may be slightly lower in 2016 than 2015. Female spawning biomass continues to increase steadily after a low in 2008. Arrowtooth total and spawning biomass estimates suggest declines after a peak in 2008.

Pollock recruitment is down in 2016 for the second year in a row and is lower than estimates for the past ten years (i.e., since 2006). Both single and multi-species models predict that recruitment will increase next year. Pacific cod recruitment is up slightly from 2015, but remains below the 10-year average. Estimates of Arrowtooth flounder recruitment are below average.

For ABC and mMSY estimates the model was projected through the year 2103 (to attain relative equilibrium). This allowed estimating a proxy for  $B_{40\%}$  using the approach of Holsman et al. (*in press*) and Moffitt et al. (*in press*) where the model is projected under no fishing (simultaneously for all three species), and then projected under fishing to iteratively solve for the harvest rate that results in and average of 40% of unfished biomass in the last 5 years of the projection (2098-2103).

To derive multispecies MSY (mMSY), we similarly projected the model to iteratively find the harvest rate that maximized aggregate (all species) yield in the last 5 years of the projection (2095-2100).

Summary of assessment results for 2016:

	Walleye pollock		Pacific cod		Arrowtooth flounder	
Quantity	SSM	MSM	SSM	MSM	SSM	MSM
2016 M (natural mortality age 1)	0.900	2.021	0.340	1.044	0.269	0.897
2016 Average 3+ M (across ages)	0.300	0.317	0.340	0.340	0.226	0.229
2016 total (age 3+) biomass (t)	14,646,800	15,043,940	1,313,105	1,308,296	517,976	513,575
2016 Female spawning biomass; (t)	5,418,040	5,570,280	241,631	239,867	375,576	372,533
*Projected $SSB_0$ (t)	5,332,960	3,907,090	435,039	413,799	482,457	446,320
*Projected $SSB_{40\%}$ (t)	2,135,160	1,562,800	174,503	165,509	192,974	178,519
**Projected $SSB_{mMSY}$	3,016,420	3,665,360	160,413	153,413	3,858	7,902
ABC <sub>2100</sub> (t)	2,364,920	2,393,050	172,224	174,295	30,941	33,030
**mMSY <sub>2100</sub> (t)	2,075,700	2,749,000	172,208	176,166	1,658	3,529
<sup>†</sup> $F_{proxy}$	0.772	1.353	0.334	0.359	0.106	0.121
$F_{mMSY}$	0.385	0.443	0.367	0.396	0.279	0.287

\* SSB is based on the projected SSB at 2100 (~equilibrium).

\*\* mMSY is aggregate multi-species yield

<sup>†</sup>  $F_{proxy}$  is the fishing mortality that reduces the multispecies spawning biomass to 40% of unfished level.

## Response to SSC and Plan Team comments

### General comments:

Comments specific the Multi-species stock assessment model (CEATTLE)

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*The BSAI Plan discussed the additive property of the natural (residual) and predation mortalities in the multispecies model. Some Team members felt that the single species model should already incorporate the main components of natural mortality, so there was concern about using these values as base levels in the multispecies model. They felt that the “residual” mortality should be specified at a lower value than the single species assessment, since predation mortality will be explicitly accounted.*

The residual mortality inputs in the model were updated to meet this recommendation. For single species mode the residual mortality matches that of current single species assessment models for pollock, Pacific cod, and arrowtooth flounder. The multi-species mode uses the same residual mortality vectors except for the ages 1 and 2 mortality rates for pollock, which were adjusted downward to 0.01 and 0.30, respectively.

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*The Team also discussed future plans and what other species might best be added. It may be useful to outline short- and long-term utilities of the multi-species approach. The Team discussed whether the predator-prey interaction between fur seals and pollock might be a logical next step for the multi-species approach. There was also a discussion about the possible short-term utility of the model to provide a potential mechanism (predation) to explain why certain cohorts that are initially predicted to be large may fail to materialize in subsequent years.*

Sections titled “short-term utility” and “long-term utility” of the multi-species approach” were added to the end of the assessment. These sections discuss potential applications of the multispecies approach for assessment advice.

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*The Team recommends using a lower (residual)  $M$  in the multi-species model for comparisons with the single-species stock assessment values.*

As stated above the residual natural mortality values were adjusted downward to meet this recommendation.

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*The Team also recommends working with MML staff to include fur seals as part of the multi-species model.*

In October 2016, MML staff and CEATTLE authors collaborated on a joint proposal to add fur seals to the CEATTLE model. This proposal was submitted and identified as a priority during an internal regional climate action plan request for “shovel ready” projects in October (funding to be determined). A similar proposed study would extend that approach to evaluate drivers of changes in fur seal pup production and is anticipated to be submitted in November as a North Pacific Research Board proposal.

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*Finally, the Team recommends including the multi-species stock assessment as an Appendix to the EBS Pollock stock assessment in November.*

This assessment is included as an appendix to the EBS pollock assessment.

## Introduction

### MSCAA models for evaluating annually varying $M$

Multi-species statistical catch-at-age models (MSCAA) are an example of a class of multi-species ‘Models with Intermediate Complexity for Ecosystem assessments’ (i.e., MICE; Plagányi et al., 2014), which have particular utility in addressing both strategic and tactical EBFM questions (Hollowed et al. 2013; Fogarty 2014; Link and Browman 2014; Plagányi et al., 2014). MSCAA models may increase

forecast accuracy, may be used to evaluate propagating effects of observation and process error on biomass estimates (e.g., Curti 2013; Ianelli et al., *in press*), and can quantify climate and trophic interactions on species productivity. As such MSCAA models can address long recognized limitations of prevailing single species management, notably non-stationarity in mortality and maximum sustainable yield (MSY), and may help reduce risk of overharvest (Link 2010; Plagányi et al., 2014; Fogarty 2014). Because multispecies biological references points (MBRPs) from MSCAA model are conditioned on the abundance of other species in the model (Collie and Gislason 2001; Plagányi et al., 2014; Fogarty 2014), they may also have utility in setting harvest limits for multi-species fleets, evaluating population dynamics in marine reserves or non-fishing areas, and quantifying trade-offs that emerge among fisheries that impact multiple species in a food web (see reviews in Pikitch et al., 2004; Link 2010; Levin et al., 2013; Link and Browman 2014; Fogarty 2014).

Depending on their structure, MSCAA models can be used to evaluate climate- and fisheries-driven changes to trophodynamic processes, recruitment, and species abundance (Plagányi et al., 2014). MSCAA models differ somewhat among systems and species, but most use abundance and diet data to estimate fishing mortality, recruitment, stock size, and predation mortality simultaneously for multiple species in a statistical framework. Similar to age structured single species stock assessment models widely used to set harvest limits, MSCAA models are based on a population dynamics model, the parameters of which are estimated using survey and fishery data and maximum likelihood methods (e.g., Jurado-Molina et al., 2005; Kinzey and Punt, 2009; Van Kirk et al., 2010; Kempf 2010; Curti et al., 2013; Tsehay et al., 2014). Unlike most single-species models (but see Hollowed et al. 2000b; Spencer et al. 2016), MSCAA models additionally separate natural mortality into residual and annually varying predation mortality, and model the latter as a series of predator-prey functional responses. Thus, natural mortality rates for each species in MSCAA models depend on the abundance of predators in a given year and vary annually with changes in recruitment and harvest of each species in the model.

MSCAA models have specific utility in quantifying direct and indirect effects of fisheries harvest on species abundance and size distributions (see reviews in Hollowed et al., 2000a, 2013; Link 2010; Fogarty 2014; Link and Browman 2014; Plagányi et al., 2014), which is important for EBFM and trade-off analyses of various management strategies. Rapidly shifting climate conditions are also of growing concern in fisheries management as changes in physical processes are known to influence individual growth, survival, and reproductive success of fish and shellfish (Hanson et al., 1997; Kitchell et al., 1977; Morita et al., 2010; Hollowed et al., 2013; Cheung et al., 2015). Climate-driven changes in water temperature can directly impact metabolic costs, prey consumption, and somatic or gonadal tissue growth, with attendant indirect effects on survival, production, and sustainable harvest rates (e.g., Hanson et al., 1997; Morita et al., 2010; Cheung et al., 2015). Temperature-dependent predation, foraging, metabolic, and growth rates are common in more complex spatially-explicit food web or whole of ecosystem models such as GADGET (e.g., Howell and Bogstad 2010; Taylor et al., 2007), Atlantis (e.g., Fulton et al., 2011; Kaplan et al., 2012; 2013), and FEAST (Ortiz et al., *in press*). Temperature functions for growth and predation can also be incorporated into MSCAA models, allowing this class of models to be used to evaluate interacting climate, trophodynamic, and fishery influences on recommended fishing mortality rates.

Numerous studies point to the importance of using multi-species models for EBFM (see review in Link 2010). Multi-species production models produced different estimates of abundances and harvest rates than single species models for Northeast US marine ecosystems (Gamble and Link, 2009; Tyrrell et al., 2011), and MSY of commercial groundfish stocks estimated from aggregated production models are different than the sum of MSY estimates from single-species assessments (Mueter and Megrey, 2006; Gaichas et al., 2012; Smith et al., 2015). Multi-species models have been used to demonstrate long-term increases in yield of Icelandic stocks of Atlantic cod (*Gadus morhua*) and reductions in capelin (*Mallotus villosus*) and Northern shrimp (*Pandalus borealis*) catch associated with short-term decreases in cod

harvest (Danielsson et al., 1997). Kaplan et al. (2013) demonstrated the disproportionately large ecosystem impacts of applying the same  $F_x$  (e.g.,  $F_x$ , or the harvest rate that reduces spawning stock biomass to  $x\%$  of unfished spawning stock biomass,  $SSB_0$ ; Caddy and Mahon, 1995; Collie and Gislason, 2001) harvest control rule approach to forage fish as is used for groundfish in the northeast Pacific, and trophodynamics in a southern Benguela ecosystem resulted in higher carrying capacity for small pelagic species under fishing (versus no-fishing) scenarios (Smith et al., 2015).

Since natural mortality and recruitment rates in a MSCAA model are conditioned on harvest rates of predators in the model, an ongoing area of research is evaluating MSCAA model analogs to single-species biological reference points (see Moffitt et al., in press), such as harvest rates that correspond to maximum yield ( $F_{MSY}$ ) or proxies thereof (e.g.,  $F_{proxy}$ ). Other multi-species models have been used to derive and evaluate MBRPs, although these have largely focused on MSY (e.g., Kaplan et al., 2013; Smith et al., 2015). A notable exception is Collie and Gislason (2001), who evaluated a variety of MBRPs using a multi-species, virtual population analysis and found MBRPs to be sensitive to variation in natural mortality (much less so to variability in growth), and as such proposed that fishing mortality reference levels for prey species with high mortality be conditioned on the level of predation mortality. Building on this approach, Moffitt et al. (in press) recently demonstrated a projection approach for using multi-species models to derive a variety of MBRPs for EBFM. This provides a basis for the application of MSCAA models for increased use in tactical and strategic EBFM decision-making across a diversity of management frameworks worldwide.

### **MSCAA for EBM in Alaska**

The eastern Bering Sea (Alaska), is defined by large, climate-driven changes to trophodynamics and species productivity that can vary on annual and multi-annual timescales (see reviews in Aydin and Mueter 2007; Hunt et al., 2011; Stabeno et al., 2012; Baker et al., 2014). Accordingly, fisheries management in Alaska has a long history of using ecosystem information and multi-species models for strategic management advice (e.g., multi-species model-based indices, such as mean trophic level, are regularly reported in the annual Ecosystem Considerations chapter of Alaska Stock Assessment and Fishery Evaluation (SAFE) reports; see review in Livingston et al., 2011). Development of multiple MSCAA models in the region (Jurado-Molina et al., 2005; Kinzey and Punt, 2009; Van Kirk, 2010) has advanced regional management closer to EBFM, facilitating use of estimates from MSCAA models in single-species models used for tactical decisions in the region. For instance, Dorn et al. (2014) recently evaluated predation mortality estimates from a regional MSCAA model developed by Van Kirk (2010) to inform natural mortality for the Gulf of Alaska walleye pollock (*Gadus chalcogrammus*, hereafter “pollock”) stock assessment.

MSCAA models may be most useful for species that exhibit strong trophic interactions (predator and prey species) or contrasting management or biological constraints that require simultaneous evaluation (Link 2010). In the eastern Bering Sea, pollock support one of the largest fisheries worldwide, with over 1.2 million metric tons (t) harvested per year (representing ~99% of the annual quota; Ianelli et al., 2014). Pollock are both predators (adults) and prey (i.e., ages <2; Dunn and Matarese, 1987; Nishiyama et al., 1986) for a variety of species including cannibalistic conspecifics (e.g., Boldt et al., 2012). Variable climate conditions, particularly the spatial extent of winter sea ice, the timing of sea ice spring melt, and subsequent summer bottom temperatures, can differentially promote survival of pollock and their predators and/or modulate predator and prey overlap in the region (e.g., Baily 1989; Zador et al., 2011; Boldt et al. 2012; Hunsicker et al. 2013; Baker and Hollowed 2014). Diet analyses suggest Pacific cod (*Gadus macrocephalus*), cannibalistic adult pollock, and arrowtooth flounder (*Atheresthes stomias*), amongst others, are important predators of pollock populations in the eastern Bering Sea (Livingston 1993; Aydin and Mueter 2007; Mueter et al., 2007).

