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Calculation of Atmospheric Radiances and Brightness Temperatures in Infrared Window Channels of Satellite Radiometers

Washington, D.C.

March 1980

U.S. DEPARTMENT OF COMMERCE
National Oceanic and Atmospheric Administration
National Environmental Satellite Service



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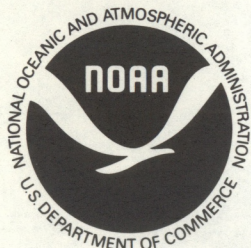
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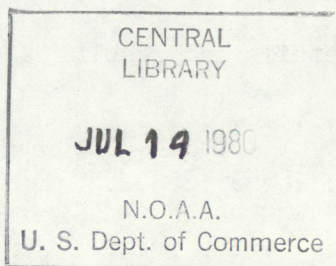


Calculation of Atmospheric Radiances and Brightness Temperatures in Infrared Window Channels of Satellite Radiometers

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U.S. DEPARTMENT OF COMMERCE

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CALCULATION OF ATMOSPHERIC RADIANCES AND BRIGHTNESS TEMPERATURES IN INFRARED WINDOW CHANNELS OF SATELLITE RADIOMETERS

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ABSTRACT. We describe a method of simulating measurements of atmospheric radiances and brightness temperatures in wide-band window channels (at 11 and 3.7 μm) of satellite radiometers. As input the simulation takes vertical profiles of atmospheric temperature and water-vapor mixing ratio, as well as the spectral response functions of the window channels. It models the atmospheric transmittances and integrates the equation of radiative transfer. We demonstrate the use of the method with applications to the Advanced Very High Resolution Radiometer on the TIROS-N satellite.

1. INTRODUCTION

The environmental satellites operated by NOAA's National Environmental Satellite Service (NESS) carry instruments that measure the intensity of radiation upwelling from the earth's surface in the infrared "windows" at wavelengths near 11 μm and 3.7 μm . Among these instruments are the Scanning Radiometers (SR) on the ITOS 1 and NOAA 2-5 satellites, the Very High Resolution Radiometers (VHRR) on the NOAA 2-5 satellites, the Visible and Infrared Spin-Scan Radiometers (VISSR) on the current SMS/GOES satellites, and the Advanced VHRR's (AVHRR) on the current TIROS-N series of satellites. Windows are spectral intervals in which the atmosphere is nearly transparent to the radiation emitted by the earth's surface. Although the atmosphere's effect on the radiation is small, it is, nevertheless, not negligible. For example, in the 11- μm region a moist atmosphere may attenuate the radiation emitted by the earth's surface to space by 5-10%. Therefore, to infer properties of the surface from measurements in windows, we need to model theoretically the radiative transfer in the atmosphere.

This report documents a procedure for computing, in the 11- and 3.7- μm windows, the radiances and brightness temperatures that would be measured by an orbiting radiometer, given the temperature of the earth's surface and the vertical temperature and water-vapor profiles of the atmosphere. The model also takes into account other gases that absorb and emit radiation at these wavelengths. For the instruments considered here, which view in the nadir or near-nadir, these gases are carbon dioxide, nitrogen, nitrous oxide, and methane. The computations apply to spectral intervals whose widths range from several tens to several hundreds of cm^{-1} . A computer program that incorporates the method described in this paper is currently in use at NESS. Copies of this program are available on request.

The literature describes a number of earlier transmittance models that have been applied in the 11- μm window (Wark et al. 1962, Davis and Viezee 1964, Saiedy and Hilleary 1967, Anding and Kauth 1969, Smith et al. 1970, and Maul and Sidran 1973). These works were published before the importance of the self-broadened water-vapor continuum (Bignell 1970) was recognized. More recently the computer code LOWTRAN (McClatchey et al. 1972, Selby et al. 1978) was developed for modelling radiative transfer in the atmosphere in 20- cm^{-1} intervals throughout the infrared spectrum, including both the 11- μm and 3.7- μm window regions.

The method described in this report evolved from the algorithm (Wark et al. 1974, Weinreb and Neuendorffer 1973) developed at NESS to calculate radiances in the 11- μm window channel of the Vertical Temperature Profile Radiometers (VTPR) (McMillin et al. 1973) on the NOAA 2-5 satellites.

The present method has the following new features:

1. It can be applied to spectral intervals that are several hundred cm^{-1} in width. (The VTPR interval was about 8 cm^{-1} in width.)
2. It applies in both the 3.7- and the 11- μm windows.
3. It incorporates recent advances in calculating transmittances, particularly those in modelling the nitrogen absorption near 4 μm and the water-vapor continua in the 11- and 3.7- μm regions.

Section 2 of this report introduces the radiative transfer equation and describes our techniques of calculating radiances and brightness temperatures while coping with the variation of the Planck function over the considerable width (in wavenumber) of the spectral intervals. Section 3 describes the transmittance calculations, which include the effects of H_2O lines and continua, the collision-induced N_2 band near 4 μm , and the "uniformly mixed" gases, particularly CO_2 , CH_4 , and N_2O . Section 4 describes the numerical procedures for calculating transmittances and integrating the radiative transfer equation. The report concludes with a few applications of the calculations to the AVHRR on TIROS-N.

2. APPLICATION OF THE RADIATIVE TRANSFER EQUATION IN WIDE SPECTRAL INTERVALS

2.1 The Radiative Transfer Equation

The upwelling radiance $R(\nu)$ at wavenumber ν can be calculated from knowledge of the temperature of the earth's surface, the atmospheric vertical temperature profile, and the vertical profiles of concentrations of the gases that absorb radiation at ν . We accomplish this by numerically integrating the equation of radiative transfer in its integral form (see, e.g., Wark and Fleming 1966),

$$R(\nu) = B(T_s, \nu) \tau(p_s, \nu) - \int_1^{\tau(p_s, \nu)} B(T(p), \nu) d\tau(p, \nu), \quad (1)$$

where B = Planck radiance,
 T = atmospheric temperature,
 s = subscript indicating that a quantity is to be evaluated at the earth's surface,
 p = atmospheric pressure, and
 $\tau(p, \nu)$ = transmittance between the satellite and the level of the atmosphere with pressure p .

The Planck radiance is given by

$$B(T, \nu) = \frac{2hc^2 \nu^3}{\exp[hc\nu/kT] - 1},$$

where h , c , and k are, respectively, Planck's constant, the speed of light, and Boltzmann's constant.

Equation (1) holds under cloudless conditions for nonscattering, plane-parallel atmospheres in local thermodynamic equilibrium.

2.2 Radiance Calculations in Wide Spectral Intervals

Equation (1) holds only for monochromatic radiation. For it to be applied to a spectral interval of a broad-band instrument, it must be convoluted with the spectral response function $\phi(\nu)$ of the interval. Figures 1 and 2 show such functions for channels 4 and 3 of the AVHRR on TIROS-N. The radiance R_ϕ that would be measured in any of these intervals is then given by

$$R_\phi = \int_0^\infty R(\nu) \phi(\nu) d\nu \bigg/ \int_0^\infty \phi(\nu) d\nu, \quad (2)$$

where $R(\nu)$ is computed from equation (1). To integrate equation (2) numerically, one must first integrate equation (1) numerically for a large number of closely spaced values of ν . This is too cumbersome for our purposes. However, if the function $\phi(\nu)$ is narrow enough (say, 30 cm^{-1} or less in half-width), we can find a wavenumber ν_0 such that R_ϕ can be approximated adequately (Wark and Fleming 1966) by

$$R_{\phi} = B(T_s, \nu_0) \tau(p_s, \nu_0) - \int_1^{\tau(p_s, \nu_0)} B(T(p), \nu_0) d\tau(p, \nu_0), \quad (3a)$$

where

$$\tau(p, \nu_0) = \int_0^{\infty} \tau(p, \nu) \phi(\nu) d\nu \quad \bigg/ \int_0^{\infty} \phi(\nu) d\nu. \quad (3b)$$

Unfortunately, we are working with spectral intervals having widths of 100 cm^{-1} or greater, for which eq. (3) produces errors comparable to or exceeding the noise in the measurements of R_{ϕ} . We resort, then, to a more accurate procedure. We first subdivide each spectral interval into rectangular subintervals, 30 or 20 cm^{-1} in width, as shown in figures 3 and 4. Within these subintervals eq. (3) is an adequate approximation (see below); i.e., if the index i labels each subinterval, we can apply eq. (3) to compute a value of radiance R_i in the subinterval. Then to estimate the radiance for the full interval, we compute the weighted mean of the R_i 's, where the weights are the heights h_i shown in figures 3 and 4. That is,

$$R_{\phi} = \sum_i h_i R_i / \sum_i h_i. \quad (4)$$

In our calculations we chose the ν_0 's to be at the center of each subinterval, and we chose the h_i 's so that in each subinterval the area under the spectral response function equals the area of the rectangle. As shown in figures 3 and 4, the widths of the subintervals are 30 cm^{-1} near $11 \mu\text{m}$ and 20 cm^{-1} in the $3.7\text{-}\mu\text{m}$ region.

The accuracy of eq. (4) depends on the behavior of not only the Planck radiance, but also the transmittance, as functions of wavenumber in the spectral interval of interest. A simple, rough way to estimate the accuracy of eq. (4) is to ignore the transmittances, i.e., work with blackbody radiances instead of atmospheric radiances. Following this approach, for fixed temperature T we computed the blackbody radiances in three separate ways, the "exact" calculation and two approximations. For the exact calculation, we convoluted the Planck function $B(T, \nu)$ with the spectral response function, i.e., we applied eq. (2) with $R(\nu)$ replaced by $B(T, \nu)$. In numerically evaluating the integrals we applied the trapezoidal rule on points spaced every 0.1 cm^{-1} . The first approximation was simply the Planck function evaluated at the centroid of the spectral response function. (This is the form of eq. (3) for blackbody radiances.) For the spectral response functions shown in figures 1 and 2, the centroids are at 913.3 cm^{-1} and 2656.3 cm^{-1} , respectively. The second approximation was the one of eq. (4),

with R_i replaced by $B(T, \nu)$. The errors in each approximation were computed as the differences between the results of the approximations and those of the "exact" calculation. The absolute values of these errors are shown in figure 5 as functions of temperature. The upper panel applies to the AVHRR's 11- μ m channel, and the lower to the AVHRR's 3.7- μ m channel. The horizontal dashed lines are the nominal values of the NEAN's (instrument noise, in radiance units) in the two channels. At 11 μ m, the first approximation (centroid) produces errors comparable in magnitude to the NEAN, while the second approximation (eq. (4)) holds the errors to values less than half of the NEAN. At 3.7 μ m, the first approximation (centroid) produces errors many times larger than the NEAN, while eq. (4) reduces these errors to values approximately equal to the NEAN. However, since we have ignored the transmittances in this analysis, the results provide only an estimate of the errors.

In the remainder of this report, eq. (4) is used in computations of atmospheric radiances.

2.3 Conversion of Atmospheric Radiances to Brightness Temperatures

In many applications, users of satellite data prefer to work with equivalent brightness temperature rather than radiance. We convert our calculated atmospheric radiances to brightness temperatures through look-up tables, one for each channel. Each table consists of 1501 pairs of blackbody radiances and their corresponding temperatures. The pairs are specified every 0.1°K between 180°K and 330°K. Each value of blackbody radiance in a table depends upon the spectral response function ϕ and is computed from eq. (4), with R_i replaced by $B(T, \nu_0)$. In other words, it is the weighted average of Planck radiances evaluated at the centers of the rectangular subintervals of figures 3 or 4, with the weights given by the heights h_i . The data in the look-up tables for channels 3 and 4 of the AVHRR are graphed in figure 6.

It is important to realize that because they are computed from eq. (4), the blackbody radiances in the look-up tables are not error-free, but carry with them the errors shown in figure 5. However, by computing the look-up table this way, we tend to minimize the errors in the inferred equivalent brightness temperatures, for the following reason: Recall that the first step in deriving an equivalent brightness temperature is the application of eqs. (3) and (4) to the atmospheric temperature profile to produce an atmospheric radiance. As previously described, this radiance carries with it an error than can be estimated from figure 5. The second step is to refer to this value of radiance in the look-up table and extract the corresponding equivalent brightness temperature. If the blackbody radiances in the look-up table are subject to exactly the same errors as are the atmospheric radiances, the errors in the two steps will compensate, and the derived equivalent brightness temperatures will be error-free. As described earlier, however, the errors in the blackbody radiances will not coincide exactly with the errors in the atmospheric radiances. Hence, using the look-up table generated from eq. (4), we will minimize the errors in the inferred equivalent brightness temperatures but not eliminate them.

3. CALCULATIONS OF TRANSMITTANCES

3.1 General

The first step in calculating radiances is to generate transmittances in each of the subintervals shown in figures 3 and 4. In the 11- μm window, eight intervals, each 30 cm^{-1} wide, span the region from 760 to 1000 cm^{-1} . In the 3.7- μm window, 23 intervals, each 20 cm^{-1} wide, span the region from 2440 to 2900 cm^{-1} . In each subinterval, the transmittance of the atmosphere is treated as a product of the transmittances of the atmospheric constituents that absorb radiation. In the 11- μm region, the constituents are water vapor and the "uniformly mixed gases" (McClatchey et al., 1972), principally carbon dioxide. In the 3.7- μm region, the constituents are water vapor, molecular nitrogen, and the uniformly mixed gases, chiefly carbon dioxide, nitrous oxide, and methane. We have intentionally neglected ozone. It is important only between 980 and 1000 cm^{-1} , whereas the responses of our satellite instruments, as measured by the $\phi(\nu)$ functions, are small, if not zero, in this subinterval. The effects of aerosols and clouds are also ignored.

3.2 Atmospheric Absorption Spectra

The purpose of this section is to describe generally the nature of atmospheric absorption in the window regions. Figures 7 and 8 are measured absorption spectra of the atmosphere in the 11- and 3.7- μm regions, respectively (Weinreb, Planet, and Jones 1977). (Figure 7 does not cover the entire 760-1000 cm^{-1} range, but it is useful, nonetheless, for the qualitative discussion here.) The spectra were taken with a spectrometer receiving solar radiation through the McMath solar telescope at the Kitt Peak National Observatory. The spectral resolution is about 0.7 cm^{-1} near 11 μm , and 7.0 cm^{-1} near 3.7 μm .