### Multispecies model

Here we present a three species MSCAA model for the Bering Sea (hereafter CEATTLE, for Climate-Enhanced, Age-based model with Temperature-specific Trophic Linkages and Energetics) that includes temperature-dependent von Bertalanffy weight-at-age functions (VBGF; von Bertalanffy, 1938) and temperature-specific, bioenergetics-based predation interactions. CEATTLE, is an example of an “environmentally-enhanced” stock assessment model (*sensu* Link 2010), where temperature-specific algorithms predict size-at-age and predation mortality. The MSCAA is programmed in AD model builder (Fournier et al., 2012), and builds on earlier models that combine catch-at-age assessment models with multi-species virtual population analysis (MSVPA) in a statistical framework (i.e., Jurado-Molina et al., 2005). Abundance and biomass of each cohort is modeled using standard population dynamics equations, accounting for a plus age group (Table 1, Eqs. T1.3, T1.4, T1.5). The initial age-structure is assumed to correspond to unfished equilibrium, and the numbers of each species at age 1 each year are treated as estimable parameters (Eqs. T1.1 and T1.2). Total mortality of each prey species  $i$ , age  $j$  (or predator species  $p$  age  $a$ ) in each year  $y$  is the sum of mortality due to predators in the model ( $M2_{ij,y}$ ), fishing mortality ( $F_{ij,y}$ ), and residual mortality ( $M1_{ij}$ ), Eq. T1.8). Predation mortality (Eq. T2.1) is based on the assumption that the annual age-specific ration of a predator is allocated to prey species of a given age according to predator selectivity (Table 2, Eq. T2.2). Predator selectivity is based on the suitability function derived by Jurado-Molina et al. (2005) and fit to available data from 1981-2015, while annual ration is a function of temperature-specific allometric relationships between ration and fish weight based on bioenergetics models for each species (Eqs. T2.4 and T2.5; Table 7; see Holsman et al. *in press*, and Holsman and Aydin, 2015 for more detail).

The length-to-weight relationships, predator size and species diet preference, bioenergetics-based, temperature-specific predator rations, and maturity are based on previous studies (Tables 1 and 2; Table 7, Table 8; Holsman et al. Holsman and Aydin, 2015, Holsman et al. *in press*). Size-specific diet compositions for each species were assumed known based on diet data collected during the AFSC bottom trawl survey (i.e., diet data are not included in the objective function) and trophic patterns in survey and fishery-based diet data were used to calculate mean (across years and stations) predator-prey suitability (Eq. T2.2).

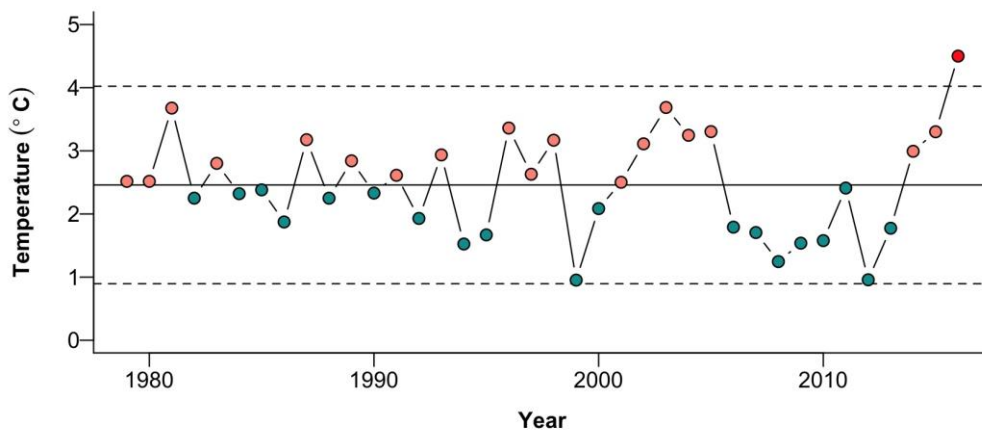


Figure 1. Mean summer bottom temperature for the Eastern Bering Sea; blue and red represent temperatures below or above (respectively) the long-term mean; dashed lines represent 2 standard deviations from the mean.

### Temperature specific weight at age

Water temperature is known to directly impact growth through influencing metabolic and digestion rates, which often scale exponentially with body weight and temperature (see Hanson et al., 1997 for an overview). Thus we modified the generalized formulation of the von Bertalanffy growth function (VBGF; von Bertalanffy 1938; Pauly 1981; Temming 1994) to predict temperature-dependent growth by allowing the allometric scaling parameter  $d$  to increase with temperature. See Essington et al. (2010) and Holsman and Aydin (2015), and Holsman et al. (in press) for descriptions on the derivation and application of the VBGF towards bioenergetics modeling. In this formulation  $d$  represents the realized allometric slope of consumption, which integrates both the direct effect of temperature on consumption and indirect ecological interactions that scale with temperature and influence relative foraging rates (see Essington et al., 2010; Holsman and Aydin, 2015). We fit the VBGF to otolith-based length- and weight-at-age data ( $n = 21,388, 14,362$ , and  $772$ , for pollock, Pacific cod, and arrowtooth flounder, respectively) collected during AFSC Bering Sea surveys and analyzed at the AFSC such that:

$$W_{ij,y} = W_{\infty,iy} \left( 1 - e^{(-K_i(1-d_{i,y})(j-t_{0,i}))} \right)^{\frac{1}{1-d_{i,y}}} e^{\varepsilon}, \text{ where } \varepsilon \sim N(0, \sigma_{di}^2) \quad \text{Eq. 1}$$

where  $t_{0,i}$  is the age at which  $W_{ij,y} = 0$ ,  $W_{\infty,iy}$  is the asymptotic mass which can vary by species  $i$  and year  $y$  (i.e.,  $W_{\infty,iy} = \left(\frac{H_i}{K_i}\right)^{1/(1-d_{i,y})}$ ),  $H_i$  is the assimilation constant  $K_i$  is the energy loss constant (Essington et al., 2010), and  $\varepsilon$  is a normally and independently distributed random variable with mean 0 and variance  $\sigma_{di}^2$ . Essington et al. (2010) and Holsman and Aydin, (2015) statistically estimated the  $d$ ,  $K$  and  $H$  parameters for various species to estimate consumption rates. In particular, Holsman and Aydin (2015) found that the  $d$  parameter varied between species and regions in Alaska (USA). We further modified this approach to estimate  $d$  annually for each year  $y$  in the dataset, as a linear function of temperature  $T_y$  such that:

$$d_{i,y} = e^{(\alpha_{0,i} + \alpha_{d,i}T_y + \beta_{d,i}T_y)} \quad \text{Eq. 2}$$

where  $\alpha_{0,i}$  and  $\alpha_{d,i}$  represent the mean  $d$  intercept and  $\beta_{d,i}$  is the coefficient for the residual effect of temperature on the  $d$  consumption parameter. We chose this formulation based on the empirical relationship between temperature and consumption, assuming that  $d$  would capture the differential effects of temperature on growth, and that waste rates scale proportionally with weight but do not vary over time with diet or temperature (i.e.  $K$  is constant but  $d$  can vary with temperature). This formulation allows both the slope and asymptotic limit of growth to vary with temperature. Similar approaches, with slightly different modifications to the VBGF, including temperature and prey specific terms for  $d$  and  $k$ , respectively, have been used elsewhere to evaluate climate impacts on fish growth (e.g., Cheung et al., 2015; Hamre, 2003).

Table 1. Population dynamics equations for species  $i$  and age  $j$  in each simulation year  $y$ . BT indicates the AFSC bottom trawl survey and EIT represents the echo-integrated acoustic-trawl survey. For all other parameter definitions see Table 3.

Definition	Equation		
Recruitment	$N_{i1,y} = R_{i,y} = R_{0,i} e^{\tau_{i,y}}$	$\tau_{i,y} \sim N(0, \sigma^2)$	T1.1
Initial abundance	$N_{ij,1} = \begin{cases} R_{0,i} e^{(-j M_{1,i})} N_{0,ij} & y=1 \quad 1 < j \leq A_i \\ R_{0,i} e^{(-j M_{1,i})} N_{0,ij} / (1 - e^{(-j M_{1,i})}) & y=1 \quad j > A_i \end{cases}$		T1.2
Numbers at age	$N_{ij+1,y+1} = N_{ij,y} e^{-Z_{ij,y}} \quad 1 \leq y \leq n_y \quad 1 \leq j < A_i$ $N_{iA_i,y+1} = N_{iA_i-1,y} e^{-Z_{iA_i-1,y}} + N_{iA_i,y} e^{-Z_{iA_i,y}} \quad 1 \leq y \leq n_y \quad j > A_i$		T1.3
Catch	$C_{ij,y} = \frac{F_{ij,y}}{Z_{ij,y}} (1 - e^{-Z_{ij,y}}) N_{ij,y}$		T1.4
Total yield (kg)	$Y_{i,y} = \sum_j \left( \frac{F_{ij,y}}{Z_{ij,y}} (1 - e^{-Z_{ij,y}}) N_{ij,y} W_{ij,y} \right)$		T1.5
Biomass at age (kg)	$B_{ij,y} = N_{ij,y} W_{ij,y}$		T1.6
Spawning biomass at age (kg)	$SSB_{ij,y} = B_{ij,y} \rho_{ij}$		T1.7
Total mortality at age	$Z_{ij,y} = M_{1,ij} + M_{2,ij,y} + F_{ij,y}$		T1.8
Fishing mortality at age	$F_{ij,y} = F_{0,i} e^{\tau_{i,y}} s_{ij}^f$	$\varepsilon_{i,y} \sim N(0, \sigma_{\varepsilon,i}^2)$	T1.9
Weight at age (kg)	$W_{ij,y} = W_{\infty,ij} \left( 1 - e^{(-K_i(1-d_{i,y})(j-t_{0,i}))} \right)^{\frac{1}{1-d_{i,y}}}$ $d_{i,y} = e^{(\alpha_{4,i} + \alpha_{0,i} + \beta_{4,i} T_y)}$ $W_{\infty,ij} = \left( \frac{H_i}{K_i} \right)^{\frac{1}{1-d_{i,y}}}$		T1.10a T1.10b T1.10c
BT survey biomass (kg)	$\hat{\rho}_{i,y}^s = \sum_j \left( N_{ij,y} e^{-0.5 Z_{ij,y}} W_{ij,y} s_{ij}^s \right)$		T1.11
EIT survey biomass (kg)	$\hat{\rho}_{i,y}^{eit} = \sum_j \left( N_{ij,y} e^{0.5(-Z_{ij,y})} W_{ij,y} s_{ij}^{eit} q_{ij}^{eit} \right)$	(pollock only)	T1.12
Fishery age composition	$\hat{O}_{ij,y}^f = \frac{C_{ij,y}}{\sum_j C_{ij,y}}$		T1.13
BT survey age composition	$\hat{O}_{ij,y}^s = \frac{N_{ij,y} e^{0.5(-Z_{ij,y})} s_{ij}^s}{\sum_j \left( N_{ij,y} e^{0.5(-Z_{ij,y})} s_{ij}^s \right)}$		T1.14
EIT survey age composition	$\hat{O}_{ij,y}^{eit} = \frac{N_{ij,y} e^{0.5(-Z_{ij,y})} s_{ij}^{eit} q_{ij}^{eit}}{\sum_j \left( N_{ij,y} e^{0.5(-Z_{ij,y})} s_{ij}^{eit} q_{ij}^{eit} \right)}$	(pollock only)	T1.15
BT selectivity	$s_{ij}^s = \frac{1}{1 + e^{(-\frac{M_{1,i}}{A_{n,i}} - \tau_i^s)}}$		T1.16
Fishery selectivity	$s_{ij}^f = \begin{cases} e^{\eta_{ij}} & j \leq A_{n,i} \\ e^{\eta_{i,A_{n,i}}} & j > A_{n,i} \end{cases}$	$\eta_{ij} \sim N(0, \sigma_{\eta,i}^2)$	T1.17
Proportion females	$\omega_{ij} = \frac{e^{-j M_{fem}}}{e^{-j M_{fem}} + e^{-j M_{male}}}$		T1.18
Proportion of mature females	$\rho_{ij} = \omega_{ij} \phi_{ij}$		T1.19
Weight at age (kg)	$W_{ij,y} = W_{ij,y}^{fem} \omega_{ij} + (1 - \omega_{ij}) W_{ij,y}^{male}$		T1.20
Residual natural mortality	$M_{1,ij} = M_{ij}^{fem} \omega_{ij} + (1 - \omega_{ij}) M_{ij}^{male}$		T1.21

We used this approach to derive annual temperature-specific coefficients of  $d$  for pollock and Pacific cod (combined sexes) and separately for male and female arrowtooth flounder (Table 3; Table 8). For arrowtooth flounder, we then used the age-specific proportions of mature females ( $\rho_{ij}$ ) and males ( $1 - \rho_{ij}$ ) to derive the mean weight-at-age for both sexes combined (Eq. T1.19 and Table 8). Lastly, male and female natural mortality rates ( $M_{male}$  and  $M_{fem}$ , respectively for arrowtooth flounder only) and age-specific maturity proportions ( $\phi_{ij}$ ) from the 2012 stock assessments for eastern Bering Sea pollock (Ianelli et al., 2012), and Bering Sea and Aleutian Islands Pacific cod (Thompson and Lauth, 2012) and arrowtooth flounder (Spies et al., 2012), were used to derive estimates of the proportion of mature females at age ( $\rho_{ij}$ ; Eq. T1.18).



Table 2. Predation mortality (M2) equations for predators  $p$  of age  $a$ , and prey  $i$  of age  $j$ .

Definition	Equation	
Predation mortality	$M2_{ij,y} = \sum_{pa} \left( \frac{N_{pa,y} \delta_{pa,y} \bar{S}_{paij}}{\sum_{ij} (\bar{S}_{paij} B_{ij,y}) + B_p^{other} \left( 1 - \sum_{ij} (\bar{S}_{paij}) \right)} \right)$	T2.1
Predator-prey suitability	$\bar{S}_{paij} = \frac{1}{n_y} \sum_y \left( \frac{\frac{\bar{U}_{paij}}{B_{ij,y}}}{\sum_{ij} \left( \frac{\bar{U}_{paij}}{B_{ij,y}} \right) + \frac{1 + \sum_{ij} \bar{U}_{paij}}{B_p^{other}}} \right)$	T2.2
Mean gravimetric diet proportion	$\bar{U}_{paij} = \frac{\sum_y U_{paij,y}}{n_y}$	T2.3
Individual specific ration (kg kg <sup>-1</sup> yr <sup>-1</sup> )	$\delta_{pa,y} = \hat{\phi}_p \alpha_\delta W_{pa,y}^{(1+\beta_\delta)} f(T_y)_p$	T2.4
Temperature scaling algorithm	$f(T_y)_p = V^X e^{(X(1-V))}$	T2.5
	$V = (T_p^{cm} - T_y) / (T_p^{cm} - T_p^{co})$	T2.5a
	$X = \left( Z^2 \left( 1 + (1 + 40/Y)^{0.5} \right)^2 \right) / 400$	T2.5b
	$Z = \ln(Q_p^c) (T_p^{cm} - T_p^{co})$	T2.5c
	$Y = \ln(Q_p^c) (T_p^{cm} - T_p^{co} + 2)$	T2.5d

### Parameter estimation and data

The parameters of the model are either pre-specified or estimated by selecting parameters that minimize the log-likelihood function (Table 9) and include fishing mortality rates ( $F_{ij,y}$ ), fishery and survey selectivity ( $s_{ij}^f$  and  $s_{ij}^s$ , respectively), initial (pre-harvest) abundance in year 1979 ( $N_{0,ij}$ ), and annual recruitment ( $R_{i,y}$ ), while the estimable parameter of the likelihood function is the catchability coefficient for the acoustic survey ( $q_1^{eit}$ ; Table 3; Table 9). We fit the model to available survey and fishery data for the eastern Bering Sea including biomass estimates and age-composition data from the annual AFSC summer bottom trawl survey with the assumption that the survey catchability ( $q$ ) equals 1—an assumption that differs from the single species assessments, biomass and age-composition data from the AFSC Acoustic-trawl (AT) survey (pollock only), and the total fishery catch and fishery age-composition data collected by AFSC observers and analyzed at AFSC (Hilborn and Walters, 1992; Quinn and Deriso, 1999). Penalties were imposed on the changes over age in fishery selectivity (Table 9). Normal likelihood penalties were applied to the log of annual recruitment and the fisheries mortality deviations, as well as initial abundances. Selectivity for the AT survey was set to previously reported values (Table 9; Honkalehto et al., 2011; Ianelli et al., 2015).