In the 11- μm window, water vapor dominates the absorption, contributing spectral lines and a continuum. The continuum (Bignell 1970) is absorption that has little dependence on wavenumber. In figure 7 its effect is most noticeable between the spectral lines, where the envelope of the spectrum has a value of transmittance less than one. In this case it is about 0.98, so the continuum absorption is about 2%. Incidentally, this spectrum was taken under very dry conditions (precipitable water = 0.6 cm). Under typical mid-latitude or tropical conditions (precipitable water \approx 2 or 6 cm, respectively), the absorption is considerably stronger. For wavenumbers lower than 820 cm^{-1} , carbon dioxide makes some contribution to the absorption. Its effect is seen in the strong line near 792 cm^{-1} and in the background absorption that increases with decreasing wavenumber. Carbon dioxide also has a small effect between 930 and 1000 cm^{-1} (not shown in figure 7). As mentioned in the preceding section, our calculations ignore the absorption by ozone, which is measurable only for $\nu > 980 \text{ cm}^{-1}$.

In the 3.7- μm window, the principal absorbers are nitrous oxide, carbon dioxide, methane, water vapor (mostly as HDO), and molecular nitrogen. Nitrous oxide contributes the band near 2570 cm^{-1} and the high-wavenumber part of the sharp fall-off between 2400 and 2500 cm^{-1} . Near 2400 cm^{-1} carbon dioxide dominates, but it rapidly loses strength toward higher wavenumbers. The region between 2400 and 2500 cm^{-1} is also affected by the collision-induced nitrogen absorption (Shapiro and Gush 1966, and Farmer and Houghton 1966). Between 2700 and 2900 cm^{-1} , water vapor and methane are the principal absorbers. Throughout the 3.7- μm window there is also a small contribution from the water-vapor continuum (White et al. 1978).

3.3 Transmittance of Atmospheric Constituents

3.3.1 Water Vapor

The transmittance of water vapor in the rectangular subintervals is treated as a product of the transmittances of spectral lines and of continua. For calculating transmittances of spectral lines, we use the method of Weinreb and Neuendorffer (1973). This method demands far less time and memory on the computer than does the line-by-line technique, yet it is nearly as accurate. The method treats the atmosphere as a succession of homogeneous layers, in each of which the pressure, temperature, and mixing ratio are constant. Over the path between the satellite and the bottom of a given layer, the transmittance τ_ℓ is computed from a function of the layer's total pressure (P) and temperature (T), and a scaled value of the water vapor amount (U). For the function of P, T, and U we chose a polynomial representation similar to that suggested by Smith (1969). In our calculation we used the following polynomial expression:

$$\ln(-\ln \tau_\ell) = \sum_{i=1}^{14} C_i(v) X_i ,$$

where τ_ℓ is transmittance averaged over the rectangular subinterval,

$$X_1 = 1, \quad X_2 = 0.1 \ln(UT/273), \quad X_3 = \ln(P/1000),$$

$$X_4 = \ln(T/273), \quad X_5 = X_2 X_3, \quad X_6 = X_2 X_4 ,$$

$$X_7 = X_2^2, \quad X_8 = X_4 X_7, \quad X_9 = X_3 X_4,$$

$$X_{10} = X_2 X_7, \quad X_{11} = X_4 X_6, \quad X_{12} = X_4^2 ,$$

$$X_{13} = X_3 X_6, \text{ and } X_{14} = X_3 X_7.$$

The polynomial coefficients C_i were derived by a least-squares fitting of the polynomial to transmittances calculated line by line (Neuendorffer 1977) and averaged over the rectangular subintervals for a large dependent sample of homogeneous paths. Table 1 lists these coefficients.

The heart of the approximation is the procedure for calculating the scaled values of U in each layer. This is described in detail by Weinreb and Neuendorffer (1973).

The two water vapor continua are usually termed the self-broadened and the foreign-broadened continua. In the former, the absorption coefficient is proportional to the partial pressure of water vapor, while in the latter it is proportional to the partial pressure of the dry atmosphere. Following Roberts et al. (1976), the atmospheric transmittance in the self-broadened continuum is given by the equation,

$$-\ln \tau_{sb}(L, \nu) = C^0(\nu) \int_0^L W_{H_2O} P_{H_2O} \exp[T_0(\frac{1}{T} - \frac{1}{296})] dl, \quad (5)$$

where $\tau_{sb}(L, \nu)$ = transmittance between the satellite and a level in the atmosphere at a distance L cm from the satellite,
 W_{H_2O} = density of water vapor, in molecules cm^{-3} ,
 P_{H_2O} = partial pressure of water vapor, in atmospheres,
 T_0 = reference temperature described below, and
 $C^0(\nu)$ = coefficient described below.

For convenience in computation we have applied the hydrostatic equation to eq. (5) and made some changes in units to obtain

$$-\ln \tau_{sb}(P, \nu) = 5.41 \times 10^{13} C^0(\nu) \sec \theta \int_0^P p r^2 \exp[T_0(\frac{1}{T} - \frac{1}{296})] dp, \quad (6)$$

where θ = angle between line of sight and the local vertical,
 P = atmospheric pressure in mb,
 r = mass mixing ratio of water vapor in g/kg, and
 $\tau_{sb}(P, \nu)$ = transmittance between the satellite and a point in the atmosphere with pressure P .

The values of C^0 in eq. (6) are listed in table 2. For the 11- μm region, these values were derived from Roberts et al. (1976). For the 3.7- μm region they came from Burch et al. (1971). For T_0 we use 1800°K in the 11- μm region, (Roberts et al. 1976), and in the 3.7- μm region we use the value of 1300°K, which was derived from the data of Burch et al. (1971).

The foreign-broadened continuum was ignored in the 11 μm region, because its effect is reported to be negligible (Roberts et al. 1976). In the 3.7- μm region, however, it cannot be ignored. The transmittance τ_f for this continuum is given by (Burch 1971),

$$-\ln \tau_f(L, \nu) = \gamma C^0(\nu) \int_0^L W_{\text{H}_2\text{O}} P_D d\ell . \quad (7)$$

The notation in eq. (7) is the same as in eq. (5). Also, P_D is the partial pressure of the dry atmosphere, and γ is the ratio of foreign broadening to self-broadening. Equation (7) contains no temperature dependence, in part because it is poorly known, and in part because it is small.

As suggested by Burch et al. (1971) we adopted the value 0.12 for γ . Inserting this into eq. (7), using the approximation P_D = total pressure, and manipulating eq. (7) as we did eq. (5), we obtain

$$-\ln \tau_f(P, \nu) = 4.04 \times 10^{15} C^0(\nu) \sec \theta \int_0^P p r dp. \quad (8)$$

Note that the coefficients $C^0(\nu)$ have been selected at the centers of the subintervals of figures 3 and 4. Since these coefficients are slowly varying functions of wavenumber, the transmittances calculated from them are representative of averages over the subintervals of figures 3 and 4.

We have discussed separately the methods of calculation of transmittances for water vapor in spectral lines and the two continua. To obtain the overall transmittance of water vapor, we take the product of the transmittances of these three components.

3.3.2 Molecular Nitrogen

Molecular nitrogen has a collision-induced absorption band centered at 2330 cm^{-1} . Following Burch et al. (1971), the transmittance τ_N in this band for homogeneous paths (paths where pressure, temperature, and mixing ratios are all constant), is given by,

$$-\ln \tau_N(L, \nu) = 5.67 \times 10^{26} C_N(T, \nu) \frac{P_A^2 L}{T}, \quad (9)$$

where P_A = atmospheric pressure in atmospheres, and $C_N(T, \nu)$ = Burch's "self-induced" coefficient for nitrogen absorption, in units of $\text{molecules}^{-1} \text{cm}^2 \text{atm}^{-1}$. The remaining notation is as in eq. (5).

The coefficient $C_N(T, \nu)$ has a pronounced dependence on temperature, which is formulated as follows: Susskind and Searl (1977) demonstrate that the quantity $\frac{\ln \tau_N}{\rho_L^2}$ is very nearly independent of T , where ρ is number density of N_2 in units of molecules cm^{-3} . By combining eq. (9) with the hydrostatic equation, we get

$$C_N(T, \nu) \sim \frac{\ln \tau_N(L, \nu)}{\rho_L^2 T}.$$

Therefore, $C_N(T, \nu)$ has a temperature dependence of $\frac{1}{T}$, and we can define a temperature-independent coefficient $C_N(296, \nu)$ by

$$C_N(296, \nu) = \frac{T}{296} C_N(T, \nu). \quad (10)$$

Combining eqs. (9) and (10) and applying the result to an atmospheric slant path, we obtain

$$-\ln \tau_N(L, \nu) = 5.67 \times 10^{26} C_N(296, \nu) \int_0^L \left(\frac{296}{T}\right) \frac{P_A^2}{T} d\ell. \quad (11)$$

Manipulating eq. (11) as we did eq. (5), we obtain the form used in our computations,

$$-\ln \tau_N(P, \nu) = 4.77 \times 10^{21} C_N(296, \nu) \sec \theta \int_0^P p/T dp. \quad (12)$$

The coefficients $C_N(296, \nu)$ were derived from Shapiro and Gush (1966) and are given in the fourth column of table 2. Since they are slowly varying functions of wavenumber, the transmittances calculated from them are representative of averages over the subintervals of figures 3 and 4.

3.3.3 Uniformly mixed gases

The uniformly-mixed gases comprise CO_2 , N_2O , CO , CH_4 , and O_2 . As mentioned in section 3.2, CO_2 absorbs weakly in the 11- μm window, whereas CO_2 , N_2O and CH_4 absorb weakly in the 3.7- μm window. The method of calculating transmittances is taken from LOWTRAN (McClatchey et al. 1972 and Selby et al. 1978) and is summarized in the following paragraphs.

The transmittances from LOWTRAN have a spectral resolution of 20 cm^{-1} and are specified at every 5 cm^{-1} throughout the visible and infrared spectrum. Transmittances are computed separately for each of the processes in the atmosphere, e.g., absorption by uniformly mixed gases, absorption by water vapor continua, molecular scattering, etc. The uniformly mixed gases are treated as a unit, with relative concentrations given in McClatchey et al. (1972). These concentrations are built into the model, so that the user does not have to specify them. The basic idea of LOWTRAN is that transmittances through any slant path can be calculated rapidly in a single operation by the equation,

$$\tau_u(\nu, P, T) = F \left[C_u(\nu) + \log_{10} \omega(P, T) \right], \quad (13)$$

where τ_u = transmittance of the uniformly mixed gases,
 $C_u(\nu)$ = wavenumber-dependent coefficient, related to the absorption coefficient representing a 20 cm^{-1} interval,
 ω = "equivalent absorber amount" in the slant path, and
 F = a known function, specified in a look-up table, as described below.

LOWTRAN applies eq. (13) in calculations of transmittances for all molecular species. However, the following material, which describes the variable ω and the coefficient $C_u(\nu)$, applies only to the uniformly mixed gases.

The "equivalent absorber amount" ω , between an atmospheric layer at altitude Z (km) and the satellite, is given by

$$\omega = \sec \theta \int_Z^{\infty} \left(\frac{P}{P_0} \right)^{7/4} \left(\frac{T_0}{T} \right)^{11/8} dz, \quad (14)$$

where T_0 and P_0 are standard temperature and pressure (273.15°K and 1013 mb in LOWTRAN).

Manipulating eq. (14) as we did eq. (5), we obtain the form used in our computations,

$$\omega = 7.89 \times 10^{-3} \sec \theta \int_0^P \left[\frac{p}{P_0} \left(\frac{T_0}{T} \right)^{1/2} \right]^{3/4} dp, \quad (15)$$

where the notation is the same as in eq. (6).

The wavenumber-dependent coefficients $C_u(\nu)$, taken from Selby et al. (1978), are listed in table 2.

For convenience in describing the function F , we define its argument to be β , i.e.,

$$\beta \equiv C_u(\nu) + \log_{10} \omega(P,T).$$

The argument β is evaluated by the procedures already described. The final step in determining τ_u is to use the look-up table relating β to τ_u . In figure 9 this relation is graphed over the part of its domain that corresponds to $.900 \leq \tau \leq .999$. This range covers the values of transmittance that are encountered in the 3.7- and 11- μm windows for the vertical or nearly vertical paths considered here. As an example of the use of the look-up table, figure 9 shows that if one enters a value of -0.5 for β , he finds a value of approximately 0.97 for τ_u . Since the values of transmittance derived in this way are averages over 20-cm^{-1} intervals, they can be applied directly in the 20-cm^{-1} rectangular subintervals in the 3.7- μm window. In the 11- μm window, we used the 20-cm^{-1} averages for LOWTRAN to represent the transmittances in the 30-cm^{-1} wide rectangular subintervals. Since the absorption is small and varying slowly with wavenumber, we are confident that this additional approximation is permissible.

4. COMPUTATIONAL DETAILS AND RESULTS

4.1 Quadrature

The computations of transmittances employ eqs. (6), (8), (12), and (15), which involve integrals with respect to atmospheric pressure. In numerically evaluating these integrals, we apply the trapezoidal rule on the 100 quadrature points listed in table 3. These points represent equal increments on the scale of $p^{2/7}$.

In computing radiances we evaluate eq. (3a) by the trapezoidal rule, specifying B and τ at the 100 quadrature points listed in table 3. Because the transmittances are already averages over the rectangular subintervals of figures 3 and 4, as discussed in the previous section, we do not use eq. (3b). As also discussed previously, the wide-band radiances are computed from eq. (4), and brightness temperatures are inferred from the look-up table as illustrated in figure 6.

With the 100 quadrature points of table 3, we can most conveniently compute radiances for those atmospheres that have their surface pressure equal to 1000 mb. However, the computer program that performs these calculations can also handle atmospheres with surface pressures different from 1000 mb. If the surface has a pressure greater than 1000 mb, we simply include that level in all the integrations as a 101st quadrature point. On the other hand, if the surface has a pressure less than 1000 mb, we retain all 100 quadrature levels in the integrations. However, to all levels whose pressures exceed the surface pressure, we assign a value of temperature equal to the surface temperature and a value of mixing ratio equal to the mixing ratio at the surface. Also, in eq. (3a) the surface term is placed at the 1000 mb level. The radiances that are computed by this procedure are identical to the

radiances that would have been computed if we had integrated from the top of the atmosphere down only as far as the actual surface.

For completeness we should also mention that the computer program is designed to use two values of temperature at the surface; one to represent the radiative temperature of the surface itself (T_s), and the second to represent the temperature of the atmosphere at the surface (the shelter temperature), e.g. the value of T at $P = 1000$ mb. Often, however, atmospheres are provided without a value of T_s being specified. In that case the program automatically picks a value of T_s equal to the shelter temperature.