Table 3. Parameter definition ( $n$  is the number of parameters for estimated parameters only, type, value (Plk: Pollock; Cod: Pacific cod; Atf: Arrowtooth flounder both sexes; Atf<sub>M</sub>: Arrowtooth flounder males; Atf<sub>F</sub>: Arrowtooth flounder females), and source. Types: I: Input parameter (assigned); M: model index; E: Estimated parameter; F: fixed parameter P: Derived quantity; D: Data.

Parameter	Definition	Type	Value	Source (see below)
$y$	Year	M	$[1,2,3 \dots n_y]$	e
$p$	Predator	M	$[1,2,3 \dots n_p]$	e
$a$	Predator age (years)	M	$[1,2,3 \dots A_p]$	e
$i$	Prey	M	$[1,2,3 \dots n_i]$	e
$j$	Prey age (years)	M	$[1,2,3 \dots A_i]$	e
$n_i$	Number of prey species	I	3	e
$n_p$	Number of predator species	I	3	e
$R_{0,i}$	Mean Recruitment; $n=[1,1,1]$	E	$\geq 0$	e
$\tau_{i,y}$	Annual recruitment deviation; $n=[34,34,34]$	E	number	e
$N_{0,ij}$	Initial abundance; $n=[11,11,20]$	E	$\geq 0$	e
$F_{0,i}$	Mean fishing mortality; $n=[1,1,1]$	E	$\geq 0$	e
$\varepsilon_{i,y}$	Annual fishing mort. deviation; $n=[34,11,20]$	E	number	e
$\eta_{ij}$	Fishery age selectivity coef. ; $n=[8,8,8]$	E	number	e
$b_i^s$	Survey age selectivity slope; $n=[1,1,1]$	E	number	e
$a_i^s$	Survey age selectivity limit ; $n=[1,1,1]$	E	number	e
$d_{i,y}$	VBGF allometric slope of consumption	P	$\geq 0$	e
$W_{\infty,iy}$	VBGF max asymptotic weight (kg)	P	$> 0$	e
$\rho_{ij}$	Proportion of mature females at age	P	$\in [0,1]$	e
$M1_{ij}$	Residual natural mortality	F	$\geq 0$	e, h
$n_y$	Number of simulation years	I	34	e
$y_0$	Start year	I	1979	e
$\omega_{ij}$	Female proportion of population	F	$\in [0,1]$	c
$\phi_{ij}$	Age-specific maturity proportions	F	$\in [0,1]$	c
$C_{i,y}^*$	Observed total yield (kg)	D	$\geq 0$	f
$O_{ij,y}^f$	Observed fishery age comp.	D	$\in [0,1]$	f
$O_{ij,y}^s$	Observed BT age comp.	D	$\in [0,1]$	b
$O_{ij,y}^{elit}$	Observed AT age comp.	D	$\in [0,1]$	g
$\beta_{i,y}^s$	Observed BT survey biomass (kg)	D	number	b
$\beta_y^{elit}$	Observed AT survey biomass (kg)	D	number	g
$T_y$	Bottom temperature ( $^{\circ}$ C)	D	number	b
$U_{paij,y}$	Gravimetric proportion of prey in predator stomach	D	$\in [0,1]$	b
$B_p^{other}$	Biomass of other prey (kg)	D	$\geq 0$	h
$S_{1j}^{elit}$	AT survey selectivity	F	$\in [0,1]$	c

### Harvest scenarios and reference points

For all future scenarios, we set the bottom temperature in the model to the mean of the historical observed temperatures and mean recruitment (Fig. 1). We used the approach for deriving biological reference points (BRPs) proposed by Moffitt et al. (*in press*) and implemented by Holsman et al. (*in press*); here we evaluated 2 of their 12 harvest scenarios. For each harvest scenario  $x$  we calculated female spawning stock biomass for species  $i$  at a given fishing mortality rate  $F$  ( $SSB_{F,x,i,y}$ ) by projecting the model forward to 2103 (87 years) under mean recruitment and according to a specified harvest rate ( $F$ ;  $F = 0$  for no fishing scenarios). Here we adopted the current over fishing limit (OFL) for Tier 3 acceptable biological catch ABC and MSY proxies for Bering Sea groundfish stocks; 40% of unfished biomass as the proxy target biomass for the ABC, and 35% as the proxy for  $B_{MSY}$  (female spawning biomass corresponding to

maximum sustainable yield, MSY, i.e., 35% of  $\overline{SSB}_{0,i}$ ; Punt et al., 2014; NPMFC, 2013; Clark et al., 1991; Brooks et al., 2010).

Table 3 (continued). Parameter definition ( $n$  is the number of parameters for estimated parameters only, value (Plk: Pollock; Cod: Pacific cod; Atf: Arrowtooth flounder both sexes; Atf<sub>M</sub>: Arrowtooth flounder males; Atf<sub>F</sub>: Arrowtooth flounder females), and source. I: Input parameter (assigned); M: model index; E: Estimated parameter; F: fixed parameter P: Derived quantity; D: Data.

Parameter	Definition	Type	Value			Source (see below)
			Pollock	Cod	ATF	
$A_i$	Number of prey ages	I	12	12	21	e
$A_p$	Number of predator ages	I	12	12	21	e
$\hat{\phi}_p$	Annual relative foraging rate (d yr <sup>-1</sup> )	I	0.119	0.041	0.125	a
$\alpha_\delta$	Intercept of the allometric maximum consumption function (g g <sup>-1</sup> yr <sup>-1</sup> )	I	0.119	0.041	0.125	a
$\beta_\delta$	Allometric slope of maximum consumption	I	-0.460	-0.122	-0.245	a
$T_p^{cm}$	Consumption maximum physiological temperature (°C)	I	15.00	21.00	34.13	a
$T_p^{co}$	Consumption optimum physiological temperature (°C)	I	10.00	13.70	19.60	a
$T_p^c$	Max consumption parameter	I	2.60	2.41	2.18	a
$\alpha_{0,d,i}$	Intercept for VBGF $d$ parameter	F	-0.817	-0.375	M: -0.213 F: -0.340	d
$\alpha_{d,i,y}$	Annual intercept for VBGF $d$ parameter	F	See Table 5			d
$\beta_{d,i}$	Temperature covariate for VBGF $d$ parameter	F	0.009	0.0045	M: -0.0057 F: -0.0115	d
$K_i$	VBGF energy loss constant (kg kg <sup>-1</sup> yr <sup>-1</sup> )	F	0.22	0.45	M: 1.08 F: 0.38	d
$H_i$	VBGF assimilation constant (kg kg <sup>-d</sup> yr <sup>-1</sup> )	F	16.34	9.30	M: 5.19 F: 5.90	d
$t_{0,i}$	VBGF age when $W_{i,j,y} = 0$ (years)	F	0.53	-0.16	M: -1.00 F: -0.28	d
$M_i^{\text{fem}}$	Female natural mortality		NA*	0.37	0.35	c
$M_i^{\text{male}}$	Male natural mortality	F	NA*	0.37	0.20	c

\* pollock age-specific M1 residual mortalities from the assessment were used (same values for male and females).

- a. Holsman and Aydin 2015
- b. Alaska Fisheries Science Center eastern Bering Sea bottom trawl survey
- c. Stock assessments (Ianelli et al., 2012; Thompson and Lauth, 2012; Spies et al., 2012)
- d. Supplemental materials, this study
- e. This study
- f. Fishery observer data
- g. Alaska Fisheries Science Center echo-integrated acoustic trawl survey
- h. Jurado Molina et al., 2005

The corresponding species-specific, acceptable biological catch ( $ABC_{x,i,y}$ ) for each harvest scenario was calculated as the fishery yield for each year  $y$  of the projection period  $[1, n_y^{\text{fut}}]$  given a constant fishing mortality rate for the projection period that satisfies each harvest scenario objective ( $F_{ABC,x,i}^*$ ), such that:

$$ABC_{x,i,y} = \left( \sum_j^{A_i} \left( \frac{F_{ABC,x,i}^* S_{ij}^f}{Z_{x,ij,y}} (1 - e^{-Z_{x,ij,y}}) N_{x,ij,y} W_{ij,y} \right) \right)$$

Eq. 3

where  $Z_{x,ij,y}$  is the control-rule specific total annual mortality for species  $i$  age  $j$  in the set  $[1, 2, \dots, A_i]$ ,  $s_{ij}^f$  is fishery age selectivity, and  $N_{x,ij,y}$  and  $W_{ij,y}$  are the annual species-specific abundance and weight-at-age for each projection year  $y$ . Using this approach, we found the species-specific fishing mortality rate ( $F_{x,i}^*$ ) that results in mean female spawning biomass ( $\overline{SSB}_{F,i}$ ) in the target projection period (i.e., last 5 years; 2046-2050) under fishing that is equal to the target proxy percentage (i.e., 40%) of mean unfished female spawning biomass ( $\overline{SSB}_{0,i}$ ; Table 5). To find  $F_{ABC,x,i}^*$ , we iteratively project the model to find the  $\overline{SSB}_{F,i}$  that corresponds to a given harvest rate  $F_{x,i}^*$ , adjusting  $F_{x,i}^*$  downwards if  $\overline{SSB}_{F,i}$  is below the target or upwards if  $\overline{SSB}_{F,i}$  is above the target, until we achieve  $\overline{SSB}_{F,i}$  near or at the proxy of 40% of  $\overline{SSB}_{0,i}$ . We ran this harvest scenario with the following variations:

- Find the ABC proxy biomass of 40% of unfished spawning biomass, where unfished biomass ( $\overline{SSB}_{0,i}$ ) is determined from projections where  $F$  is set to 0 for all species simultaneously.
- Iterate (i.e., eight iterations of the optimization algorithm) to find the species-specific fishing mortality rates that maximize the total combined yield (i.e., sum of yield for all three species) over the last 5 years of the projection period and where female spawning biomass for each species is not permitted to drop below 35% of the corresponding unfished female spawning biomass.

## Results

### Model parameterization

The multi-species mode of the model achieved a slightly higher over-all fit to the data (i.e., lower negative log-likelihood with the same number of estimated parameters for both models) for pollock and similar fits to the data for P. cod and arrowtooth. We observed similar fits to survey biomass and age composition data from the single-species (i.e.,  $M2_{ij,y}$  set to 0, hereafter “single-species model”) and multi-species modes of CEATTLE (see Table 5 for more detail). Although both models predicted similar total and female spawning biomass, inclusion of trophic interactions in the multi-species model resulted in slightly higher estimates of total biomass for pollock (Fig. 3).

Inclusion of predation interactions in CEATTLE improved model fit to observations of survey age composition for pollock, with average annual Pearson correlation coefficient (i.e.,  $R^2$ ) values from CEATTLE model in multi-species mode of 0.85 versus single-species version of CEATTLE model  $R^2$  values of 0.82. The single- and multi-species models performed equally well for the annual Pacific cod and arrowtooth survey age composition data ( $R^2 = 0.76$  and  $0.65$ , respectively), and fishery age composition data for all three species ( $R^2 = 0.81$ ,  $0.96$ , and  $0.89$  for pollock, Pacific cod, and arrowtooth flounder, respectively). The single- and multi-species models fit the survey estimates of biomass with similar accuracy (single- and multi-species  $R^2$ , respectively, of 55.5% and 54.5% for pollock, 81% and 81.3% for Pacific cod, and 68.6% and 68.5% for arrowtooth), although the multi-species model fit the survey data slightly better (negative log-likelihood = 351.3 and 350.9 for the single- and multi-species models, respectively). Both models mimicked annual total catch for all three species closely ( $R^2 > 0.997$ ; Fig. 2). Slight differences in total and female spawning biomass estimates between the models partially reflect divergent survey selectivity curves for the two models, with the multi-species model predicting higher survey selectivity for cod (Fig. 13e) and 5+ pollock (Fig. 13d).

Table 4. Correlation coefficients for survey biomass and age composition data from the model run in single-species mode (SSM) and multi-species mode (MSM).

	SSM	MSM
<b>Total survey biomass</b>		
Pollock	0.55	0.54
P. cod	0.81	0.81
Arrowtooth	0.69	0.68
<b>Survey age composition</b>		
Pollock	0.82	0.85
P. cod	0.76	0.76
Arrowtooth	0.65	0.65

Predation mortality varied considerably with changes in predator abundance over time (Fig. 5). Cannibalism was the largest source of predation mortality for pollock (Figs. 6) with older conspecifics exhibiting a high preference (i.e., total pollock suitability  $>0.75$ ; Fig. 13) for juvenile pollock (ages 1-3; Fig. 13.g). Larger pollock also appear to target small arrowtooth flounder, as evidenced by a slight increase in total suitability of arrowtooth for pollock ages 6-10 (Fig. 13.g). Similarly, younger Pacific cod (ages 2-6) also target arrowtooth flounder (Fig. 13.h). Pacific cod increasingly target pollock prey as they age, and larger, older Pacific cod diets are dominated by age 1 pollock prey. Pacific cod also appear to be cannibalistic from ages 4 through 9. In contrast arrowtooth flounder prefer pollock throughout their lives, with total suitability coefficients (for all pollock ages) between 0.5 and 1.0 for arrowtooth flounder ages 1 through 18 (Fig. 13.i).

Natural mortality ( $M1_{ij} + M2_{ij,y}$ ) was highest for age 1 fish of all three species (Fig. 4), and greatest for pollock (relative to Pacific cod or arrowtooth flounder). Age 1 mortality was estimated to be higher in 2016 (2.02) than it had been in the entire time series (since 1987; Fig. 4). Mortality was lower for age 1 Pacific cod and arrowtooth flounder, with total age 1 natural mortality stable at around 0.68 and 0.64  $yr^{-1}$ , respectively, although both were slightly higher in 2015 and 2016. High predation mortality estimated for 1980-1990 for pollock reflected patterns in combined annual demand for prey by all three predators that was highest in the mid 1980's (collectively 8.97 billion t per year; Fig. 6a), and in recent years (collectively  $\sim 7.74$  billion t per year 2014-2016). The peak in predation mortality of age 1 pollock in 2006 corresponds to the maturation of a large age class of 5-7 year old pollock and 2 year old Pacific cod that dominated the age composition of the two species in 2006. Similarly, the recent peaks in 2011 and 2014 reflect maturation of the large 2008 year class (Fig. 14). In 2016, the high mortality rates observe for pollock and Pacific cod are due to combined impacts of elevated bottom temperatures, which increases individual predator demand for pollock prey, and maturation of cannibalistic conspecific predators.

Pollock are both the dominant predator and a primary prey species in the multi-species model, second only to the 'other prey' category (Fig. 5a, b). After 'other prey' and pollock, the next most dominant prey category consumed is Pacific cod, followed by arrowtooth flounder (Fig. 5b). Pollock are primarily consumed by older conspecifics, and pollock cannibalism accounted for 56% (on average) of total predation mortality for age 1 pollock except for 2006-2008 when predation by arrowtooth flounder exceeded cannibalism as the largest source of predation mortality of age 1 pollock; Fig. 6).

The multi-species version of CEATTLE compensates for elevated predation mortality on younger age classes by increasing estimates of recruitment. Thus, recruitment is higher in the multi-species model than in the single-species model for all three species, especially those with high predation rates (i.e., pollock). The direction of change in annual recruitment estimates from year-to-year was generally the same for both models (i.e., both models increased or decreased recruitment in the same year) with a notable

exception; the multi-species model predicted a significant drop in recruitment in recent years for pollock, whereas the single-species model estimated only a slight decline in recruitment (Fig. 7a). Pollock recruitment from the single-species version of CEATTLE was positively correlated with Pacific cod recruitment ( $R^2 = 0.65$ ) and slightly inversely correlated with arrowtooth recruitment ( $R^2 = -0.02$ ). Correlations between pollock recruitment and Pacific cod or arrowtooth recruitment were similar between the single- and multispecies versions, although correlations were weaker in the multi-species model for Pacific cod ( $R^2 = 0.59$  and  $-0.03$ , respectively).

The single- and multi-species models estimate similar fishing mortality rates for pollock that have remained relatively stable at around 0.13 since the early 1980's (Fig. 8). Both models also estimate low and relatively steady fishing mortality rates for arrowtooth flounder (i.e.,  $\sim 0.03$ ). Both models estimate higher fishing mortality for Pacific cod (0.24-0.45), with indications of declines in fishing mortality in recent years (Fig. 8).

### Harvest scenarios and reference points

Projecting CEATTLE forward under mean recruitment produces trajectories of female spawning stock biomass that can be used to derive multi-species biological reference points and attendant fishing mortality rates (Holsman et al. in press). Projections under the Ricker stock-recruitment model lead to over-compensation recruitment dynamics in the first years of the projection (especially for single-species models; Fig. 9; *sensu* Botsford, 1986). However, a long term ( $>70$  year) projection period appeared sufficient for the dynamics to stabilize (Fig. 9).

In general, unfished and harvested female spawning stock biomass ( $\overline{SSB}_{0,i}$  and  $\overline{SSB}_{F,i}$ , respectively) were lower for projections of the multi- than the single-species model (with the exception of harvest scenario 4.3 of mMSY; Fig. 9). Unfished female spawning biomass from the multi-species version of CEATTLE was higher than historical female spawning biomass for Pacific cod and arrowtooth flounder, and approximately equal to recent female spawning biomass for pollock (Fig. 9).

Estimates of  $\overline{ABC}_{x,i}$  for pollock were similar but slightly higher for multi-species than single- and models for harvest scenarios with individual species yield targets (scenario 1.1; Fig. 10). In contrast, for pooled yield targets, multi-species yield exceeded single species yield (scenarios 4.3; Fig 10) in the short-term but led to long-term declines in yield due to overharvest of arrowtooth flounder.

### Application of MBRPs toward EBFM

Development of diverse multi-species biological reference points (MBRPs) from multi-species models is a necessary step in moving forward with EBFM (Link, 2010; Link and Browman, 2014). Projecting CEATTLE provides proxies for MBRPs that can readily be implemented in current OFL control rules for Alaska fisheries management and demonstrates the range of possible considerations as well as individual strengths and weaknesses of each control rule approach. Proxies for ABCs in multi-species models have been found to be lower compared to single-species counterparts (e.g., Gaichas et al., 2012). That said, Holsman et al. (in press) found that MBRPs do not inherently result in lower harvest recommendations than single-species corollaries (i.e., BRPs); comparative risk of over- or under-harvest depends on the degree of inter-specific predation and cannibalism. They also found that recommended harvest rates were relatively consistent between harvest scenarios, especially if target minimum biomasses are included for individual species. They also found that climate and trophic drivers can interact to affect MBRPs, but for prey species with high predation rates, trophic and management-driven changes may exceed direct effects of temperature on growth and predation. Given this, MSCAA models can readily be used for tactical EBFM decisions under changing climate conditions, if, as suggested by Holsman et al. (in press) and by various authors previously, harvest scenarios used for deriving MBRPs combined a minimum biomass threshold with yield targets to meet biodiversity and yield objectives (Worm et al., 2009; Gaichas et al.,

2012). Biomass thresholds will require development of criteria for minimum limits in order represents a necessary advancement of the current approach.

#### **Short-term utility: potential application within current single species assessments**

This work demonstrates some alternative applications of multispecies trophic models within a management setting and there may be immediate relevance for current stock assessment models. For example, the estimated historical time series of natural mortality at age over time ( $M1 + M2$ ) could be used directly within the assessment or used as priors in alternative assessment models with estimated annually varying natural mortality. Similarly, for the case of EBS pollock, the stock recruitment relationship may provide a basis for better estimates or prior distribution specification. It may be that by adding the time series of estimated total natural mortality at age that the estimated stock recruitment relationship may differ substantially given the relative differences in age 1 abundances. Further research on applying alternative stock recruitment relationships is needed as well, especially since the application of the Ricker curve has traditionally been justified due to cannibalistic nature of pollock—a situation that is partially accounted for in this application. In general, monitoring predator trends in a comprehensive way is an important element to link EBFM and climate change research.

#### **Long-term utility: climate- and trophic-specific biological reference points**

Because the natural mortality and growth functions are temperature dependent, long-term applications of the CEATTLE model could also include recruitment functions with climate-covariates. In this, the model could be combined with short-term forecasts of physical and lower trophic conditions in the Bering Sea, and used to refine estimates of recruitment and spawning stock biomass under changing conditions. (note that extensive model validation would be needed to evaluate predictive performance and potential utility). Incorporating additional species into the model, such as northern fur seals and Pacific halibut could help provide quantitative estimates of changes in juvenile pollock forage resources associated with different harvest rates of groundfish species in the EBS, as well as refined estimates of predation mortality for prey species in the model under changing conditions. Finally, planned incorporating technical interactions into the model may add realism to projections both for assessment purposes and for research and policy evaluation.

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## Figures

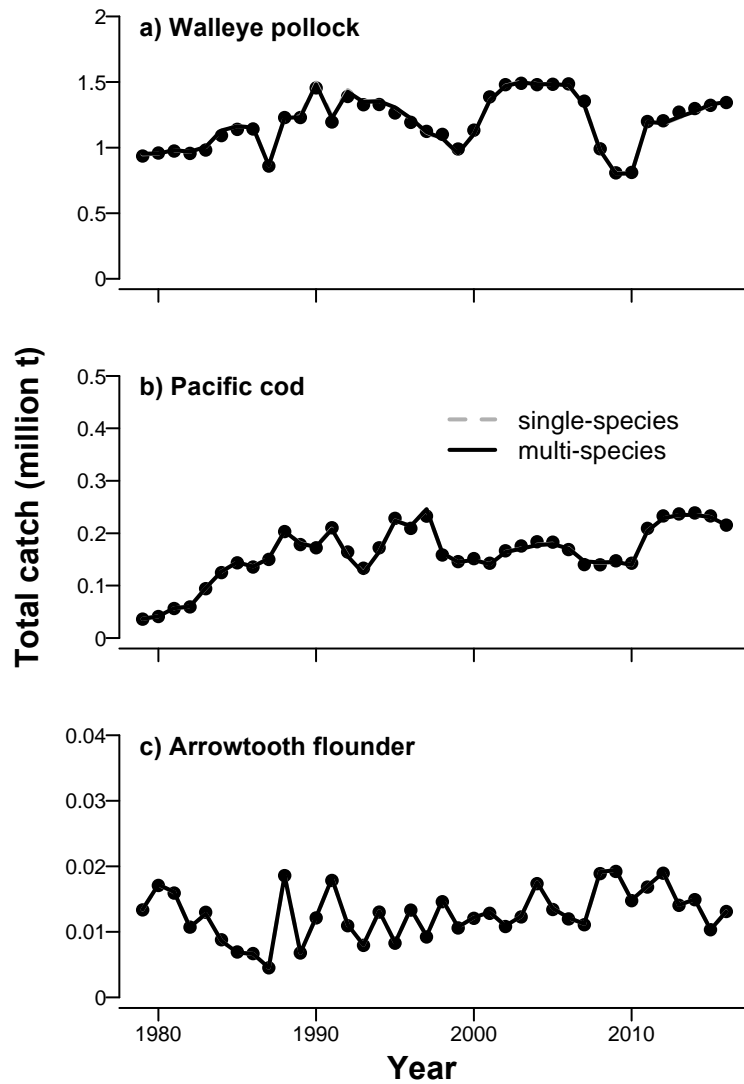


Figure 2. Total observed catch (circles) and model estimates of annual catch (lines) for single- and multi-species models (note that single species lines may not be visible as they overlap with multi-species estimates).

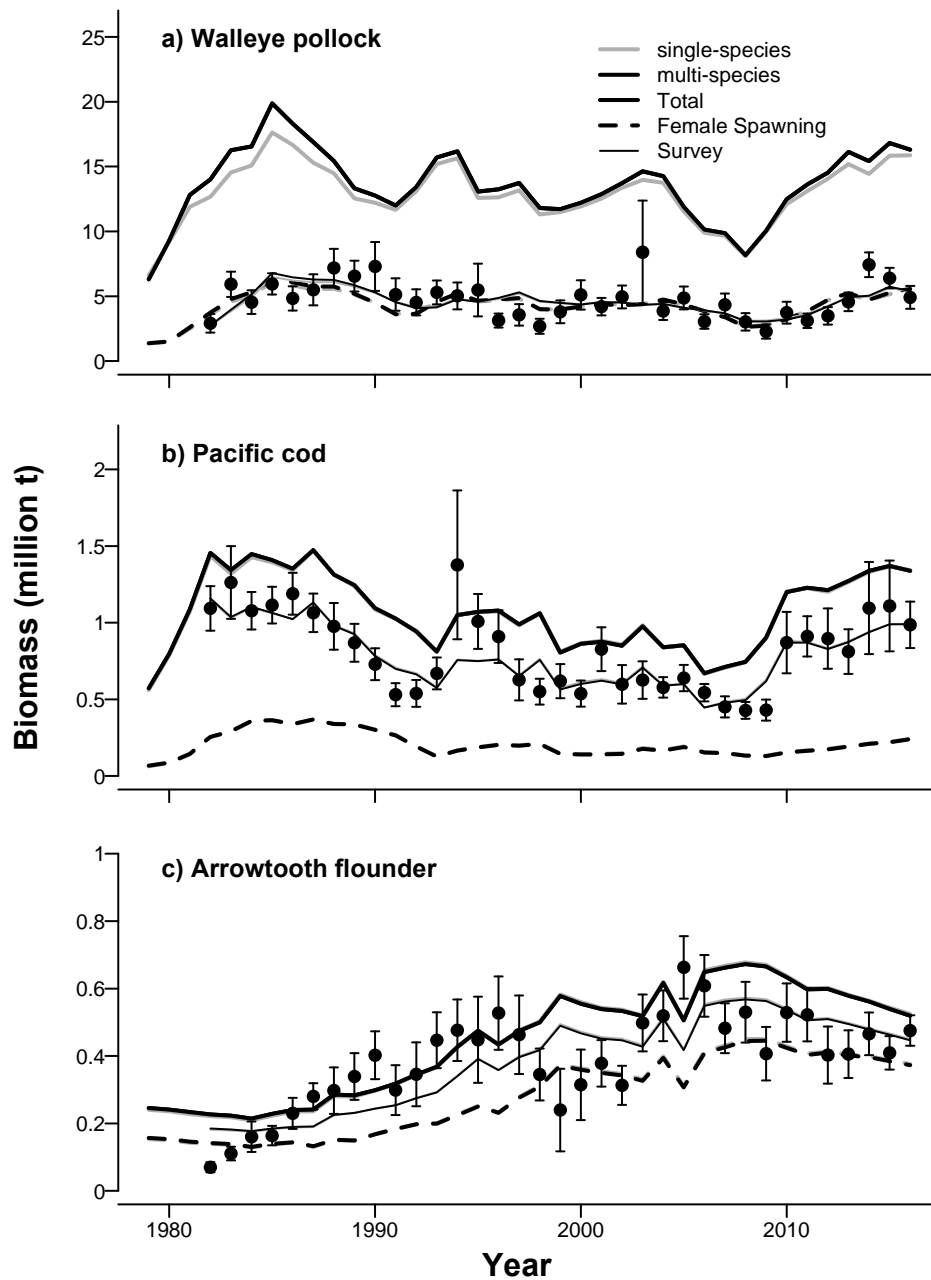


Figure 3. Single- (gray lines) and multi-species (black lines) retrospective model estimates of total (thick solid lines), female spawning (dashed lines), and bottom-trawl survey biomass (thin solid lines). Filled circles represent mean observed groundfish survey biomass and standard errors of the mean (error bars).