4.2 Examples

4.2.1 Atmospheres

All calculations were done for the three atmospheres whose temperature profiles are shown in figure 10, and whose profiles of water-vapor mixing ratio are shown in figure 11. They represent a diversity of conditions. All three of these examples have $P = 1000$ mb at the earth's surface.

4.2.2. Transmittances

Figures 12 and 13 show transmittances calculated in each of the sub-intervals in the 11- and 3.7- μ m windows, respectively, for water-vapor, nitrogen, and the uniformly-mixed gases. The AVHRR spectral response functions also appear in these figures. In figure 12 the water-vapor transmittances were calculated for two atmospheres -- 64°N, labelled "dry" (total precipitable water = 0.75 cm), and 9°N, labelled "moist" (total precipitable water = 4.86 cm). The absorption by the uniformly mixed gases is unchanged for the two atmospheres. Not only is water vapor the strongest absorber in this spectral region, but it is also the most variable. In figure 13 the transmittances were calculated for only the moist (9°N) atmosphere. Since the absorption is weak in this region of the spectrum, its variability from wet to dry is less than that observed at 11 μ m. In any case, water vapor is the principal absorber for wavenumbers higher than about 2600 cm^{-1} . Below 2600 cm^{-1} , the nitrogen collision-induced absorption is of significance, and it becomes dominant below 2500 cm^{-1} .

4.2.3 Atmospheric Attenuation

Atmospheric attenuation is used here to mean the difference between the earth's surface temperature and the brightness temperature measured at the satellite. This quantity is of interest because one of the major applications of data from satellite-borne radiometers is in determining surface temperature. In operational sounding we seldom have available the atmospheric temperature and humidity profiles necessary to calculate attenuation by the method of this report. However, these calculations are useful for simulations and for case studies, where data from both the satellite radiometer and concurrent radiosondes are available.

Figure 14 shows the variation of attenuation with total precipitable water in the atmosphere for a vertical path ($\sec\theta = 1$). The calculations were done for the AVHRR's channel 4 (lower panel) and channel 3 (upper panel). In all calculations the surface temperatures were set equal to the temperatures at 1000 mb. Calculations were done separately for each of the three atmospheres of figures 10 and 11. We varied the total precipitable water by multiplying the mixing ratio profiles from figure 10 by 0.1, 0.2, 0.5, 1, 2, 3, and 4. However, the mixing-ratios were never allowed to exceed values at saturation.

As expected, the attenuation at $11\ \mu\text{m}$ is a stronger function of precipitable water than is the attenuation at $3.7\ \mu\text{m}$. One interesting result is that for precipitable water less than about 2 cm, the attenuation is greater at $3.7\ \mu\text{m}$ than it is at $11\ \mu\text{m}$, while for the higher water vapor amounts the reverse is true. This is a consequence of the fact that water vapor is the major absorber in one interval, while the uniformly mixed gases and nitrogen predominate in the other.

Figure 15 illustrates a second, perhaps more realistic, approach to demonstrate the dependence of attenuation on total precipitable water in the $11\text{-}\mu\text{m}$ window. The data in this figure were compiled by E.P. McClain (1979) from a set of 60 atmospheres representing a range of typical maritime conditions around the globe. From our computer program, he obtained the attenuation in a vertical path for each atmosphere, and these are plotted as the '+'s in the figure. Incidentally, in all calculations, he set the surface temperatures equal to the temperatures at 1000 mb. The solid lines in the figure are the data from figure 14, which are included for the purpose of comparison.

Figures 16 and 17 show the variation of attenuation with surface temperature for channels 4 and 3, respectively, for vertical paths. These calculations were also done separately for each of the three atmospheres. In each, we varied the surface temperature about the 1000 mb value given in figure 10 by 0°K , $+3^\circ\text{K}$, $+6^\circ\text{K}$, $+9^\circ\text{K}$, and $+12^\circ\text{K}$. The arrows indicate the temperature at 1000 mb for each atmosphere.

5. CONCLUSION

The method described here enables us to calculate atmospheric radiances, brightness temperatures, and attenuations in the wide spectral intervals of satellite radiometers in the 3.7- and $11\text{-}\mu\text{m}$ windows. The method involves integrating the radiative transfer equation. Because transmittances are modelled rather than computed line by line, the calculations are rapid. As input, the method requires vertical profiles of atmospheric temperature and water-vapor mixing ratio. Hence its main utility is in case studies and simulations, not in real-time retrievals of surface temperatures from satellite data.

We are better able to estimate the accuracy of the calculations at $11\text{ }\mu\text{m}$ than at $3.7\text{ }\mu\text{m}$. Since we have considerable experience (dating back to the SIRS instruments on the Nimbus 3 and 4 satellites in the late 1960s) with calculations and measurements at $11\text{ }\mu\text{m}$, we feel that these calculations are not grossly in error. The error is probably less than $1\text{ mW}/(\text{m}^2\text{ sr cm}^{-1})$. However, at $3.7\text{ }\mu\text{m}$ we have little experience, and we are not in a position to offer an estimate of accuracy. There is a need for work on the absorption properties of atmospheric gases in this spectral region. In addition, studies comparing measurements with the calculations have yet to be carried out.

The method described here is incorporated in a computer program that is available by writing to the authors.

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Table 1.--Polynomial coefficients for spectral lines of water vapor

| Subinterval | $\nu_0(\text{cm}^{-1})^*$ | c_1 | c_2 | c_3 | c_4 | c_5 | c_6 |
|-------------|---------------------------|----------|----------|----------|----------|---------|----------|
| 1 | 775.0 | -2.23135 | 6.12346 | 0.45051 | 2.71498 | 1.20255 | -1.96786 |
| 2 | 805.0 | -1.85030 | 5.82894 | 0.41698 | 2.97656 | 1.11404 | -2.67401 |
| 3 | 835.0 | -3.09180 | 7.02594 | 0.32994 | 3.39958 | 1.23004 | -3.45263 |
| 4 | 865.0 | -2.81430 | 6.57833 | 0.39086 | 3.97101 | 1.26900 | -4.46690 |
| 5 | 895.0 | -3.27104 | 7.08477 | 0.36451 | 3.99316 | 1.13824 | -2.29048 |
| 6 | 925.0 | -3.87608 | 7.84570 | 0.28824 | 5.04843 | 1.23165 | -2.31676 |
| 7 | 955.0 | -3.96672 | 7.95368 | 0.26595 | 4.60590 | 1.02471 | -1.36628 |
| 8 | 985.0 | -4.05978 | 8.80584 | 0.18746 | 5.10449 | 1.06154 | -2.46299 |
| 9 | 2450.0 | -8.43013 | 15.21933 | 0.60791 | 0.0 | 0.0 | 15.86929 |
| 10 | 2470.0 | -8.72307 | 23.63057 | 0.0 | 0.0 | 0.0 | 0.0 |
| 11 | 2490.0 | -6.99218 | 8.24594 | 0.0 | 0.0 | 0.0 | 38.69545 |
| 12 | 2510.0 | -6.38534 | 8.55110 | 0.0 | 0.0 | 0.91916 | 35.69487 |
| 13 | 2530.0 | -5.98694 | 9.68929 | -0.17617 | 3.36765 | 0.0 | 2.67673 |
| 14 | 2550.0 | -5.33819 | 9.31851 | 0.0 | 2.95701 | 0.0 | 0.0 |
| 15 | 2570.0 | -4.24407 | 9.72573 | 0.0 | 1.91971 | 0.0 | -0.94502 |
| 16 | 2590.0 | -3.75231 | 9.61935 | 0.05234 | 1.04405 | 0.46435 | -0.50525 |
| 17 | 2610.0 | -3.24848 | 9.12599 | 0.06984 | 0.27549 | 0.57222 | -0.48066 |
| 18 | 2630.0 | -2.55092 | 8.73256 | 0.16667 | -0.41303 | 1.24934 | 1.04954 |
| 19 | 2650.0 | -2.62371 | 8.72498 | 0.18783 | -0.92050 | 1.16865 | 1.31301 |
| 20 | 2670.0 | -2.57342 | 8.50253 | 0.21895 | -1.35674 | 1.28026 | 1.95386 |
| 21 | 2690.0 | -3.01532 | 8.69507 | 0.13112 | -1.49397 | 0.79516 | 1.75717 |
| 22 | 2710.0 | -2.63606 | 9.24895 | 0.15824 | -0.27694 | 0.80061 | 1.56005 |
| 23 | 2730.0 | -2.07502 | 8.20344 | 0.12908 | -1.29617 | 1.31776 | 1.96238 |
| 24 | 2750.0 | -3.17113 | 8.81213 | 0.12185 | -1.67030 | 0.65181 | 1.46866 |
| 25 | 2770.0 | -2.57576 | 8.39041 | 0.19882 | -1.78166 | 1.26947 | 1.64839 |
| 26 | 2790.0 | -2.31882 | 8.75249 | 0.20187 | -1.25449 | 1.13656 | 1.53516 |
| 27 | 2810.0 | -2.29242 | 8.58541 | 0.17273 | -0.74559 | 1.09597 | 1.18283 |
| 28 | 2830.0 | -2.58936 | 9.27357 | 0.10902 | -0.05086 | 0.83697 | 0.96999 |
| 29 | 2850.0 | -3.20658 | 9.73757 | 0.02928 | 0.23195 | 0.32549 | -0.47011 |
| 30 | 2870.0 | -3.38421 | 9.50275 | 0.04329 | 0.74368 | 0.34426 | -0.78017 |
| 31 | 2890.0 | -3.36249 | 8.32141 | 0.18909 | 1.40180 | 0.59159 | -2.23602 |

*Midpoint of subinterval

Table 1.--Polynomial coefficients for spectral lines of water vapor (continued)

| Subinterval | C ₇ | C ₈ | C ₉ | C ₁₀ | C ₁₁ | C ₁₂ | C ₁₃ | C ₁₄ |
|-------------|----------------|----------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 1 | -3.76620 | 0.16593 | 0.43179 | 3.83257 | 2.18960 | -1.57369 | 3.31522 | -1.34526 |
| 2 | -3.92641 | -2.77498 | 0.31976 | 2.79153 | 0.32945 | -1.52147 | 3.42676 | -1.05728 |
| 3 | -6.40380 | -1.00006 | 0.61283 | 5.99156 | 0.66930 | -0.59443 | 7.08475 | -4.82659 |
| 4 | -5.74839 | -0.50223 | 0.78782 | 6.00689 | 0.48105 | -2.76763 | 7.00733 | -4.61433 |
| 5 | -5.69290 | -0.64269 | 0.30803 | 7.74251 | -2.16183 | -0.78133 | 3.28952 | -5.12407 |
| 6 | -5.89552 | -3.71300 | 0.36473 | 6.08009 | -3.61897 | -0.21804 | 6.03967 | -4.22350 |
| 7 | -4.72846 | -3.68452 | 0.30339 | 5.13370 | -1.26021 | -0.67621 | 5.42607 | -4.19546 |
| 8 | -5.15066 | -9.38148 | 0.43482 | 2.28616 | 0.52204 | -2.57286 | 6.41268 | -3.49313 |
| 9 | -20.04587 | 0.0 | -8.89374 | 20.63594 | -116.74747 | 33.37996 | 0.0 | 0.0 |
| 10 | -50.03848 | 36.53720 | -10.09401 | 55.29951 | -134.74405 | 40.28809 | 0.0 | 16.65234 |
| 11 | 2.24573 | 74.76546 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 5.02699 |
| 12 | 0.0 | 71.44127 | 0.0 | 5.61771 | -35.20401 | 8.97379 | -7.05114 | 0.0 |
| 13 | 4.28756 | 10.06262 | 0.0 | -13.55549 | -9.75042 | 0.0 | 0.0 | 9.83851 |
| 14 | 5.48571 | -3.73073 | 0.0 | -17.92360 | 0.0 | -2.39925 | 0.0 | 4.49243 |
| 15 | 0.74369 | -2.64936 | 0.0 | -13.21884 | 0.0 | -1.99500 | 0.0 | 6.24828 |
| 16 | -1.28595 | -2.82817 | 0.0 | -10.27634 | 0.0 | -1.52861 | 0.0 | 3.20704 |
| 17 | -3.49510 | -0.91434 | 0.0 | -7.74922 | 0.0 | -0.96192 | 0.0 | 1.88804 |
| 18 | -6.33610 | -3.22005 | -0.00891 | 0.95724 | 0.0 | -0.57106 | 3.56149 | -3.29910 |
| 19 | -5.87246 | -3.23284 | 0.0 | 3.32840 | 0.0 | -0.48695 | 3.61152 | -3.90407 |
| 20 | -6.16732 | -2.35241 | -0.09758 | 4.72198 | 0.0 | 0.0 | 3.52096 | -4.33986 |
| 21 | -3.80712 | 1.72189 | -0.11658 | -1.68104 | 0.0 | 0.0 | 0.0 | 1.11738 |
| 22 | -4.91668 | -3.52099 | 0.01092 | 0.41617 | 0.0 | 0.0 | 5.75246 | -4.60047 |
| 23 | -6.62488 | 0.0 | -0.16732 | 1.01783 | -2.43217 | 0.0 | 4.34945 | -2.02269 |
| 24 | -3.44052 | 1.19814 | 0.0 | -1.70164 | 0.0 | 0.0 | 0.0 | 0.98203 |
| 25 | -6.19237 | 0.0 | -0.44376 | 4.41116 | 0.0 | 0.0 | 0.0 | -3.59585 |
| 26 | -5.86578 | -2.40387 | -0.15961 | 3.21334 | 0.0 | 0.0 | 2.97682 | -4.05581 |
| 27 | -5.80459 | -3.41682 | 0.0 | 4.01662 | 0.0 | -0.45678 | 3.43357 | -3.93663 |
| 28 | -4.70158 | -6.29812 | 0.0 | 1.21437 | 0.0 | 0.0 | 5.65174 | -3.46406 |
| 29 | -1.50509 | -0.80652 | 0.0 | -6.04562 | 0.0 | 0.0 | 0.0 | 1.16613 |
| 30 | -1.87255 | 0.0 | 0.0 | -3.55467 | 0.0 | 0.85632 | 0.0 | 0.0 |
| 31 | -2.62032 | 2.13675 | 0.22333 | 2.59861 | 2.14038 | 0.38428 | 0.0 | -0.41753 |