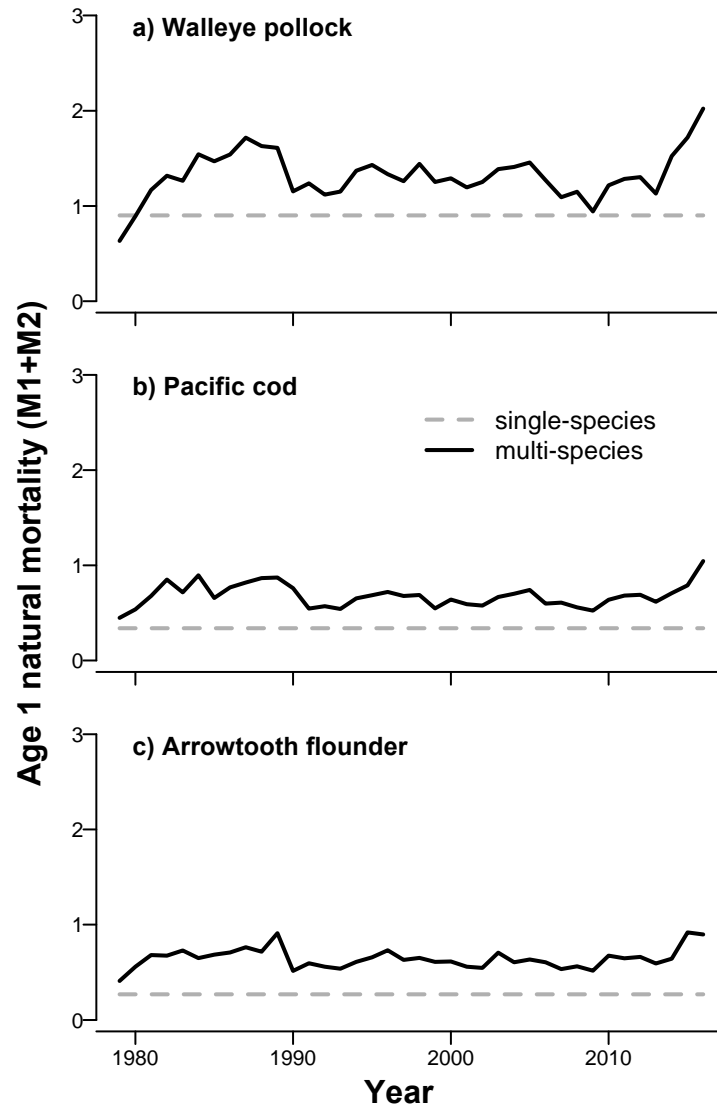


Figure 4. Annual variation in total mortality ( $M1_{i1}+M2_{i1,y}$ ) for age 1 pollock (a), Pacific cod (b), and arrowtooth flounder (c) from the single-species models (dashed line), multi-species models with temperature (black line).

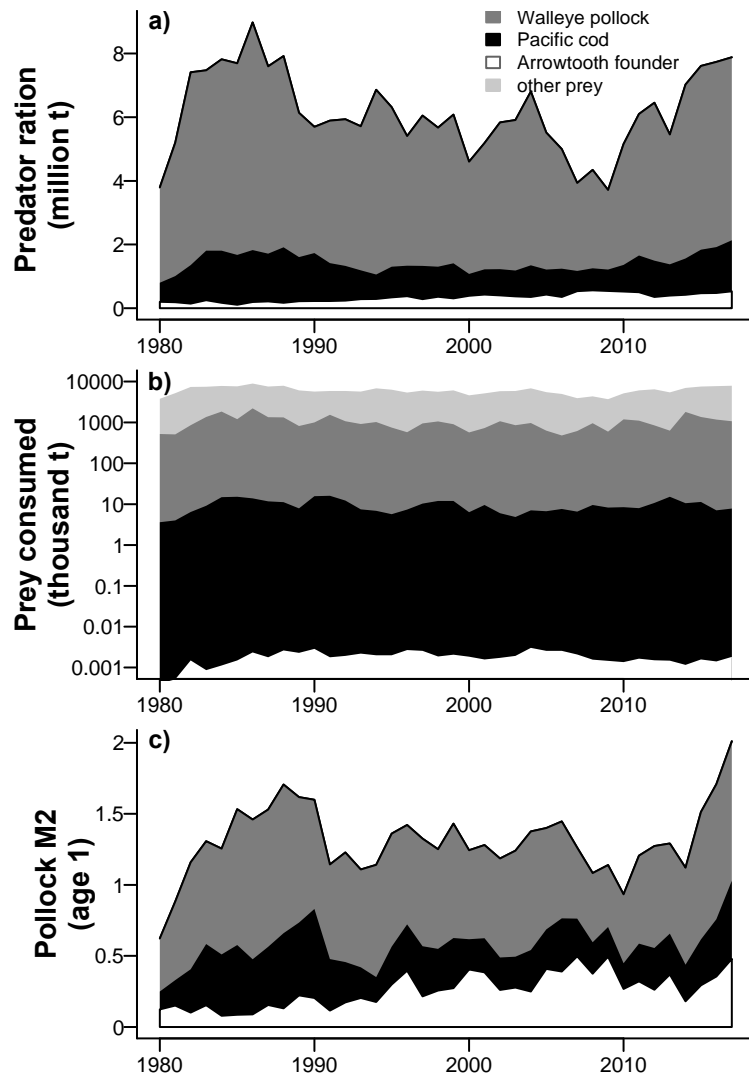


Figure 5. a) Combined total predator ratio (all three predators combined) over time grouped by predator. b) Total prey consumed by all three predators combined (note the log scale). c) Pollock predation mortality (M2; age 1 only) consumed by each predator species.

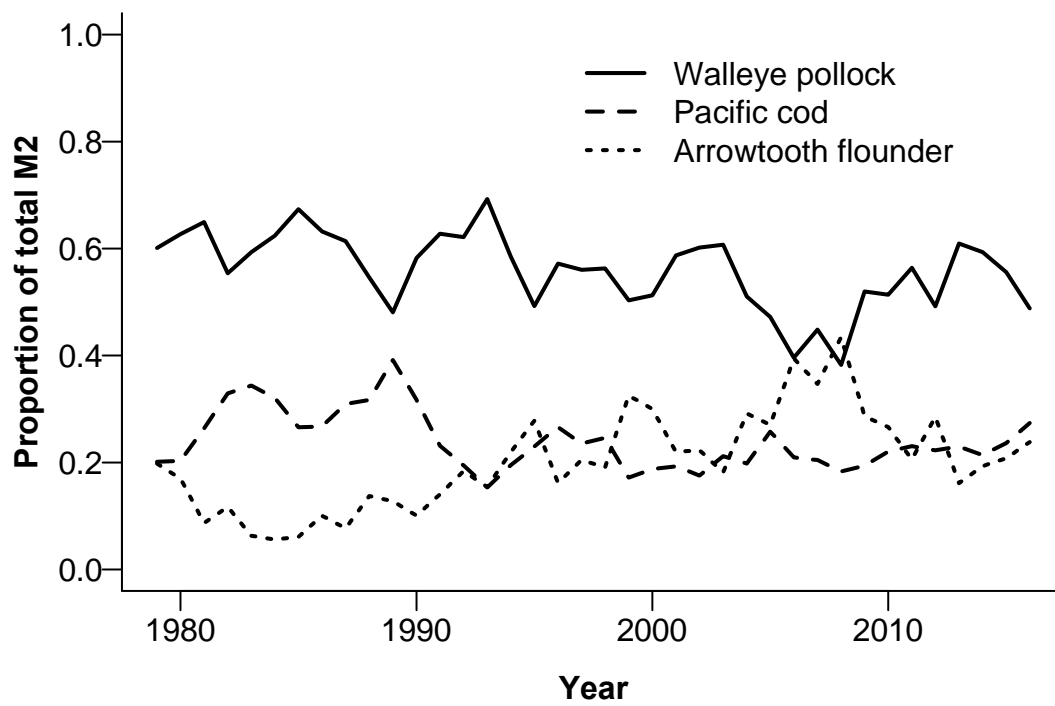


Figure 6. Proportion of total predation mortality for age 1 pollock from pollock (solid), Pacific cod (dashed), and arrowtooth flounder (dotted) predators across years.



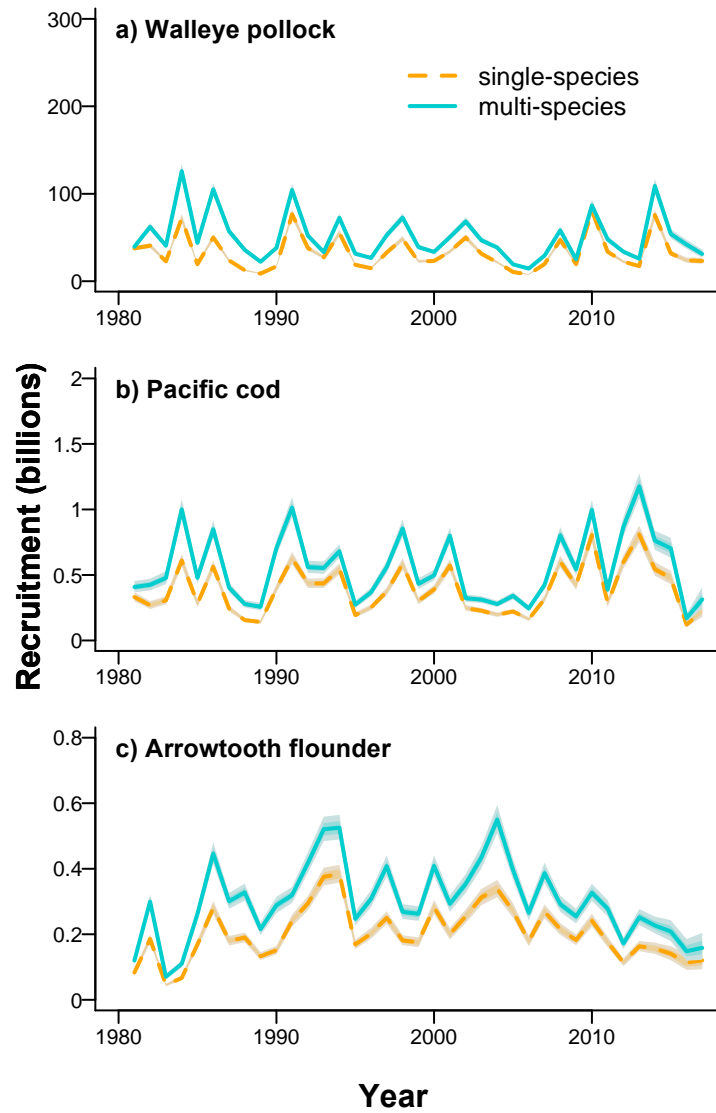


Figure 7. Annual single- and multi-species CEATTLE model estimates of recruitment (age 1) for pollock (a), Pacific cod (b), and arrowtooth flounder (c). Lighter shading represents the 95% CI around mean estimates. Darker shading represents  $\pm 1$  standard error of the mean estimate.

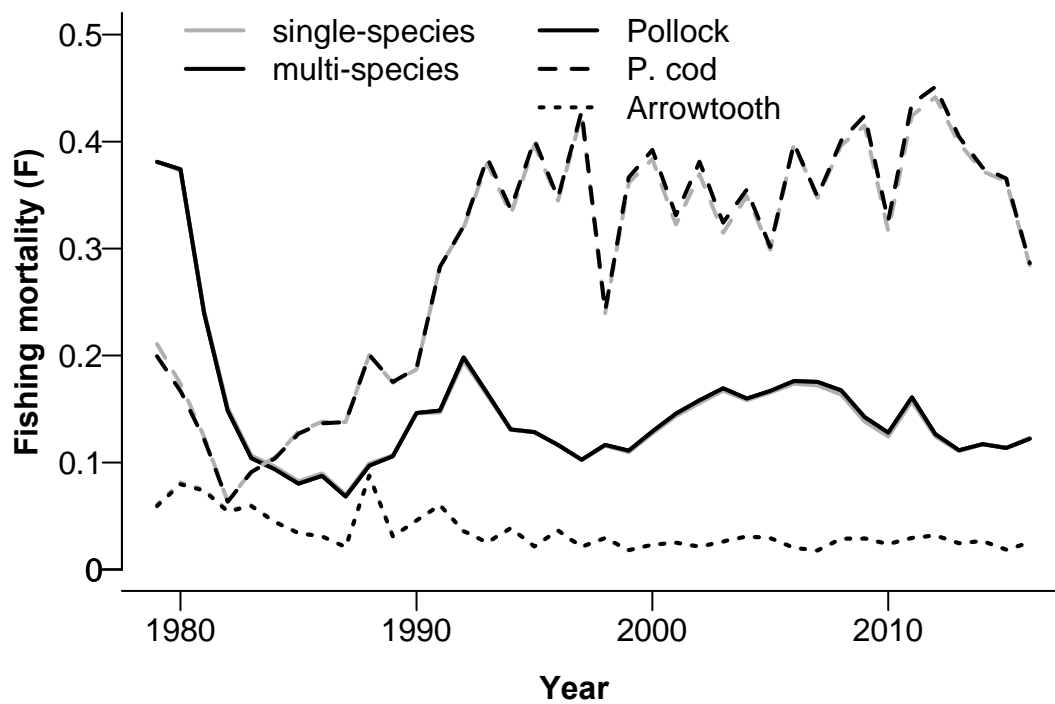


Figure 8. Time-trajectories of single- and multi-species (gray and black, respectively) CEATTLE model estimates of fishing mortality rate for eastern Bering Sea walleye pollock (solid lines), Pacific cod (dashed lines), and arrowtooth flounder (dotted lines). Note that the single- and multi-species lines for arrowtooth flounder overlap.

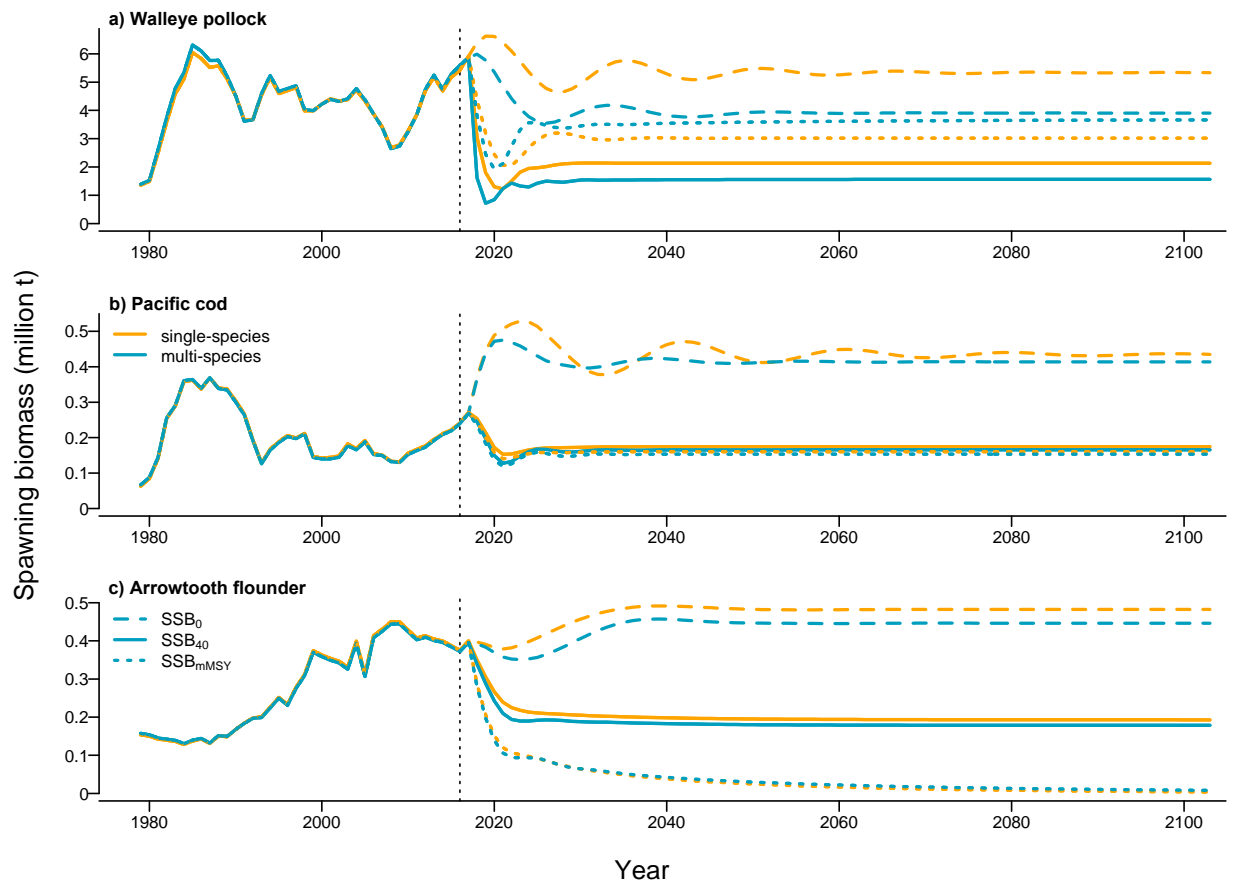


Figure 9. Single- and multi-species (orange and blue, respectively) CEATTLE model projections of unfished (dashed;  $SSB_0$ ) and fished spawning stock biomass at the harvest rate corresponding with the ABC proxy and aggregate maximum yield ( $SSB_{40}$  and  $SSB_{mMSY}$ , solid and dotted lines, respectively) for each species.

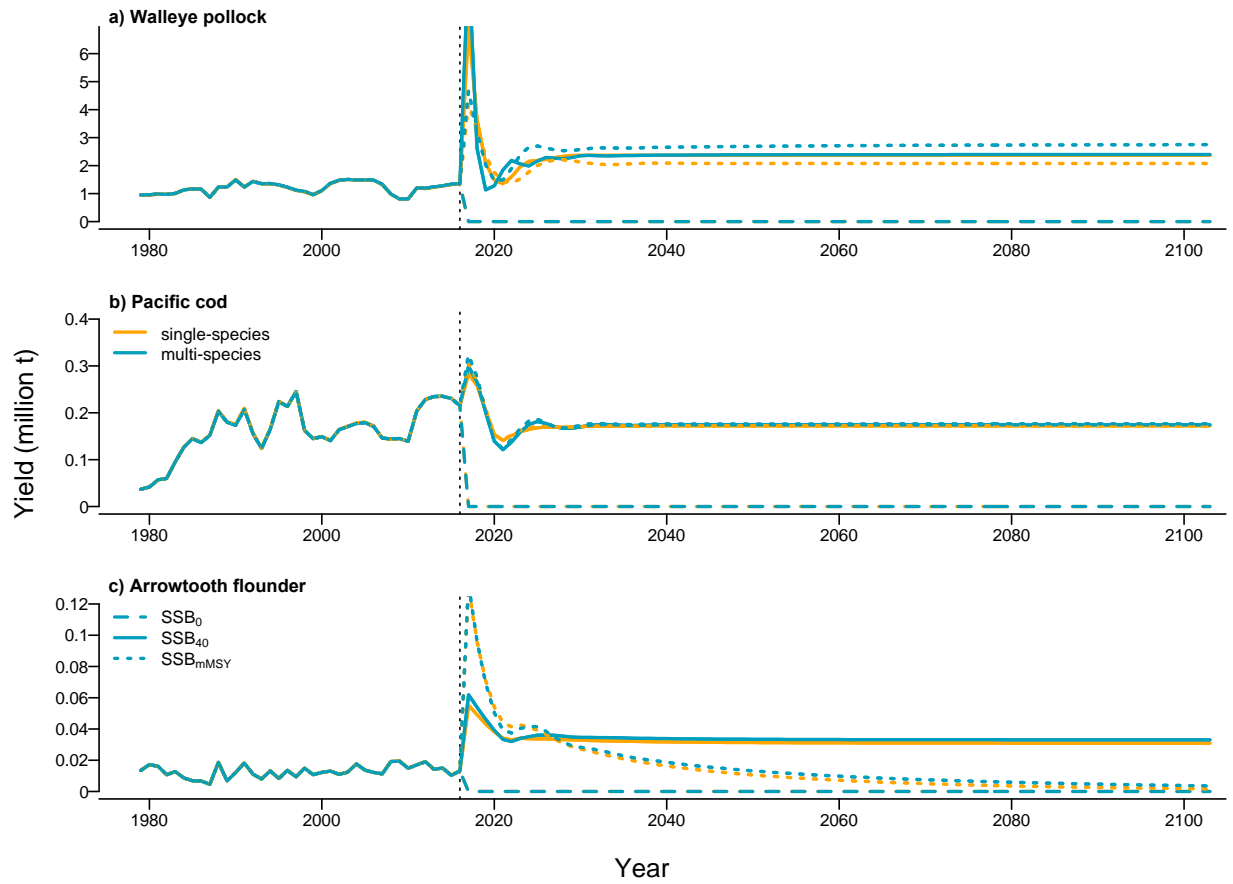


Figure 10. Single- and multi-species (orange and blue, respectively) CEATTLE model projections of annual yield at the harvest rates corresponding with the ABC proxy and aggregate maximum yield ( $F_{proxy}$  and  $F_{mMSY}$ , solid and dotted lines, respectively) for each species.

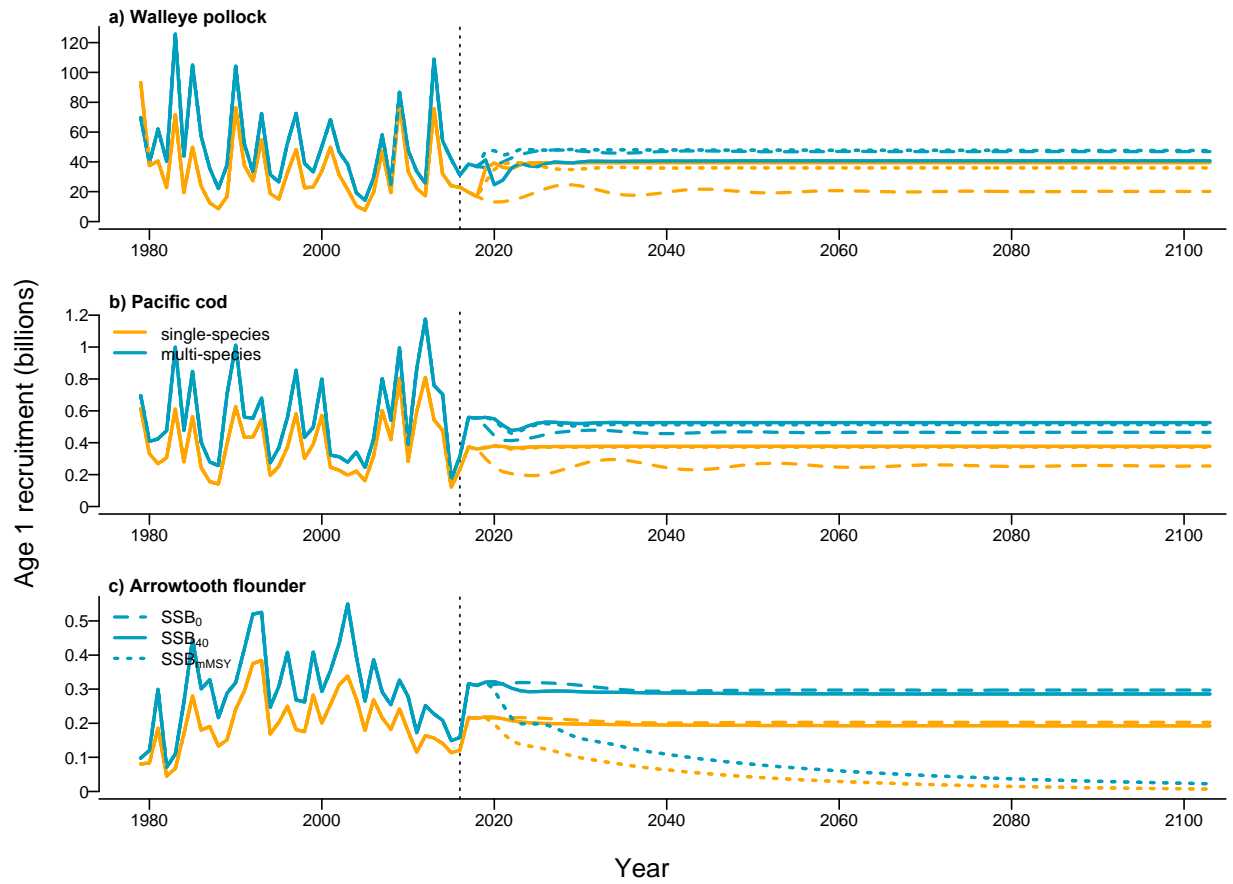


Figure 11. Single- and multi-species (orange and blue, respectively) CEATTLE model projections of age 1 recruitment at unfished spawning stock biomass (dashed;  $SSB_0$ ) and at fished spawning stock biomass corresponding with the harvest rate at the ABC proxy and aggregate maximum yield ( $SSB_{40}$  and  $SSB_{mMSY}$ , solid and dotted lines, respectively) for each species.



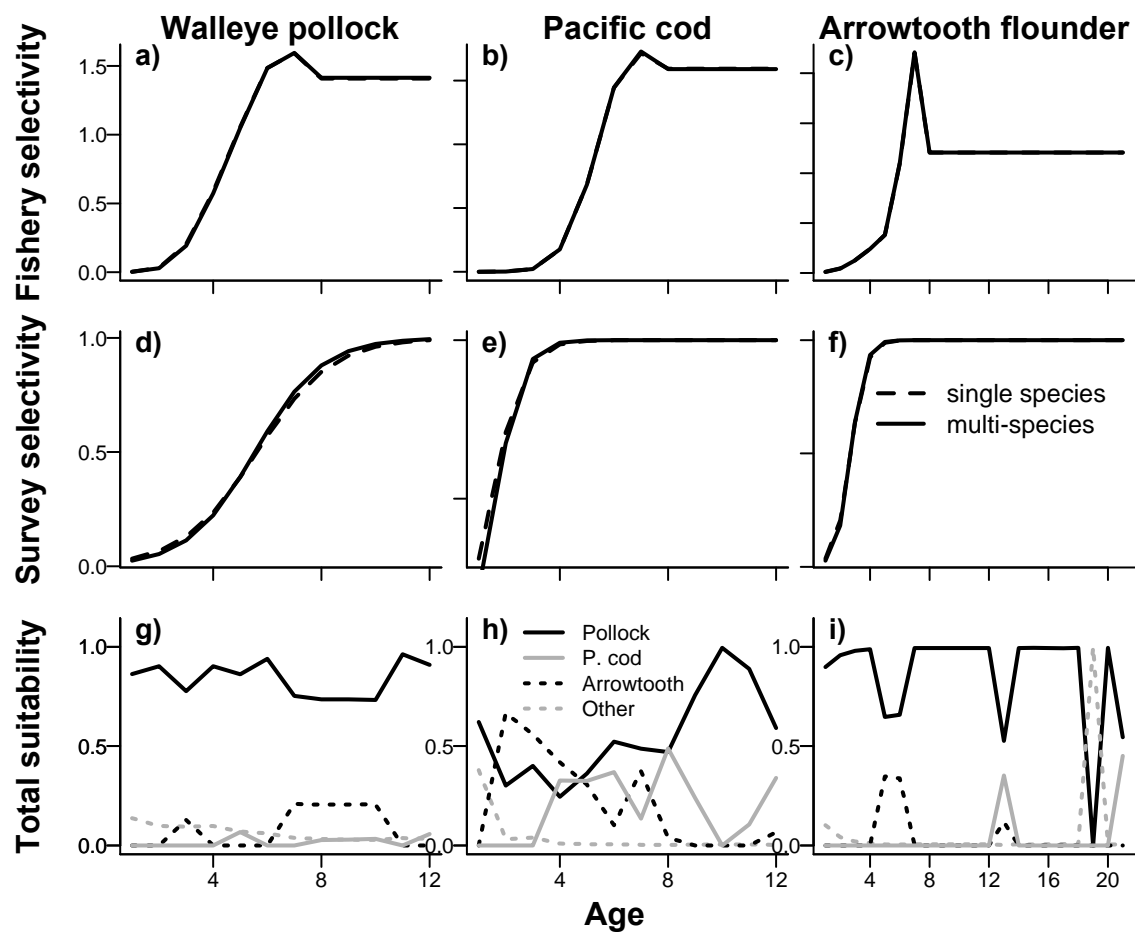


Figure 13. Single-species and multi-species fishery (first row; a-c) or survey selectivity (second row; d-f). Total suitability (across all prey species) for each predator age (third row; g-i).