Table 2.--Coefficients for water-vapor continuum, nitrogen absorption,
and uniformly mixed gases

| Subinterval | $\nu_o (\text{cm}^{-1})^*$ | $C^O(\nu) \times 10^{24}$ (molec ⁻¹ cm ² atm ⁻¹) | $C_N(296, \nu) \times 10^{28}$ (molec ⁻¹ cm ² atm ⁻¹) | $C_u(\nu)$ |
|-------------|----------------------------|---------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|------------|
| 1 | 775 | 500 | | -0.53 |
| 2 | 805 | 421 | | -1.18 |
| 3 | 835 | 359 | | -2.51 |
| 4 | 865 | 310 | | -5.00 |
| 5 | 895 | 271 | | -5.00 |
| 6 | 925 | 240 | | -1.71 |
| 7 | 955 | 216 | | -1.11 |
| 8 | 985 | 197 | | -1.33 |
| 9 | 2450 | 4.30 | 323 | -1.12 |
| 10 | 2470 | 3.95 | 240 | -1.20 |
| 11 | 2490 | 3.65 | 164 | -1.54 |
| 12 | 2510 | 3.40 | 99.9 | -2.26 |
| 13 | 2530 | 3.15 | 64.6 | -1.06 |
| 14 | 2550 | 2.90 | 47.0 | -0.45 |
| 15 | 2570 | 2.75 | 29.4 | -0.37 |
| 16 | 2590 | 2.70 | 23.5 | -0.75 |
| 17 | 2610 | 2.70 | 17.6 | -2.60 |
| 18 | 2630 | 2.75 | 5.88 | -2.51 |
| 19 | 2650 | 2.95 | | -2.42 |
| 20 | 2670 | 3.20 | | -2.43 |
| 21 | 2690 | 3.45 | | -2.68 |
| 22 | 2710 | 3.70 | | -2.83 |
| 23 | 2730 | 4.00 | | -2.66 |
| 24 | 2750 | 4.35 | | -2.26 |
| 25 | 2770 | 4.65 | | -2.02 |
| 26 | 2790 | 5.00 | | -1.86 |
| 27 | 2810 | 5.35 | | -1.79 |
| 28 | 2830 | 5.70 | | -1.69 |
| 29 | 2850 | 6.05 | | -1.78 |
| 30 | 2870 | 6.40 | | -1.21 |
| 31 | 2890 | 6.80 | | -0.53 |

*Midpoint of subinterval

Table 3.--The 100 quadrature points for integrations over atmospheric pressure

| Level | Pressure (mb) | Level | Pressure (mb) | Level | Pressure |
|-------|------------------|-------|------------------|-------|-----------|
| 1 | .0100 | 35 | 30.2057 | 68 | 271.2454 |
| 2 | .0225 | 36 | 33.0936 | 69 | 284.8863 |
| 3 | .0435 | 37 | 36.1736 | 70 | 299.0103 |
| 4 | .0756 | 38 | 39.4530 | 71 | 313.6276 |
| 5 | .1220 | 39 | 42.9395 | 72 | 328.7482 |
| 6 | .1858 | 40 | 46.6407 | 73 | 344.3825 |
| 7 | .2704 | 41 | 50.5644 | 74 | 360.5409 |
| 8 | .3795 | 42 | 54.7183 | 75 | 377.2336 |
| 9 | .5169 | 43 | 59.1104 | 76 | 394.4712 |
| 10 | .6866 | 44 | 63.7488 | 77 | 412.2642 |
| 11 | .8928 | 45 | 68.6414 | 78 | 430.6233 |
| 12 | 1.1399 | 46 | 73.7966 | 79 | 449.5590 |
| 13 | 1.4323 | 47 | 79.2226 | 80 | 469.0821 |
| 14 | 1.7747 | 48 | 84.9277 | 81 | 489.2034 |
| 15 | 2.1719 | 49 | 90.9204 | 82 | 509.9338 |
| 16 | 2.6289 | 50 | 97.2092 | 83 | 531.2841 |
| 17 | 3.1507 | 51 | 103.8028 | 84 | 553.2655 |
| 18 | 3.7427 | 52 | 110.7098 | 85 | 575.8890 |
| 19 | 4.4101 | 53 | 117.9389 | 86 | 599.1656 |
| 20 | 5.1584 | 54 | 125.4991 | 87 | 623.1066 |
| 21 | 5.9934 | 55 | 133.3993 | 88 | 647.7232 |
| 22 | 6.9207 | 56 | 141.6485 | 89 | 673.0267 |
| 23 | 7.9462 | 57 | 150.2558 | 90 | 699.0285 |
| 24 | 9.0758 | 58 | 159.2303 | 91 | 725.7401 |
| 25 | 10.3158 | 59 | 168.5813 | 92 | 753.1729 |
| 26 | 11.6724 | 60 | 178.3181 | 93 | 781.3385 |
| 27 | 13.1517 | 61 | 188.4501 | 94 | 810.2486 |
| 28 | 14.7804 | 62 | 198.9869 | 95 | 839.9147 |
| 29 | 16.5050 | 63 | 209.9378 | 96 | 870.3487 |
| 30 | 18.3920 | 64 | 221.3126 | 97 | 901.5623 |
| 31 | 20.4284 | 65 | 233.1210 | 98 | 933.5674 |
| 32 | 22.6209 | 66 | 245.3727 | 99 | 966.3760 |
| 33 | 24.9766 | 67 | 258.0775 | 100 | 1000.0000 |
| 34 | 27.5025 | | | | |

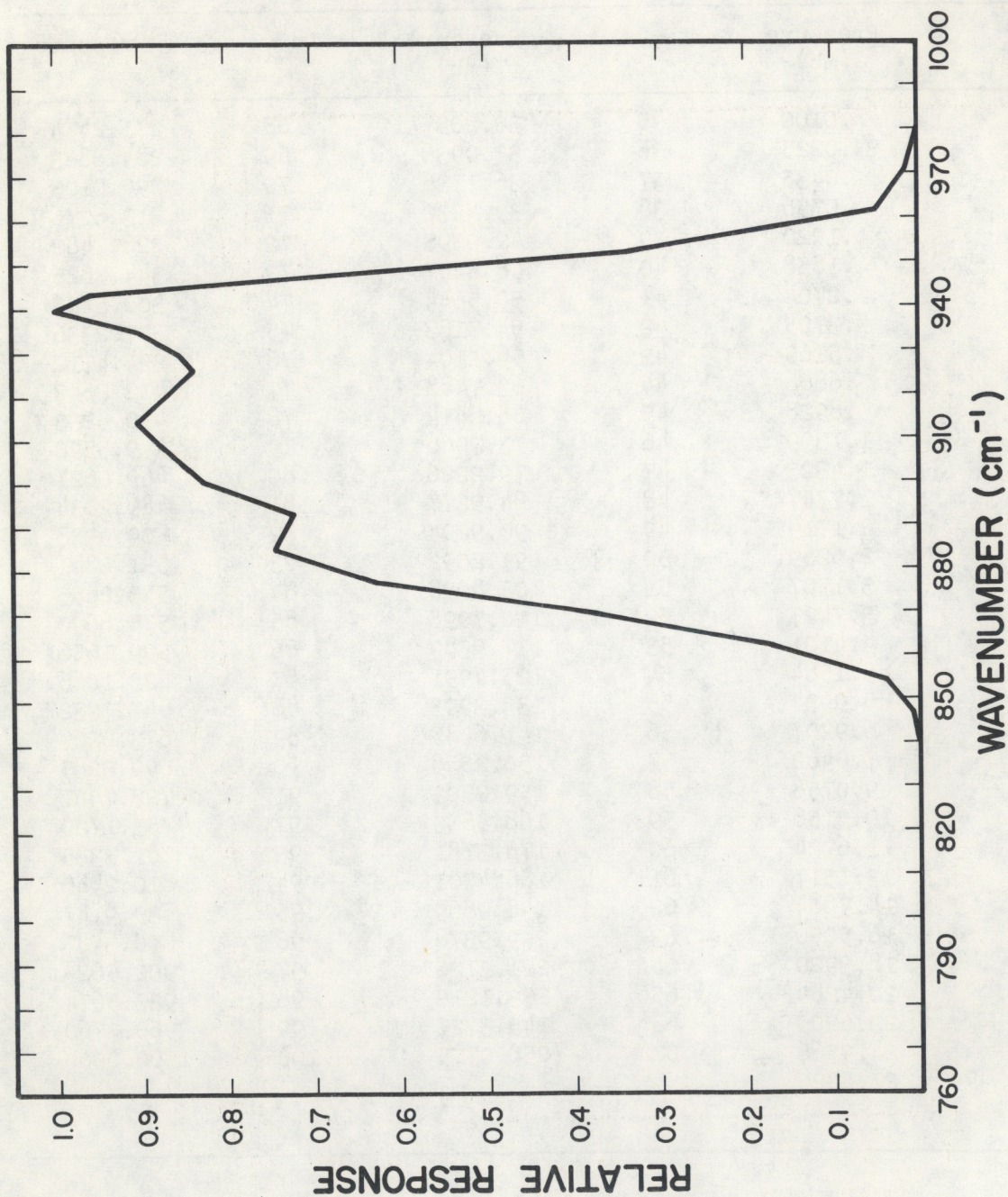


Figure 1.--Spectral response function for channel 4 of AVHRR on TIROS-N (Lauritson 1979).

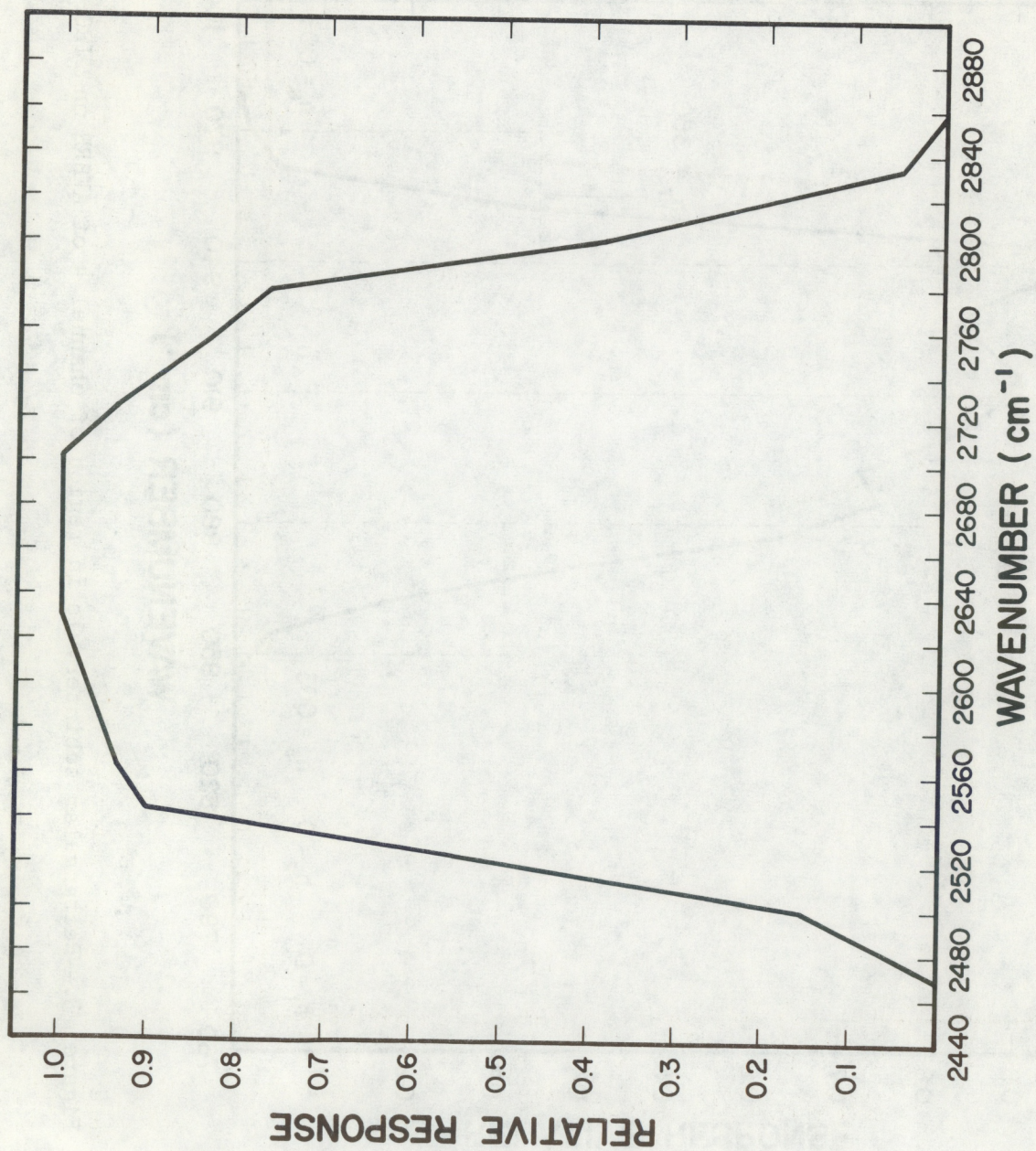


Figure 2.--As in figure 1, for channel 3.