	Age 1	Age 2	Age 3	Age 4	Age 5	Age 6	Age 7	Age 8	Age 9	Age 10	Age 11	Age 12
1979	0.921	1.505	1.025	0.661	0.604	0.374	0.210	0.182	0.206	0.202	0.174	0.240
1980	0.521	3.476	2.420	1.154	0.559	0.391	0.193	0.100	0.090	0.099	0.096	0.189
1981	0.824	1.540	5.691	2.797	1.005	0.374	0.210	0.096	0.051	0.045	0.049	0.134
1982	1.339	1.284	1.807	6.165	2.055	0.722	0.278	0.138	0.059	0.033	0.029	0.099
1983	2.056	1.143	2.051	2.652	5.787	1.736	0.471	0.172	0.084	0.030	0.015	0.054
1984	0.740	2.251	1.298	2.959	2.431	4.762	1.427	0.401	0.125	0.063	0.032	0.064
1985	2.255	0.780	3.753	1.800	2.719	2.094	4.744	1.207	0.348	0.069	0.041	0.066
1986	0.996	2.017	0.845	5.231	1.432	2.405	1.561	2.688	0.781	0.225	0.063	0.065
1987	0.849	1.077	2.833	1.389	4.309	1.100	1.696	1.100	1.831	0.499	0.130	0.078
1988	0.455	0.518	1.483	3.526	1.227	3.509	0.825	1.203	0.782	1.360	0.409	0.134
1989	0.811	0.309	0.645	1.712	2.922	0.938	2.671	0.588	0.939	0.544	0.928	0.307
1990	1.942	0.655	0.365	0.889	1.532	2.474	0.677	1.892	0.428	0.662	0.413	0.836
1991	0.944	2.780	0.712	0.571	0.753	1.110	1.775	0.472	1.365	0.294	0.416	0.803
1992	0.977	1.409	4.323	1.192	0.544	0.608	0.877	1.248	0.339	0.915	0.216	0.777
1993	1.272	0.824	2.589	6.582	1.046	0.351	0.356	0.488	0.804	0.216	0.595	0.577
1994	0.670	1.858	1.424	3.391	5.595	0.823	0.257	0.295	0.415	0.542	0.151	0.758
1995	0.505	0.512	1.753	1.977	2.354	3.925	0.513	0.182	0.181	0.257	0.345	0.568
1996	1.068	0.418	0.599	3.313	1.761	1.864	2.786	0.384	0.129	0.122	0.175	0.622
1997	1.213	0.949	0.849	1.141	3.585	1.381	1.528	2.172	0.284	0.086	0.084	0.470
1998	0.810	1.237	1.208	0.963	1.157	2.472	0.993	1.005	1.351	0.189	0.057	0.370
1999	0.586	0.575	2.041	2.204	0.813	0.887	1.865	0.697	0.742	0.933	0.130	0.248
2000	0.804	0.564	1.039	3.425	1.938	0.667	0.652	1.288	0.442	0.456	0.692	0.249
2001	1.349	0.855	0.810	1.599	3.300	1.685	0.592	0.487	0.956	0.328	0.324	0.584
2002	0.887	1.569	2.063	1.711	1.535	2.522	1.313	0.422	0.320	0.647	0.219	0.514
2003	0.911	1.108	3.270	2.787	1.651	1.211	1.671	0.775	0.234	0.202	0.394	0.413
2004	0.493	0.762	1.827	4.523	2.352	1.223	0.790	1.017	0.509	0.148	0.130	0.489
2005	0.324	0.326	1.298	2.406	3.259	1.609	0.736	0.482	0.670	0.305	0.097	0.385
2006	0.687	0.243	0.474	1.476	2.021	2.362	1.092	0.476	0.312	0.458	0.237	0.307
2007	1.231	0.652	0.577	0.803	1.453	1.608	1.724	0.711	0.313	0.216	0.286	0.281
2008	0.607	1.056	0.989	0.581	0.654	1.046	1.027	1.056	0.448	0.209	0.138	0.352
2009	1.731	0.617	2.094	1.472	0.528	0.518	0.828	0.775	0.683	0.316	0.136	0.340
2010	1.186	2.373	1.261	3.551	1.337	0.399	0.413	0.541	0.479	0.485	0.200	0.266
2011	0.806	1.225	3.796	1.581	3.234	1.017	0.335	0.280	0.377	0.318	0.332	0.308
2012	0.548	0.646	1.907	5.585	1.322	2.509	0.738	0.194	0.199	0.247	0.223	0.403
2013	2.499	0.438	1.006	2.718	5.211	0.999	1.906	0.539	0.137	0.125	0.163	0.393
2014	1.228	2.847	0.749	1.485	2.103	4.204	0.659	1.267	0.344	0.089	0.090	0.351
2015	0.947	0.898	4.677	1.238	1.645	1.814	3.474	0.577	0.925	0.232	0.065	0.326
2016	0.734	0.530	1.455	6.774	1.096	1.161	1.258	2.074	0.325	0.514	0.151	0.236

Figure 14. Multi-species estimates of total biomass (million t) by age of walleye pollock in the EBS.



## Tables

Table 5. Temperature-dependent Von Bertalanffy parameter (parm) estimates, standard deviation in parameter estimates (stdev), and confidence intervals (CI).

	Parm.	Estimate	stdev	lwr 95%ile	Upper						
Pollock	$t_{0,i}$	0.527	0.015	0.498	0.556						
	$\alpha_{d,i,y}$	-0.817	0.184	-1.175	-0.458						
	$\alpha_{d,i,y}$	-0.056	0.183	-0.413	0.301						
		-0.007	0.183	-0.363	0.349						
		-0.011	0.183	-0.367	0.345						
		-0.012	0.183	-0.368	0.344						
		-0.017	0.183	-0.373	0.339						
		-0.005	0.183	-0.361	0.351						
		0.002	0.183	-0.354	0.358						
		0.000	0.183	-0.356	0.356						
		-0.023	0.183	-0.379	0.333						
		-0.009	0.183	-0.365	0.347						
		0.014	0.183	-0.342	0.370						
		0.020	0.183	-0.337	0.376						
		0.036	0.183	-0.320	0.392						
		0.048	0.183	-0.308	0.404						
		0.020	0.183	-0.336	0.376						
	$\beta_{d,i}$	0.010	0.001	0.008	0.011						
	$\log(\sigma)$	-0.919	0.005	-0.928	-0.909						
$\log(K)$	-1.498	0.051	-1.598	-1.398							
$\log(H)$	2.794	0.036	2.723	2.864							
Pacific cod	$t_{0,i}$	-0.157	0.055	-0.265	-0.049						
	$\alpha_{d,i,y}$	-0.375	0.197	-0.759	0.010						
	$\alpha_{d,i,y}$	-0.024	0.196	-0.407	0.358						
		0.011	0.196	-0.372	0.393						
		-0.006	0.196	-0.388	0.377						
		-0.008	0.196	-0.390	0.375						
		-0.012	0.196	-0.394	0.371						
		-0.019	0.196	-0.402	0.363						
		-0.004	0.196	-0.386	0.379						
		-0.007	0.196	-0.390	0.375						
		0.001	0.196	-0.381	0.384						
		0.014	0.196	-0.368	0.397						
		0.017	0.196	-0.366	0.399						
		0.015	0.196	-0.367	0.398						
		0.022	0.196	-0.361	0.404						
		$\beta_{d,i}$	0.005	0.000	0.004	0.005					
		$\log(\sigma)$	-0.816	0.006	-0.828	-0.804					
	$\log(K)$	-0.796	0.117	-1.025	-0.567						
	$\log(H)$	2.230	0.042	2.147	2.313						
Arrowtooth flounder, male					Arrowtooth flounder, female						
1996 2004	$t_{0,i}$	-1.000	0.000	-1.001	-0.999	1996 2004	$t_{0,i}$	-0.275	0.257	-0.777	0.227
	$\alpha_{d,i,y}$	-0.213	0.501	-1.189	0.763		$\alpha_{d,i,y}$	-0.340	0.504	-1.323	0.642
	$\alpha_{d,i,y}$	0.001	0.500	-0.974	0.976		$\alpha_{d,i,y}$	-0.005	0.500	-0.980	0.970
		-0.001	0.500	-0.976	0.974			0.005	0.500	-0.970	0.980
	$\beta_{d,i}$	-0.006	0.004	-0.014	0.003		$\beta_{d,i}$	-0.011	0.004	-0.020	-0.003
	$\log(\sigma)$	-1.003	0.046	-1.092	-0.913		$\log(\sigma)$	-1.068	0.031	-1.127	-1.008
	$\log(K)$	0.081	0.218	-0.344	0.505		$\log(K)$	-0.974	0.369	-1.694	-0.255
	$\log(H)$	1.646	0.051	1.546	1.746		$\log(H)$	1.784	0.127	1.535	2.032

Table 6. Effective foraging days (Holsman and Aydin, 2015)

Age	Walleye pollock	Pacific cod	Arrowtooth flounder
1	365	365	365
2	365	365	365
3	365	348.66	365
4	365	315.85	365
5	360.41	292.01	359.14
6	347.8	273.87	341.22
7	338.01	259.63	326.9
8	330.18	248.2	315.17
9	323.81	238.88	305.38
10	318.54	231.2	297.1
11	314.13	224.8	290.03
12	307.91	216.75	283.94
13			278.67
14			274.08
15			270.07
16			266.57
17			263.5
18			260.81
19			258.44
20			256.36
21			254.52

Table 7. Relative foraging rate (Holsman and Aydin, 2015).

Walleye pollock												
Year	Age											
	1	2	3	4	5	6	7	8	9	10	11	12
1979	0.19	0.20	0.20	0.21	0.21	0.22	0.23	0.23	0.24	0.25	0.25	0.26
1980	0.19	0.20	0.20	0.21	0.21	0.22	0.23	0.23	0.24	0.25	0.25	0.26
1981	0.21	0.21	0.21	0.22	0.22	0.23	0.23	0.23	0.24	0.24	0.25	0.25
1982	0.21	0.22	0.22	0.23	0.24	0.24	0.25	0.26	0.27	0.27	0.28	0.29
1983	0.18	0.18	0.19	0.19	0.20	0.20	0.21	0.21	0.21	0.22	0.22	0.23
1984	0.21	0.21	0.22	0.22	0.23	0.23	0.24	0.24	0.25	0.25	0.26	0.27
1985	0.21	0.21	0.22	0.22	0.23	0.24	0.24	0.25	0.26	0.26	0.27	0.28
1986	0.20	0.20	0.20	0.21	0.22	0.23	0.23	0.24	0.25	0.25	0.26	0.27
1987	0.20	0.21	0.21	0.22	0.22	0.23	0.23	0.24	0.24	0.25	0.25	0.26
1988	0.19	0.20	0.20	0.21	0.22	0.22	0.23	0.24	0.24	0.25	0.26	0.27
1989	0.19	0.20	0.20	0.20	0.21	0.22	0.22	0.23	0.23	0.24	0.24	0.25
1990	0.20	0.20	0.20	0.21	0.21	0.22	0.22	0.23	0.23	0.24	0.24	0.25
1991	0.20	0.20	0.21	0.21	0.22	0.23	0.23	0.24	0.25	0.25	0.26	0.27
1992	0.19	0.20	0.20	0.21	0.22	0.22	0.23	0.24	0.25	0.25	0.26	0.27
1993	0.20	0.20	0.21	0.21	0.22	0.23	0.23	0.24	0.24	0.25	0.25	0.26
1994	0.20	0.20	0.21	0.22	0.22	0.23	0.24	0.25	0.26	0.26	0.27	0.28
1995	0.20	0.20	0.21	0.21	0.22	0.23	0.24	0.25	0.25	0.26	0.27	0.28
1996	0.20	0.20	0.21	0.21	0.21	0.22	0.22	0.23	0.23	0.24	0.24	0.25
1997	0.18	0.18	0.19	0.19	0.20	0.20	0.21	0.22	0.22	0.23	0.23	0.24
1998	0.21	0.21	0.22	0.22	0.23	0.23	0.24	0.24	0.25	0.25	0.26	0.27
1999	0.19	0.20	0.20	0.21	0.22	0.23	0.23	0.24	0.25	0.26	0.27	0.28
2000	0.19	0.20	0.20	0.21	0.21	0.22	0.23	0.23	0.24	0.24	0.25	0.26
2001	0.20	0.20	0.21	0.21	0.22	0.22	0.23	0.23	0.24	0.24	0.25	0.26
2002	0.19	0.19	0.19	0.20	0.20	0.21	0.21	0.22	0.22	0.23	0.23	0.24
2003	0.20	0.21	0.21	0.21	0.22	0.22	0.23	0.23	0.24	0.24	0.25	0.25
2004	0.19	0.19	0.19	0.20	0.20	0.21	0.21	0.22	0.22	0.22	0.23	0.24
2005	0.20	0.20	0.21	0.21	0.22	0.22	0.23	0.23	0.23	0.24	0.24	0.25
2006	0.19	0.19	0.20	0.20	0.21	0.22	0.23	0.23	0.24	0.25	0.25	0.27
2007	0.19	0.20	0.20	0.21	0.22	0.23	0.24	0.24	0.25	0.26	0.27	0.28
2008	0.19	0.19	0.20	0.20	0.21	0.22	0.23	0.24	0.25	0.26	0.27	0.28
2009	0.19	0.20	0.20	0.21	0.22	0.23	0.24	0.25	0.26	0.27	0.28	0.29
2010	0.19	0.20	0.20	0.21	0.22	0.23	0.24	0.25	0.26	0.27	0.28	0.30
2011	0.20	0.21	0.21	0.22	0.22	0.23	0.23	0.24	0.25	0.25	0.26	0.28
2012	0.19	0.20	0.20	0.21	0.21	0.22	0.23	0.23	0.24	0.25	0.25	0.26

Table 7. (continued) Relative foraging rate (Holsman and Aydin, 2015).