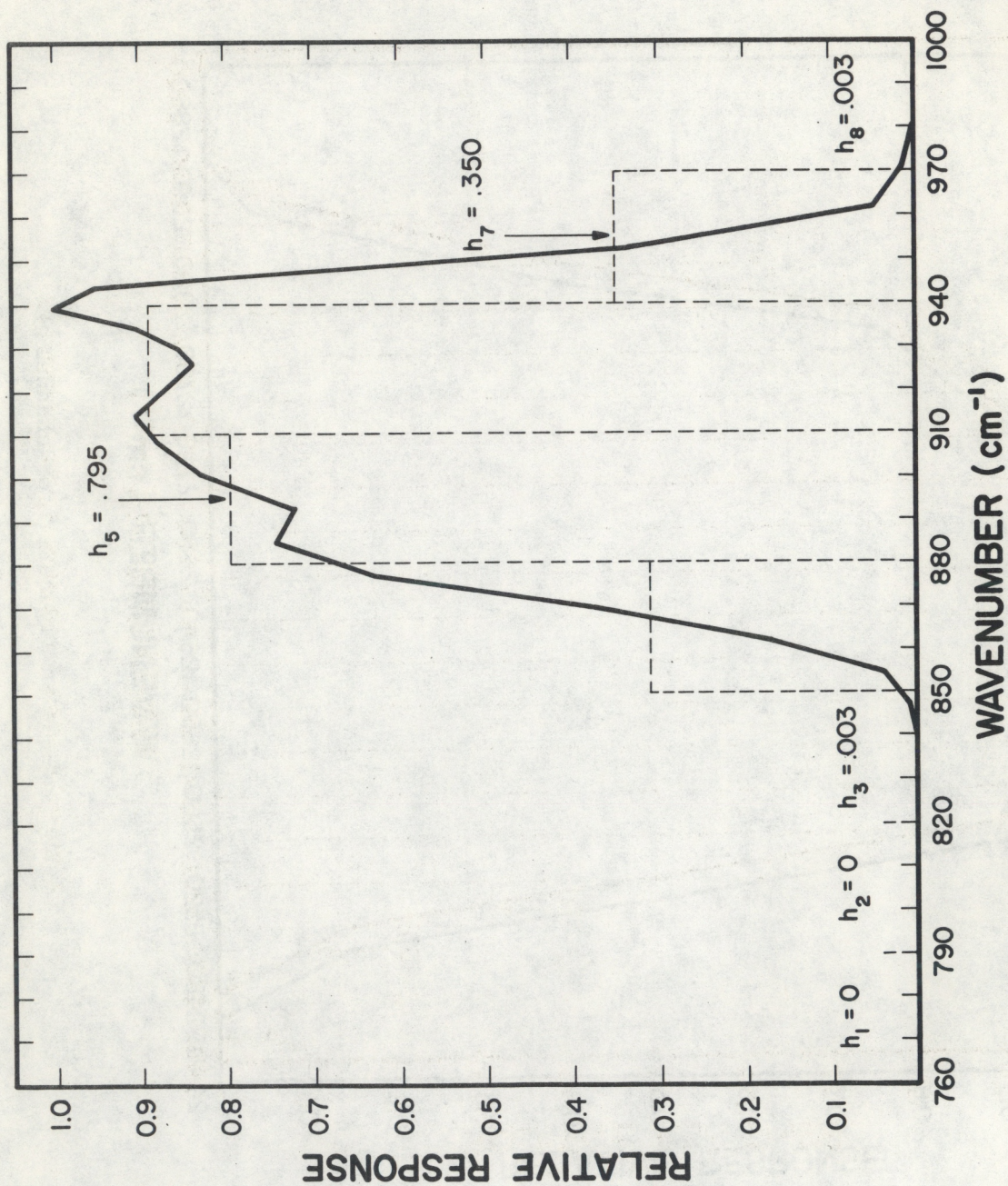


Figure 3.--Rectangular subintervals in region of channel 4 of AVHRR on TIROS-N.

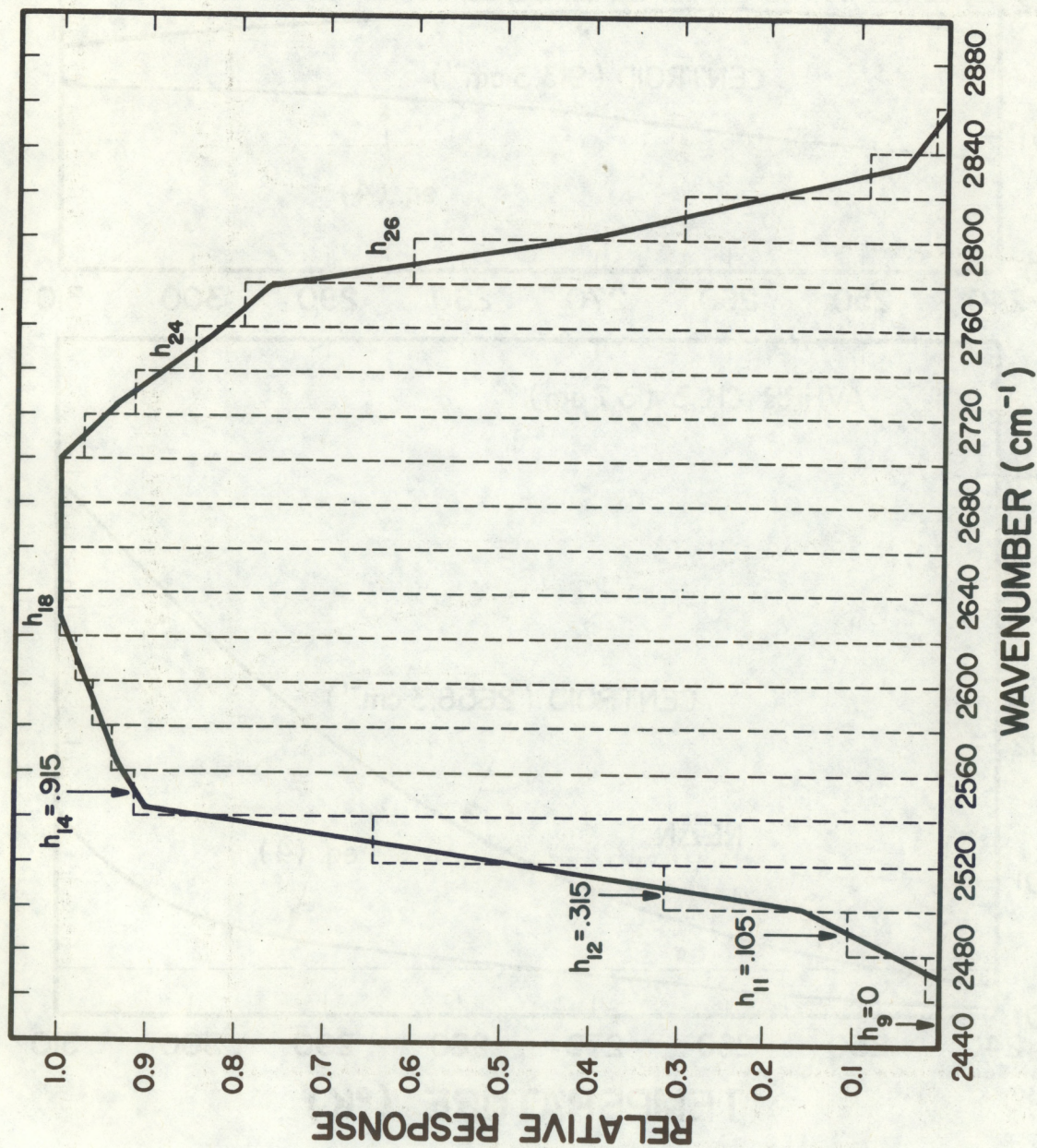


Figure 4.--As in figure 3, for channel 3

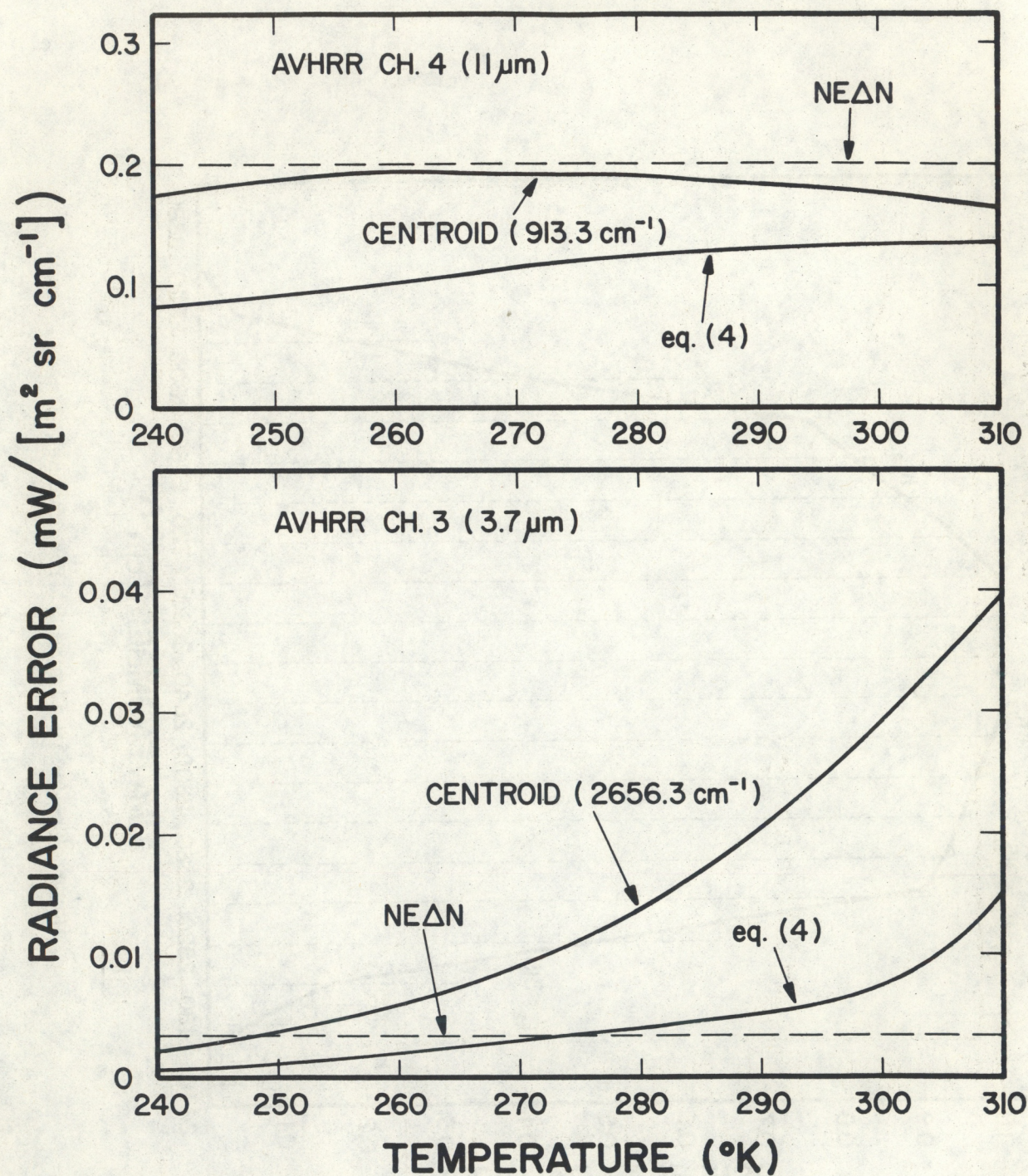


Figure 5.--Errors in calculated blackbody radiances vs temperature, for the "centroid" approximation and for the approximation of eq. 4.

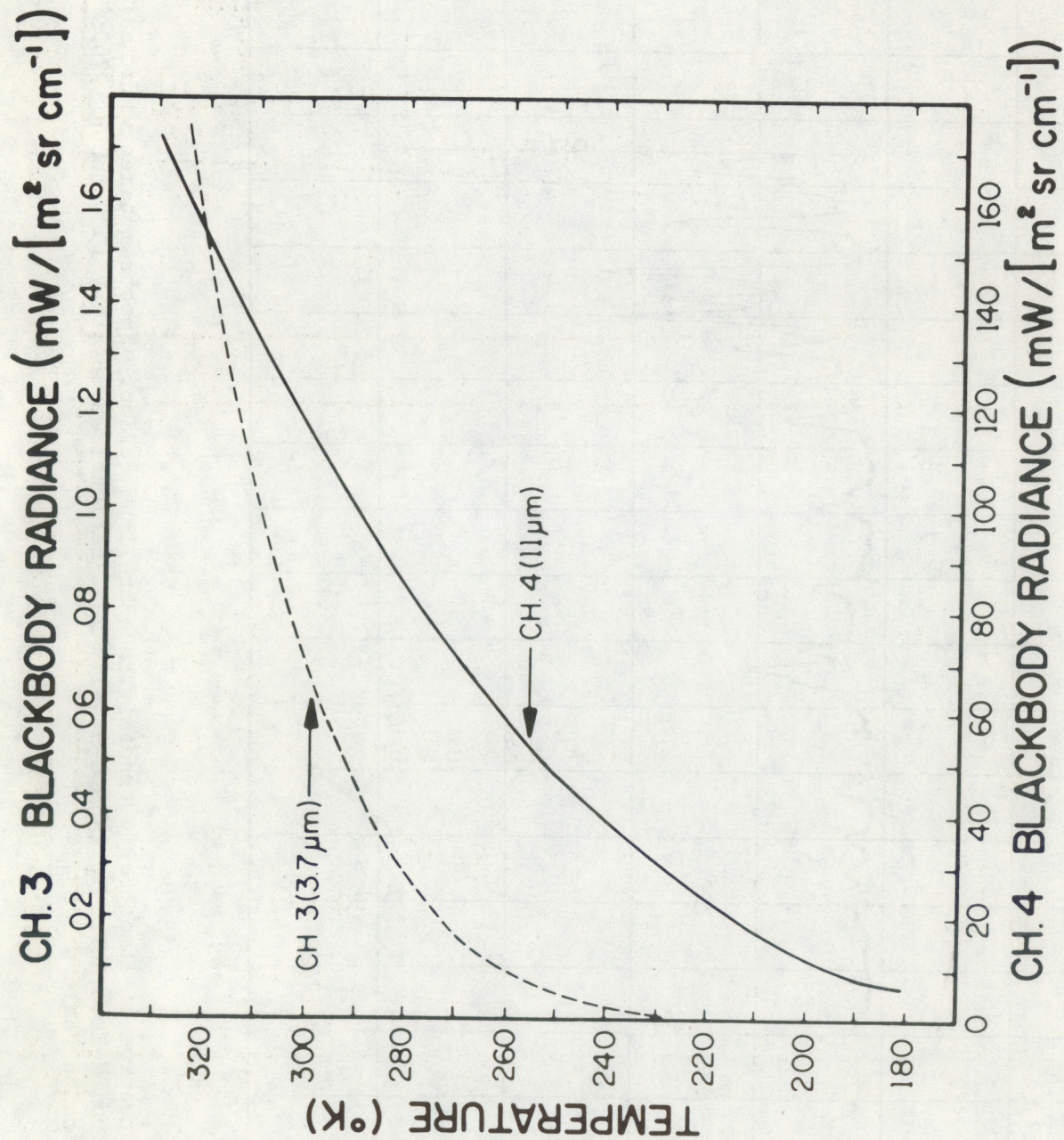


Figure 6.--Look-up table relating blackbody radiance to temperature. Solid curve (scale at bottom) for AVHRR channel 4; dashed curve (scale at top) for AVHRR channel 3.

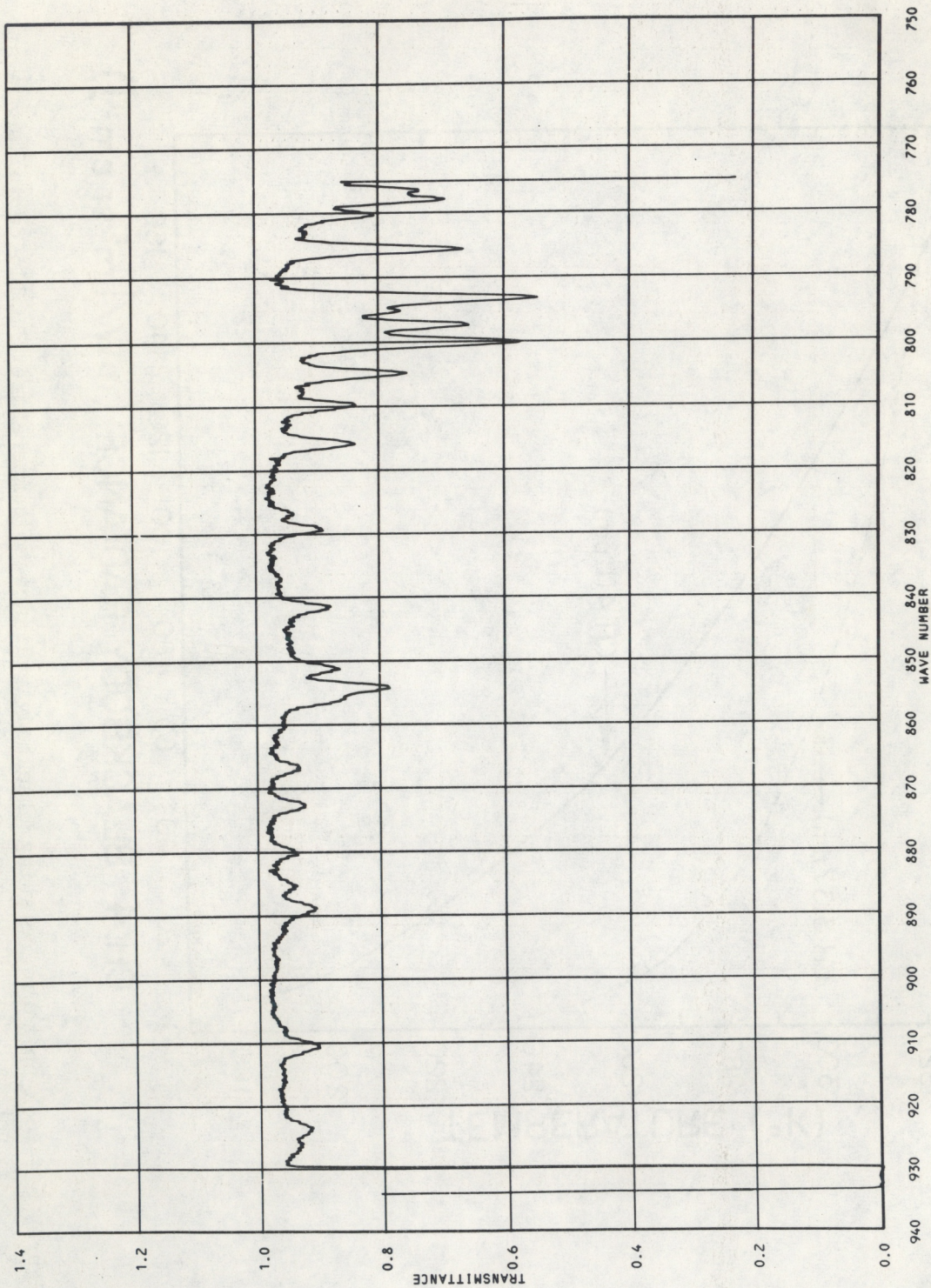


Figure 7.--Spectrum of atmospheric transmittance in 11- μ m region. Spectrum taken with radiation from McMath Solar Telescope at Kitt Peak National Observatory in October 1976. Solar zenith angle was 65.5°.

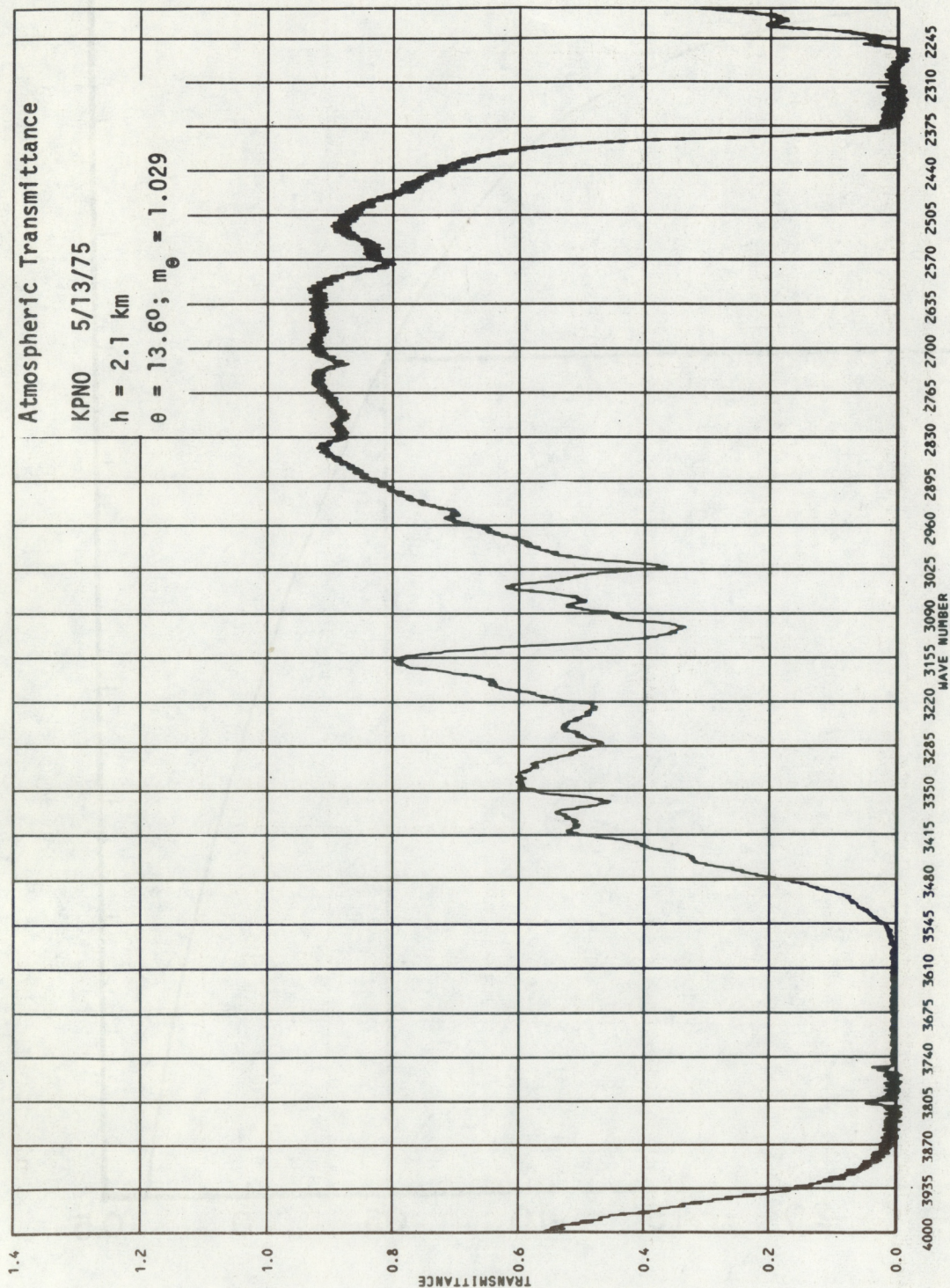


Figure 8.--As in figure 7, for 2.5- 4.5- μm region. Spectrum taken in May 1975. Solar zenith angle was 13.6° .

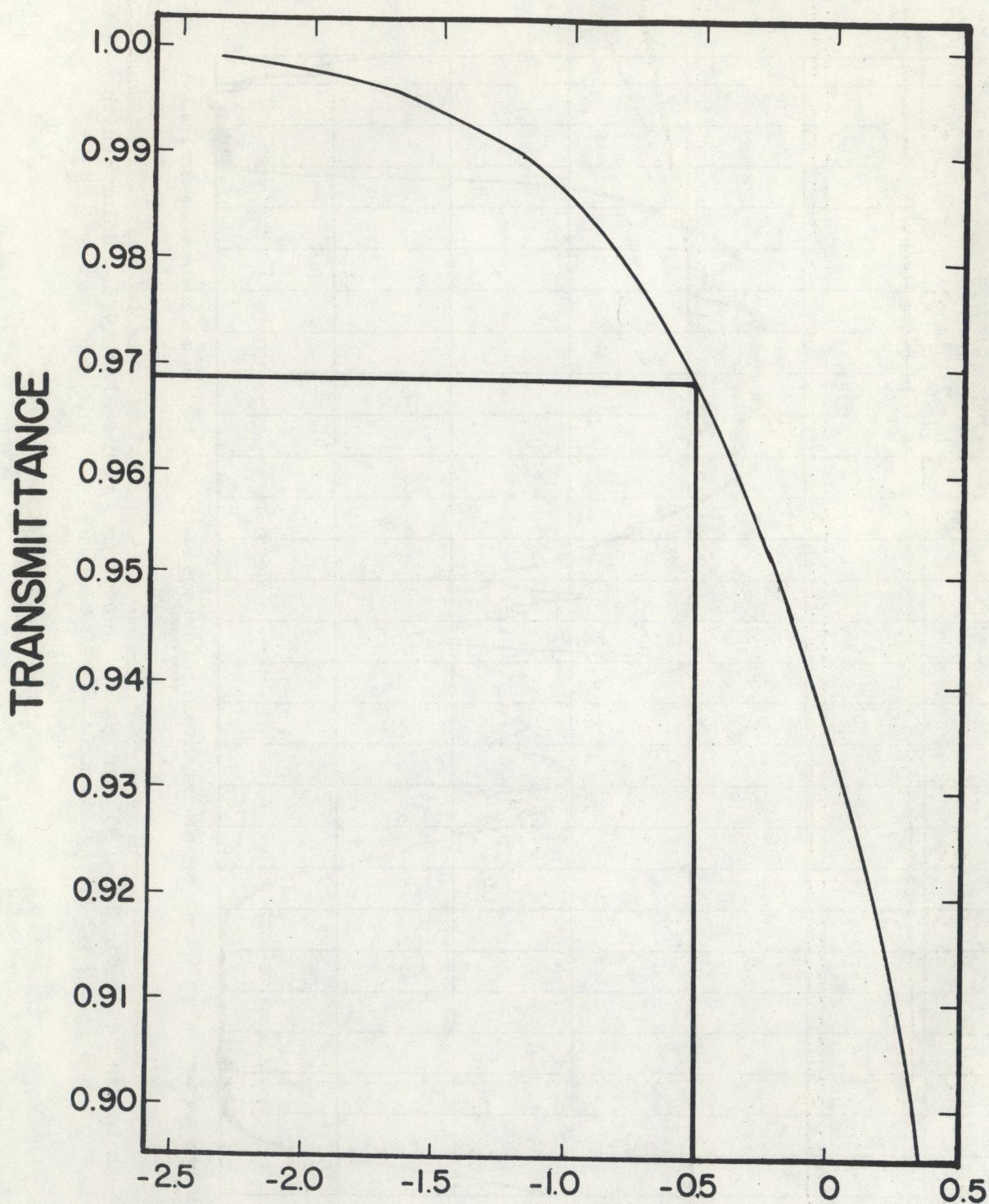


Figure 9.--Look-up table form LOWTRAN 4 (Selby et al. 1978), relating β (see text) to transmittance τ_u for uniformly - mixed gases.

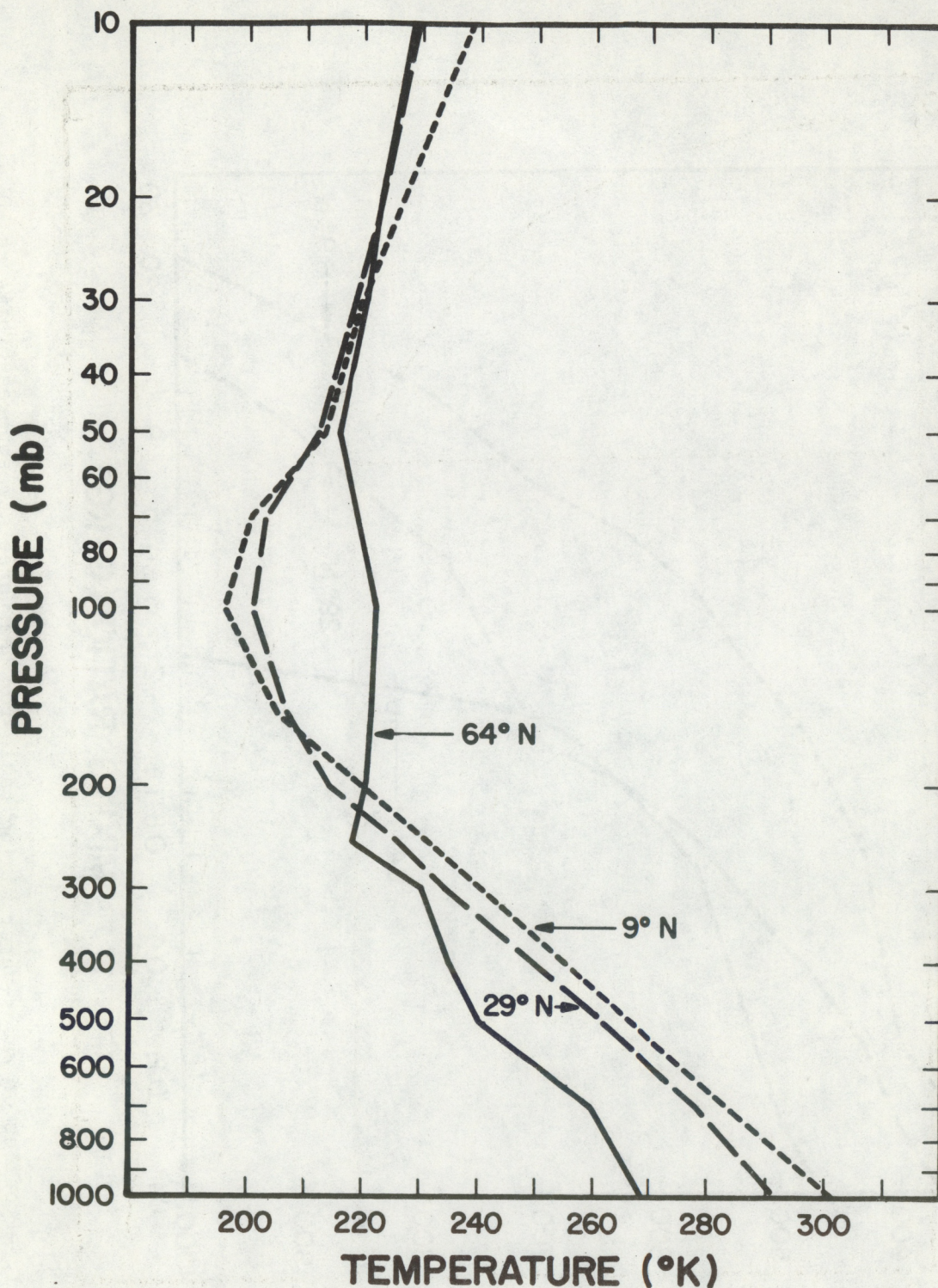


Figure 10.--Temperature profiles for three atmospheres: 64°N latitude (Ft. Greeley, Alaska, 10/14/66), 29°N latitude (Cape Canaveral, Florida, 11/18/66), and 9° latitude (Ft. Sherman, Canal Zone, 5/20/68).