Pacific Cod	Age											
	1	2	3	4	5	6	7	8	9	10	11	12
1979	0.33	0.35	0.39	0.45	0.55	0.69	0.83	0.97	1.07	1.13	1.16	1.20
1980	0.33	0.35	0.39	0.45	0.55	0.69	0.83	0.97	1.07	1.13	1.16	1.20
1981	0.32	0.34	0.37	0.44	0.53	0.67	0.84	1.03	1.21	1.33	1.38	1.31
1982	0.32	0.34	0.39	0.48	0.61	0.78	0.93	1.03	1.07	1.11	1.20	1.57
1983	0.36	0.38	0.42	0.49	0.59	0.73	0.90	1.08	1.23	1.35	1.42	1.45
1984	0.33	0.34	0.38	0.44	0.53	0.67	0.82	1.00	1.15	1.27	1.33	1.33
1985	0.35	0.36	0.40	0.47	0.57	0.71	0.86	1.00	1.13	1.21	1.26	1.30
1986	0.35	0.37	0.41	0.48	0.59	0.72	0.86	0.99	1.08	1.13	1.16	1.19
1987	0.32	0.34	0.38	0.44	0.54	0.67	0.83	1.00	1.14	1.24	1.29	1.29
1988	0.34	0.35	0.39	0.46	0.56	0.69	0.83	0.96	1.05	1.10	1.13	1.16
1989	0.35	0.37	0.41	0.48	0.59	0.73	0.90	1.07	1.21	1.31	1.36	1.37
1990	0.34	0.35	0.39	0.46	0.56	0.69	0.84	0.98	1.09	1.16	1.19	1.23
1991	0.33	0.35	0.39	0.45	0.55	0.68	0.83	0.96	1.07	1.13	1.16	1.20
1992	0.33	0.35	0.38	0.45	0.55	0.68	0.81	0.93	1.00	1.03	1.05	1.07
1993	0.31	0.32	0.35	0.40	0.46	0.54	0.63	0.73	0.83	0.92	0.99	1.08
1994	0.34	0.35	0.39	0.46	0.57	0.70	0.83	0.95	1.02	1.05	1.07	1.09
1995	0.33	0.35	0.39	0.46	0.57	0.69	0.83	0.94	1.00	1.02	1.02	1.04
1996	0.31	0.32	0.35	0.41	0.51	0.63	0.79	0.95	1.09	1.20	1.25	1.23
1997	0.33	0.34	0.38	0.45	0.55	0.68	0.83	0.97	1.07	1.13	1.17	1.20
1998	0.30	0.32	0.36	0.43	0.54	0.70	0.89	1.08	1.21	1.26	1.21	1.02
1999	0.33	0.35	0.39	0.45	0.55	0.66	0.78	0.88	0.94	0.96	0.95	0.92
2000	0.33	0.34	0.38	0.44	0.53	0.64	0.76	0.88	0.98	1.04	1.08	1.10
2001	0.32	0.34	0.37	0.43	0.51	0.61	0.73	0.85	0.97	1.06	1.12	1.18
2002	0.32	0.33	0.36	0.41	0.48	0.57	0.68	0.80	0.91	1.02	1.11	1.20
2003	0.31	0.33	0.36	0.41	0.50	0.62	0.77	0.94	1.10	1.23	1.30	1.31
2004	0.31	0.32	0.35	0.40	0.48	0.58	0.71	0.84	0.96	1.07	1.15	1.21
2005	0.32	0.33	0.37	0.43	0.53	0.66	0.83	0.99	1.14	1.25	1.30	1.27
2006	0.35	0.37	0.41	0.48	0.59	0.72	0.86	0.97	1.04	1.07	1.07	1.09
2007	0.34	0.36	0.41	0.50	0.63	0.80	0.95	1.04	1.07	1.09	1.14	1.42
2008	0.34	0.36	0.41	0.50	0.63	0.79	0.94	1.01	1.03	1.04	1.10	1.47
2009	0.33	0.35	0.40	0.50	0.64	0.82	0.97	1.04	1.05	1.10	1.25	1.94
2010	0.33	0.35	0.41	0.51	0.68	0.87	1.02	1.07	1.11	1.25	1.66	3.43
2011	0.32	0.34	0.38	0.45	0.56	0.71	0.89	1.08	1.24	1.33	1.34	1.23
2012	0.33	0.35	0.39	0.45	0.55	0.69	0.83	0.97	1.07	1.13	1.16	1.20

Table 7. (continued) Relative foraging rate (Holsman and Aydin, 2015).

Arrowtooth flounder	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
1979	0.35	0.34	0.34	0.33	0.33	0.33	0.33	0.34	0.36	0.40	0.45	0.52	0.60	0.68	0.76	0.82	0.86	0.87	0.86	0.83	0.79
1980	0.35	0.34	0.34	0.33	0.33	0.33	0.33	0.34	0.36	0.40	0.45	0.52	0.60	0.68	0.76	0.82	0.86	0.87	0.86	0.83	0.79
1981	0.27	0.26	0.25	0.24	0.22	0.21	0.20	0.20	0.22	0.25	0.30	0.38	0.47	0.57	0.66	0.73	0.75	0.73	0.67	0.60	0.51
1982	0.48	0.48	0.48	0.48	0.48	0.48	0.49	0.51	0.54	0.59	0.66	0.74	0.83	0.93	1.02	1.09	1.15	1.18	1.19	1.18	1.15
1983	0.34	0.34	0.33	0.32	0.30	0.29	0.28	0.29	0.31	0.34	0.40	0.48	0.58	0.68	0.78	0.86	0.90	0.90	0.87	0.82	0.75
1984	0.24	0.24	0.23	0.22	0.21	0.20	0.19	0.19	0.20	0.23	0.26	0.32	0.38	0.46	0.53	0.60	0.64	0.66	0.65	0.62	0.58
1985	0.37	0.37	0.36	0.35	0.34	0.34	0.34	0.35	0.37	0.41	0.47	0.55	0.65	0.74	0.83	0.90	0.94	0.95	0.92	0.88	0.82
1986	0.39	0.39	0.39	0.39	0.39	0.39	0.40	0.42	0.44	0.48	0.54	0.60	0.67	0.75	0.82	0.88	0.92	0.95	0.96	0.96	0.95
1987	0.29	0.29	0.28	0.27	0.26	0.24	0.24	0.24	0.25	0.27	0.31	0.36	0.43	0.50	0.58	0.65	0.71	0.75	0.77	0.77	0.75
1988	0.33	0.33	0.33	0.33	0.32	0.33	0.33	0.35	0.37	0.41	0.45	0.52	0.58	0.65	0.72	0.77	0.80	0.81	0.81	0.79	0.77
1989	0.34	0.34	0.33	0.32	0.30	0.29	0.29	0.29	0.31	0.35	0.40	0.48	0.57	0.66	0.76	0.83	0.88	0.89	0.88	0.84	0.78
1990	0.33	0.33	0.32	0.32	0.31	0.31	0.31	0.32	0.34	0.37	0.41	0.47	0.54	0.62	0.69	0.76	0.80	0.83	0.83	0.82	0.80
1991	0.32	0.32	0.32	0.31	0.31	0.31	0.31	0.32	0.34	0.37	0.42	0.48	0.55	0.62	0.69	0.75	0.79	0.81	0.81	0.80	0.77
1992	0.35	0.35	0.36	0.36	0.37	0.37	0.38	0.40	0.43	0.47	0.51	0.57	0.63	0.69	0.75	0.80	0.84	0.87	0.89	0.89	0.89
1993	0.33	0.32	0.32	0.31	0.30	0.29	0.29	0.29	0.31	0.35	0.40	0.48	0.56	0.65	0.74	0.80	0.84	0.84	0.82	0.78	0.72
1994	0.35	0.36	0.36	0.36	0.37	0.38	0.39	0.41	0.44	0.48	0.53	0.58	0.65	0.71	0.77	0.82	0.86	0.88	0.90	0.90	0.89
1995	0.34	0.34	0.34	0.35	0.36	0.37	0.39	0.41	0.44	0.48	0.52	0.57	0.63	0.69	0.74	0.79	0.83	0.87	0.90	0.92	0.93
1996	0.28	0.28	0.27	0.26	0.24	0.23	0.22	0.22	0.23	0.25	0.28	0.32	0.37	0.43	0.50	0.57	0.63	0.68	0.72	0.74	0.75
1997	0.33	0.33	0.32	0.32	0.31	0.31	0.31	0.32	0.33	0.36	0.40	0.45	0.51	0.58	0.65	0.71	0.77	0.80	0.83	0.83	0.83
1998	0.29	0.28	0.27	0.26	0.25	0.23	0.22	0.23	0.24	0.26	0.31	0.37	0.44	0.53	0.61	0.69	0.75	0.78	0.78	0.75	0.71
1999	0.29	0.30	0.31	0.32	0.34	0.37	0.39	0.42	0.45	0.47	0.49	0.51	0.53	0.56	0.60	0.66	0.73	0.81	0.92	1.04	1.18
2000	0.35	0.35	0.35	0.35	0.34	0.35	0.35	0.37	0.39	0.43	0.48	0.55	0.62	0.69	0.76	0.81	0.85	0.86	0.86	0.85	0.82
2001	0.34	0.34	0.33	0.32	0.31	0.31	0.30	0.31	0.33	0.36	0.41	0.48	0.56	0.64	0.72	0.79	0.84	0.86	0.86	0.84	0.81
2002	0.30	0.30	0.29	0.28	0.27	0.26	0.25	0.25	0.27	0.30	0.34	0.40	0.47	0.56	0.64	0.71	0.77	0.80	0.80	0.79	0.75
2003	0.28	0.28	0.27	0.25	0.24	0.23	0.22	0.21	0.22	0.24	0.27	0.32	0.38	0.46	0.54	0.62	0.69	0.74	0.77	0.78	0.78
2004	0.28	0.28	0.27	0.26	0.25	0.24	0.23	0.24	0.26	0.30	0.37	0.45	0.55	0.65	0.72	0.75	0.73	0.67	0.59	0.49	0.41
2005	0.30	0.29	0.29	0.27	0.26	0.25	0.24	0.24	0.24	0.26	0.28	0.32	0.37	0.42	0.48	0.55	0.61	0.67	0.72	0.75	0.78
2006	0.35	0.35	0.35	0.36	0.37	0.38	0.40	0.42	0.45	0.49	0.53	0.59	0.64	0.70	0.76	0.81	0.85	0.88	0.91	0.93	0.94
2007	0.36	0.37	0.37	0.37	0.38	0.39	0.41	0.43	0.46	0.50	0.56	0.62	0.68	0.75	0.81	0.86	0.90	0.92	0.93	0.94	0.93
2008	0.36	0.37	0.37	0.38	0.39	0.40	0.42	0.45	0.48	0.52	0.56	0.62	0.67	0.73	0.79	0.84	0.89	0.93	0.97	1.00	1.03
2009	0.35	0.35	0.36	0.36	0.37	0.38	0.39	0.41	0.44	0.48	0.54	0.59	0.66	0.72	0.78	0.83	0.87	0.89	0.90	0.91	0.90
2010	0.37	0.37	0.37	0.37	0.37	0.38	0.39	0.41	0.43	0.47	0.52	0.58	0.65	0.72	0.78	0.84	0.88	0.90	0.91	0.91	0.90
2011	0.28	0.28	0.27	0.26	0.24	0.23	0.22	0.22	0.24	0.27	0.32	0.38	0.47	0.56	0.65	0.72	0.76	0.77	0.74	0.70	0.63
2012	0.35	0.34	0.34	0.33	0.33	0.33	0.33	0.34	0.36	0.40	0.45	0.52	0.60	0.68	0.76	0.82	0.86	0.87	0.86	0.83	0.79

Table 8. Proportion mature and residual natural mortality for each species in the model.

[illegible]

Table 9. Components of the likelihood function for each species  $i$  of age  $j$  in year  $y$ . See Tables 2 and 3 for parameter definitions.

Description	Equation	Data source
<b>Data components</b>		
BT survey biomass	$\sum_i \sum_y \frac{[\ln(\hat{\rho}_{iy}^s) - \ln(\hat{\rho}_{iy}^s)]^2}{2\sigma_{sl}^2}$	NFMS annual EBS BT survey (1979–2012)
BT survey age composition	$-\sum_i n_i \sum_y \sum_j (O_{ij,y}^s + v) \ln(\hat{O}_{ij,y}^s + v)$	NFMS annual EBS BT survey (1979–2012)
EIT survey biomass	$\sum_y \frac{[\ln(\hat{\rho}_y^{eit}) - \ln(\hat{\rho}_y^{eit})]^2}{2\sigma_{eit}^2}, \sigma_{eit} = 0.2$	Pollock acoustic trawl survey (1979–2012)
EIT age composition	$-n \sum_y \sum_j (O_{ij,y}^{eit} + v) \ln(\hat{O}_{ij,y}^{eit} + v)$	Pollock acoustic trawl survey (1979–2012)
Total catch	$\sum_i \sum_y \frac{[\ln(\hat{c}_{iy}^*) - \ln(\hat{c}_{iy}^*)]^2}{2\sigma_c^2}, \sigma_c = 0.05$	Fishery observer data (1979–2012)
Fishery age composition	$-\sum_i n_i \sum_y \sum_j (O_{ij,y}^f + v) \ln(\hat{O}_{ij,y}^f + v)$	Fishery observer data (1979–2012)
<b>Penalties</b>		
Fishery selectivity	$\sum_i \sum_j^{A_i-1} \chi \cdot \left[ \ln\left(\frac{\eta_{ij}^f}{\eta_{ij+1}^f}\right) - \ln\left(\frac{\eta_{ij+1}^f}{\eta_{ij+2}^f}\right) \right]^2, \chi = \begin{cases} 20, & \text{if } \eta_{ij}^f > \eta_{ji+1}^f \\ 0, & \text{if } \eta_{ij}^f \leq \eta_{ji+1}^f \end{cases}$	
<b>Priors</b>		
	$\sum_i \sum_y (\tau_{iy})^2$	
	$\sum_i \sum_y (N_{0,ij})^2$	
	$\sum_i \sum_y (\varepsilon_{iy})^2$	
$v = 0.001.$		