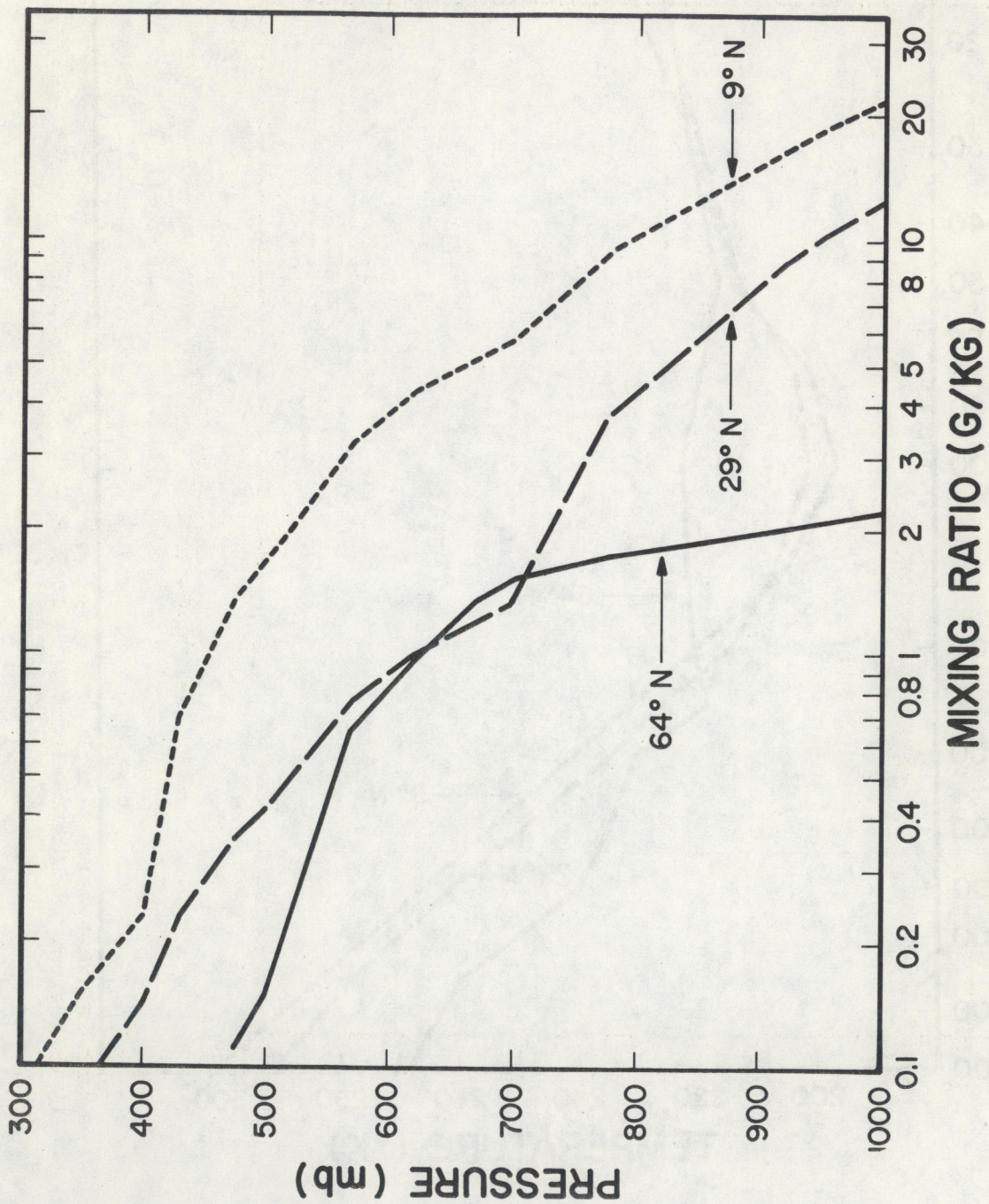


Figure 11.--Profiles of water-vapor mixing ratio for the three atmospheres of figure 10.

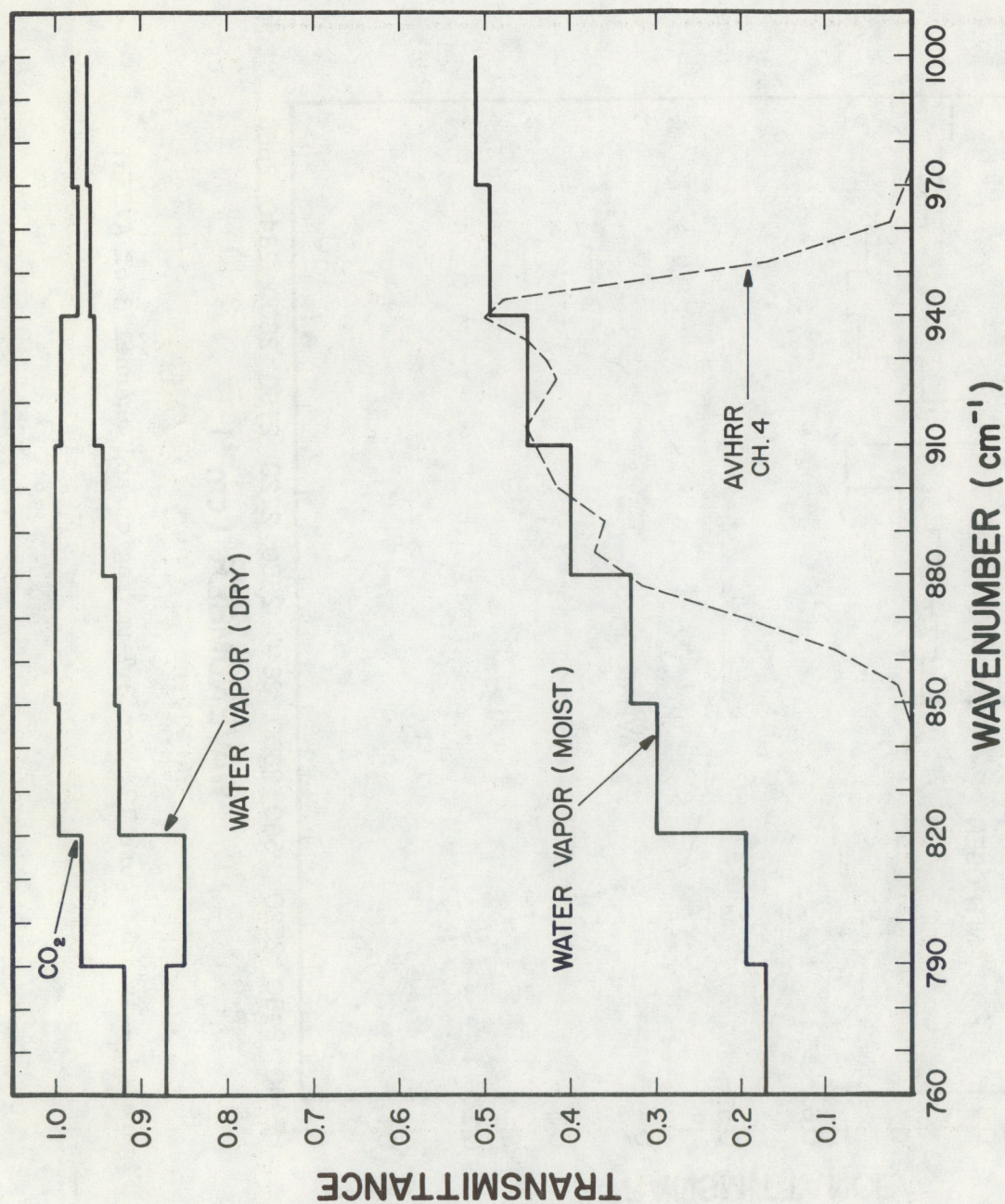


Figure 12.--Transmittances calculated for vertical path between top of atmosphere and surface in 11- μ m region. Relative response in channel 4 of TIROS-N AVHRR is superimposed.

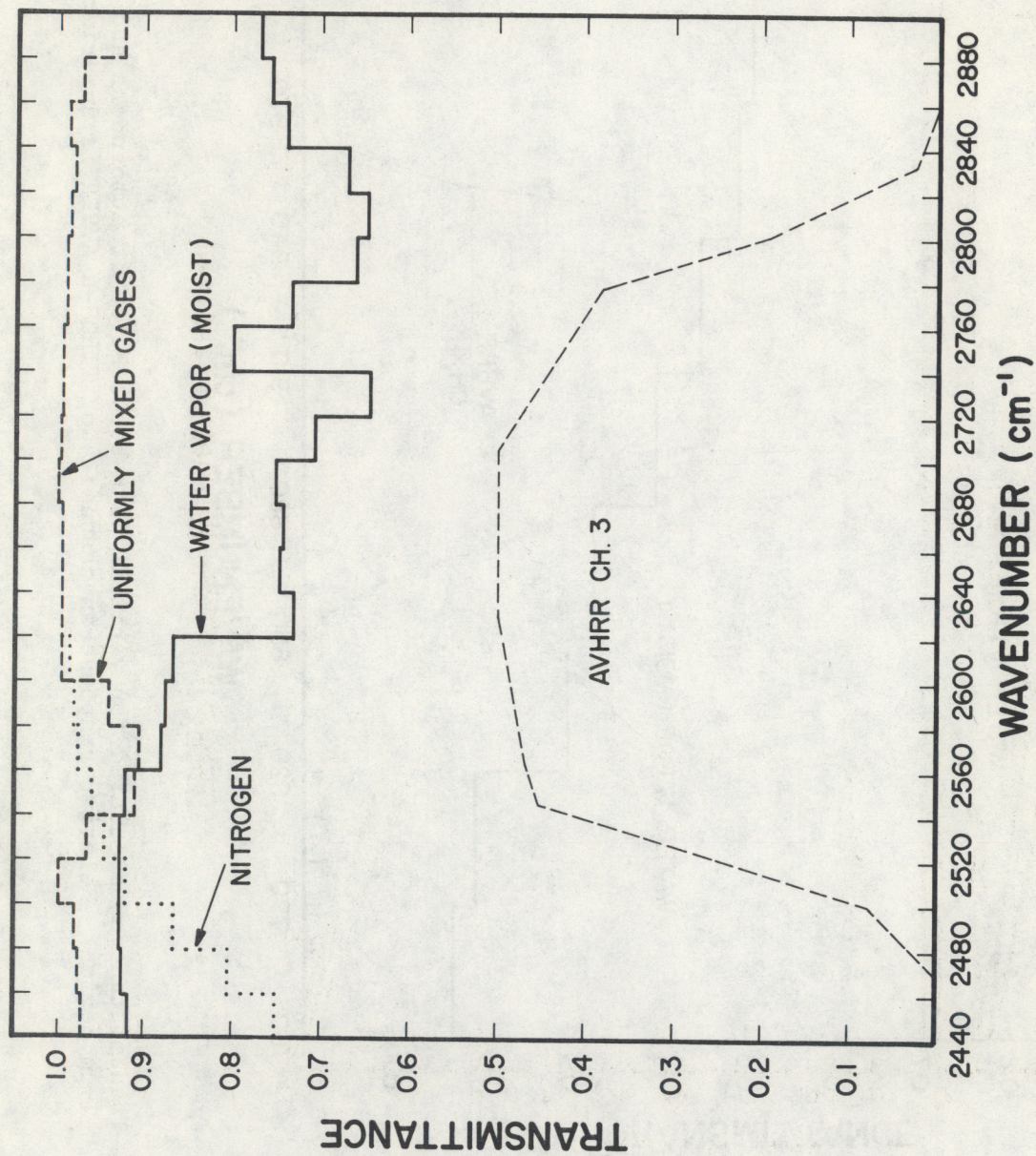


Figure 13.--As in figure 12, for 3.7- μ m region and channel 3 of AVHRR.

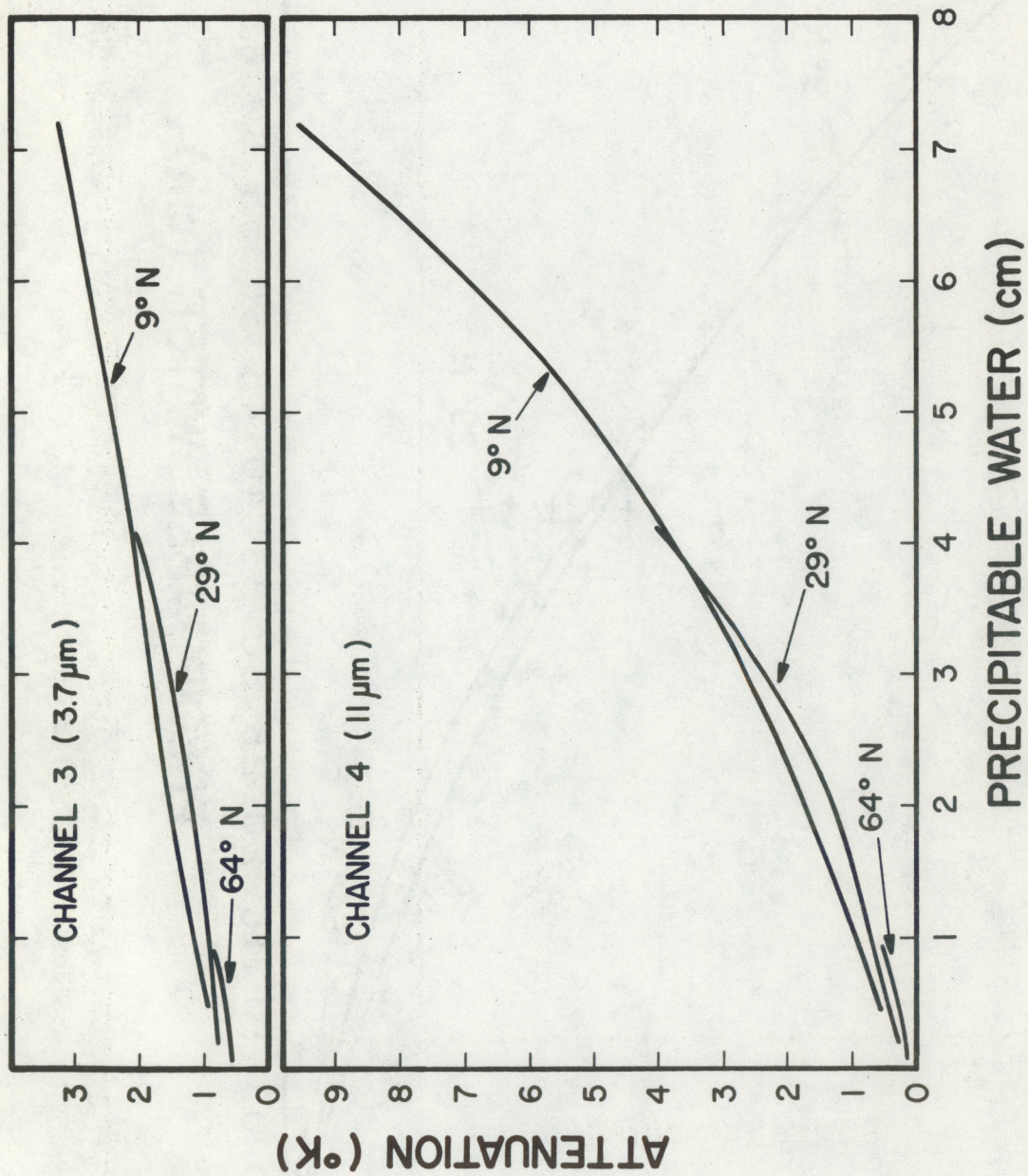


Figure 14.--Attenuation vs precipitable water for TIROS-N AVHRR.

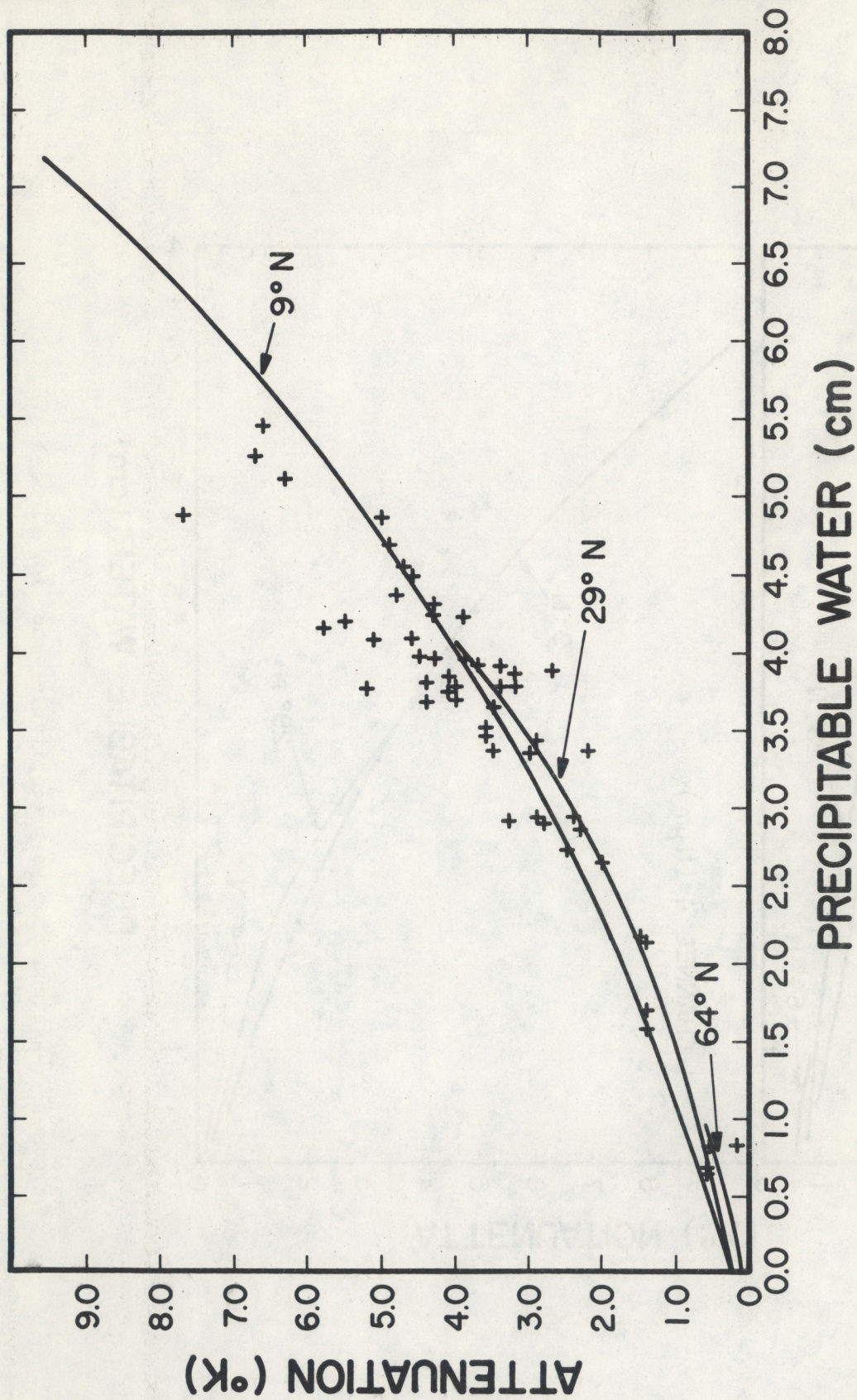


Figure 15.---Attenuation vs precipitable water for channel 4 (11 μ m) of TIROS-N AVHRR. Points designated by +'s are from McClain (1979).

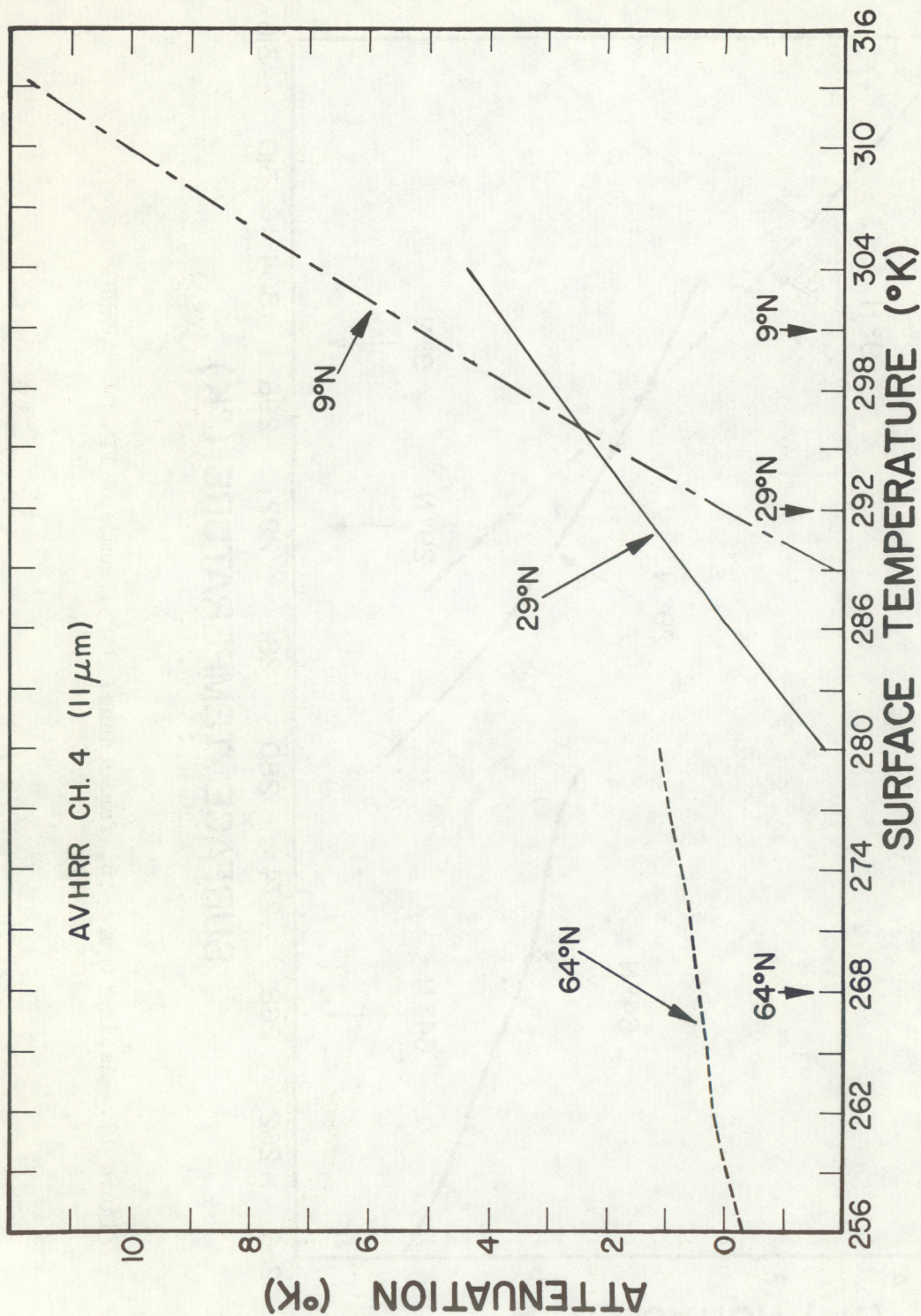


Figure 16.--Attenuation vs surface temperature for channel 4 (11 μm) of TIROS-N AVHRR, for 3 atmospheres. Arrows at bottom designate 1000 mb temperature for each atmosphere.

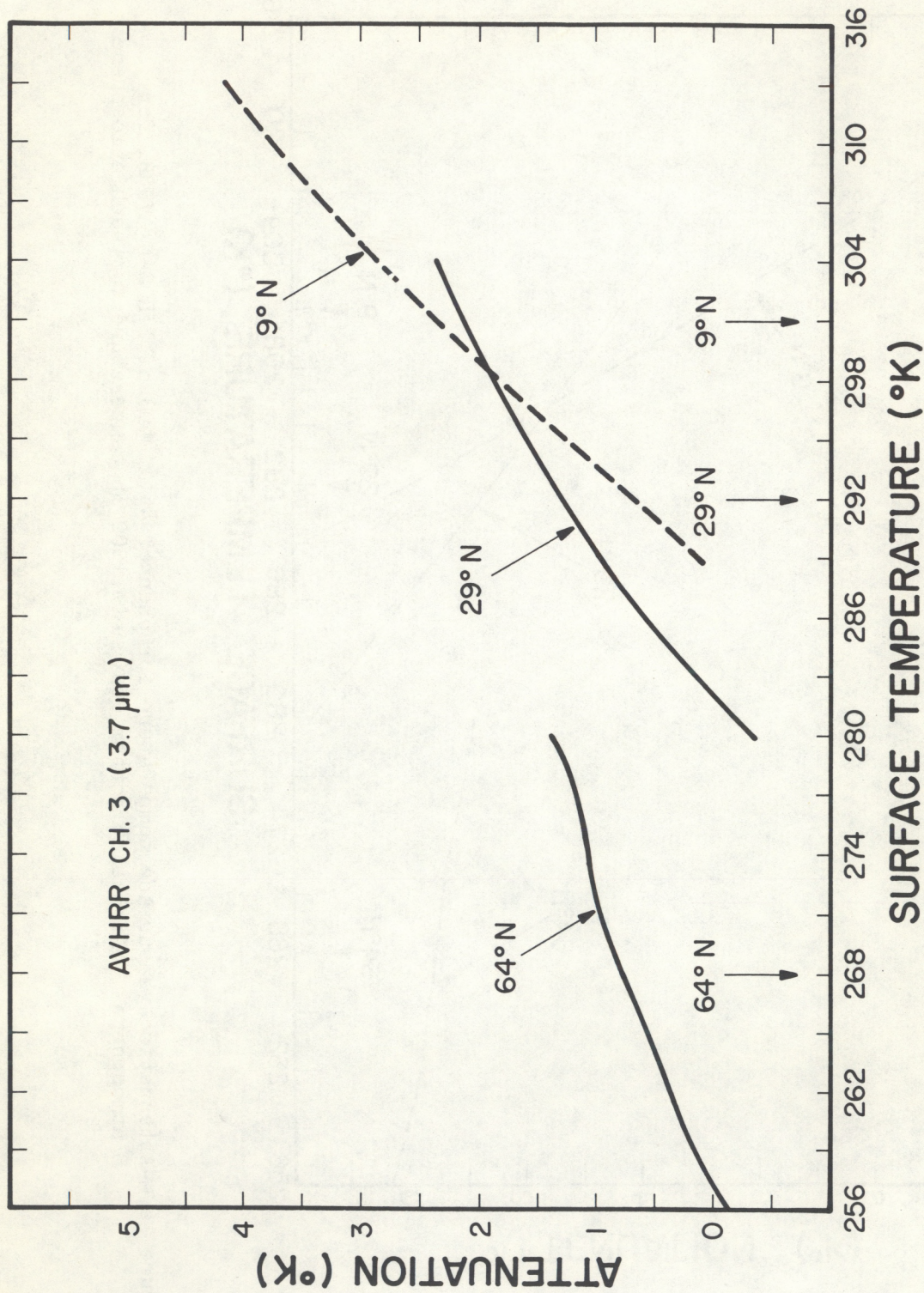


Figure 17.---As in figure 16, for channel 3 (3.7 μm) of TIROS-N AVHRR.

(Continued from inside front cover)

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